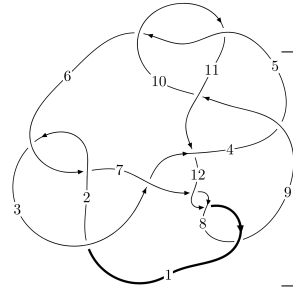
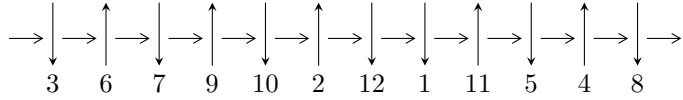


12a₀₂₂₀ (K12a₀₂₂₀)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$7,12 \xrightarrow{c_7} 8 \xrightarrow{c_{12}} 1 \xrightarrow{c_8} 4,9 \xrightarrow{c_4} 5 \xrightarrow{c_3} 3 \xrightarrow{c_1} 2 \xrightarrow{c_6} 6 \xrightarrow{c_{11}} 11 \xrightarrow{c_{10}} 10 \rightsquigarrow c_2, c_5, c_9$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -1.49096 \times 10^{181} u^{106} + 9.13411 \times 10^{180} u^{105} + \dots + 5.06627 \times 10^{181} b - 7.23078 \times 10^{182}, \\ 6.06637 \times 10^{182} u^{106} - 1.74049 \times 10^{183} u^{105} + \dots + 1.31723 \times 10^{183} a - 2.71243 \times 10^{184}, \\ u^{107} - 3u^{106} + \dots - 111u - 13 \rangle$$

$$I_2^u = \langle b^2 - b + 1, a^4 - 2a^2 + 2, u + 1 \rangle$$

$$I_3^u = \langle b^2 + b + 1, a^3, u - 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 121 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.49 \times 10^{181} u^{106} + 9.13 \times 10^{180} u^{105} + \dots + 5.07 \times 10^{181} b - 7.23 \times 10^{182}, 6.07 \times 10^{182} u^{106} - 1.74 \times 10^{183} u^{105} + \dots + 1.32 \times 10^{183} a - 2.71 \times 10^{184}, u^{107} - 3u^{106} + \dots - 111u - 13 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.460540u^{106} + 1.32132u^{105} + \dots + 177.538u + 20.5919 \\ 0.294291u^{106} - 0.180293u^{105} + \dots + 132.884u + 14.2724 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.339961u^{106} + 1.59337u^{105} + \dots + 324.599u + 34.4376 \\ 0.183891u^{106} - 0.141636u^{105} + \dots + 110.762u + 12.7655 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.166249u^{106} + 1.14103u^{105} + \dots + 310.421u + 34.8643 \\ 0.294291u^{106} - 0.180293u^{105} + \dots + 132.884u + 14.2724 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.813218u^{106} + 2.47693u^{105} + \dots + 392.711u + 41.8323 \\ -0.137167u^{106} + 0.176247u^{105} + \dots - 14.8599u - 0.292318 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.455592u^{106} - 2.01489u^{105} + \dots + 4.63244u + 13.1807 \\ 0.102062u^{106} + 0.00933752u^{105} + \dots - 49.6066u - 10.5866 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.832717u^{106} + 1.95875u^{105} + \dots + 267.318u + 30.0119 \\ -0.325817u^{106} + 0.776598u^{105} + \dots + 23.5117u + 1.24472 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.816162u^{106} + 2.12713u^{105} + \dots + 317.788u + 27.2416 \\ 0.127653u^{106} - 0.129996u^{105} + \dots - 43.6773u - 7.17967 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-0.703236u^{106} + 1.11367u^{105} + \dots + 8.19553u + 10.4291$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|---|
| c_1 | $u^{107} + 54u^{106} + \dots - 8u - 1$ |
| c_2, c_6 | $u^{107} - 2u^{106} + \dots + 2u - 1$ |
| c_3 | $u^{107} + 2u^{106} + \dots - 188610u - 36209$ |
| c_4 | $u^{107} + u^{106} + \dots + 3876u + 3764$ |
| c_5, c_{10} | $u^{107} - u^{106} + \dots + 4u + 4$ |
| c_7, c_8, c_{12} | $u^{107} + 3u^{106} + \dots - 111u + 13$ |
| c_9 | $u^{107} - 51u^{106} + \dots - 80u + 16$ |
| c_{11} | $u^{107} - 5u^{106} + \dots - 692004u + 563884$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------|--|
| c_1 | $y^{107} + 6y^{106} + \dots + 40y - 1$ |
| c_2, c_6 | $y^{107} + 54y^{106} + \dots - 8y - 1$ |
| c_3 | $y^{107} - 42y^{106} + \dots + 2264493656y - 1311091681$ |
| c_4 | $y^{107} - 21y^{106} + \dots + 424757360y - 14167696$ |
| c_5, c_{10} | $y^{107} + 51y^{106} + \dots - 80y - 16$ |
| c_7, c_8, c_{12} | $y^{107} - 103y^{106} + \dots - 9207y - 169$ |
| c_9 | $y^{107} + 15y^{106} + \dots - 2304y - 256$ |
| c_{11} | $y^{107} + 39y^{106} + \dots - 10755598905296y - 317965165456$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -0.904262 + 0.431584I$ $a = -0.133296 - 0.339278I$ $b = 0.530938 - 0.189035I$ | $-1.99885 + 5.17052I$ | 0 |
| $u = -0.904262 - 0.431584I$ $a = -0.133296 + 0.339278I$ $b = 0.530938 + 0.189035I$ | $-1.99885 - 5.17052I$ | 0 |
| $u = 0.787760 + 0.643206I$ $a = 0.871626 + 0.708841I$ $b = -1.096750 + 0.335060I$ | $-4.40852 + 2.42869I$ | 0 |
| $u = 0.787760 - 0.643206I$ $a = 0.871626 - 0.708841I$ $b = -1.096750 - 0.335060I$ | $-4.40852 - 2.42869I$ | 0 |
| $u = -0.956946 + 0.360565I$ $a = -0.597535 + 0.227282I$ $b = 0.958606 + 0.767416I$ | $-0.373093 - 0.971380I$ | 0 |
| $u = -0.956946 - 0.360565I$ $a = -0.597535 - 0.227282I$ $b = 0.958606 - 0.767416I$ | $-0.373093 + 0.971380I$ | 0 |
| $u = -0.358282 + 0.896448I$ $a = -1.10747 + 1.21913I$ $b = 1.41980 - 0.65124I$ | $-1.00079 + 12.66400I$ | 0 |
| $u = -0.358282 - 0.896448I$ $a = -1.10747 - 1.21913I$ $b = 1.41980 + 0.65124I$ | $-1.00079 - 12.66400I$ | 0 |
| $u = 0.992483 + 0.309368I$ $a = -0.160962 - 0.486626I$ $b = -0.269567 - 0.291149I$ | $-3.00656 - 1.10116I$ | 0 |
| $u = 0.992483 - 0.309368I$ $a = -0.160962 + 0.486626I$ $b = -0.269567 + 0.291149I$ | $-3.00656 + 1.10116I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.608114 + 0.728544I$ | | |
| $a = -0.691648 + 0.449361I$ | $-2.81110 + 0.44680I$ | 0 |
| $b = 1.128540 - 0.315477I$ | | |
| $u = -0.608114 - 0.728544I$ | | |
| $a = -0.691648 - 0.449361I$ | $-2.81110 - 0.44680I$ | 0 |
| $b = 1.128540 + 0.315477I$ | | |
| $u = 1.033090 + 0.207124I$ | | |
| $a = -0.748487 - 0.391269I$ | $-1.89971 - 0.44446I$ | 0 |
| $b = 0.001488 - 0.410585I$ | | |
| $u = 1.033090 - 0.207124I$ | | |
| $a = -0.748487 + 0.391269I$ | $-1.89971 + 0.44446I$ | 0 |
| $b = 0.001488 + 0.410585I$ | | |
| $u = 0.391004 + 0.857866I$ | | |
| $a = 0.99548 + 1.11660I$ | $-3.15539 - 7.60366I$ | 0 |
| $b = -1.36178 - 0.60152I$ | | |
| $u = 0.391004 - 0.857866I$ | | |
| $a = 0.99548 - 1.11660I$ | $-3.15539 + 7.60366I$ | 0 |
| $b = -1.36178 + 0.60152I$ | | |
| $u = -0.541436 + 0.770509I$ | | |
| $a = -0.741344 + 1.076260I$ | $-2.59503 + 4.68959I$ | 0 |
| $b = 0.858958 - 0.011904I$ | | |
| $u = -0.541436 - 0.770509I$ | | |
| $a = -0.741344 - 1.076260I$ | $-2.59503 - 4.68959I$ | 0 |
| $b = 0.858958 + 0.011904I$ | | |
| $u = 0.606025 + 0.712743I$ | | |
| $a = 0.766219 + 0.966722I$ | $-4.40673 + 0.22528I$ | 0 |
| $b = -0.916895 + 0.108302I$ | | |
| $u = 0.606025 - 0.712743I$ | | |
| $a = 0.766219 - 0.966722I$ | $-4.40673 - 0.22528I$ | 0 |
| $b = -0.916895 - 0.108302I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.023130 + 0.308756I$ | | |
| $a = 0.835122 + 0.060413I$ | $1.30429 + 3.26731I$ | 0 |
| $b = -0.362952 - 0.673846I$ | | |
| $u = -1.023130 - 0.308756I$ | | |
| $a = 0.835122 - 0.060413I$ | $1.30429 - 3.26731I$ | 0 |
| $b = -0.362952 + 0.673846I$ | | |
| $u = 0.517016 + 0.772169I$ | | |
| $a = 0.775725 + 0.721111I$ | $-4.10761 - 5.28481I$ | 0 |
| $b = -1.220000 - 0.429494I$ | | |
| $u = 0.517016 - 0.772169I$ | | |
| $a = 0.775725 - 0.721111I$ | $-4.10761 + 5.28481I$ | 0 |
| $b = -1.220000 + 0.429494I$ | | |
| $u = -0.873419 + 0.646269I$ | | |
| $a = -0.961755 + 0.599798I$ | $-2.58534 - 7.32575I$ | 0 |
| $b = 1.201530 + 0.414908I$ | | |
| $u = -0.873419 - 0.646269I$ | | |
| $a = -0.961755 - 0.599798I$ | $-2.58534 + 7.32575I$ | 0 |
| $b = 1.201530 - 0.414908I$ | | |
| $u = -1.073390 + 0.173489I$ | | |
| $a = 1.185970 - 0.495544I$ | $0.62750 - 3.83015I$ | 0 |
| $b = 0.025415 - 0.404365I$ | | |
| $u = -1.073390 - 0.173489I$ | | |
| $a = 1.185970 + 0.495544I$ | $0.62750 + 3.83015I$ | 0 |
| $b = 0.025415 + 0.404365I$ | | |
| $u = -0.347205 + 0.789149I$ | | |
| $a = 0.98779 - 1.36315I$ | $1.55865 + 7.81274I$ | 0 |
| $b = -0.998853 + 0.689661I$ | | |
| $u = -0.347205 - 0.789149I$ | | |
| $a = 0.98779 + 1.36315I$ | $1.55865 - 7.81274I$ | 0 |
| $b = -0.998853 - 0.689661I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -0.697681 + 0.486866I$ $a = 1.017260 - 0.382052I$ $b = -0.787593 - 0.084239I$ | $0.26585 - 3.31149I$ | 0 |
| $u = -0.697681 - 0.486866I$ $a = 1.017260 + 0.382052I$ $b = -0.787593 + 0.084239I$ | $0.26585 + 3.31149I$ | 0 |
| $u = -0.305416 + 0.776614I$ $a = -0.73060 + 1.37269I$ $b = 1.24517 - 0.72111I$ | $1.49738 + 5.20503I$ | 0 |
| $u = -0.305416 - 0.776614I$ $a = -0.73060 - 1.37269I$ $b = 1.24517 + 0.72111I$ | $1.49738 - 5.20503I$ | 0 |
| $u = 0.366231 + 0.724436I$ $a = -0.89880 - 1.21010I$ $b = 0.918174 + 0.589822I$ | $-0.58468 - 2.93122I$ | 0 |
| $u = 0.366231 - 0.724436I$ $a = -0.89880 + 1.21010I$ $b = 0.918174 - 0.589822I$ | $-0.58468 + 2.93122I$ | 0 |
| $u = -1.193830 + 0.133951I$ $a = 1.186440 + 0.254501I$ $b = 0.478845 - 0.410517I$ | $1.09290 + 3.87383I$ | 0 |
| $u = -1.193830 - 0.133951I$ $a = 1.186440 - 0.254501I$ $b = 0.478845 + 0.410517I$ | $1.09290 - 3.87383I$ | 0 |
| $u = 1.201360 + 0.183444I$ $a = 0.419710 - 0.338240I$ $b = -0.79913 + 1.21442I$ | $-0.18627 + 3.28365I$ | 0 |
| $u = 1.201360 - 0.183444I$ $a = 0.419710 + 0.338240I$ $b = -0.79913 - 1.21442I$ | $-0.18627 - 3.28365I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 1.24303$ $a = -0.920747$ $b = -0.643030$ | -2.16232 | 0 |
| $u = -0.222910 + 0.706813I$ $a = 0.57898 - 1.45300I$ $b = -0.731318 + 0.783769I$ | $3.66702 + 0.52581I$ | $4.89543 - 0.81246I$ |
| $u = -0.222910 - 0.706813I$ $a = 0.57898 + 1.45300I$ $b = -0.731318 - 0.783769I$ | $3.66702 - 0.52581I$ | $4.89543 + 0.81246I$ |
| $u = 0.504839 + 0.540212I$ $a = -0.851823 - 0.684157I$ $b = 0.771656 + 0.223252I$ | $-1.33042 - 1.16536I$ | $-4.57238 + 3.59666I$ |
| $u = 0.504839 - 0.540212I$ $a = -0.851823 + 0.684157I$ $b = 0.771656 - 0.223252I$ | $-1.33042 + 1.16536I$ | $-4.57238 - 3.59666I$ |
| $u = 1.245520 + 0.201441I$ $a = -0.458006 + 0.563615I$ $b = 0.050412 - 1.311980I$ | $0.58850 - 1.75903I$ | 0 |
| $u = 1.245520 - 0.201441I$ $a = -0.458006 - 0.563615I$ $b = 0.050412 + 1.311980I$ | $0.58850 + 1.75903I$ | 0 |
| $u = -1.346650 + 0.022218I$ $a = -0.127155 - 0.744802I$ $b = 0.49820 + 1.55717I$ | $-3.79047 - 1.76476I$ | 0 |
| $u = -1.346650 - 0.022218I$ $a = -0.127155 + 0.744802I$ $b = 0.49820 - 1.55717I$ | $-3.79047 + 1.76476I$ | 0 |
| $u = -1.349610 + 0.062394I$ $a = -1.345650 + 0.408342I$ $b = -1.030110 + 0.398339I$ | $-1.64321 - 0.63614I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -1.349610 - 0.062394I$ $a = -1.345650 - 0.408342I$ $b = -1.030110 - 0.398339I$ | $-1.64321 + 0.63614I$ | 0 |
| $u = -1.356410 + 0.112287I$ $a = 0.202197 + 0.820758I$ $b = 0.17434 - 1.59862I$ | $-3.53567 + 3.73820I$ | 0 |
| $u = -1.356410 - 0.112287I$ $a = 0.202197 - 0.820758I$ $b = 0.17434 + 1.59862I$ | $-3.53567 - 3.73820I$ | 0 |
| $u = -1.358470 + 0.143026I$ $a = -1.353580 - 0.228884I$ $b = -1.160700 + 0.526570I$ | $-1.26765 + 7.94095I$ | 0 |
| $u = -1.358470 - 0.143026I$ $a = -1.353580 + 0.228884I$ $b = -1.160700 - 0.526570I$ | $-1.26765 - 7.94095I$ | 0 |
| $u = 1.368360 + 0.085834I$ $a = 0.290701 - 0.765642I$ $b = -0.64968 + 1.59002I$ | $-2.02551 - 3.00487I$ | 0 |
| $u = 1.368360 - 0.085834I$ $a = 0.290701 + 0.765642I$ $b = -0.64968 - 1.59002I$ | $-2.02551 + 3.00487I$ | 0 |
| $u = 1.379890 + 0.160353I$ $a = -0.317648 + 0.896210I$ $b = -0.05306 - 1.66215I$ | $-1.56942 - 8.60645I$ | 0 |
| $u = 1.379890 - 0.160353I$ $a = -0.317648 - 0.896210I$ $b = -0.05306 + 1.66215I$ | $-1.56942 + 8.60645I$ | 0 |
| $u = 1.390970 + 0.096096I$ $a = 1.103970 + 0.103885I$ $b = 1.152920 + 0.397138I$ | $-4.97509 - 3.82300I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 1.390970 - 0.096096I$ $a = 1.103970 - 0.103885I$ $b = 1.152920 - 0.397138I$ | $-4.97509 + 3.82300I$ | 0 |
| $u = -0.037503 + 0.596397I$ $a = 0.36414 - 1.92620I$ $b = 0.261674 + 1.022480I$ | $4.52566 - 1.15109I$ | $6.23436 + 0.38594I$ |
| $u = -0.037503 - 0.596397I$ $a = 0.36414 + 1.92620I$ $b = 0.261674 - 1.022480I$ | $4.52566 + 1.15109I$ | $6.23436 - 0.38594I$ |
| $u = 1.40667 + 0.26184I$ $a = -0.485247 + 0.970070I$ $b = -1.141110 - 0.816619I$ | $-1.56131 - 4.01030I$ | 0 |
| $u = 1.40667 - 0.26184I$ $a = -0.485247 - 0.970070I$ $b = -1.141110 + 0.816619I$ | $-1.56131 + 4.01030I$ | 0 |
| $u = -0.298161 + 0.443295I$ $a = -0.549122 + 0.963108I$ $b = 0.444626 + 0.356044I$ | $-0.15371 - 1.58994I$ | $-1.42624 + 1.98288I$ |
| $u = -0.298161 - 0.443295I$ $a = -0.549122 - 0.963108I$ $b = 0.444626 - 0.356044I$ | $-0.15371 + 1.58994I$ | $-1.42624 - 1.98288I$ |
| $u = 1.46362 + 0.17385I$ $a = 0.304404 - 1.032320I$ $b = 0.846992 + 0.221001I$ | $-6.17519 - 0.76182I$ | 0 |
| $u = 1.46362 - 0.17385I$ $a = 0.304404 + 1.032320I$ $b = 0.846992 - 0.221001I$ | $-6.17519 + 0.76182I$ | 0 |
| $u = -0.155990 + 0.497529I$ $a = 1.04483 - 2.35071I$ $b = 0.015047 + 1.085040I$ | $3.36815 + 6.26844I$ | $3.96391 - 7.68382I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.155990 - 0.497529I$ $a = 1.04483 + 2.35071I$ $b = 0.015047 - 1.085040I$ | $3.36815 - 6.26844I$ | $3.96391 + 7.68382I$ |
| $u = 1.44935 + 0.30104I$ $a = 0.526429 - 1.065710I$ $b = 1.52911 + 0.71038I$ | $-4.15695 - 9.12120I$ | 0 |
| $u = 1.44935 - 0.30104I$ $a = 0.526429 + 1.065710I$ $b = 1.52911 - 0.71038I$ | $-4.15695 + 9.12120I$ | 0 |
| $u = -1.46542 + 0.27690I$ $a = 0.254920 + 1.037850I$ $b = 1.32007 - 0.86889I$ | $-6.50073 + 6.60004I$ | 0 |
| $u = -1.46542 - 0.27690I$ $a = 0.254920 - 1.037850I$ $b = 1.32007 + 0.86889I$ | $-6.50073 - 6.60004I$ | 0 |
| $u = 1.46386 + 0.30484I$ $a = -0.263373 + 1.147230I$ $b = -1.31153 - 0.95461I$ | $-4.27302 - 11.79580I$ | 0 |
| $u = 1.46386 - 0.30484I$ $a = -0.263373 - 1.147230I$ $b = -1.31153 + 0.95461I$ | $-4.27302 + 11.79580I$ | 0 |
| $u = -1.48495 + 0.19479I$ $a = 0.167816 + 0.722945I$ $b = 1.38966 - 0.61548I$ | $-7.76705 + 3.90228I$ | 0 |
| $u = -1.48495 - 0.19479I$ $a = 0.167816 - 0.722945I$ $b = 1.38966 + 0.61548I$ | $-7.76705 - 3.90228I$ | 0 |
| $u = 1.49176 + 0.14550I$ $a = -0.134205 + 0.537263I$ $b = -1.41496 - 0.46095I$ | $-6.68330 + 1.19848I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $u = 1.49176 - 0.14550I$ $a = -0.134205 - 0.537263I$ $b = -1.41496 + 0.46095I$ | $-6.68330 - 1.19848I$ | 0 |
| $u = 0.066760 + 0.486078I$ $a = -0.41695 + 2.46615I$ $b = -0.881052 - 0.937770I$ | $3.30433 - 5.76662I$ | $3.79923 + 6.91273I$ |
| $u = 0.066760 - 0.486078I$ $a = -0.41695 - 2.46615I$ $b = -0.881052 + 0.937770I$ | $3.30433 + 5.76662I$ | $3.79923 - 6.91273I$ |
| $u = 1.48454 + 0.34898I$ $a = 0.254201 - 1.213360I$ $b = 1.65526 + 0.76856I$ | $-6.9227 - 17.1759I$ | 0 |
| $u = 1.48454 - 0.34898I$ $a = 0.254201 + 1.213360I$ $b = 1.65526 - 0.76856I$ | $-6.9227 + 17.1759I$ | 0 |
| $u = -1.49146 + 0.32588I$ $a = -0.272333 - 1.094210I$ $b = -1.64360 + 0.71264I$ | $-9.2253 + 11.9036I$ | 0 |
| $u = -1.49146 - 0.32588I$ $a = -0.272333 + 1.094210I$ $b = -1.64360 - 0.71264I$ | $-9.2253 - 11.9036I$ | 0 |
| $u = 0.066503 + 0.460813I$ $a = -1.13702 - 1.73349I$ $b = -0.034938 + 0.934134I$ | $0.95866 - 1.83427I$ | $0.73406 + 3.89858I$ |
| $u = 0.066503 - 0.460813I$ $a = -1.13702 + 1.73349I$ $b = -0.034938 - 0.934134I$ | $0.95866 + 1.83427I$ | $0.73406 - 3.89858I$ |
| $u = -1.52227 + 0.25706I$ $a = -0.251276 - 0.717849I$ $b = -1.62467 + 0.53247I$ | $-10.77400 + 9.01109I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.52227 - 0.25706I$ | | |
| $a = -0.251276 + 0.717849I$ | $-10.77400 - 9.01109I$ | 0 |
| $b = -1.62467 - 0.53247I$ | | |
| $u = 1.53098 + 0.21479I$ | | |
| $a = 0.265871 - 0.505711I$ | $-9.84860 - 3.77356I$ | 0 |
| $b = 1.58794 + 0.43363I$ | | |
| $u = 1.53098 - 0.21479I$ | | |
| $a = 0.265871 + 0.505711I$ | $-9.84860 + 3.77356I$ | 0 |
| $b = 1.58794 - 0.43363I$ | | |
| $u = 1.52612 + 0.24737I$ | | |
| $a = 0.153500 - 1.100690I$ | $-9.36969 - 8.34998I$ | 0 |
| $b = 0.833157 + 0.473629I$ | | |
| $u = 1.52612 - 0.24737I$ | | |
| $a = 0.153500 + 1.100690I$ | $-9.36969 + 8.34998I$ | 0 |
| $b = 0.833157 - 0.473629I$ | | |
| $u = -1.53189 + 0.21291I$ | | |
| $a = -0.156064 - 1.042910I$ | $-11.43450 + 3.06093I$ | 0 |
| $b = -0.907267 + 0.417953I$ | | |
| $u = -1.53189 - 0.21291I$ | | |
| $a = -0.156064 + 1.042910I$ | $-11.43450 - 3.06093I$ | 0 |
| $b = -0.907267 - 0.417953I$ | | |
| $u = -1.55684 + 0.12305I$ | | |
| $a = -0.148490 - 0.836226I$ | $-12.31450 + 0.01828I$ | 0 |
| $b = -1.116250 + 0.286900I$ | | |
| $u = -1.55684 - 0.12305I$ | | |
| $a = -0.148490 + 0.836226I$ | $-12.31450 - 0.01828I$ | 0 |
| $b = -1.116250 - 0.286900I$ | | |
| $u = 1.56528 + 0.07740I$ | | |
| $a = 0.149063 - 0.704571I$ | $-11.02690 + 5.25826I$ | 0 |
| $b = 1.211780 + 0.210713I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 1.56528 - 0.07740I$ $a = 0.149063 + 0.704571I$ $b = 1.211780 - 0.210713I$ | $-11.02690 - 5.25826I$ | 0 |
| $u = -0.154957 + 0.386807I$ $a = -0.836798 + 0.702949I$ $b = 0.264901 + 0.471924I$ | $-0.14462 - 1.60637I$ | $-1.48281 + 3.72848I$ |
| $u = -0.154957 - 0.386807I$ $a = -0.836798 - 0.702949I$ $b = 0.264901 - 0.471924I$ | $-0.14462 + 1.60637I$ | $-1.48281 - 3.72848I$ |
| $u = -0.156750 + 0.282652I$ $a = 2.02349 + 1.65973I$ $b = 0.732640 - 0.821272I$ | $0.05214 + 2.40475I$ | $-0.47032 - 3.52067I$ |
| $u = -0.156750 - 0.282652I$ $a = 2.02349 - 1.65973I$ $b = 0.732640 + 0.821272I$ | $0.05214 - 2.40475I$ | $-0.47032 + 3.52067I$ |
| $u = -0.048155 + 0.266320I$ $a = -1.69653 + 4.39859I$ $b = -0.672555 - 0.967240I$ | $2.63765 + 1.71529I$ | $3.42382 - 0.87900I$ |
| $u = -0.048155 - 0.266320I$ $a = -1.69653 - 4.39859I$ $b = -0.672555 + 0.967240I$ | $2.63765 - 1.71529I$ | $3.42382 + 0.87900I$ |

$$\text{II. } I_2^u = \langle b^2 - b + 1, a^4 - 2a^2 + 2, u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ b - a \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b + a \\ b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} ba + b \\ b - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a \\ -b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^2 \\ ba - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2a^2 - 2 \\ a^3b - a^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4a^2 + 4b$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--------------------------------|
| c_1, c_2 | $(u^2 - u + 1)^4$ |
| c_3, c_6 | $(u^2 + u + 1)^4$ |
| c_4, c_{11} | $(u^4 - 2u^2 + 2)^2$ |
| c_5, c_{10} | $(u^4 + 2u^2 + 2)^2$ |
| c_7, c_8 | $(u + 1)^8$ |
| c_9 | $(u^2 + 2u + 2)^4$ |
| c_{12} | $(u - 1)^8$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|------------------------------------|
| c_1, c_2, c_3 c_6 | $(y^2 + y + 1)^4$ |
| c_4, c_{11} | $(y^2 - 2y + 2)^4$ |
| c_5, c_{10} | $(y^2 + 2y + 2)^4$ |
| c_7, c_8, c_{12} | $(y - 1)^8$ |
| c_9 | $(y^2 + 4)^4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -1.00000$ $a = 1.098680 + 0.455090I$ $b = 0.500000 + 0.866025I$ | $0.82247 + 1.63398I$ | $-2.00000 - 0.53590I$ |
| $u = -1.00000$ $a = 1.098680 + 0.455090I$ $b = 0.500000 - 0.866025I$ | $0.82247 + 5.69375I$ | $-2.00000 - 7.46410I$ |
| $u = -1.00000$ $a = 1.098680 - 0.455090I$ $b = 0.500000 + 0.866025I$ | $0.82247 - 5.69375I$ | $-2.00000 + 7.46410I$ |
| $u = -1.00000$ $a = 1.098680 - 0.455090I$ $b = 0.500000 - 0.866025I$ | $0.82247 - 1.63398I$ | $-2.00000 + 0.53590I$ |
| $u = -1.00000$ $a = -1.098680 + 0.455090I$ $b = 0.500000 + 0.866025I$ | $0.82247 - 5.69375I$ | $-2.00000 + 7.46410I$ |
| $u = -1.00000$ $a = -1.098680 + 0.455090I$ $b = 0.500000 - 0.866025I$ | $0.82247 - 1.63398I$ | $-2.00000 + 0.53590I$ |
| $u = -1.00000$ $a = -1.098680 - 0.455090I$ $b = 0.500000 + 0.866025I$ | $0.82247 + 1.63398I$ | $-2.00000 - 0.53590I$ |
| $u = -1.00000$ $a = -1.098680 - 0.455090I$ $b = 0.500000 - 0.866025I$ | $0.82247 + 5.69375I$ | $-2.00000 - 7.46410I$ |

$$\text{III. } I_3^u = \langle b^2 + b + 1, a^3, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ b - a \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b + a \\ b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -ba + b \\ b + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -a^2 \\ -ba + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -a^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $2a^2 - 4b - 8$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-------------------------------------|--------------------------------|
| c_1, c_3, c_6 | $(u^2 - u + 1)^3$ |
| c_2 | $(u^2 + u + 1)^3$ |
| c_4, c_5, c_9 c_{10}, c_{11} | u^6 |
| c_7, c_8 | $(u - 1)^6$ |
| c_{12} | $(u + 1)^6$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-------------------------------------|------------------------------------|
| c_1, c_2, c_3 c_6 | $(y^2 + y + 1)^3$ |
| c_4, c_5, c_9 c_{10}, c_{11} | y^6 |
| c_7, c_8, c_{12} | $(y - 1)^6$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 1.00000$ $a = 0$ $b = -0.500000 + 0.866025I$ | $-1.64493 + 2.02988I$ | $-6.00000 - 3.46410I$ |
| $u = 1.00000$ $a = 0$ $b = -0.500000 + 0.866025I$ | $-1.64493 + 2.02988I$ | $-6.00000 - 3.46410I$ |
| $u = 1.00000$ $a = 0$ $b = -0.500000 + 0.866025I$ | $-1.64493 + 2.02988I$ | $-6.00000 - 3.46410I$ |
| $u = 1.00000$ $a = 0$ $b = -0.500000 - 0.866025I$ | $-1.64493 - 2.02988I$ | $-6.00000 + 3.46410I$ |
| $u = 1.00000$ $a = 0$ $b = -0.500000 - 0.866025I$ | $-1.64493 - 2.02988I$ | $-6.00000 + 3.46410I$ |
| $u = 1.00000$ $a = 0$ $b = -0.500000 - 0.866025I$ | $-1.64493 - 2.02988I$ | $-6.00000 + 3.46410I$ |

IV. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $((u^2 - u + 1)^7)(u^{107} + 54u^{106} + \dots - 8u - 1)$ |
| c_2 | $((u^2 - u + 1)^4)(u^2 + u + 1)^3(u^{107} - 2u^{106} + \dots + 2u - 1)$ |
| c_3 | $((u^2 - u + 1)^3)(u^2 + u + 1)^4(u^{107} + 2u^{106} + \dots - 188610u - 36209)$ |
| c_4 | $u^6(u^4 - 2u^2 + 2)^2(u^{107} + u^{106} + \dots + 3876u + 3764)$ |
| c_5, c_{10} | $u^6(u^4 + 2u^2 + 2)^2(u^{107} - u^{106} + \dots + 4u + 4)$ |
| c_6 | $((u^2 - u + 1)^3)(u^2 + u + 1)^4(u^{107} - 2u^{106} + \dots + 2u - 1)$ |
| c_7, c_8 | $((u - 1)^6)(u + 1)^8(u^{107} + 3u^{106} + \dots - 111u + 13)$ |
| c_9 | $u^6(u^2 + 2u + 2)^4(u^{107} - 51u^{106} + \dots - 80u + 16)$ |
| c_{11} | $u^6(u^4 - 2u^2 + 2)^2(u^{107} - 5u^{106} + \dots - 692004u + 563884)$ |
| c_{12} | $((u - 1)^8)(u + 1)^6(u^{107} + 3u^{106} + \dots - 111u + 13)$ |

V. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------|--|
| c_1 | $((y^2 + y + 1)^7)(y^{107} + 6y^{106} + \dots + 40y - 1)$ |
| c_2, c_6 | $((y^2 + y + 1)^7)(y^{107} + 54y^{106} + \dots - 8y - 1)$ |
| c_3 | $((y^2 + y + 1)^7)(y^{107} - 42y^{106} + \dots + 2.26449 \times 10^9 y - 1.31109 \times 10^9)$ |
| c_4 | $y^6(y^2 - 2y + 2)^4(y^{107} - 21y^{106} + \dots + 4.24757 \times 10^8 y - 1.41677 \times 10^7)$ |
| c_5, c_{10} | $y^6(y^2 + 2y + 2)^4(y^{107} + 51y^{106} + \dots - 80y - 16)$ |
| c_7, c_8, c_{12} | $((y - 1)^{14})(y^{107} - 103y^{106} + \dots - 9207y - 169)$ |
| c_9 | $y^6(y^2 + 4)^4(y^{107} + 15y^{106} + \dots - 2304y - 256)$ |
| c_{11} | $y^6(y^2 - 2y + 2)^4$ $\cdot (y^{107} + 39y^{106} + \dots - 10755598905296y - 317965165456)$ |