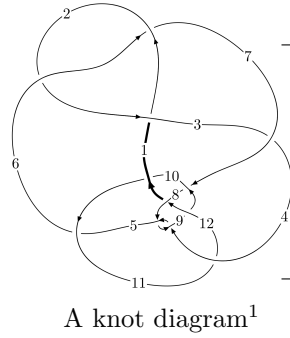
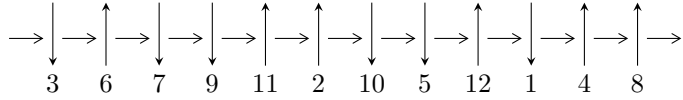


12a<sub>0222</sub> (K12a<sub>0222</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$2,6 \xrightarrow{c_2} 3 \xrightarrow{c_6} 7 \xrightarrow{c_3} 4,10 \xrightarrow{c_7} 8 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 5 \xrightarrow{c_{12}} 12 \xrightarrow{c_9} 9 \twoheadrightarrow c_4, c_8, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2u^{36} + u^{35} + \dots + b - 9, 3u^{36} - 3u^{35} + \dots + a + 1, u^{37} - 2u^{36} + \dots + 2u - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 37 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 2u^{36} + u^{35} + \dots + b - 9, 3u^{36} - 3u^{35} + \dots + a + 1, u^{37} - 2u^{36} + \dots + 2u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3u^{36} + 3u^{35} + \dots + 5u - 1 \\ -2u^{36} - u^{35} + \dots + u + 9 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -4u^{35} + 10u^{34} + \dots - 11u + 11 \\ -6u^{36} + 17u^{35} + \dots + 18u - 12 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 6u^{36} - 10u^{35} + \dots - 12u + 1 \\ 5u^{36} - 14u^{35} + \dots - 14u + 15 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -3u^{36} + 2u^{35} + \dots + 9u + 1 \\ 11u^{36} - 15u^{35} + \dots - 6u - 8 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2u^{36} - 3u^{35} + \dots - 2u + 1 \\ 3u^{36} - 7u^{35} + \dots - 6u + 10 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^{36} - u^{35} + \dots + u - 15 \\ 5u^{36} - 12u^{35} + \dots - 11u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$\begin{aligned} &= 50u^{36} - 53u^{35} + 513u^{34} - 472u^{33} + 2604u^{32} - 2103u^{31} + 8527u^{30} - 6002u^{29} + 19933u^{28} - \\ &12090u^{27} + 34843u^{26} - 17999u^{25} + 46330u^{24} - 20392u^{23} + 46429u^{22} - 18028u^{21} + 33354u^{20} - \\ &12865u^{19} + 14474u^{18} - 7621u^{17} + 482u^{16} - 3677u^{15} - 3764u^{14} - 1370u^{13} - 1746u^{12} - \\ &705u^{11} + 628u^{10} - 954u^9 + 992u^8 - 1056u^7 + 361u^6 - 706u^5 - 43u^4 - 276u^3 - 89u^2 - 49u - 37 \end{aligned}$$

(iv)  $u$ -Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{37} - 20u^{36} + \dots - 10u + 1$
$c_2$	$u^{37} - 2u^{36} + \dots + 2u - 1$
$c_3$	$u^{37} + 2u^{36} + \dots + 8u - 1$
$c_4$	$u^{37} + u^{36} + \dots - u - 1$
$c_5$	$u^{37} - 7u^{35} + \dots - 2u - 1$
$c_6$	$u^{37} + 2u^{36} + \dots + 2u + 1$
$c_7$	$u^{37} - 3u^{36} + \dots - 7u - 1$
$c_8$	$u^{37} - u^{36} + \dots - u + 1$
$c_9$	$u^{37} + 20u^{36} + \dots + 23u + 1$
$c_{10}$	$u^{37} - 17u^{36} + \dots + 23u - 1$
$c_{11}$	$u^{37} - 4u^{36} + \dots - 2u + 1$
$c_{12}$	$u^{37} + 7u^{36} + \dots + 3u - 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{37} + 4y^{36} + \dots - 10y - 1$
$c_2, c_6$	$y^{37} + 20y^{36} + \dots - 10y - 1$
$c_3$	$y^{37} - 6y^{36} + \dots + 8y - 1$
$c_4, c_8$	$y^{37} + 21y^{36} + \dots - 29y - 1$
$c_5$	$y^{37} - 14y^{36} + \dots - 12y - 1$
$c_7$	$y^{37} - 17y^{36} + \dots + 17y - 1$
$c_9$	$y^{37} + 4y^{36} + \dots + 13y - 1$
$c_{10}$	$y^{37} + 7y^{36} + \dots + 35y - 1$
$c_{11}$	$y^{37} + 4y^{36} + \dots + 24y - 1$
$c_{12}$	$y^{37} - 17y^{36} + \dots + 17y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.149884 + 0.975736I$ $a = -0.898991 + 0.581003I$ $b = -1.59695 + 0.70098I$	$-1.70560 + 1.29082I$	$-4.10550 - 4.13500I$
$u = -0.149884 - 0.975736I$ $a = -0.898991 - 0.581003I$ $b = -1.59695 - 0.70098I$	$-1.70560 - 1.29082I$	$-4.10550 + 4.13500I$
$u = -0.600365 + 0.704581I$ $a = 0.757124 + 0.641967I$ $b = -0.204265 + 0.747533I$	$0.834960 + 0.285553I$	$-0.434596 + 0.220919I$
$u = -0.600365 - 0.704581I$ $a = 0.757124 - 0.641967I$ $b = -0.204265 - 0.747533I$	$0.834960 - 0.285553I$	$-0.434596 - 0.220919I$
$u = -0.479565 + 0.990246I$ $a = 0.864069 + 0.151474I$ $b = -0.0946240 + 0.0662065I$	$-0.363148 - 0.677922I$	$0.56726 + 2.15135I$
$u = -0.479565 - 0.990246I$ $a = 0.864069 - 0.151474I$ $b = -0.0946240 - 0.0662065I$	$-0.363148 + 0.677922I$	$0.56726 - 2.15135I$
$u = -0.532442 + 0.982690I$ $a = -0.780782 - 0.630467I$ $b = -0.290116 - 1.327480I$	$-0.06388 - 4.77621I$	$-1.68090 + 5.53681I$
$u = -0.532442 - 0.982690I$ $a = -0.780782 + 0.630467I$ $b = -0.290116 + 1.327480I$	$-0.06388 + 4.77621I$	$-1.68090 - 5.53681I$
$u = -0.204733 + 0.857295I$ $a = -1.38015 + 0.70474I$ $b = 0.0824504 + 0.0328733I$	$-1.37034 - 3.02368I$	$-8.36272 + 7.29707I$
$u = -0.204733 - 0.857295I$ $a = -1.38015 - 0.70474I$ $b = 0.0824504 - 0.0328733I$	$-1.37034 + 3.02368I$	$-8.36272 - 7.29707I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.459092 + 1.035940I$ $a = 0.59291 + 1.57136I$ $b = -0.33683 + 2.07268I$	$2.24562 - 1.84888I$	$1.43556 + 1.62892I$
$u = 0.459092 - 1.035940I$ $a = 0.59291 - 1.57136I$ $b = -0.33683 - 2.07268I$	$2.24562 + 1.84888I$	$1.43556 - 1.62892I$
$u = 0.477509 + 1.033510I$ $a = -1.05702 + 2.06127I$ $b = -0.71022 + 2.96225I$	$2.36710 + 8.22059I$	$0.94025 - 9.93315I$
$u = 0.477509 - 1.033510I$ $a = -1.05702 - 2.06127I$ $b = -0.71022 - 2.96225I$	$2.36710 - 8.22059I$	$0.94025 + 9.93315I$
$u = 0.834958$ $a = -2.24679$ $b = 0.265283$	$-3.19671$	$32.4830$
$u = 0.325483 + 1.152650I$ $a = 0.15406 - 1.63598I$ $b = 0.69492 - 2.01501I$	$-4.68461 - 1.11526I$	$-3.13705 + 0.65063I$
$u = 0.325483 - 1.152650I$ $a = 0.15406 + 1.63598I$ $b = 0.69492 + 2.01501I$	$-4.68461 + 1.11526I$	$-3.13705 - 0.65063I$
$u = -0.500299 + 0.608166I$ $a = -0.471582 - 0.257960I$ $b = -0.12074 - 1.48951I$	$0.79654 - 3.35515I$	$4.80142 + 6.29346I$
$u = -0.500299 - 0.608166I$ $a = -0.471582 + 0.257960I$ $b = -0.12074 + 1.48951I$	$0.79654 + 3.35515I$	$4.80142 - 6.29346I$
$u = -0.743965 + 0.168516I$ $a = -1.330750 + 0.223235I$ $b = -0.105331 + 0.292541I$	$2.40521 + 5.56732I$	$3.26355 - 5.71144I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.743965 - 0.168516I$ $a = -1.330750 - 0.223235I$ $b = -0.105331 - 0.292541I$	$2.40521 - 5.56732I$	$3.26355 + 5.71144I$
$u = -0.314889 + 1.198120I$ $a = 0.053522 + 0.871053I$ $b = 0.06739 + 1.50640I$	$-1.73005 + 1.92880I$	$-3.35941 - 1.64027I$
$u = -0.314889 - 1.198120I$ $a = 0.053522 - 0.871053I$ $b = 0.06739 - 1.50640I$	$-1.73005 - 1.92880I$	$-3.35941 + 1.64027I$
$u = 0.714811 + 0.247691I$ $a = -2.06738 - 0.58596I$ $b = -0.967121 - 0.060412I$	$-0.67794 - 4.35069I$	$2.48170 + 5.54176I$
$u = 0.714811 - 0.247691I$ $a = -2.06738 + 0.58596I$ $b = -0.967121 + 0.060412I$	$-0.67794 + 4.35069I$	$2.48170 - 5.54176I$
$u = 0.533806 + 1.137330I$ $a = -0.38517 - 2.11869I$ $b = -0.58596 - 2.85980I$	$-3.23500 + 9.09894I$	$0. - 9.05167I$
$u = 0.533806 - 1.137330I$ $a = -0.38517 + 2.11869I$ $b = -0.58596 + 2.85980I$	$-3.23500 - 9.09894I$	$0. + 9.05167I$
$u = -0.521067 + 1.151720I$ $a = -0.140342 + 1.155190I$ $b = 0.15772 + 1.99777I$	$-0.38678 - 10.27070I$	$0. + 8.69635I$
$u = -0.521067 - 1.151720I$ $a = -0.140342 - 1.155190I$ $b = 0.15772 - 1.99777I$	$-0.38678 + 10.27070I$	$0. - 8.69635I$
$u = 0.897315 + 0.915050I$ $a = -0.059712 - 0.132929I$ $b = -0.232633 + 0.073399I$	$7.99878 + 3.29456I$	$-79.2024 - 47.4542I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.897315 - 0.915050I$ $a = -0.059712 + 0.132929I$ $b = -0.232633 - 0.073399I$	$7.99878 - 3.29456I$	$-79.2024 + 47.4542I$
$u = 0.404936 + 0.589401I$ $a = 1.90809 - 1.55602I$ $b = 0.60872 - 1.28187I$	$3.85891 - 4.38520I$	$4.22215 + 3.53032I$
$u = 0.404936 - 0.589401I$ $a = 1.90809 + 1.55602I$ $b = 0.60872 + 1.28187I$	$3.85891 + 4.38520I$	$4.22215 - 3.53032I$
$u = 0.451703 + 1.222140I$ $a = 0.26811 - 1.73234I$ $b = 0.44350 - 3.82544I$	$-6.86605 + 4.55927I$	$40.6626 - 31.2987I$
$u = 0.451703 - 1.222140I$ $a = 0.26811 + 1.73234I$ $b = 0.44350 + 3.82544I$	$-6.86605 - 4.55927I$	$40.6626 + 31.2987I$
$u = 0.365073 + 0.561552I$ $a = 1.097390 - 0.689191I$ $b = 1.05744 + 0.96070I$	$3.81957 + 5.52202I$	$4.99553 - 7.13279I$
$u = 0.365073 - 0.561552I$ $a = 1.097390 + 0.689191I$ $b = 1.05744 - 0.96070I$	$3.81957 - 5.52202I$	$4.99553 + 7.13279I$

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^{37} - 20u^{36} + \dots - 10u + 1$
$c_2$	$u^{37} - 2u^{36} + \dots + 2u - 1$
$c_3$	$u^{37} + 2u^{36} + \dots + 8u - 1$
$c_4$	$u^{37} + u^{36} + \dots - u - 1$
$c_5$	$u^{37} - 7u^{35} + \dots - 2u - 1$
$c_6$	$u^{37} + 2u^{36} + \dots + 2u + 1$
$c_7$	$u^{37} - 3u^{36} + \dots - 7u - 1$
$c_8$	$u^{37} - u^{36} + \dots - u + 1$
$c_9$	$u^{37} + 20u^{36} + \dots + 23u + 1$
$c_{10}$	$u^{37} - 17u^{36} + \dots + 23u - 1$
$c_{11}$	$u^{37} - 4u^{36} + \dots - 2u + 1$
$c_{12}$	$u^{37} + 7u^{36} + \dots + 3u - 1$

### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{37} + 4y^{36} + \dots - 10y - 1$
$c_2, c_6$	$y^{37} + 20y^{36} + \dots - 10y - 1$
$c_3$	$y^{37} - 6y^{36} + \dots + 8y - 1$
$c_4, c_8$	$y^{37} + 21y^{36} + \dots - 29y - 1$
$c_5$	$y^{37} - 14y^{36} + \dots - 12y - 1$
$c_7$	$y^{37} - 17y^{36} + \dots + 17y - 1$
$c_9$	$y^{37} + 4y^{36} + \dots + 13y - 1$
$c_{10}$	$y^{37} + 7y^{36} + \dots + 35y - 1$
$c_{11}$	$y^{37} + 4y^{36} + \dots + 24y - 1$
$c_{12}$	$y^{37} - 17y^{36} + \dots + 17y - 1$