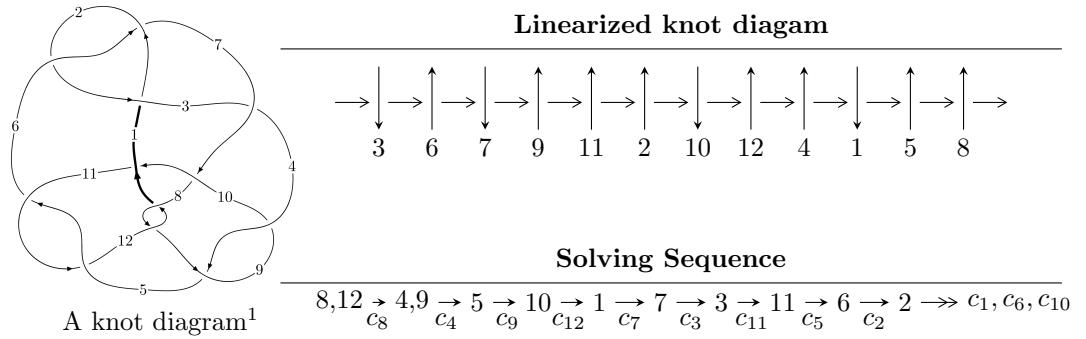


$$12a_{0223} \ (K12a_{0223})$$



Ideals for irreducible components² of X_{par}

$$\begin{aligned} I_1^u &= \langle 769u^{45} + 22195u^{44} + \cdots + 2048b + 18618368, -1645u^{45} - 50133u^{44} + \cdots + 8192a - 21766144, \\ &\quad u^{46} + 29u^{45} + \cdots + 172032u + 8192 \rangle \\ I_2^u &= \langle -5.15204 \times 10^{18}a^{19}u^2 - 9.61919 \times 10^{18}a^{18}u^2 + \cdots - 5.70417 \times 10^{21}a - 2.02099 \times 10^{21}, \\ &\quad - 2a^{19}u^2 - 5a^{18}u^2 + \cdots + 389a + 155, u^3 - u^2 + 2u - 1 \rangle \\ I_3^u &= \langle 4u^{29} + u^{28} + \cdots + b + 33, -29u^{29} + 70u^{28} + \cdots + 2a - 55, u^{30} - 2u^{29} + \cdots + u + 2 \rangle \\ I_4^u &= \langle 67a^5u^2 + 102a^4u^2 + \cdots + 362a + 422, -2a^4u^2 - 2a^3u^2 + \cdots - 11a + 1, u^3 - u^2 + 2u - 1 \rangle \end{aligned}$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 154 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILS/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 769u^{45} + 22195u^{44} + \dots + 2048b + 18618368, -1645u^{45} - 5.01 \times 10^4 u^{44} + \dots + 8192a - 2.18 \times 10^7, u^{46} + 29u^{45} + \dots + 172032u + 8192 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.200806u^{45} + 6.11975u^{44} + \dots + 46599.5u + 2657 \\ -0.375488u^{45} - 10.8374u^{44} + \dots - 180404u - 9091 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1.40613u^{45} - 39.1708u^{44} + \dots - 186438.u - 8862 \\ -0.296387u^{45} - 7.36377u^{44} + \dots + 31888u + 1645 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{8192}u^{45} + \frac{119}{8192}u^{44} + \dots + 933u + 46 \\ 0.505615u^{45} + 14.1682u^{44} + \dots + 82866u + 4141 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.274048u^{45} - 7.68079u^{44} + \dots - 42145.5u - 2100 \\ 0.982910u^{45} + 27.7881u^{44} + \dots + 203839u + 10297 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2.30249u^{45} - 65.0942u^{44} + \dots - 648664.u - 33111 \\ 1.45679u^{45} + 41.2253u^{44} + \dots + 186450u + 9592 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.494507u^{45} - 13.8463u^{44} + \dots - 81908u - 4096 \\ \frac{45}{4096}u^{45} + \frac{1259}{4096}u^{44} + \dots + 25u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2.72314u^{45} - 76.9080u^{44} + \dots - 541748.u - 26895 \\ 0.812256u^{45} + 23.5637u^{44} + \dots + 155986u + 7758 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -5.37744u^{45} - 152.656u^{44} + \dots - 1.53361 \times 10^6 u - 79260.5 \\ 1.09839u^{45} + 31.0549u^{44} + \dots + 140452.u + 7392 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-\frac{5013}{1024}u^{45} - \frac{144727}{1024}u^{44} + \dots - 1843566u - 96850$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|---|
| c_1 | $u^{46} + 23u^{45} + \cdots + 160u + 64$ |
| c_2, c_6 | $u^{46} - 9u^{45} + \cdots - 80u + 8$ |
| c_3 | $u^{46} + 9u^{45} + \cdots + 48000u + 8768$ |
| c_4, c_5, c_9 c_{11} | $u^{46} + 22u^{44} + \cdots + 2u + 1$ |
| c_7, c_{10} | $u^{46} - 3u^{45} + \cdots + 15u + 1$ |
| c_8, c_{12} | $u^{46} - 29u^{45} + \cdots - 172032u + 8192$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $y^{46} + 3y^{45} + \cdots + 34304y + 4096$ |
| c_2, c_6 | $y^{46} + 23y^{45} + \cdots + 160y + 64$ |
| c_3 | $y^{46} - 17y^{45} + \cdots + 657339392y + 76877824$ |
| c_4, c_5, c_9 c_{11} | $y^{46} + 44y^{45} + \cdots + 2y + 1$ |
| c_7, c_{10} | $y^{46} - 21y^{45} + \cdots - 131y + 1$ |
| c_8, c_{12} | $y^{46} + 23y^{45} + \cdots - 301989888y + 67108864$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------------------------------|---------------------------------------|------------|
| $u = -0.799771 + 0.573925I$ | | |
| $a = 0.364393 + 0.335556I$ | $0.23982 - 5.32921I$ | 0 |
| $b = -0.066790 - 0.489318I$ | | |
| $u = -0.799771 - 0.573925I$ | | |
| $a = 0.364393 - 0.335556I$ | $0.23982 + 5.32921I$ | 0 |
| $b = -0.066790 + 0.489318I$ | | |
| $u = 0.893801 + 0.251608I$ | | |
| $a = 0.044626 + 1.229910I$ | $1.15969 + 2.64455I$ | 0 |
| $b = 0.58367 - 1.51957I$ | | |
| $u = 0.893801 - 0.251608I$ | | |
| $a = 0.044626 - 1.229910I$ | $1.15969 - 2.64455I$ | 0 |
| $b = 0.58367 + 1.51957I$ | | |
| $u = -0.512458 + 0.963987I$ | | |
| $a = -0.430313 + 0.180490I$ | $0.14368 - 3.22065I$ | 0 |
| $b = -0.0655666 - 0.0544458I$ | | |
| $u = -0.512458 - 0.963987I$ | | |
| $a = -0.430313 - 0.180490I$ | $0.14368 + 3.22065I$ | 0 |
| $b = -0.0655666 + 0.0544458I$ | | |
| $u = -0.388129 + 1.023260I$ | | |
| $a = -0.426674 + 0.589584I$ | $-1.19630 - 3.09642I$ | 0 |
| $b = -0.183361 + 0.160958I$ | | |
| $u = -0.388129 - 1.023260I$ | | |
| $a = -0.426674 - 0.589584I$ | $-1.19630 + 3.09642I$ | 0 |
| $b = -0.183361 - 0.160958I$ | | |
| $u = -0.324185 + 1.064380I$ | | |
| $a = 0.399633 - 0.786327I$ | $-4.51131 + 0.55103I$ | 0 |
| $b = 0.197166 - 0.347962I$ | | |
| $u = -0.324185 - 1.064380I$ | | |
| $a = 0.399633 + 0.786327I$ | $-4.51131 - 0.55103I$ | 0 |
| $b = 0.197166 + 0.347962I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.636420 + 0.928507I$ | | |
| $a = 0.487473 + 0.128530I$ | $-0.796799 + 0.099834I$ | 0 |
| $b = -0.118282 + 0.098125I$ | | |
| $u = -0.636420 - 0.928507I$ | | |
| $a = 0.487473 - 0.128530I$ | $-0.796799 - 0.099834I$ | 0 |
| $b = -0.118282 - 0.098125I$ | | |
| $u = -0.400449 + 1.071460I$ | | |
| $a = 0.563394 - 0.645136I$ | $-4.04848 - 7.39004I$ | 0 |
| $b = 0.312197 - 0.165596I$ | | |
| $u = -0.400449 - 1.071460I$ | | |
| $a = 0.563394 + 0.645136I$ | $-4.04848 + 7.39004I$ | 0 |
| $b = 0.312197 + 0.165596I$ | | |
| $u = -0.065239 + 0.801819I$ | | |
| $a = 0.118295 + 0.879729I$ | $-1.90599 - 1.35920I$ | 0 |
| $b = 0.403205 + 0.174145I$ | | |
| $u = -0.065239 - 0.801819I$ | | |
| $a = 0.118295 - 0.879729I$ | $-1.90599 + 1.35920I$ | 0 |
| $b = 0.403205 - 0.174145I$ | | |
| $u = -0.636988 + 0.468513I$ | | |
| $a = -0.399061 - 0.335733I$ | $1.55277 - 1.12061I$ | 0 |
| $b = -0.186385 + 0.345366I$ | | |
| $u = -0.636988 - 0.468513I$ | | |
| $a = -0.399061 + 0.335733I$ | $1.55277 + 1.12061I$ | 0 |
| $b = -0.186385 - 0.345366I$ | | |
| $u = -1.293830 + 0.240209I$ | | |
| $a = -0.125234 - 0.391120I$ | $-9.2090 - 11.8951I$ | 0 |
| $b = 0.17398 + 1.95216I$ | | |
| $u = -1.293830 - 0.240209I$ | | |
| $a = -0.125234 + 0.391120I$ | $-9.2090 + 11.8951I$ | 0 |
| $b = 0.17398 - 1.95216I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------|
| $u = -1.343470 + 0.254073I$ | | |
| $a = 0.121901 + 0.415510I$ | $-6.15188 - 6.52811I$ | 0 |
| $b = -0.26873 - 2.00701I$ | | |
| $u = -1.343470 - 0.254073I$ | | |
| $a = 0.121901 - 0.415510I$ | $-6.15188 + 6.52811I$ | 0 |
| $b = -0.26873 + 2.00701I$ | | |
| $u = -1.374360 + 0.172869I$ | | |
| $a = -0.081685 - 0.416558I$ | $-11.06560 - 2.43248I$ | 0 |
| $b = 0.18781 + 2.15232I$ | | |
| $u = -1.374360 - 0.172869I$ | | |
| $a = -0.081685 + 0.416558I$ | $-11.06560 + 2.43248I$ | 0 |
| $b = 0.18781 - 2.15232I$ | | |
| $u = -0.597343 + 0.091283I$ | | |
| $a = 0.532629 + 0.097217I$ | $-1.30110 + 3.67557I$ | 0 |
| $b = 0.581340 - 0.128594I$ | | |
| $u = -0.597343 - 0.091283I$ | | |
| $a = 0.532629 - 0.097217I$ | $-1.30110 - 3.67557I$ | 0 |
| $b = 0.581340 + 0.128594I$ | | |
| $u = -0.474804 + 0.228895I$ | | |
| $a = -0.606283 - 0.281711I$ | $1.036500 - 0.329167I$ | $9.79847 + 0.I$ |
| $b = -0.394151 + 0.170715I$ | | |
| $u = -0.474804 - 0.228895I$ | | |
| $a = -0.606283 + 0.281711I$ | $1.036500 + 0.329167I$ | $9.79847 + 0.I$ |
| $b = -0.394151 - 0.170715I$ | | |
| $u = -0.50438 + 1.51379I$ | | |
| $a = 0.54133 + 1.59621I$ | $-14.8126 - 18.1675I$ | 0 |
| $b = -0.81797 + 2.47099I$ | | |
| $u = -0.50438 - 1.51379I$ | | |
| $a = 0.54133 - 1.59621I$ | $-14.8126 + 18.1675I$ | 0 |
| $b = -0.81797 - 2.47099I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.50748 + 1.52626I$ | $-11.8567 - 12.9387I$ | 0 |
| $a = -0.53256 - 1.55965I$ | | |
| $b = 0.81772 - 2.47947I$ | | |
| $u = -0.50748 - 1.52626I$ | $-11.8567 + 12.9387I$ | 0 |
| $a = -0.53256 + 1.55965I$ | | |
| $b = 0.81772 + 2.47947I$ | | |
| $u = -0.52920 + 1.52540I$ | $-16.5662 - 9.0443I$ | 0 |
| $a = 0.58432 + 1.52852I$ | | |
| $b = -0.83326 + 2.47604I$ | | |
| $u = -0.52920 - 1.52540I$ | $-16.5662 + 9.0443I$ | 0 |
| $a = 0.58432 - 1.52852I$ | | |
| $b = -0.83326 - 2.47604I$ | | |
| $u = -0.49940 + 1.60831I$ | $-7.89455 - 10.71430I$ | 0 |
| $a = -0.43900 - 1.41526I$ | | |
| $b = 0.80667 - 2.59864I$ | | |
| $u = -0.49940 - 1.60831I$ | $-7.89455 + 10.71430I$ | 0 |
| $a = -0.43900 + 1.41526I$ | | |
| $b = 0.80667 + 2.59864I$ | | |
| $u = -0.66884 + 1.57562I$ | $-15.5284 - 5.1709I$ | 0 |
| $a = -0.632758 - 1.225720I$ | | |
| $b = 1.10252 - 2.37452I$ | | |
| $u = -0.66884 - 1.57562I$ | $-15.5284 + 5.1709I$ | 0 |
| $a = -0.632758 + 1.225720I$ | | |
| $b = 1.10252 + 2.37452I$ | | |
| $u = -0.79157 + 1.55497I$ | $-12.99410 + 4.22647I$ | 0 |
| $a = -0.635987 - 1.056940I$ | | |
| $b = 1.37706 - 2.08974I$ | | |
| $u = -0.79157 - 1.55497I$ | $-12.99410 - 4.22647I$ | 0 |
| $a = -0.635987 + 1.056940I$ | | |
| $b = 1.37706 + 2.08974I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------------|---------------------------------------|------------|
| $u = -0.53627 + 1.66484I$ | | |
| $a = 0.439767 + 1.323980I$ | $-7.40589 - 5.18365I$ | 0 |
| $b = -0.90517 + 2.71062I$ | | |
| $u = -0.53627 - 1.66484I$ | | |
| $a = 0.439767 - 1.323980I$ | $-7.40589 + 5.18365I$ | 0 |
| $b = -0.90517 - 2.71062I$ | | |
| $u = -1.75426 + 0.12015I$ | | |
| $a = 0.035438 + 0.550581I$ | $-1.59220 - 3.11488I$ | 0 |
| $b = -0.30850 - 2.94126I$ | | |
| $u = -1.75426 - 0.12015I$ | | |
| $a = 0.035438 - 0.550581I$ | $-1.59220 + 3.11488I$ | 0 |
| $b = -0.30850 + 2.94126I$ | | |
| $u = -0.75494 + 1.61988I$ | | |
| $a = 0.576352 + 1.115620I$ | $-10.17990 - 1.41035I$ | 0 |
| $b = -1.39518 + 2.33963I$ | | |
| $u = -0.75494 - 1.61988I$ | | |
| $a = 0.576352 - 1.115620I$ | $-10.17990 + 1.41035I$ | 0 |
| $b = -1.39518 - 2.33963I$ | | |

$$\text{II. } I_2^u = \langle -5.15 \times 10^{18} a^{19} u^2 - 9.62 \times 10^{18} a^{18} u^2 + \dots - 5.70 \times 10^{21} a - 2.02 \times 10^{21}, -2a^{19}u^2 - 5a^{18}u^2 + \dots + 389a + 155, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} a \\ 0.00624366a^{19}u^2 + 0.0116573a^{18}u^2 + \dots + 6.91278a + 2.44921 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.00624366a^{19}u^2 + 0.0116573a^{18}u^2 + \dots + 7.91278a + 2.44921 \\ 0.00589498a^{19}u^2 + 0.00970531a^{18}u^2 + \dots + 4.98347a + 1.02435 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.0222268a^{19}u^2 + 0.0385989a^{18}u^2 + \dots - 1.52939a + 3.00132 \\ \frac{1}{5}a^2u^2 + \frac{2}{5}u^2 + \dots + \frac{4}{5}a^2 + \frac{8}{5} \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.0255730a^{19}u^2 - 0.0386005a^{18}u^2 + \dots - 4.61675a - 5.17283 \\ -0.280000a^4u^2 - 1.12000a^2u^2 + \dots - 2.08000a^2 - 2.08000 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.00811715a^{19}u^2 - 0.0185732a^{18}u^2 + \dots + 2.73016a + 0.0448430 \\ 0.00840339a^{19}u^2 - 0.0245270a^{18}u^2 + \dots - 2.51095a - 3.00433 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0300738a^{19}u^2 + 0.0495554a^{18}u^2 + \dots - 1.67353a + 3.99775 \\ -0.00784700a^{19}u^2 + 0.0109564a^{18}u^2 + \dots - 0.144142a + 2.59644 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.0116152a^{19}u^2 - 0.0203774a^{18}u^2 + \dots - 6.28641a - 7.47013 \\ \frac{1}{5}a^3u^2 + \frac{2}{5}u^2a + \dots - \frac{1}{5}a^3 - \frac{2}{5}a \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.00249033a^{19}u^2 + 0.0238687a^{18}u^2 + \dots + 12.0177a + 7.16327 \\ -0.00531474a^{19}u^2 + 0.0136319a^{18}u^2 + \dots - 0.592585a + 0.0240514 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{21229213881407898776}{825162189597541015625}a^{19}u^2 - \frac{99261565058430515616}{825162189597541015625}a^{18}u^2 + \dots - \frac{4819014882020878281412}{825162189597541015625}a - \frac{14886800916766629307678}{825162189597541015625}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|---|
| c_1 | $(u^{10} + 5u^9 + 13u^8 + 19u^7 + 17u^6 + 7u^5 - 2u^3 + u^2 + 2u + 1)^6$ |
| c_2, c_6 | $(u^{10} + u^9 + 3u^8 + 3u^7 + 5u^6 + 5u^5 + 4u^4 + 4u^3 + 3u^2 + 2u + 1)^6$ |
| c_3 | $(u^{10} + 2u^9 - u^8 - 5u^7 - 3u^6 + 4u^5 + 12u^4 + 13u^3 + 5u^2 + u + 2)^6$ |
| c_4, c_5, c_9 c_{11} | $u^{60} + u^{59} + \dots - 626u + 3383$ |
| c_7, c_{10} | $u^{60} - 11u^{59} + \dots - 53768u + 6593$ |
| c_8, c_{12} | $(u^3 + u^2 + 2u + 1)^{20}$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|---|
| c_1 | $(y^{10} + y^9 + 13y^8 + 11y^7 + 45y^6 + 35y^5 + 12y^4 + 2y^3 + 9y^2 - 2y + 1)^6$ |
| c_2, c_6 | $(y^{10} + 5y^9 + 13y^8 + 19y^7 + 17y^6 + 7y^5 - 2y^3 + y^2 + 2y + 1)^6$ |
| c_3 | $(y^{10} - 6y^9 + \dots + 19y + 4)^6$ |
| c_4, c_5, c_9 c_{11} | $y^{60} + 55y^{59} + \dots - 363644884y + 11444689$ |
| c_7, c_{10} | $y^{60} - 17y^{59} + \dots + 11794588y + 43467649$ |
| c_8, c_{12} | $(y^3 + 3y^2 + 2y - 1)^{20}$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-------------------------|
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.753681 - 0.475251I$ | $-8.34008 - 5.45819I$ | $-3.68536 + 3.16937I$ |
| $b = -1.78844 - 0.37957I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.546194 - 0.474142I$ | $-8.34008 + 11.11440I$ | $-3.68536 - 9.12826I$ |
| $b = 0.403352 - 0.051960I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.574901 + 0.335993I$ | $-5.54533 - 0.65027I$ | $-0.314721 - 0.184301I$ |
| $b = 1.57210 + 0.28523I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.285753 + 1.351650I$ | $-8.40699 + 4.05981I$ | $-4.41153 - 8.42852I$ |
| $b = -0.543510 + 1.072600I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.428457 + 0.424908I$ | $-5.54533 + 6.30651I$ | $-0.31472 - 5.77459I$ |
| $b = -0.499901 + 0.057312I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.91047 - 1.17250I$ | $-8.40699 + 1.59643I$ | $-4.41153 + 2.46963I$ |
| $b = 1.24405 - 1.35425I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.46161 - 1.63922I$ | $-8.34008 - 5.45819I$ | $-3.68536 + 3.16937I$ |
| $b = -0.57315 - 1.54354I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.37848 + 1.70556I$ | $-5.54533 - 0.65027I$ | $-0.314721 - 0.184301I$ |
| $b = 0.61872 + 1.65480I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.249866 + 0.028485I$ | $-3.02174 + 5.13818I$ | $1.35393 - 6.50078I$ |
| $b = -0.749845 - 0.180326I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.12162 - 1.79476I$ | $-12.8356 + 6.9740I$ | $-8.49110 - 6.95545I$ |
| $b = 0.097878 - 1.186300I$ | | |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.065417 + 0.174229I$ | $-3.02174 + 0.51807I$ | $1.35393 + 0.54188I$ |
| $b = 0.948493 + 0.296744I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.22681 - 1.88180I$ | $-12.83560 - 1.31773I$ | $-8.49110 + 0.99655I$ |
| $b = 0.054342 - 1.297810I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.50665 + 1.84019I$ | $-8.40699 + 1.59643I$ | $-4.41153 + 2.46963I$ |
| $b = -0.17308 + 1.65844I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.09218 + 1.91765I$ | $-3.02174 + 0.51807I$ | $1.35393 + 0.54188I$ |
| $b = 0.92173 + 2.04017I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.83452 - 1.90639I$ | $-8.40699 + 4.05981I$ | $-4.41153 - 8.42852I$ |
| $b = 0.57676 - 2.18544I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.08612 - 2.09921I$ | $-3.02174 + 5.13818I$ | $1.35393 - 6.50078I$ |
| $b = -0.91359 - 2.30802I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -1.44111 + 1.58193I$ | $-12.83560 - 1.31773I$ | $-8.49110 + 0.99655I$ |
| $b = -1.61358 + 2.16592I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -1.37238 + 1.80234I$ | $-12.8356 + 6.9740I$ | $-8.49110 - 6.95545I$ |
| $b = -1.39612 + 2.41080I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.23996 - 2.36391I$ | $-5.54533 + 6.30651I$ | $-0.31472 - 5.77459I$ |
| $b = -0.68840 - 2.73151I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.23228 + 2.46167I$ | $-8.34008 + 11.11440I$ | $-3.68536 - 9.12826I$ |
| $b = 0.71727 + 2.88385I$ | | |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-------------------------|
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.753681 + 0.475251I$ | $-8.34008 + 5.45819I$ | $-3.68536 - 3.16937I$ |
| $b = -1.78844 + 0.37957I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.546194 + 0.474142I$ | $-8.34008 - 11.11440I$ | $-3.68536 + 9.12826I$ |
| $b = 0.403352 + 0.051960I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.574901 - 0.335993I$ | $-5.54533 + 0.65027I$ | $-0.314721 + 0.184301I$ |
| $b = 1.57210 - 0.28523I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.285753 - 1.351650I$ | $-8.40699 - 4.05981I$ | $-4.41153 + 8.42852I$ |
| $b = -0.543510 - 1.072600I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.428457 - 0.424908I$ | $-5.54533 - 6.30651I$ | $-0.31472 + 5.77459I$ |
| $b = -0.499901 - 0.057312I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.91047 + 1.17250I$ | $-8.40699 - 1.59643I$ | $-4.41153 - 2.46963I$ |
| $b = 1.24405 + 1.35425I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.46161 + 1.63922I$ | $-8.34008 + 5.45819I$ | $-3.68536 - 3.16937I$ |
| $b = -0.57315 + 1.54354I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.37848 - 1.70556I$ | $-5.54533 + 0.65027I$ | $-0.314721 + 0.184301I$ |
| $b = 0.61872 - 1.65480I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.249866 - 0.028485I$ | $-3.02174 - 5.13818I$ | $1.35393 + 6.50078I$ |
| $b = -0.749845 + 0.180326I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.12162 + 1.79476I$ | $-12.8356 - 6.9740I$ | $-8.49110 + 6.95545I$ |
| $b = 0.097878 + 1.186300I$ | | |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.065417 - 0.174229I$ | $-3.02174 - 0.51807I$ | $1.35393 - 0.54188I$ |
| $b = 0.948493 - 0.296744I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.22681 + 1.88180I$ | $-12.83560 + 1.31773I$ | $-8.49110 - 0.99655I$ |
| $b = 0.054342 + 1.297810I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.50665 - 1.84019I$ | $-8.40699 - 1.59643I$ | $-4.41153 - 2.46963I$ |
| $b = -0.17308 - 1.65844I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.09218 - 1.91765I$ | $-3.02174 - 0.51807I$ | $1.35393 - 0.54188I$ |
| $b = 0.92173 - 2.04017I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.83452 + 1.90639I$ | $-8.40699 - 4.05981I$ | $-4.41153 + 8.42852I$ |
| $b = 0.57676 + 2.18544I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.08612 + 2.09921I$ | $-3.02174 - 5.13818I$ | $1.35393 + 6.50078I$ |
| $b = -0.91359 + 2.30802I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -1.44111 - 1.58193I$ | $-12.83560 + 1.31773I$ | $-8.49110 - 0.99655I$ |
| $b = -1.61358 - 2.16592I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -1.37238 - 1.80234I$ | $-12.8356 - 6.9740I$ | $-8.49110 + 6.95545I$ |
| $b = -1.39612 - 2.41080I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.23996 + 2.36391I$ | $-5.54533 - 6.30651I$ | $-0.31472 + 5.77459I$ |
| $b = -0.68840 + 2.73151I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.23228 - 2.46167I$ | $-8.34008 - 11.11440I$ | $-3.68536 + 9.12826I$ |
| $b = 0.71727 - 2.88385I$ | | |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.569840$ | | |
| $a = -0.691753 + 0.900274I$ | $-1.40774 + 3.47839I$ | $6.21454 - 2.79515I$ |
| $b = -0.198932 - 1.368010I$ | | |
| $u = 0.569840$ | | |
| $a = -0.691753 - 0.900274I$ | $-1.40774 - 3.47839I$ | $6.21454 + 2.79515I$ |
| $b = -0.198932 + 1.368010I$ | | |
| $u = 0.569840$ | | |
| $a = 0.833453 + 0.905620I$ | $-4.20250 - 8.28632I$ | $2.84391 + 6.14881I$ |
| $b = 0.22342 - 1.43186I$ | | |
| $u = 0.569840$ | | |
| $a = 0.833453 - 0.905620I$ | $-4.20250 + 8.28632I$ | $2.84391 - 6.14881I$ |
| $b = 0.22342 + 1.43186I$ | | |
| $u = 0.569840$ | | |
| $a = 0.869132 + 0.956638I$ | $-8.69800 + 4.14585I$ | $-1.96183 - 3.97600I$ |
| $b = -0.535562 + 1.131840I$ | | |
| $u = 0.569840$ | | |
| $a = 0.869132 - 0.956638I$ | $-8.69800 - 4.14585I$ | $-1.96183 + 3.97600I$ |
| $b = -0.535562 - 1.131840I$ | | |
| $u = 0.569840$ | | |
| $a = -0.254094 + 1.301160I$ | $-4.26940 + 1.23169I$ | $2.11774 - 5.44908I$ |
| $b = 0.288722 + 0.604570I$ | | |
| $u = 0.569840$ | | |
| $a = -0.254094 - 1.301160I$ | $-4.26940 - 1.23169I$ | $2.11774 + 5.44908I$ |
| $b = 0.288722 - 0.604570I$ | | |
| $u = 0.569840$ | | |
| $a = -0.363696 + 1.279380I$ | $1.11584 + 2.31006I$ | $7.88320 - 3.52133I$ |
| $b = -0.262040 - 1.092640I$ | | |
| $u = 0.569840$ | | |
| $a = -0.363696 - 1.279380I$ | $1.11584 - 2.31006I$ | $7.88320 + 3.52133I$ |
| $b = -0.262040 + 1.092640I$ | | |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.569840$ | | |
| $a = -0.389163 + 0.475675I$ | $-4.26940 - 1.23169I$ | $2.11774 + 5.44908I$ |
| $b = 0.153653 + 1.172260I$ | | |
| $u = 0.569840$ | | |
| $a = -0.389163 - 0.475675I$ | $-4.26940 + 1.23169I$ | $2.11774 - 5.44908I$ |
| $b = 0.153653 - 1.172260I$ | | |
| $u = 0.569840$ | | |
| $a = 0.795483 + 1.164250I$ | $-8.69800 - 4.14585I$ | $-1.96183 + 3.97600I$ |
| $b = -0.609211 + 0.989056I$ | | |
| $u = 0.569840$ | | |
| $a = 0.795483 - 1.164250I$ | $-8.69800 + 4.14585I$ | $-1.96183 - 3.97600I$ |
| $b = -0.609211 - 0.989056I$ | | |
| $u = 0.569840$ | | |
| $a = 0.24323 + 1.53155I$ | $1.11584 + 2.31006I$ | $7.88320 - 3.52133I$ |
| $b = 0.344886 - 0.840470I$ | | |
| $u = 0.569840$ | | |
| $a = 0.24323 - 1.53155I$ | $1.11584 - 2.31006I$ | $7.88320 + 3.52133I$ |
| $b = 0.344886 + 0.840470I$ | | |
| $u = 0.569840$ | | |
| $a = 0.10774 + 1.78772I$ | $-1.40774 + 3.47839I$ | $6.21454 - 2.79515I$ |
| $b = 0.600562 - 0.480557I$ | | |
| $u = 0.569840$ | | |
| $a = 0.10774 - 1.78772I$ | $-1.40774 - 3.47839I$ | $6.21454 + 2.79515I$ |
| $b = 0.600562 + 0.480557I$ | | |
| $u = 0.569840$ | | |
| $a = -0.11054 + 1.86439I$ | $-4.20250 - 8.28632I$ | $2.84391 + 6.14881I$ |
| $b = -0.720573 - 0.473098I$ | | |
| $u = 0.569840$ | | |
| $a = -0.11054 - 1.86439I$ | $-4.20250 + 8.28632I$ | $2.84391 - 6.14881I$ |
| $b = -0.720573 + 0.473098I$ | | |

$$\text{III. } I_3^u = \langle 4u^{29} + u^{28} + \dots + b + 33, -29u^{29} + 70u^{28} + \dots + 2a - 55, u^{30} - 2u^{29} + \dots + u + 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{29}{2}u^{29} - 35u^{28} + \dots + 58u + \frac{55}{2} \\ -4u^{29} - u^{28} + \dots + 19u - 33 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} \frac{21}{2}u^{29} - 25u^{28} + \dots + 54u + \frac{13}{2} \\ -6u^{29} + 12u^{28} + \dots + 13u - 29 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -\frac{3}{2}u^{29} + 2u^{28} + \dots - 12u - \frac{3}{2} \\ -u^{29} + 2u^{28} + \dots - 2u + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{1}{2}u^{29} + 3u^{28} + \dots + 17u + \frac{21}{2} \\ 2u^{29} - 2u^{28} + \dots + 8u + 3 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -\frac{3}{2}u^{29} + 10u^{28} + \dots - 4u + \frac{53}{2} \\ 4u^{29} - 2u^{28} + \dots - 3u + 37 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -\frac{3}{2}u^{29} + 3u^{28} + \dots - 10u + \frac{1}{2} \\ -u^{29} + 3u^{28} + \dots + 12u^2 + 3 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 15u^{29} - 31u^{28} + \dots + 33u + 19 \\ 8u^{29} - 28u^{28} + \dots + 50u - 40 \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{33}{2}u^{29} - 19u^{28} + \dots + 54u + \frac{159}{2} \\ 24u^{29} - 57u^{28} + \dots + 105u - 3 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -47u^{29} + 95u^{28} - 548u^{27} + 913u^{26} - 2523u^{25} + 3700u^{24} - \\ &5843u^{23} + 8328u^{22} - 6732u^{21} + 11019u^{20} - 2264u^{19} + 5985u^{18} + 726u^{17} - 9012u^{16} - \\ &9505u^{15} - 26913u^{14} - 30055u^{13} - 34426u^{12} - 40817u^{11} - 25858u^{10} - 31373u^9 - \\ &10806u^8 - 14162u^7 - 2007u^6 - 3834u^5 - 328u^4 - 894u^3 - 340u^2 - 176u - 76 \end{aligned}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---------------------------------------|
| c_1 | $u^{30} - 16u^{29} + \cdots - 8u + 1$ |
| c_2 | $u^{30} - 2u^{29} + \cdots - 2u + 1$ |
| c_3 | $u^{30} + 2u^{29} + \cdots + 9u + 2$ |
| c_4, c_{11} | $u^{30} + 17u^{28} + \cdots - u + 1$ |
| c_5, c_9 | $u^{30} + 17u^{28} + \cdots + u + 1$ |
| c_6 | $u^{30} + 2u^{29} + \cdots + 2u + 1$ |
| c_7, c_{10} | $u^{30} - 3u^{29} + \cdots - 10u + 1$ |
| c_8 | $u^{30} - 2u^{29} + \cdots + u + 2$ |
| c_{12} | $u^{30} + 2u^{29} + \cdots - u + 2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $y^{30} + 4y^{29} + \cdots - 12y + 1$ |
| c_2, c_6 | $y^{30} + 16y^{29} + \cdots + 8y + 1$ |
| c_3 | $y^{30} - 8y^{29} + \cdots + 51y + 4$ |
| c_4, c_5, c_9 c_{11} | $y^{30} + 34y^{29} + \cdots - 9y + 1$ |
| c_7, c_{10} | $y^{30} - 7y^{29} + \cdots - 30y + 1$ |
| c_8, c_{12} | $y^{30} + 20y^{29} + \cdots + 63y + 4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.954358 + 0.210669I$ | | |
| $a = -0.157797 + 1.396290I$ | $0.90437 - 2.79385I$ | $-11.1621 + 9.0861I$ |
| $b = -0.42289 - 1.97188I$ | | |
| $u = -0.954358 - 0.210669I$ | | |
| $a = -0.157797 - 1.396290I$ | $0.90437 + 2.79385I$ | $-11.1621 - 9.0861I$ |
| $b = -0.42289 + 1.97188I$ | | |
| $u = -0.487760 + 0.913151I$ | | |
| $a = 0.282967 + 0.414413I$ | $-0.262375 - 0.129830I$ | $7.66829 + 1.39620I$ |
| $b = -0.469527 + 0.371738I$ | | |
| $u = -0.487760 - 0.913151I$ | | |
| $a = 0.282967 - 0.414413I$ | $-0.262375 + 0.129830I$ | $7.66829 - 1.39620I$ |
| $b = -0.469527 - 0.371738I$ | | |
| $u = -0.452089 + 0.844145I$ | | |
| $a = -0.552166 - 0.021065I$ | $-0.00756 - 3.73651I$ | $0.40463 + 10.05332I$ |
| $b = 0.009729 - 0.587148I$ | | |
| $u = -0.452089 - 0.844145I$ | | |
| $a = -0.552166 + 0.021065I$ | $-0.00756 + 3.73651I$ | $0.40463 - 10.05332I$ |
| $b = 0.009729 + 0.587148I$ | | |
| $u = 0.395534 + 1.115610I$ | | |
| $a = 1.05638 - 1.22612I$ | $-11.11260 - 2.62022I$ | $-4.33545 + 2.54697I$ |
| $b = 0.257277 - 0.768700I$ | | |
| $u = 0.395534 - 1.115610I$ | | |
| $a = 1.05638 + 1.22612I$ | $-11.11260 + 2.62022I$ | $-4.33545 - 2.54697I$ |
| $b = 0.257277 + 0.768700I$ | | |
| $u = 0.282007 + 1.171250I$ | | |
| $a = 0.99630 - 1.51825I$ | $-11.60570 + 5.64781I$ | $-4.91183 - 3.78174I$ |
| $b = 0.609476 - 1.061230I$ | | |
| $u = 0.282007 - 1.171250I$ | | |
| $a = 0.99630 + 1.51825I$ | $-11.60570 - 5.64781I$ | $-4.91183 + 3.78174I$ |
| $b = 0.609476 + 1.061230I$ | | |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.194470 + 1.267770I$ | $-8.33239 + 3.05072I$ | $-3.41230 - 0.35327I$ |
| $a = -0.69601 + 1.67138I$ | | |
| $b = -0.75988 + 1.50055I$ | | |
| $u = 0.194470 - 1.267770I$ | $-8.33239 - 3.05072I$ | $-3.41230 + 0.35327I$ |
| $a = -0.69601 - 1.67138I$ | | |
| $b = -0.75988 - 1.50055I$ | | |
| $u = -0.220342 + 0.677642I$ | $-5.82568 - 8.71515I$ | $-4.10097 + 7.30655I$ |
| $a = 1.72214 - 0.32654I$ | | |
| $b = 0.274742 + 1.101150I$ | | |
| $u = -0.220342 - 0.677642I$ | $-5.82568 + 8.71515I$ | $-4.10097 - 7.30655I$ |
| $a = 1.72214 + 0.32654I$ | | |
| $b = 0.274742 - 1.101150I$ | | |
| $u = 0.374108 + 1.234240I$ | $-8.13358 + 1.89857I$ | $-60.10 - 0.703598I$ |
| $a = -0.84930 + 1.32789I$ | | |
| $b = -0.232711 + 1.180040I$ | | |
| $u = 0.374108 - 1.234240I$ | $-8.13358 - 1.89857I$ | $-60.10 + 0.703598I$ |
| $a = -0.84930 - 1.32789I$ | | |
| $b = -0.232711 - 1.180040I$ | | |
| $u = 0.113491 + 1.305880I$ | $-10.39040 + 0.41896I$ | $-6.15304 + 1.26264I$ |
| $a = 0.48876 - 1.74372I$ | | |
| $b = 0.90956 - 1.71662I$ | | |
| $u = 0.113491 - 1.305880I$ | $-10.39040 - 0.41896I$ | $-6.15304 - 1.26264I$ |
| $a = 0.48876 + 1.74372I$ | | |
| $b = 0.90956 + 1.71662I$ | | |
| $u = -0.265692 + 0.625254I$ | $-2.88017 - 3.92346I$ | $-1.21214 + 4.26144I$ |
| $a = -1.61215 + 0.54381I$ | | |
| $b = -0.279464 - 1.065660I$ | | |
| $u = -0.265692 - 0.625254I$ | $-2.88017 + 3.92346I$ | $-1.21214 - 4.26144I$ |
| $a = -1.61215 - 0.54381I$ | | |
| $b = -0.279464 + 1.065660I$ | | |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.05808 + 1.41627I$ | $-9.22090 + 7.68788I$ | $-4.49738 - 6.93831I$ |
| $a = 0.30999 - 1.58553I$ | | |
| $b = 0.92701 - 2.00489I$ | | |
| $u = 0.05808 - 1.41627I$ | $-9.22090 - 7.68788I$ | $-4.49738 + 6.93831I$ |
| $a = 0.30999 + 1.58553I$ | | |
| $b = 0.92701 + 2.00489I$ | | |
| $u = -0.160117 + 0.556209I$ | $-6.93501 - 0.20087I$ | $-6.34680 + 0.65586I$ |
| $a = 2.02259 - 0.64113I$ | | |
| $b = 0.298497 + 1.049780I$ | | |
| $u = -0.160117 - 0.556209I$ | $-6.93501 + 0.20087I$ | $-6.34680 - 0.65586I$ |
| $a = 2.02259 + 0.64113I$ | | |
| $b = 0.298497 - 1.049780I$ | | |
| $u = 0.17114 + 1.44043I$ | $-7.14969 + 3.03258I$ | $0. - 2.04340I$ |
| $a = -0.44043 + 1.48846I$ | | |
| $b = -0.63512 + 1.99041I$ | | |
| $u = 0.17114 - 1.44043I$ | $-7.14969 - 3.03258I$ | $0. + 2.04340I$ |
| $a = -0.44043 - 1.48846I$ | | |
| $b = -0.63512 - 1.99041I$ | | |
| $u = 0.446808 + 0.301559I$ | $-5.10854 - 0.65478I$ | $-7.03551 - 0.27211I$ |
| $a = -1.211930 - 0.717774I$ | | |
| $b = 0.006603 - 0.798556I$ | | |
| $u = 0.446808 - 0.301559I$ | $-5.10854 + 0.65478I$ | $-7.03551 + 0.27211I$ |
| $a = -1.211930 + 0.717774I$ | | |
| $b = 0.006603 + 0.798556I$ | | |
| $u = 1.50472 + 0.21618I$ | $-1.12126 + 2.86817I$ | 0 |
| $a = -0.109336 + 0.422908I$ | | |
| $b = 0.50671 - 2.07597I$ | | |
| $u = 1.50472 - 0.21618I$ | $-1.12126 - 2.86817I$ | 0 |
| $a = -0.109336 - 0.422908I$ | | |
| $b = 0.50671 + 2.07597I$ | | |

$$\text{IV. } I_4^u = \langle 67a^5u^2 + 102a^4u^2 + \cdots + 362a + 422, -2a^4u^2 - 2a^3u^2 + \cdots - 11a + 1, u^3 - u^2 + 2u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned}
a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_4 &= \begin{pmatrix} a \\ -0.116522a^5u^2 - 0.177391a^4u^2 + \cdots - 0.629565a - 0.733913 \end{pmatrix} \\
a_9 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\
a_5 &= \begin{pmatrix} -0.116522a^5u^2 - 0.177391a^4u^2 + \cdots + 0.370435a - 0.733913 \\ -0.147826a^5u^2 - 0.0608696a^4u^2 + \cdots - 1.84348a - 1.40870 \end{pmatrix} \\
a_{10} &= \begin{pmatrix} 0.177391a^5u^2 - 0.00695652a^4u^2 + \cdots + 0.212174a + 0.0104348 \\ \frac{1}{5}a^2u^2 + \frac{2}{5}u^2 + \cdots + \frac{4}{5}a^2 + \frac{8}{5} \end{pmatrix} \\
a_1 &= \begin{pmatrix} u \\ u \end{pmatrix} \\
a_7 &= \begin{pmatrix} -0.177391a^5u^2 + 0.00695652a^4u^2 + \cdots + 0.787826a + 0.389565 \\ -0.280000a^4u^2 - 1.12000a^2u^2 + \cdots - 2.08000a^2 - 2.08000 \end{pmatrix} \\
a_3 &= \begin{pmatrix} 0.177391a^5u^2 - 0.00695652a^4u^2 + \cdots + 0.212174a - 0.389565 \\ -0.116522a^5u^2 + 0.102609a^4u^2 + \cdots - 0.629565a + 1.34609 \end{pmatrix} \\
a_{11} &= \begin{pmatrix} 0.293913a^5u^2 - 0.109565a^4u^2 + \cdots + 0.841739a + 1.06435 \\ 0.116522a^5u^2 - 0.102609a^4u^2 + \cdots + 0.629565a + 2.65391 \end{pmatrix} \\
a_6 &= \begin{pmatrix} \frac{1}{5}a^3u^2 + \frac{2}{5}u^2a + \cdots - \frac{2}{5}a + 2 \\ \frac{1}{5}a^3u^2 + \frac{2}{5}u^2a + \cdots - \frac{1}{5}a^3 - \frac{2}{5}a \end{pmatrix} \\
a_2 &= \begin{pmatrix} 0.0608696a^5u^2 - 0.0243478a^4u^2 + \cdots + 0.582609a - 0.963478 \\ -0.349565a^5u^2 - 0.0921739a^4u^2 + \cdots - 1.88870a + 0.0382609 \end{pmatrix}
\end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = $4u^2 - 4u + 2$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $(u^3 + 2u^2 + u - 1)^6$ |
| c_2, c_6 | $(u^3 + u - 1)^6$ |
| c_3 | $(u - 1)^{18}$ |
| c_4, c_5, c_9 c_{11} | $u^{18} + 10u^{16} + \cdots - 106u + 23$ |
| c_7, c_{10} | $u^{18} - 4u^{17} + \cdots - 292u + 89$ |
| c_8, c_{12} | $(u^3 + u^2 + 2u + 1)^6$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $(y^3 - 2y^2 + 5y - 1)^6$ |
| c_2, c_6 | $(y^3 + 2y^2 + y - 1)^6$ |
| c_3 | $(y - 1)^{18}$ |
| c_4, c_5, c_9 c_{11} | $y^{18} + 20y^{17} + \cdots + 356y + 529$ |
| c_7, c_{10} | $y^{18} - 12y^{17} + \cdots - 77788y + 7921$ |
| c_8, c_{12} | $(y^3 + 3y^2 + 2y - 1)^6$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.784997 - 0.039230I$ | $-9.60386 + 2.82812I$ | $-5.50976 - 2.97945I$ |
| $b = -1.69200 + 0.07253I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.330614 - 0.633892I$ | $-9.60386 + 2.82812I$ | $-5.50976 - 2.97945I$ |
| $b = 0.492761 - 0.237412I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.22941 + 1.78152I$ | $-9.60386 + 2.82812I$ | $-5.50976 - 2.97945I$ |
| $b = -0.145783 + 1.273280I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 0.47175 - 1.81160I$ | $-9.60386 + 2.82812I$ | $-5.50976 - 2.97945I$ |
| $b = -0.43525 - 1.69984I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = 1.28006 - 1.65694I$ | $-9.60386 + 2.82812I$ | $-5.50976 - 2.97945I$ |
| $b = 1.36368 - 2.16518I$ | | |
| $u = 0.215080 + 1.307140I$ | | |
| $a = -0.40679 + 2.36014I$ | $-9.60386 + 2.82812I$ | $-5.50976 - 2.97945I$ |
| $b = 0.41659 + 2.75662I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.784997 + 0.039230I$ | $-9.60386 - 2.82812I$ | $-5.50976 + 2.97945I$ |
| $b = -1.69200 - 0.07253I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.330614 + 0.633892I$ | $-9.60386 - 2.82812I$ | $-5.50976 + 2.97945I$ |
| $b = 0.492761 + 0.237412I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.22941 - 1.78152I$ | $-9.60386 - 2.82812I$ | $-5.50976 + 2.97945I$ |
| $b = -0.145783 - 1.273280I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = 0.47175 + 1.81160I$ | $-9.60386 - 2.82812I$ | $-5.50976 + 2.97945I$ |
| $b = -0.43525 + 1.69984I$ | | |

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.215080 - 1.307140I$ | $-9.60386 - 2.82812I$ | $-5.50976 + 2.97945I$ |
| $a = 1.28006 + 1.65694I$ | | |
| $b = 1.36368 + 2.16518I$ | | |
| $u = 0.215080 - 1.307140I$ | | |
| $a = -0.40679 - 2.36014I$ | $-9.60386 - 2.82812I$ | $-5.50976 + 2.97945I$ |
| $b = 0.41659 - 2.75662I$ | | |
| $u = 0.569840$ | | |
| $a = 0.693291 + 0.635785I$ | -5.46628 | 1.01950 |
| $b = 0.094590 - 1.402580I$ | | |
| $u = 0.569840$ | | |
| $a = 0.693291 - 0.635785I$ | -5.46628 | 1.01950 |
| $b = 0.094590 + 1.402580I$ | | |
| $u = 0.569840$ | | |
| $a = -0.709483 + 1.021010I$ | -5.46628 | 1.01950 |
| $b = 0.487919 + 1.021010I$ | | |
| $u = 0.569840$ | | |
| $a = -0.709483 - 1.021010I$ | -5.46628 | 1.01950 |
| $b = 0.487919 - 1.021010I$ | | |
| $u = 0.569840$ | | |
| $a = 0.01619 + 1.77975I$ | -5.46628 | 1.01950 |
| $b = -0.582509 - 0.258612I$ | | |
| $u = 0.569840$ | | |
| $a = 0.01619 - 1.77975I$ | -5.46628 | 1.01950 |
| $b = -0.582509 + 0.258612I$ | | |

V. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1 | $(u^3 + 2u^2 + u - 1)^6$ $\cdot (u^{10} + 5u^9 + 13u^8 + 19u^7 + 17u^6 + 7u^5 - 2u^3 + u^2 + 2u + 1)^6$ $\cdot (u^{30} - 16u^{29} + \dots - 8u + 1)(u^{46} + 23u^{45} + \dots + 160u + 64)$ |
| c_2 | $(u^3 + u - 1)^6$ $\cdot (u^{10} + u^9 + 3u^8 + 3u^7 + 5u^6 + 5u^5 + 4u^4 + 4u^3 + 3u^2 + 2u + 1)^6$ $\cdot (u^{30} - 2u^{29} + \dots - 2u + 1)(u^{46} - 9u^{45} + \dots - 80u + 8)$ |
| c_3 | $(u - 1)^{18}$ $\cdot (u^{10} + 2u^9 - u^8 - 5u^7 - 3u^6 + 4u^5 + 12u^4 + 13u^3 + 5u^2 + u + 2)^6$ $\cdot (u^{30} + 2u^{29} + \dots + 9u + 2)(u^{46} + 9u^{45} + \dots + 48000u + 8768)$ |
| c_4, c_{11} | $(u^{18} + 10u^{16} + \dots - 106u + 23)(u^{30} + 17u^{28} + \dots - u + 1)$ $\cdot (u^{46} + 22u^{44} + \dots + 2u + 1)(u^{60} + u^{59} + \dots - 626u + 3383)$ |
| c_5, c_9 | $(u^{18} + 10u^{16} + \dots - 106u + 23)(u^{30} + 17u^{28} + \dots + u + 1)$ $\cdot (u^{46} + 22u^{44} + \dots + 2u + 1)(u^{60} + u^{59} + \dots - 626u + 3383)$ |
| c_6 | $(u^3 + u - 1)^6$ $\cdot (u^{10} + u^9 + 3u^8 + 3u^7 + 5u^6 + 5u^5 + 4u^4 + 4u^3 + 3u^2 + 2u + 1)^6$ $\cdot (u^{30} + 2u^{29} + \dots + 2u + 1)(u^{46} - 9u^{45} + \dots - 80u + 8)$ |
| c_7, c_{10} | $(u^{18} - 4u^{17} + \dots - 292u + 89)(u^{30} - 3u^{29} + \dots - 10u + 1)$ $\cdot (u^{46} - 3u^{45} + \dots + 15u + 1)(u^{60} - 11u^{59} + \dots - 53768u + 6593)$ |
| c_8 | $((u^3 + u^2 + 2u + 1)^{26})(u^{30} - 2u^{29} + \dots + u + 2)$ $\cdot (u^{46} - 29u^{45} + \dots - 172032u + 8192)$ |
| c_{12} | $((u^3 + u^2 + 2u + 1)^{26})(u^{30} + 2u^{29} + \dots - u + 2)$ $\cdot (u^{46} - 29u^{45} + \dots - 172032u + 8192)$ |

VI. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $(y^3 - 2y^2 + 5y - 1)^6$ $\cdot (y^{10} + y^9 + 13y^8 + 11y^7 + 45y^6 + 35y^5 + 12y^4 + 2y^3 + 9y^2 - 2y + 1)^6$ $\cdot (y^{30} + 4y^{29} + \dots - 12y + 1)(y^{46} + 3y^{45} + \dots + 34304y + 4096)$ |
| c_2, c_6 | $(y^3 + 2y^2 + y - 1)^6$ $\cdot (y^{10} + 5y^9 + 13y^8 + 19y^7 + 17y^6 + 7y^5 - 2y^3 + y^2 + 2y + 1)^6$ $\cdot (y^{30} + 16y^{29} + \dots + 8y + 1)(y^{46} + 23y^{45} + \dots + 160y + 64)$ |
| c_3 | $((y - 1)^{18})(y^{10} - 6y^9 + \dots + 19y + 4)^6(y^{30} - 8y^{29} + \dots + 51y + 4)$ $\cdot (y^{46} - 17y^{45} + \dots + 657339392y + 76877824)$ |
| c_4, c_5, c_9 c_{11} | $(y^{18} + 20y^{17} + \dots + 356y + 529)(y^{30} + 34y^{29} + \dots - 9y + 1)$ $\cdot (y^{46} + 44y^{45} + \dots + 2y + 1)$ $\cdot (y^{60} + 55y^{59} + \dots - 363644884y + 11444689)$ |
| c_7, c_{10} | $(y^{18} - 12y^{17} + \dots - 77788y + 7921)(y^{30} - 7y^{29} + \dots - 30y + 1)$ $\cdot (y^{46} - 21y^{45} + \dots - 131y + 1)$ $\cdot (y^{60} - 17y^{59} + \dots + 11794588y + 43467649)$ |
| c_8, c_{12} | $((y^3 + 3y^2 + 2y - 1)^{26})(y^{30} + 20y^{29} + \dots + 63y + 4)$ $\cdot (y^{46} + 23y^{45} + \dots - 301989888y + 67108864)$ |