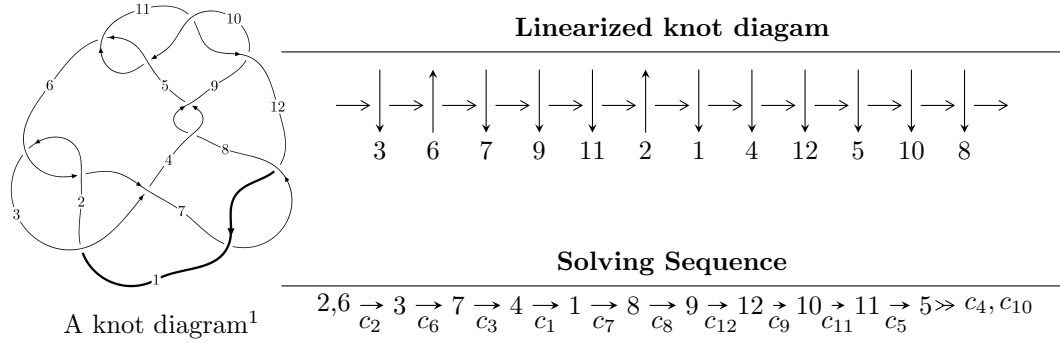


12a<sub>0226</sub> (K12a<sub>0226</sub>)



A knot diagram<sup>1</sup>

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{90} + u^{89} + \dots + u - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 90 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle u^{90} + u^{89} + \dots + u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^7 - 2u^5 - 2u^3 \\ u^9 + u^7 + u^5 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{17} - 4u^{15} - 9u^{13} - 12u^{11} - 11u^9 - 8u^7 - 6u^5 - 4u^3 - u \\ -u^{17} - 3u^{15} - 5u^{13} - 4u^{11} - u^9 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{12} + 3u^{10} + 5u^8 + 4u^6 + 2u^4 + u^2 + 1 \\ -u^{14} - 2u^{12} - 3u^{10} - 2u^8 - 2u^6 - 2u^4 - u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{43} + 10u^{41} + \dots - 5u^3 - 2u \\ -u^{45} - 9u^{43} + \dots + u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{74} + 17u^{72} + \dots + 3u^2 + 1 \\ -u^{76} - 16u^{74} + \dots - 3u^4 - 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{30} - 7u^{28} + \dots - 4u^4 + 1 \\ -u^{30} - 6u^{28} + \dots + 2u^4 + u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^{89} - 4u^{88} + \dots + 4u - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{90} + 41u^{89} + \dots - 3u + 1$
$c_2, c_6$	$u^{90} - u^{89} + \dots - u - 1$
$c_3$	$u^{90} + u^{89} + \dots + 11u - 1$
$c_4, c_8$	$u^{90} - u^{89} + \dots - 3u - 1$
$c_5, c_{10}$	$u^{90} + u^{89} + \dots - 3u - 1$
$c_7, c_{12}$	$u^{90} - 5u^{89} + \dots + 145u - 21$
$c_9, c_{11}$	$u^{90} + 31u^{89} + \dots + 3u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{90} + 17y^{89} + \dots - 51y + 1$
$c_2, c_6$	$y^{90} + 41y^{89} + \dots - 3y + 1$
$c_3$	$y^{90} - 7y^{89} + \dots + 125y + 1$
$c_4, c_8$	$y^{90} - 51y^{89} + \dots - 83y + 1$
$c_5, c_{10}$	$y^{90} - 31y^{89} + \dots - 3y + 1$
$c_7, c_{12}$	$y^{90} + 61y^{89} + \dots + 51089y + 441$
$c_9, c_{11}$	$y^{90} + 57y^{89} + \dots - 3y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.501963 + 0.898997I$	$1.67262 - 2.04573I$	0
$u = -0.501963 - 0.898997I$	$1.67262 + 2.04573I$	0
$u = 0.016868 + 1.030800I$	$3.00085 - 2.77316I$	0
$u = 0.016868 - 1.030800I$	$3.00085 + 2.77316I$	0
$u = 0.249218 + 1.008390I$	$-2.02407 - 1.06219I$	0
$u = 0.249218 - 1.008390I$	$-2.02407 + 1.06219I$	0
$u = -0.355572 + 0.888939I$	$-0.53261 - 1.53431I$	0
$u = -0.355572 - 0.888939I$	$-0.53261 + 1.53431I$	0
$u = 0.525356 + 0.925869I$	$0.94370 + 7.33842I$	0
$u = 0.525356 - 0.925869I$	$0.94370 - 7.33842I$	0
$u = 0.177394 + 1.050490I$	$-1.87659 - 1.33249I$	0
$u = 0.177394 - 1.050490I$	$-1.87659 + 1.33249I$	0
$u = 0.723590 + 0.554540I$	$3.94277 + 8.63048I$	$-4.05227 - 7.29473I$
$u = 0.723590 - 0.554540I$	$3.94277 - 8.63048I$	$-4.05227 + 7.29473I$
$u = 0.407249 + 1.012720I$	$-3.09800 + 3.08334I$	0
$u = 0.407249 - 1.012720I$	$-3.09800 - 3.08334I$	0
$u = -0.723374 + 0.544890I$	$5.04502 - 3.02424I$	$-2.05045 + 2.44739I$
$u = -0.723374 - 0.544890I$	$5.04502 + 3.02424I$	$-2.05045 - 2.44739I$
$u = -0.206935 + 1.078590I$	$-3.26676 - 3.36781I$	0
$u = -0.206935 - 1.078590I$	$-3.26676 + 3.36781I$	0
$u = 0.141824 + 1.094660I$	$-0.62220 - 3.55946I$	0
$u = 0.141824 - 1.094660I$	$-0.62220 + 3.55946I$	0
$u = -0.754490 + 0.481579I$	$8.22286 - 1.43634I$	$0. + 2.56189I$
$u = -0.754490 - 0.481579I$	$8.22286 + 1.43634I$	$0. - 2.56189I$
$u = 0.758461 + 0.471953I$	$8.16996 - 4.24799I$	$0. + 3.40241I$
$u = 0.758461 - 0.471953I$	$8.16996 + 4.24799I$	$0. - 3.40241I$
$u = -0.170343 + 1.093900I$	$-6.56383 + 2.91091I$	0
$u = -0.170343 - 1.093900I$	$-6.56383 - 2.91091I$	0
$u = -0.145257 + 1.104810I$	$-1.82142 + 9.11969I$	0
$u = -0.145257 - 1.104810I$	$-1.82142 - 9.11969I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.692194 + 0.551325I$	$-0.96504 + 2.69141I$	$-9.30626 - 3.76557I$
$u = 0.692194 - 0.551325I$	$-0.96504 - 2.69141I$	$-9.30626 + 3.76557I$
$u = -0.779428 + 0.408233I$	$3.15401 + 11.35790I$	$-5.13106 - 7.30784I$
$u = -0.779428 - 0.408233I$	$3.15401 - 11.35790I$	$-5.13106 + 7.30784I$
$u = 0.775037 + 0.413272I$	$4.33585 - 5.73221I$	$-3.09381 + 2.62769I$
$u = 0.775037 - 0.413272I$	$4.33585 + 5.73221I$	$-3.09381 - 2.62769I$
$u = -0.699433 + 0.507173I$	$3.25860 - 0.93323I$	$-1.98235 + 2.97328I$
$u = -0.699433 - 0.507173I$	$3.25860 + 0.93323I$	$-1.98235 - 2.97328I$
$u = -0.762752 + 0.398359I$	$-1.77122 + 5.17263I$	$-10.25794 - 3.78971I$
$u = -0.762752 - 0.398359I$	$-1.77122 - 5.17263I$	$-10.25794 + 3.78971I$
$u = 0.744383 + 0.417449I$	$2.78033 - 3.35446I$	$-3.31785 + 3.49388I$
$u = 0.744383 - 0.417449I$	$2.78033 + 3.35446I$	$-3.31785 - 3.49388I$
$u = 0.405058 + 1.093730I$	$-3.77807 + 2.56808I$	0
$u = 0.405058 - 1.093730I$	$-3.77807 - 2.56808I$	0
$u = 0.582288 + 1.013010I$	$-2.33340 + 2.22713I$	0
$u = 0.582288 - 1.013010I$	$-2.33340 - 2.22713I$	0
$u = -0.727699 + 0.389178I$	$1.22174 - 1.10018I$	$-7.10486 + 1.96284I$
$u = -0.727699 - 0.389178I$	$1.22174 + 1.10018I$	$-7.10486 - 1.96284I$
$u = -0.400532 + 1.107050I$	$-5.12142 + 2.61021I$	0
$u = -0.400532 - 1.107050I$	$-5.12142 - 2.61021I$	0
$u = 0.608187 + 1.017900I$	$2.56703 - 3.54065I$	0
$u = 0.608187 - 1.017900I$	$2.56703 + 3.54065I$	0
$u = 0.441817 + 1.101300I$	$-3.52532 + 4.80773I$	0
$u = 0.441817 - 1.101300I$	$-3.52532 - 4.80773I$	0
$u = -0.422685 + 1.110300I$	$-9.04985 - 3.77247I$	0
$u = -0.422685 - 1.110300I$	$-9.04985 + 3.77247I$	0
$u = -0.605703 + 1.024670I$	$3.62058 - 2.05673I$	0
$u = -0.605703 - 1.024670I$	$3.62058 + 2.05673I$	0
$u = -0.442733 + 1.111360I$	$-4.83695 - 10.14260I$	0
$u = -0.442733 - 1.111360I$	$-4.83695 + 10.14260I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.584864 + 1.044800I$	$1.66537 - 4.01436I$	0
$u = -0.584864 - 1.044800I$	$1.66537 + 4.01436I$	0
$u = 0.560377 + 1.066900I$	$0.01118 + 7.69723I$	0
$u = 0.560377 - 1.066900I$	$0.01118 - 7.69723I$	0
$u = -0.473389 + 0.634112I$	$2.39074 - 2.06952I$	$-2.67251 + 3.85924I$
$u = -0.473389 - 0.634112I$	$2.39074 + 2.06952I$	$-2.67251 - 3.85924I$
$u = 0.556806 + 0.552055I$	$1.92931 - 2.99812I$	$-4.64252 + 2.70074I$
$u = 0.556806 - 0.552055I$	$1.92931 + 2.99812I$	$-4.64252 - 2.70074I$
$u = -0.607693 + 1.068190I$	$6.48101 - 3.73161I$	0
$u = -0.607693 - 1.068190I$	$6.48101 + 3.73161I$	0
$u = 0.607083 + 1.073890I$	$6.38293 + 9.42351I$	0
$u = 0.607083 - 1.073890I$	$6.38293 - 9.42351I$	0
$u = 0.625319 + 0.432375I$	$1.84509 - 2.98280I$	$-5.82371 + 4.10556I$
$u = 0.625319 - 0.432375I$	$1.84509 + 2.98280I$	$-5.82371 - 4.10556I$
$u = -0.576053 + 1.098500I$	$-0.85267 - 3.87735I$	0
$u = -0.576053 - 1.098500I$	$-0.85267 + 3.87735I$	0
$u = 0.587200 + 1.093990I$	$0.78468 + 8.41873I$	0
$u = 0.587200 - 1.093990I$	$0.78468 - 8.41873I$	0
$u = -0.588705 + 1.105070I$	$-3.85739 - 10.28380I$	0
$u = -0.588705 - 1.105070I$	$-3.85739 + 10.28380I$	0
$u = 0.597219 + 1.103510I$	$2.29023 + 10.90840I$	0
$u = 0.597219 - 1.103510I$	$2.29023 - 10.90840I$	0
$u = -0.597318 + 1.106640I$	$1.0834 - 16.5446I$	0
$u = -0.597318 - 1.106640I$	$1.0834 + 16.5446I$	0
$u = -0.625268 + 0.058000I$	$-1.95110 + 6.19847I$	$-9.59402 - 5.63729I$
$u = -0.625268 - 0.058000I$	$-1.95110 - 6.19847I$	$-9.59402 + 5.63729I$
$u = -0.621508$	$-6.02816$	$-14.3370$
$u = 0.592899 + 0.061563I$	$-0.725428 - 0.939411I$	$-7.71421 + 0.78565I$
$u = 0.592899 - 0.061563I$	$-0.725428 + 0.939411I$	$-7.71421 - 0.78565I$
$u = 0.374226$	$-0.816002$	$-12.1280$

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^{90} + 41u^{89} + \dots - 3u + 1$
$c_2, c_6$	$u^{90} - u^{89} + \dots - u - 1$
$c_3$	$u^{90} + u^{89} + \dots + 11u - 1$
$c_4, c_8$	$u^{90} - u^{89} + \dots - 3u - 1$
$c_5, c_{10}$	$u^{90} + u^{89} + \dots - 3u - 1$
$c_7, c_{12}$	$u^{90} - 5u^{89} + \dots + 145u - 21$
$c_9, c_{11}$	$u^{90} + 31u^{89} + \dots + 3u + 1$



### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{90} + 17y^{89} + \dots - 51y + 1$
$c_2, c_6$	$y^{90} + 41y^{89} + \dots - 3y + 1$
$c_3$	$y^{90} - 7y^{89} + \dots + 125y + 1$
$c_4, c_8$	$y^{90} - 51y^{89} + \dots - 83y + 1$
$c_5, c_{10}$	$y^{90} - 31y^{89} + \dots - 3y + 1$
$c_7, c_{12}$	$y^{90} + 61y^{89} + \dots + 51089y + 441$
$c_9, c_{11}$	$y^{90} + 57y^{89} + \dots - 3y + 1$