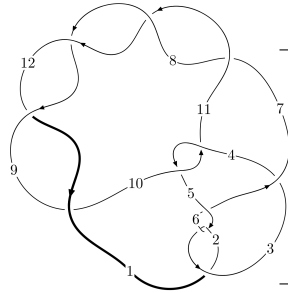
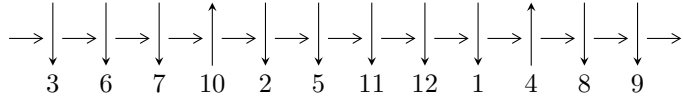


12a₀₂₃₆ (K12a₀₂₃₆)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$8,11 \xrightarrow{c_{11}} 12 \xrightarrow{c_8} 9 \xrightarrow{c_{12}} 1 \xrightarrow{c_7} 4,7 \xrightarrow{c_3} 3 \xrightarrow{c_{10}} 10 \xrightarrow{c_4} 5 \xrightarrow{c_6} 6 \xrightarrow{c_2} 2 \rightsquigarrow c_1, c_5, c_9$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 15u^{53} + 20u^{52} + \dots + 2b - 8, 49u^{53} + 76u^{52} + \dots + 4a - 12, u^{54} + 3u^{53} + \dots + 3u - 1 \rangle$$

$$I_2^u = \langle b, a^3 - a^2u + a^2 - 2au + 4a - 2u + 3, u^2 - u - 1 \rangle$$

$$I_3^u = \langle b + 1, a, u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 61 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle 15u^{53} + 20u^{52} + \dots + 2b - 8, 49u^{53} + 76u^{52} + \dots + 4a - 12, u^{54} + 3u^{53} + \dots + 3u - 1 \rangle$$

I. $I_1^u =$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{49}{4}u^{53} - 19u^{52} + \dots - \frac{105}{4}u + 3 \\ -\frac{15}{2}u^{53} - 10u^{52} + \dots - \frac{27}{2}u + 4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{7}{4}u^{53} - \frac{17}{4}u^{52} + \dots - \frac{23}{4}u - \frac{9}{4} \\ 3u^{53} + \frac{19}{4}u^{52} + \dots + 7u - \frac{5}{4} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 - 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{9}{4}u^{53} - \frac{327}{4}u^{51} + \dots + \frac{9}{4}u - 5 \\ \frac{19}{2}u^{53} + 12u^{52} + \dots + \frac{39}{2}u - 5 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{4}u^{53} + \frac{3}{4}u^{52} + \dots + \frac{23}{4}u + \frac{5}{4} \\ -u^{16} + 10u^{14} + \dots - 6u^3 - 4u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{4}u^{52} - \frac{1}{2}u^{51} + \dots - \frac{9}{2}u - \frac{1}{4} \\ \frac{1}{4}u^{53} + \frac{1}{2}u^{52} + \dots + \frac{11}{2}u^2 + \frac{5}{4}u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-8u^{53} - 6u^{52} + \dots - 19u + \frac{1}{2}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_6	$u^{54} + 18u^{53} + \dots + 28u + 1$
c_2, c_5	$u^{54} + 2u^{53} + \dots - 14u^2 + 1$
c_3	$u^{54} - 4u^{53} + \dots - 2672u + 433$
c_4, c_{10}	$u^{54} + 2u^{53} + \dots - 224u - 64$
c_7, c_8, c_9 c_{11}, c_{12}	$u^{54} + 3u^{53} + \dots + 3u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_6	$y^{54} + 38y^{53} + \dots - 252y + 1$
c_2, c_5	$y^{54} - 18y^{53} + \dots - 28y + 1$
c_3	$y^{54} - 22y^{53} + \dots - 7170760y + 187489$
c_4, c_{10}	$y^{54} + 36y^{53} + \dots - 1024y + 4096$
c_7, c_8, c_9 c_{11}, c_{12}	$y^{54} - 73y^{53} + \dots - 33y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.996240 + 0.174836I$ $a = -0.046917 - 0.171089I$ $b = -1.041700 + 0.270047I$	$-0.93612 + 5.33064I$	0
$u = -0.996240 - 0.174836I$ $a = -0.046917 + 0.171089I$ $b = -1.041700 - 0.270047I$	$-0.93612 - 5.33064I$	0
$u = -0.921952 + 0.190975I$ $a = 0.120199 + 0.149841I$ $b = 0.923078 - 0.334826I$	$-0.122335 + 0.095210I$	$-8.00000 + 0.I$
$u = -0.921952 - 0.190975I$ $a = 0.120199 - 0.149841I$ $b = 0.923078 + 0.334826I$	$-0.122335 - 0.095210I$	$-8.00000 + 0.I$
$u = 1.064210 + 0.209793I$ $a = -0.63295 - 1.61348I$ $b = 0.282300 - 1.168280I$	$-4.75278 - 2.80286I$	0
$u = 1.064210 - 0.209793I$ $a = -0.63295 + 1.61348I$ $b = 0.282300 + 1.168280I$	$-4.75278 + 2.80286I$	0
$u = 1.030910 + 0.348284I$ $a = -0.95535 - 1.48256I$ $b = 0.541961 - 1.230030I$	$-3.03671 - 5.51505I$	0
$u = 1.030910 - 0.348284I$ $a = -0.95535 + 1.48256I$ $b = 0.541961 + 1.230030I$	$-3.03671 + 5.51505I$	0
$u = 1.050340 + 0.376575I$ $a = 0.96873 + 1.41375I$ $b = -0.57619 + 1.29485I$	$-4.25463 - 11.21320I$	0
$u = 1.050340 - 0.376575I$ $a = 0.96873 - 1.41375I$ $b = -0.57619 - 1.29485I$	$-4.25463 + 11.21320I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.851855 + 0.026742I$ $a = -0.20081 - 2.78618I$ $b = 0.052036 - 0.745442I$	$1.33981 - 2.97841I$	$-16.2532 + 3.7844I$
$u = 0.851855 - 0.026742I$ $a = -0.20081 + 2.78618I$ $b = 0.052036 + 0.745442I$	$1.33981 + 2.97841I$	$-16.2532 - 3.7844I$
$u = 1.113960 + 0.306274I$ $a = 0.77810 + 1.39695I$ $b = -0.384474 + 1.331420I$	$-9.35844 - 4.90130I$	0
$u = 1.113960 - 0.306274I$ $a = 0.77810 - 1.39695I$ $b = -0.384474 - 1.331420I$	$-9.35844 + 4.90130I$	0
$u = 1.175560 + 0.167588I$ $a = 0.43398 + 1.38174I$ $b = -0.143925 + 1.276040I$	$-6.63511 + 1.61390I$	0
$u = 1.175560 - 0.167588I$ $a = 0.43398 - 1.38174I$ $b = -0.143925 - 1.276040I$	$-6.63511 - 1.61390I$	0
$u = -0.519490 + 0.531321I$ $a = -0.713490 - 0.165731I$ $b = -0.208766 + 1.145180I$	$-1.05139 - 3.92853I$	$-12.01559 + 2.10078I$
$u = -0.519490 - 0.531321I$ $a = -0.713490 + 0.165731I$ $b = -0.208766 - 1.145180I$	$-1.05139 + 3.92853I$	$-12.01559 - 2.10078I$
$u = -0.723166$ $a = 0.147422$ $b = 0.462202$	-1.27288	-6.75210
$u = -0.542660 + 0.430784I$ $a = 0.615074 + 0.066547I$ $b = 0.268273 - 0.941014I$	$-0.103530 + 1.138840I$	$-10.54250 - 3.54234I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.542660 - 0.430784I$		
$a = 0.615074 - 0.066547I$	$-0.103530 - 1.138840I$	$-10.54250 + 3.54234I$
$b = 0.268273 + 0.941014I$		
$u = -0.364228 + 0.577449I$		
$a = -0.934188 - 0.148020I$	$-4.71225 + 1.89294I$	$-15.7177 - 3.8918I$
$b = 0.138461 + 1.174430I$		
$u = -0.364228 - 0.577449I$		
$a = -0.934188 + 0.148020I$	$-4.71225 - 1.89294I$	$-15.7177 + 3.8918I$
$b = 0.138461 - 1.174430I$		
$u = -0.250036 + 0.633419I$		
$a = -1.104300 - 0.206805I$	$-0.22294 + 7.78581I$	$-9.62304 - 7.92359I$
$b = 0.417478 + 1.191560I$		
$u = -0.250036 - 0.633419I$		
$a = -1.104300 + 0.206805I$	$-0.22294 - 7.78581I$	$-9.62304 + 7.92359I$
$b = 0.417478 - 1.191560I$		
$u = -0.225695 + 0.589084I$		
$a = 1.140710 + 0.141782I$	$0.86035 + 2.32908I$	$-7.32309 - 3.24267I$
$b = -0.419400 - 1.081010I$		
$u = -0.225695 - 0.589084I$		
$a = 1.140710 - 0.141782I$	$0.86035 - 2.32908I$	$-7.32309 + 3.24267I$
$b = -0.419400 + 1.081010I$		
$u = 1.55391 + 0.02757I$		
$a = -0.098217 - 0.452334I$	$-6.99883 - 2.48049I$	0
$b = -0.140479 - 0.824642I$		
$u = 1.55391 - 0.02757I$		
$a = -0.098217 + 0.452334I$	$-6.99883 + 2.48049I$	0
$b = -0.140479 + 0.824642I$		
$u = -0.281495 + 0.312842I$		
$a = 0.916828 - 0.383169I$	$-0.459739 + 0.937129I$	$-7.88969 - 7.07124I$
$b = -0.123921 - 0.686515I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.281495 - 0.312842I$ $a = 0.916828 + 0.383169I$ $b = -0.123921 + 0.686515I$	$-0.459739 - 0.937129I$	$-7.88969 + 7.07124I$
$u = 0.135244 + 0.362504I$ $a = 2.08092 + 0.05555I$ $b = -0.644171 - 0.344545I$	$3.08884 + 1.84557I$	$-1.95761 - 1.92890I$
$u = 0.135244 - 0.362504I$ $a = 2.08092 - 0.05555I$ $b = -0.644171 + 0.344545I$	$3.08884 - 1.84557I$	$-1.95761 + 1.92890I$
$u = 0.208405 + 0.314817I$ $a = -2.34049 - 0.17879I$ $b = 0.644426 + 0.215596I$	$2.77868 - 3.61490I$	$-2.24333 + 5.08342I$
$u = 0.208405 - 0.314817I$ $a = -2.34049 + 0.17879I$ $b = 0.644426 - 0.215596I$	$2.77868 + 3.61490I$	$-2.24333 - 5.08342I$
$u = 1.63895$ $a = -0.245628$ $b = -0.507248$	-9.62995	0
$u = -1.69921 + 0.00586I$ $a = 0.06322 - 2.33836I$ $b = -0.045647 - 1.071130I$	$-7.84998 + 3.09710I$	0
$u = -1.69921 - 0.00586I$ $a = 0.06322 + 2.33836I$ $b = -0.045647 + 1.071130I$	$-7.84998 - 3.09710I$	0
$u = 1.70201 + 0.03703I$ $a = -0.494003 - 0.097988I$ $b = -1.107300 - 0.281751I$	$-9.45410 - 0.92395I$	0
$u = 1.70201 - 0.03703I$ $a = -0.494003 + 0.097988I$ $b = -1.107300 + 0.281751I$	$-9.45410 + 0.92395I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.72317 + 0.04214I$		
$a = 0.547011 + 0.098121I$	$-10.67310 - 6.19112I$	0
$b = 1.263400 + 0.305417I$		
$u = 1.72317 - 0.04214I$		
$a = 0.547011 - 0.098121I$	$-10.67310 + 6.19112I$	0
$b = 1.263400 - 0.305417I$		
$u = 1.72764$		
$a = 0.546125$	-14.7580	0
$b = 1.28414$		
$u = -1.72994 + 0.09259I$		
$a = 0.38653 - 1.80892I$	$-12.8350 + 7.3215I$	0
$b = -0.64312 - 1.34017I$		
$u = -1.72994 - 0.09259I$		
$a = 0.38653 + 1.80892I$	$-12.8350 - 7.3215I$	0
$b = -0.64312 + 1.34017I$		
$u = -1.73510 + 0.10150I$		
$a = -0.37724 + 1.76762I$	$-14.1294 + 13.1902I$	0
$b = 0.69739 + 1.37855I$		
$u = -1.73510 - 0.10150I$		
$a = -0.37724 - 1.76762I$	$-14.1294 - 13.1902I$	0
$b = 0.69739 - 1.37855I$		
$u = -1.73884 + 0.05594I$		
$a = 0.26375 - 1.92837I$	$-14.8035 + 3.9179I$	0
$b = -0.39367 - 1.37924I$		
$u = -1.73884 - 0.05594I$		
$a = 0.26375 + 1.92837I$	$-14.8035 - 3.9179I$	0
$b = -0.39367 + 1.37924I$		
$u = -1.75253 + 0.07823I$		
$a = -0.27989 + 1.81978I$	$-19.6252 + 6.5170I$	0
$b = 0.53764 + 1.48090I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.75253 - 0.07823I$ $a = -0.27989 - 1.81978I$ $b = 0.53764 - 1.48090I$	$-19.6252 - 6.5170I$	0
$u = -1.75789 + 0.04187I$ $a = -0.16460 + 1.90001I$ $b = 0.29057 + 1.50492I$	$-17.1812 - 0.7272I$	0
$u = -1.75789 - 0.04187I$ $a = -0.16460 - 1.90001I$ $b = 0.29057 - 1.50492I$	$-17.1812 + 0.7272I$	0
$u = 0.168072$ $a = -3.39312$ $b = 0.392381$	-1.32970	-6.13160

$$\text{II. } I_2^u = \langle b, a^3 - a^2u + a^2 - 2au + 4a - 2u + 3, u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -au \\ -au - a \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^2u + u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -a^2u - a^2 - u \\ -2a^2u - a^2 - u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-10a^2u - 9a^2 + 6au + a - 3u - 21$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$(u^3 - u^2 + 2u - 1)^2$
c_2	$(u^3 + u^2 - 1)^2$
c_4, c_{10}	u^6
c_5	$(u^3 - u^2 + 1)^2$
c_6	$(u^3 + u^2 + 2u + 1)^2$
c_7, c_8, c_9	$(u^2 + u - 1)^3$
c_{11}, c_{12}	$(u^2 - u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6	$(y^3 + 3y^2 + 2y - 1)^2$
c_2, c_5	$(y^3 - y^2 + 2y - 1)^2$
c_4, c_{10}	y^6
c_7, c_8, c_9 c_{11}, c_{12}	$(y^2 - 3y + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$ $a = -0.922021$ $b = 0$	-2.10041	-19.0460
$u = -0.618034$ $a = -0.34801 + 2.11500I$ $b = 0$	$2.03717 + 2.82812I$	$-5.93195 - 1.57712I$
$u = -0.618034$ $a = -0.34801 - 2.11500I$ $b = 0$	$2.03717 - 2.82812I$	$-5.93195 + 1.57712I$
$u = 1.61803$ $a = 0.132927 + 0.807858I$ $b = 0$	$-5.85852 - 2.82812I$	$-8.44207 + 3.24268I$
$u = 1.61803$ $a = 0.132927 - 0.807858I$ $b = 0$	$-5.85852 + 2.82812I$	$-8.44207 - 3.24268I$
$u = 1.61803$ $a = 0.352181$ $b = 0$	-9.99610	-25.2060

$$\text{III. } I_3^u = \langle b + 1, a, u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -18

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
c_1, c_2, c_3 c_5, c_6, c_7 c_8, c_9, c_{11} c_{12}	$u + 1$
c_4, c_{10}	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3	$y - 1$
c_4, c_5, c_6	
c_7, c_8, c_9	
c_{10}, c_{11}, c_{12}	

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 0$	-4.93480	-18.0000
$b = -1.00000$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u + 1)(u^3 - u^2 + 2u - 1)^2(u^{54} + 18u^{53} + \dots + 28u + 1)$
c_2	$(u + 1)(u^3 + u^2 - 1)^2(u^{54} + 2u^{53} + \dots - 14u^2 + 1)$
c_3	$(u + 1)(u^3 - u^2 + 2u - 1)^2(u^{54} - 4u^{53} + \dots - 2672u + 433)$
c_4, c_{10}	$u^6(u - 1)(u^{54} + 2u^{53} + \dots - 224u - 64)$
c_5	$(u + 1)(u^3 - u^2 + 1)^2(u^{54} + 2u^{53} + \dots - 14u^2 + 1)$
c_6	$(u + 1)(u^3 + u^2 + 2u + 1)^2(u^{54} + 18u^{53} + \dots + 28u + 1)$
c_7, c_8, c_9	$(u + 1)(u^2 + u - 1)^3(u^{54} + 3u^{53} + \dots + 3u - 1)$
c_{11}, c_{12}	$(u + 1)(u^2 - u - 1)^3(u^{54} + 3u^{53} + \dots + 3u - 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_6	$(y - 1)(y^3 + 3y^2 + 2y - 1)^2(y^{54} + 38y^{53} + \dots - 252y + 1)$
c_2, c_5	$(y - 1)(y^3 - y^2 + 2y - 1)^2(y^{54} - 18y^{53} + \dots - 28y + 1)$
c_3	$(y - 1)(y^3 + 3y^2 + 2y - 1)^2(y^{54} - 22y^{53} + \dots - 7170760y + 187489)$
c_4, c_{10}	$y^6(y - 1)(y^{54} + 36y^{53} + \dots - 1024y + 4096)$
c_7, c_8, c_9 c_{11}, c_{12}	$(y - 1)(y^2 - 3y + 1)^3(y^{54} - 73y^{53} + \dots - 33y + 1)$