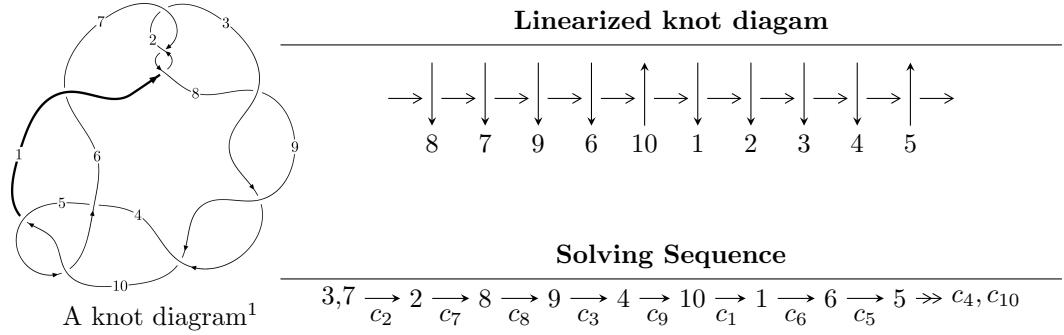


10₂₁ ($K10a_{60}$)



Ideals for irreducible components² of X_{par}

$$\begin{aligned} I_1^u &= \langle u^{16} - u^{15} + \cdots - 2u + 1 \rangle \\ I_2^u &= \langle u^6 + 2u^4 + u^3 + u^2 + u - 1 \rangle \end{aligned}$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 22 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{16} - u^{15} + 7u^{14} - 7u^{13} + 20u^{12} - 20u^{11} + 27u^{10} - 27u^9 + 12u^8 - 12u^7 - 8u^6 + 8u^5 - 6u^4 + 6u^3 + 3u^2 - 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^6 - 3u^4 - 2u^2 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^9 + 4u^7 + 5u^5 - 3u \\ -u^9 - 3u^7 - 3u^5 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^{15} + 7u^{13} + \dots - 3u^2 + u \\ -u^{15} - 7u^{13} + \dots + 3u^2 + 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

$$\text{(iii) Cusp Shapes} = 4u^{15} - 4u^{14} + 28u^{13} - 24u^{12} + 76u^{11} - 56u^{10} + 88u^9 - 52u^8 + 8u^7 + 4u^6 - 64u^5 + 28u^4 - 24u^3 - 4u^2 + 20u - 14$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|--------------------------------------|
| c_1, c_2, c_7 | $u^{16} + u^{15} + \cdots + 2u + 1$ |
| c_3, c_6, c_8 c_9 | $u^{16} + 2u^{15} + \cdots + u + 2$ |
| c_4 | $u^{16} + 9u^{15} + \cdots + 2u + 1$ |
| c_5, c_{10} | $u^{16} + u^{15} + \cdots + u^2 + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|--|
| c_1, c_2, c_7 | $y^{16} + 13y^{15} + \cdots + 2y + 1$ |
| c_3, c_6, c_8 c_9 | $y^{16} - 18y^{15} + \cdots + 19y + 4$ |
| c_4 | $y^{16} - 3y^{15} + \cdots - 2y + 1$ |
| c_5, c_{10} | $y^{16} + 9y^{15} + \cdots + 2y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.913611 + 0.024079I$ | $-12.72960 - 4.85972I$ | $-13.14726 + 3.11789I$ |
| $u = 0.913611 - 0.024079I$ | $-12.72960 + 4.85972I$ | $-13.14726 - 3.11789I$ |
| $u = 0.186298 + 1.238560I$ | $2.77285 - 2.45923I$ | $-2.72504 + 3.25382I$ |
| $u = 0.186298 - 1.238560I$ | $2.77285 + 2.45923I$ | $-2.72504 - 3.25382I$ |
| $u = 0.048176 + 1.278470I$ | $4.14984 - 1.95072I$ | $-0.93886 + 4.17042I$ |
| $u = 0.048176 - 1.278470I$ | $4.14984 + 1.95072I$ | $-0.93886 - 4.17042I$ |
| $u = -0.255012 + 1.283570I$ | $0.60263 + 6.60937I$ | $-6.51664 - 7.40663I$ |
| $u = -0.255012 - 1.283570I$ | $0.60263 - 6.60937I$ | $-6.51664 + 7.40663I$ |
| $u = -0.650102 + 0.127920I$ | $-3.75337 + 3.37292I$ | $-12.93248 - 5.20888I$ |
| $u = -0.650102 - 0.127920I$ | $-3.75337 - 3.37292I$ | $-12.93248 + 5.20888I$ |
| $u = -0.427423 + 1.281870I$ | $-4.90049 + 4.73480I$ | $-6.47201 - 3.02289I$ |
| $u = -0.427423 - 1.281870I$ | $-4.90049 - 4.73480I$ | $-6.47201 + 3.02289I$ |
| $u = 0.434047 + 1.303760I$ | $-8.59381 - 9.67514I$ | $-9.50822 + 5.97678I$ |
| $u = 0.434047 - 1.303760I$ | $-8.59381 + 9.67514I$ | $-9.50822 - 5.97678I$ |
| $u = 0.250406 + 0.342321I$ | $-0.577111 - 1.084380I$ | $-7.75949 + 5.90127I$ |
| $u = 0.250406 - 0.342321I$ | $-0.577111 + 1.084380I$ | $-7.75949 - 5.90127I$ |

$$\text{II. } I_2^u = \langle u^6 + 2u^4 + u^3 + u^2 + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^4 + u^3 - u^2 + u \\ -u^3 - u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^4 - u^2 - 1 \\ -u^3 - u + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^5 + 2u^3 + u \\ -u^5 + u^4 - u^3 + u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^3 \\ -u^5 - u^3 + u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -10

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|----------------------------------|---|
| c_1, c_2, c_5 c_7, c_{10} | $u^6 + 2u^4 - u^3 + u^2 - u - 1$ |
| c_3, c_6, c_8 c_9 | $(u^2 - u - 1)^3$ |
| c_4 | $u^6 + 4u^5 + 6u^4 + u^3 - 5u^2 - 3u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|----------------------------------|--|
| c_1, c_2, c_5 c_7, c_{10} | $y^6 + 4y^5 + 6y^4 + y^3 - 5y^2 - 3y + 1$ |
| c_3, c_6, c_8 c_9 | $(y^2 - 3y + 1)^3$ |
| c_4 | $y^6 - 4y^5 + 18y^4 - 35y^3 + 43y^2 - 19y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.896795$ | -8.88264 | -10.0000 |
| $u = -0.248003 + 1.088360I$ | -0.986960 | -10.0000 |
| $u = -0.248003 - 1.088360I$ | -0.986960 | -10.0000 |
| $u = 0.448397 + 1.266170I$ | -8.88264 | -10.0000 |
| $u = 0.448397 - 1.266170I$ | -8.88264 | -10.0000 |
| $u = 0.496006$ | -0.986960 | -10.0000 |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|--------------------------|--|
| c_1, c_2, c_7 | $(u^6 + 2u^4 - u^3 + u^2 - u - 1)(u^{16} + u^{15} + \dots + 2u + 1)$ |
| c_3, c_6, c_8 c_9 | $((u^2 - u - 1)^3)(u^{16} + 2u^{15} + \dots + u + 2)$ |
| c_4 | $(u^6 + 4u^5 + 6u^4 + u^3 - 5u^2 - 3u + 1)(u^{16} + 9u^{15} + \dots + 2u + 1)$ |
| c_5, c_{10} | $(u^6 + 2u^4 - u^3 + u^2 - u - 1)(u^{16} + u^{15} + \dots + u^2 + 1)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------|---|
| c_1, c_2, c_7 | $(y^6 + 4y^5 + 6y^4 + y^3 - 5y^2 - 3y + 1)(y^{16} + 13y^{15} + \dots + 2y + 1)$ |
| c_3, c_6, c_8 c_9 | $((y^2 - 3y + 1)^3)(y^{16} - 18y^{15} + \dots + 19y + 4)$ |
| c_4 | $(y^6 - 4y^5 + \dots - 19y + 1)(y^{16} - 3y^{15} + \dots - 2y + 1)$ |
| c_5, c_{10} | $(y^6 + 4y^5 + 6y^4 + y^3 - 5y^2 - 3y + 1)(y^{16} + 9y^{15} + \dots + 2y + 1)$ |