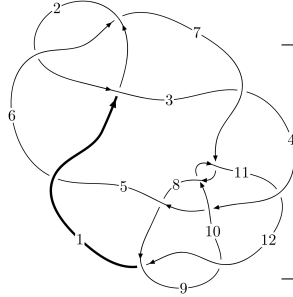
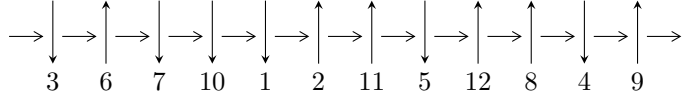


12a<sub>0260</sub> (K12a<sub>0260</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,6 \xrightarrow{c_2} 3 \xrightarrow{c_6} 7 \xrightarrow{c_3} 4,11 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 12 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \xrightarrow{c_9} 9 \twoheadrightarrow c_4, c_8, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -1.75234 \times 10^{17} u^{39} + 5.61074 \times 10^{17} u^{38} + \dots + 1.58801 \times 10^{18} b - 1.77103 \times 10^{18}, \\ -9.73786 \times 10^{17} u^{39} - 2.24750 \times 10^{17} u^{38} + \dots + 3.17601 \times 10^{18} a + 6.50880 \times 10^{18}, \\ u^{40} + 2u^{39} + \dots - 15u - 4 \rangle$$

$$I_2^u = \langle 142u^{29}a + u^{29} + \dots - 811a + 77, 4u^{28}a + u^{29} + \dots - 5a + 16, u^{30} + u^{29} + \dots + u - 1 \rangle$$

$$I_3^u = \langle 2u^4 - 2u^3 + 2u^2 + 2b - u, -2u^2 + 2a + u - 2, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle$$

$$I_4^u = \langle -au + b - 2a + u + 1, a^2 - 2a + 2, u^2 + u + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 109 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.75 \times 10^{17} u^{39} + 5.61 \times 10^{17} u^{38} + \dots + 1.59 \times 10^{18} b - 1.77 \times 10^{18}, -9.74 \times 10^{17} u^{39} - 2.25 \times 10^{17} u^{38} + \dots + 3.18 \times 10^{18} a + 6.51 \times 10^{18}, u^{40} + 2u^{39} + \dots - 15u - 4 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.306607u^{39} + 0.0707647u^{38} + \dots - 2.18335u - 2.04936 \\ 0.110349u^{39} - 0.353320u^{38} + \dots + 4.43538u + 1.11525 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.330016u^{39} + 0.209936u^{38} + \dots - 2.54790u - 1.41013 \\ 0.167912u^{39} - 0.146809u^{38} + \dots + 3.63862u + 0.864836 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.233887u^{39} + 0.0964315u^{38} + \dots - 2.14298u - 1.71555 \\ 0.223896u^{39} + 0.0820644u^{38} + \dots + 1.09448u + 0.165309 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - u^5 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.606364u^{39} + 0.274704u^{38} + \dots - 4.91727u - 2.84677 \\ 0.385943u^{39} - 0.202353u^{38} + \dots + 5.39621u + 1.32664 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.263635u^{39} + 0.0269093u^{38} + \dots - 1.67340u - 1.47960 \\ 0.148444u^{39} - 0.225204u^{38} + \dots + 3.90113u + 0.775015 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{1027807058031671441}{794003375424954487} u^{39} - \frac{7796249979768242351}{3176013501699817948} u^{38} + \dots - \frac{1978648037828171537}{794003375424954487} u + \frac{67049658634384246}{794003375424954487}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{40} + 22u^{39} + \dots - u + 16$
$c_2, c_6$	$u^{40} - 2u^{39} + \dots + 15u - 4$
$c_3, c_5$	$u^{40} + 2u^{39} + \dots + 871u - 676$
$c_4$	$u^{40} - 3u^{39} + \dots + 512u + 2048$
$c_7, c_9, c_{10}$ $c_{12}$	$u^{40} - 5u^{39} + \dots - 3u - 1$
$c_8, c_{11}$	$32(32u^{40} + 48u^{39} + \dots + 8u + 4)$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{40} - 6y^{39} + \dots - 3905y + 256$
$c_2, c_6$	$y^{40} + 22y^{39} + \dots - y + 16$
$c_3, c_5$	$y^{40} - 34y^{39} + \dots + 2269839y + 456976$
$c_4$	$y^{40} - 13y^{39} + \dots - 63176704y + 4194304$
$c_7, c_9, c_{10}$ $c_{12}$	$y^{40} + 27y^{39} + \dots + 25y + 1$
$c_8, c_{11}$	$1024(1024y^{40} - 27904y^{39} + \dots + 16y + 16)$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.748783 + 0.635787I$		
$a = 0.497441 - 0.487921I$	$-3.86456 - 4.42335I$	$-6.59807 + 7.34601I$
$b = -0.443502 + 0.321931I$		
$u = -0.748783 - 0.635787I$		
$a = 0.497441 + 0.487921I$	$-3.86456 + 4.42335I$	$-6.59807 - 7.34601I$
$b = -0.443502 - 0.321931I$		
$u = 0.370444 + 0.884043I$		
$a = -0.741241 - 0.879542I$	$1.27740 + 1.88898I$	$-6.0015 - 15.6995I$
$b = -0.990076 + 0.305719I$		
$u = 0.370444 - 0.884043I$		
$a = -0.741241 + 0.879542I$	$1.27740 - 1.88898I$	$-6.0015 + 15.6995I$
$b = -0.990076 - 0.305719I$		
$u = 0.936692 + 0.132944I$		
$a = -0.36069 - 2.07229I$	$-10.28620 - 2.94658I$	$-8.50665 + 2.50672I$
$b = -0.283700 - 0.679214I$		
$u = 0.936692 - 0.132944I$		
$a = -0.36069 + 2.07229I$	$-10.28620 + 2.94658I$	$-8.50665 - 2.50672I$
$b = -0.283700 + 0.679214I$		
$u = -0.893287 + 0.111704I$		
$a = -0.24516 + 2.54481I$	$-11.6323 + 12.6478I$	$-5.02011 - 6.24043I$
$b = -0.611222 + 0.896510I$		
$u = -0.893287 - 0.111704I$		
$a = -0.24516 - 2.54481I$	$-11.6323 - 12.6478I$	$-5.02011 + 6.24043I$
$b = -0.611222 - 0.896510I$		
$u = -0.433282 + 1.016950I$		
$a = -0.826445 + 0.289312I$	$-1.48385 - 1.77946I$	$-1.213579 + 0.177328I$
$b = -1.227630 + 0.661551I$		
$u = -0.433282 - 1.016950I$		
$a = -0.826445 - 0.289312I$	$-1.48385 + 1.77946I$	$-1.213579 - 0.177328I$
$b = -1.227630 - 0.661551I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.735196 + 0.474957I$		
$a = 0.73676 + 1.52515I$	$-4.66772 - 7.25009I$	$-3.73082 + 5.45853I$
$b = 0.299735 + 0.089122I$		
$u = 0.735196 - 0.474957I$		
$a = 0.73676 - 1.52515I$	$-4.66772 + 7.25009I$	$-3.73082 - 5.45853I$
$b = 0.299735 - 0.089122I$		
$u = 0.590773 + 1.005950I$		
$a = 0.968619 + 0.798321I$	$-6.21633 + 12.24890I$	$-5.37332 - 9.94766I$
$b = 2.11021 + 1.04129I$		
$u = 0.590773 - 1.005950I$		
$a = 0.968619 - 0.798321I$	$-6.21633 - 12.24890I$	$-5.37332 + 9.94766I$
$b = 2.11021 - 1.04129I$		
$u = -0.691554 + 0.944218I$		
$a = 0.219338 - 0.024885I$	$-4.74262 - 0.98558I$	$-10.53556 - 1.39688I$
$b = 0.996837 - 0.702945I$		
$u = -0.691554 - 0.944218I$		
$a = 0.219338 + 0.024885I$	$-4.74262 + 0.98558I$	$-10.53556 + 1.39688I$
$b = 0.996837 + 0.702945I$		
$u = -0.429290 + 1.094810I$		
$a = 1.52361 + 0.07658I$	$-1.51361 - 4.99339I$	$-1.46170 + 7.63475I$
$b = 2.25201 + 0.30626I$		
$u = -0.429290 - 1.094810I$		
$a = 1.52361 - 0.07658I$	$-1.51361 + 4.99339I$	$-1.46170 - 7.63475I$
$b = 2.25201 - 0.30626I$		
$u = -0.810513$		
$a = -1.68768$	$-1.48600$	$-8.82010$
$b = 0.0637912$		
$u = -0.298599 + 0.749021I$		
$a = -0.230770 + 0.654861I$	$-0.340785 - 1.228130I$	$-3.72246 + 5.05532I$
$b = -0.010961 + 0.514630I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.298599 - 0.749021I$ $a = -0.230770 - 0.654861I$ $b = -0.010961 - 0.514630I$	$-0.340785 + 1.228130I$	$-3.72246 - 5.05532I$
$u = 0.043335 + 1.221830I$ $a = -1.41988 + 0.07791I$ $b = -2.52419 - 0.17469I$	$-10.36550 - 5.41067I$	$-11.07269 + 4.06686I$
$u = 0.043335 - 1.221830I$ $a = -1.41988 - 0.07791I$ $b = -2.52419 + 0.17469I$	$-10.36550 + 5.41067I$	$-11.07269 - 4.06686I$
$u = 0.340574 + 0.682840I$ $a = -0.201912 - 1.203320I$ $b = -1.136840 - 0.348081I$	$1.86966 + 1.36297I$	$7.37182 + 2.84076I$
$u = 0.340574 - 0.682840I$ $a = -0.201912 + 1.203320I$ $b = -1.136840 + 0.348081I$	$1.86966 - 1.36297I$	$7.37182 - 2.84076I$
$u = 0.732733$ $a = 0.0215748$ $b = 0.419703$	$-1.91322$	$-6.72230$
$u = 0.455122 + 1.187290I$ $a = 0.297888 + 0.394001I$ $b = 0.358967 + 0.124690I$	$-5.28776 + 4.30879I$	$-10.28965 - 3.19866I$
$u = 0.455122 - 1.187290I$ $a = 0.297888 - 0.394001I$ $b = 0.358967 - 0.124690I$	$-5.28776 - 4.30879I$	$-10.28965 + 3.19866I$
$u = -0.459206 + 1.219680I$ $a = 0.496160 + 0.913959I$ $b = 0.85669 + 1.97796I$	$-5.08353 - 4.54254I$	$-11.30086 + 4.03212I$
$u = -0.459206 - 1.219680I$ $a = 0.496160 - 0.913959I$ $b = 0.85669 - 1.97796I$	$-5.08353 + 4.54254I$	$-11.30086 - 4.03212I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.395526 + 1.274220I$ $a = 1.88050 + 0.61513I$ $b = 2.81622 - 0.05833I$	$-15.9475 + 8.1867I$	$-9.06394 - 3.34621I$
$u = -0.395526 - 1.274220I$ $a = 1.88050 - 0.61513I$ $b = 2.81622 + 0.05833I$	$-15.9475 - 8.1867I$	$-9.06394 + 3.34621I$
$u = -0.521628 + 1.236120I$ $a = -2.58052 + 0.56454I$ $b = -3.72507 + 0.61373I$	$-15.0274 - 17.7587I$	$-7.82233 + 9.25326I$
$u = -0.521628 - 1.236120I$ $a = -2.58052 - 0.56454I$ $b = -3.72507 - 0.61373I$	$-15.0274 + 17.7587I$	$-7.82233 - 9.25326I$
$u = 0.380735 + 1.301160I$ $a = 1.75721 - 0.48165I$ $b = 2.71281 - 0.14779I$	$-14.8538 + 1.6038I$	$-12.02430 - 0.97260I$
$u = 0.380735 - 1.301160I$ $a = 1.75721 + 0.48165I$ $b = 2.71281 + 0.14779I$	$-14.8538 - 1.6038I$	$-12.02430 + 0.97260I$
$u = 0.538772 + 1.252000I$ $a = -1.97956 - 0.36072I$ $b = -2.92363 - 0.63492I$	$-13.7050 + 8.2667I$	$-10.58240 - 5.91047I$
$u = 0.538772 - 1.252000I$ $a = -1.97956 + 0.36072I$ $b = -2.92363 + 0.63492I$	$-13.7050 - 8.2667I$	$-10.58240 + 5.91047I$
$u = -0.481597 + 0.152677I$ $a = -0.83330 - 1.69163I$ $b = -0.018409 - 0.472499I$	$1.02330 + 1.25064I$	$5.09440 - 3.99293I$
$u = -0.481597 - 0.152677I$ $a = -0.83330 + 1.69163I$ $b = -0.018409 + 0.472499I$	$1.02330 - 1.25064I$	$5.09440 + 3.99293I$



$$\langle 142u^{29}a + u^{29} + \dots - 811a + 77, 4u^{28}a + u^{29} + \dots - 5a + 16, u^{30} + u^{29} + \dots + u - 1 \rangle$$

II.  $I_2^u =$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -0.181354au^{29} - 0.00127714u^{29} + \dots + 1.03576a - 0.0983397 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1.07791au^{29} - 1.96424u^{29} + \dots - 0.00127714a + 2.75351 \\ 1.96424au^{29} - 1.90166u^{29} + \dots + 0.246488a + 3.57216 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.494253au^{29} - 0.609195u^{29} + \dots + 0.0574713a + 0.0919540 \\ 0.132822au^{29} - 0.365262u^{29} + \dots + 0.227331a + 0.874840 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - u^5 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{29} + 8u^{27} + \dots + 4u^3 + u \\ u^{29} + 7u^{27} + \dots - u^3 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1.03576au^{29} - 2.09834u^{29} + \dots - 0.246488a + 1.42784 \\ 0.937420au^{29} + 0.922095u^{29} + \dots + 0.181354a + 2.00128 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -4u^{29} - 4u^{28} - 32u^{27} - 28u^{26} - 120u^{25} - 96u^{24} - 260u^{23} - \\ &196u^{22} - 332u^{21} - 256u^{20} - 196u^{19} - 204u^{18} + 76u^{17} - 72u^{16} + 224u^{15} + 52u^{14} + 136u^{13} + \\ &108u^{12} - 12u^{11} + 100u^{10} - 60u^9 + 44u^8 - 32u^7 - 12u^6 - 8u^5 - 24u^4 + 8u^3 - 12u^2 + 8u - 6 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{30} + 17u^{29} + \dots - u + 1)^2$
$c_2, c_6$	$(u^{30} - u^{29} + \dots - u - 1)^2$
$c_3, c_5$	$(u^{30} + u^{29} + \dots + 7u - 1)^2$
$c_4$	$(u^{30} + u^{29} + \dots + u - 1)^2$
$c_7, c_9, c_{10}$ $c_{12}$	$u^{60} + 11u^{59} + \dots + 20u + 1$
$c_8, c_{11}$	$u^{60} + 5u^{59} + \dots - 23472726u + 8156149$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{30} - 7y^{29} + \dots - 25y + 1)^2$
$c_2, c_6$	$(y^{30} + 17y^{29} + \dots - y + 1)^2$
$c_3, c_5$	$(y^{30} - 31y^{29} + \dots - 49y + 1)^2$
$c_4$	$(y^{30} - 11y^{29} + \dots - y + 1)^2$
$c_7, c_9, c_{10}$ $c_{12}$	$y^{60} + 43y^{59} + \dots + 64y + 1$
$c_8, c_{11}$	$y^{60} - 37y^{59} + \dots - 1403816325059308y + 66522766510201$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.095027 + 1.028250I$		
$a = 1.034680 + 0.226441I$	$-5.04140 - 2.04857I$	$-7.94351 + 2.92796I$
$b = 2.30549 + 0.52767I$		
$u = 0.095027 + 1.028250I$		
$a = 0.716670 + 0.339240I$	$-5.04140 - 2.04857I$	$-7.94351 + 2.92796I$
$b = 0.426153 - 0.394651I$		
$u = 0.095027 - 1.028250I$		
$a = 1.034680 - 0.226441I$	$-5.04140 + 2.04857I$	$-7.94351 - 2.92796I$
$b = 2.30549 - 0.52767I$		
$u = 0.095027 - 1.028250I$		
$a = 0.716670 - 0.339240I$	$-5.04140 + 2.04857I$	$-7.94351 - 2.92796I$
$b = 0.426153 + 0.394651I$		
$u = -0.486868 + 0.916512I$		
$a = -0.940915 - 0.299954I$	$-1.61342 - 2.06909I$	$-0.15841 + 3.38718I$
$b = -1.039270 - 0.311684I$		
$u = -0.486868 + 0.916512I$		
$a = -0.447231 + 0.917418I$	$-1.61342 - 2.06909I$	$-0.15841 + 3.38718I$
$b = -1.24616 + 1.37787I$		
$u = -0.486868 - 0.916512I$		
$a = -0.940915 + 0.299954I$	$-1.61342 + 2.06909I$	$-0.15841 - 3.38718I$
$b = -1.039270 + 0.311684I$		
$u = -0.486868 - 0.916512I$		
$a = -0.447231 - 0.917418I$	$-1.61342 + 2.06909I$	$-0.15841 - 3.38718I$
$b = -1.24616 - 1.37787I$		
$u = 0.336716 + 1.031390I$		
$a = -0.398995 + 0.561283I$	$-6.92657 + 2.97945I$	$-9.92079 - 5.34085I$
$b = -1.50734 - 0.06821I$		
$u = 0.336716 + 1.031390I$		
$a = 0.64157 + 1.48251I$	$-6.92657 + 2.97945I$	$-9.92079 - 5.34085I$
$b = 1.74824 + 1.30378I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.336716 - 1.031390I$ $a = -0.398995 - 0.561283I$ $b = -1.50734 + 0.06821I$	$-6.92657 - 2.97945I$	$-9.92079 + 5.34085I$
$u = 0.336716 - 1.031390I$ $a = 0.64157 - 1.48251I$ $b = 1.74824 - 1.30378I$	$-6.92657 - 2.97945I$	$-9.92079 + 5.34085I$
$u = 0.500817 + 0.966472I$ $a = 0.522463 + 0.779303I$ $b = 0.877769 + 0.011516I$	$-2.27531 + 7.42449I$	$-2.02063 - 8.82247I$
$u = 0.500817 + 0.966472I$ $a = -0.759314 - 1.014940I$ $b = -1.98900 - 1.15324I$	$-2.27531 + 7.42449I$	$-2.02063 - 8.82247I$
$u = 0.500817 - 0.966472I$ $a = 0.522463 - 0.779303I$ $b = 0.877769 - 0.011516I$	$-2.27531 - 7.42449I$	$-2.02063 + 8.82247I$
$u = 0.500817 - 0.966472I$ $a = -0.759314 + 1.014940I$ $b = -1.98900 + 1.15324I$	$-2.27531 - 7.42449I$	$-2.02063 + 8.82247I$
$u = -0.272716 + 0.834978I$ $a = 4.75539 + 1.58121I$ $b = 5.93533 + 1.26168I$	$-3.79299 - 1.32269I$	$-1.12281 + 4.79072I$
$u = -0.272716 + 0.834978I$ $a = 2.73856 - 4.77786I$ $b = 1.76585 - 4.35750I$	$-3.79299 - 1.32269I$	$-1.12281 + 4.79072I$
$u = -0.272716 - 0.834978I$ $a = 4.75539 - 1.58121I$ $b = 5.93533 - 1.26168I$	$-3.79299 + 1.32269I$	$-1.12281 - 4.79072I$
$u = -0.272716 - 0.834978I$ $a = 2.73856 + 4.77786I$ $b = 1.76585 + 4.35750I$	$-3.79299 + 1.32269I$	$-1.12281 - 4.79072I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.856648$		
$a = 0.36456 + 2.45841I$	$-10.8641$	$-7.49220$
$b = -0.369614 + 0.732227I$		
$u = -0.856648$		
$a = 0.36456 - 2.45841I$	$-10.8641$	$-7.49220$
$b = -0.369614 - 0.732227I$		
$u = -0.851057 + 0.073998I$		
$a = 1.134850 + 0.440270I$	$-6.70542 + 6.72016I$	$-3.40084 - 4.93754I$
$b = -0.235397 + 0.177357I$		
$u = -0.851057 + 0.073998I$		
$a = 0.02043 - 2.70525I$	$-6.70542 + 6.72016I$	$-3.40084 - 4.93754I$
$b = 0.471768 - 0.912252I$		
$u = -0.851057 - 0.073998I$		
$a = 1.134850 - 0.440270I$	$-6.70542 - 6.72016I$	$-3.40084 + 4.93754I$
$b = -0.235397 - 0.177357I$		
$u = -0.851057 - 0.073998I$		
$a = 0.02043 + 2.70525I$	$-6.70542 - 6.72016I$	$-3.40084 + 4.93754I$
$b = 0.471768 + 0.912252I$		
$u = 0.814472 + 0.061657I$		
$a = -0.211672 - 0.026337I$	$-5.23568 - 1.35458I$	$-1.234126 + 0.230757I$
$b = -0.622855 + 0.448979I$		
$u = 0.814472 + 0.061657I$		
$a = 0.71424 + 2.65174I$	$-5.23568 - 1.35458I$	$-1.234126 + 0.230757I$
$b = 0.706924 + 1.195690I$		
$u = 0.814472 - 0.061657I$		
$a = -0.211672 + 0.026337I$	$-5.23568 + 1.35458I$	$-1.234126 - 0.230757I$
$b = -0.622855 - 0.448979I$		
$u = 0.814472 - 0.061657I$		
$a = 0.71424 - 2.65174I$	$-5.23568 + 1.35458I$	$-1.234126 - 0.230757I$
$b = 0.706924 - 1.195690I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.517153 + 0.543315I$		
$a = 0.374179 + 1.229410I$	$-0.57483 - 2.05267I$	$2.41797 + 3.48780I$
$b = 0.087079 + 0.755551I$		
$u = -0.517153 + 0.543315I$		
$a = -1.328260 + 0.442484I$	$-0.57483 - 2.05267I$	$2.41797 + 3.48780I$
$b = -0.139959 - 0.267825I$		
$u = -0.517153 - 0.543315I$		
$a = 0.374179 - 1.229410I$	$-0.57483 + 2.05267I$	$2.41797 - 3.48780I$
$b = 0.087079 - 0.755551I$		
$u = -0.517153 - 0.543315I$		
$a = -1.328260 - 0.442484I$	$-0.57483 + 2.05267I$	$2.41797 - 3.48780I$
$b = -0.139959 + 0.267825I$		
$u = 0.552271 + 0.456360I$		
$a = 0.048193 + 0.721700I$	$-0.86006 - 3.18388I$	$1.51706 + 3.33039I$
$b = 0.879122 + 0.103276I$		
$u = 0.552271 + 0.456360I$		
$a = -1.00716 - 1.45803I$	$-0.86006 - 3.18388I$	$1.51706 + 3.33039I$
$b = -0.385363 + 0.145063I$		
$u = 0.552271 - 0.456360I$		
$a = 0.048193 - 0.721700I$	$-0.86006 + 3.18388I$	$1.51706 - 3.33039I$
$b = 0.879122 - 0.103276I$		
$u = 0.552271 - 0.456360I$		
$a = -1.00716 + 1.45803I$	$-0.86006 + 3.18388I$	$1.51706 - 3.33039I$
$b = -0.385363 - 0.145063I$		
$u = 0.429988 + 1.221650I$		
$a = -0.770876 - 0.449946I$	$-9.03965 + 2.99724I$	$-4.94829 - 3.11480I$
$b = -0.527325 - 0.034027I$		
$u = 0.429988 + 1.221650I$		
$a = -2.43427 + 1.26220I$	$-9.03965 + 2.99724I$	$-4.94829 - 3.11480I$
$b = -3.31200 + 0.90775I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.429988 - 1.221650I$ $a = -0.770876 + 0.449946I$ $b = -0.527325 + 0.034027I$	$-9.03965 - 2.99724I$	$-4.94829 + 3.11480I$
$u = 0.429988 - 1.221650I$ $a = -2.43427 - 1.26220I$ $b = -3.31200 - 0.90775I$	$-9.03965 - 2.99724I$	$-4.94829 + 3.11480I$
$u = 0.484811 + 1.215220I$ $a = -0.098795 - 0.799736I$ $b = -0.458370 - 0.566062I$	$-8.64541 + 6.07028I$	$-4.34155 - 3.40396I$
$u = 0.484811 + 1.215220I$ $a = 2.83314 + 0.69066I$ $b = 3.72402 + 0.94519I$	$-8.64541 + 6.07028I$	$-4.34155 - 3.40396I$
$u = 0.484811 - 1.215220I$ $a = -0.098795 + 0.799736I$ $b = -0.458370 + 0.566062I$	$-8.64541 - 6.07028I$	$-4.34155 + 3.40396I$
$u = 0.484811 - 1.215220I$ $a = 2.83314 - 0.69066I$ $b = 3.72402 - 0.94519I$	$-8.64541 - 6.07028I$	$-4.34155 + 3.40396I$
$u = -0.420533 + 1.243280I$ $a = -0.106443 - 0.515997I$ $b = -0.26568 - 1.43136I$	$-10.69750 + 2.28828I$	$-7.38974 - 1.78470I$
$u = -0.420533 + 1.243280I$ $a = -2.05833 - 0.35082I$ $b = -3.04741 + 0.37403I$	$-10.69750 + 2.28828I$	$-7.38974 - 1.78470I$
$u = -0.420533 - 1.243280I$ $a = -0.106443 + 0.515997I$ $b = -0.26568 + 1.43136I$	$-10.69750 - 2.28828I$	$-7.38974 + 1.78470I$
$u = -0.420533 - 1.243280I$ $a = -2.05833 + 0.35082I$ $b = -3.04741 - 0.37403I$	$-10.69750 - 2.28828I$	$-7.38974 + 1.78470I$



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.496075 + 1.226990I$ $a = -0.788632 - 0.515998I$ $b = -1.20409 - 1.35223I$	$-10.1523 - 11.5895I$	$-6.39391 + 7.89908I$
$u = -0.496075 + 1.226990I$ $a = 2.65406 - 0.36532I$ $b = 3.86845 - 0.40313I$	$-10.1523 - 11.5895I$	$-6.39391 + 7.89908I$
$u = -0.496075 - 1.226990I$ $a = -0.788632 + 0.515998I$ $b = -1.20409 + 1.35223I$	$-10.1523 + 11.5895I$	$-6.39391 - 7.89908I$
$u = -0.496075 - 1.226990I$ $a = 2.65406 + 0.36532I$ $b = 3.86845 + 0.40313I$	$-10.1523 + 11.5895I$	$-6.39391 - 7.89908I$
$u = -0.462371 + 1.241170I$ $a = 1.76758 - 0.00509I$ $b = 2.68786 - 0.84395I$	$-14.5974 - 4.6970I$	$-10.66421 + 3.29760I$
$u = -0.462371 + 1.241170I$ $a = -2.42951 + 0.13001I$ $b = -3.65543 + 0.03686I$	$-14.5974 - 4.6970I$	$-10.66421 + 3.29760I$
$u = -0.462371 - 1.241170I$ $a = 1.76758 + 0.00509I$ $b = 2.68786 + 0.84395I$	$-14.5974 + 4.6970I$	$-10.66421 - 3.29760I$
$u = -0.462371 - 1.241170I$ $a = -2.42951 - 0.13001I$ $b = -3.65543 - 0.03686I$	$-14.5974 + 4.6970I$	$-10.66421 - 3.29760I$
$u = 0.441992$ $a = 0.45986 + 1.89002I$ $b = 1.021210 - 0.572546I$	$-4.34249$	$-5.30020$
$u = 0.441992$ $a = 0.45986 - 1.89002I$ $b = 1.021210 + 0.572546I$	$-4.34249$	$-5.30020$

**III.**

$$I_3^u = \langle 2u^4 - 2u^3 + 2u^2 + 2b - u, -2u^2 + 2a + u - 2, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 - \frac{1}{2}u + 1 \\ -u^4 + u^3 - u^2 + \frac{1}{2}u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + \frac{1}{2}u + 1 \\ -u^4 + u^3 - u^2 + \frac{3}{2}u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{3}{2}u^2 + \frac{3}{2} \\ -\frac{3}{2}u^4 + u^3 - u^2 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u^2 + 2 \\ -2u^4 + 2u^3 - 2u^2 + 2u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u^2 + \frac{1}{2} \\ -\frac{1}{2}u^4 + u^3 - u^2 + u \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $\frac{17}{4}u^4 - \frac{17}{4}u^3 + \frac{33}{4}u^2 - 4u + \frac{9}{4}$**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^5 - 3u^4 + 4u^3 - u^2 - u + 1$
$c_2$	$u^5 - u^4 + 2u^3 - u^2 + u - 1$
$c_3$	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
$c_4$	$u^5$
$c_5$	$u^5 - u^4 - 2u^3 + u^2 + u + 1$
$c_6$	$u^5 + u^4 + 2u^3 + u^2 + u + 1$
$c_7, c_9$	$(u + 1)^5$
$c_8$	$32(32u^5 - 16u^4 - 16u^3 + 4u^2 + 2u + 1)$
$c_{10}, c_{12}$	$(u - 1)^5$
$c_{11}$	$32(32u^5 + 16u^4 - 16u^3 - 4u^2 + 2u - 1)$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$
$c_2, c_6$	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$
$c_3, c_5$	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$
$c_4$	$y^5$
$c_7, c_9, c_{10}$ $c_{12}$	$(y - 1)^5$
$c_8, c_{11}$	$1024(1024y^5 - 1280y^4 + 512y^3 - 48y^2 - 4y - 1)$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.339110 + 0.822375I$ $a = 0.608249 - 0.968939I$ $b = 1.036800 + 0.070336I$	$1.31583 - 1.53058I$	$-3.76579 - 4.07189I$
$u = -0.339110 - 0.822375I$ $a = 0.608249 + 0.968939I$ $b = 1.036800 - 0.070336I$	$1.31583 + 1.53058I$	$-3.76579 + 4.07189I$
$u = 0.766826$ $a = 1.20461$ $b = -0.0994683$	$-0.756147$	$3.58700$
$u = 0.455697 + 1.200150I$ $a = -0.460554 + 0.493736I$ $b = -0.73706 + 1.22197I$	$-4.22763 + 4.40083I$	$-0.40273 - 3.06842I$
$u = 0.455697 - 1.200150I$ $a = -0.460554 - 0.493736I$ $b = -0.73706 - 1.22197I$	$-4.22763 - 4.40083I$	$-0.40273 + 3.06842I$

$$\text{IV. } I_4^u = \langle -au + b - 2a + u + 1, a^2 - 2a + 2, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ au + 2a - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a + u - 2 \\ a - 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ a - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} au - u \\ au - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} au + a - u - 2 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$	$(u^2 - u + 1)^2$
$c_2, c_5$	$(u^2 + u + 1)^2$
$c_4$	$u^4 - u^2 + 1$
$c_7, c_9, c_{10}$ $c_{12}$	$(u^2 + 1)^2$
$c_8$	$u^4 - 2u^3 + 2u^2 - 4u + 4$
$c_{11}$	$u^4 + 2u^3 + 2u^2 + 4u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5, c_6$	$(y^2 + y + 1)^2$
$c_4$	$(y^2 - y + 1)^2$
$c_7, c_9, c_{10}$ $c_{12}$	$(y + 1)^4$
$c_8, c_{11}$	$y^4 - 4y^2 + 16$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 1.00000 + 1.00000I$	$-3.28987 - 2.02988I$	$-6.00000 + 3.46410I$
$b = 0.13397 + 1.50000I$		
$u = -0.500000 + 0.866025I$		
$a = 1.00000 - 1.00000I$	$-3.28987 - 2.02988I$	$-6.00000 + 3.46410I$
$b = 1.86603 - 1.50000I$		
$u = -0.500000 - 0.866025I$		
$a = 1.00000 + 1.00000I$	$-3.28987 + 2.02988I$	$-6.00000 - 3.46410I$
$b = 1.86603 + 1.50000I$		
$u = -0.500000 - 0.866025I$		
$a = 1.00000 - 1.00000I$	$-3.28987 + 2.02988I$	$-6.00000 - 3.46410I$
$b = 0.13397 - 1.50000I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^2)(u^5 - 3u^4 + \dots - u + 1)(u^{30} + 17u^{29} + \dots - u + 1)^2 \cdot (u^{40} + 22u^{39} + \dots - u + 16)$
$c_2$	$((u^2 + u + 1)^2)(u^5 - u^4 + \dots + u - 1)(u^{30} - u^{29} + \dots - u - 1)^2 \cdot (u^{40} - 2u^{39} + \dots + 15u - 4)$
$c_3$	$((u^2 - u + 1)^2)(u^5 + u^4 + \dots + u - 1)(u^{30} + u^{29} + \dots + 7u - 1)^2 \cdot (u^{40} + 2u^{39} + \dots + 871u - 676)$
$c_4$	$u^5(u^4 - u^2 + 1)(u^{30} + u^{29} + \dots + u - 1)^2 \cdot (u^{40} - 3u^{39} + \dots + 512u + 2048)$
$c_5$	$((u^2 + u + 1)^2)(u^5 - u^4 + \dots + u + 1)(u^{30} + u^{29} + \dots + 7u - 1)^2 \cdot (u^{40} + 2u^{39} + \dots + 871u - 676)$
$c_6$	$((u^2 - u + 1)^2)(u^5 + u^4 + \dots + u + 1)(u^{30} - u^{29} + \dots - u - 1)^2 \cdot (u^{40} - 2u^{39} + \dots + 15u - 4)$
$c_7, c_9$	$((u + 1)^5)(u^2 + 1)^2(u^{40} - 5u^{39} + \dots - 3u - 1) \cdot (u^{60} + 11u^{59} + \dots + 20u + 1)$
$c_8$	$1024(u^4 - 2u^3 + \dots - 4u + 4)(32u^5 - 16u^4 + \dots + 2u + 1) \cdot (32u^{40} + 48u^{39} + \dots + 8u + 4) \cdot (u^{60} + 5u^{59} + \dots - 23472726u + 8156149)$
$c_{10}, c_{12}$	$((u - 1)^5)(u^2 + 1)^2(u^{40} - 5u^{39} + \dots - 3u - 1) \cdot (u^{60} + 11u^{59} + \dots + 20u + 1)$
$c_{11}$	$1024(u^4 + 2u^3 + \dots + 4u + 4)(32u^5 + 16u^4 + \dots + 2u - 1) \cdot (32u^{40} + 48u^{39} + \dots + 8u + 4) \cdot (u^{60} + 5u^{59} + \dots - 23472726u + 8156149)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 + y + 1)^2(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)$ $\cdot ((y^{30} - 7y^{29} + \dots - 25y + 1)^2)(y^{40} - 6y^{39} + \dots - 3905y + 256)$
$c_2, c_6$	$((y^2 + y + 1)^2)(y^5 + 3y^4 + \dots - y - 1)(y^{30} + 17y^{29} + \dots - y + 1)^2$ $\cdot (y^{40} + 22y^{39} + \dots - y + 16)$
$c_3, c_5$	$(y^2 + y + 1)^2(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)$ $\cdot (y^{30} - 31y^{29} + \dots - 49y + 1)^2$ $\cdot (y^{40} - 34y^{39} + \dots + 2269839y + 456976)$
$c_4$	$y^5(y^2 - y + 1)^2(y^{30} - 11y^{29} + \dots - y + 1)^2$ $\cdot (y^{40} - 13y^{39} + \dots - 63176704y + 4194304)$
$c_7, c_9, c_{10}$ $c_{12}$	$((y - 1)^5)(y + 1)^4(y^{40} + 27y^{39} + \dots + 25y + 1)$ $\cdot (y^{60} + 43y^{59} + \dots + 64y + 1)$
$c_8, c_{11}$	$1048576(y^4 - 4y^2 + 16)(1024y^5 - 1280y^4 + \dots - 4y - 1)$ $\cdot (1024y^{40} - 27904y^{39} + \dots + 16y + 16)$ $\cdot (y^{60} - 37y^{59} + \dots - 1403816325059308y + 66522766510201)$