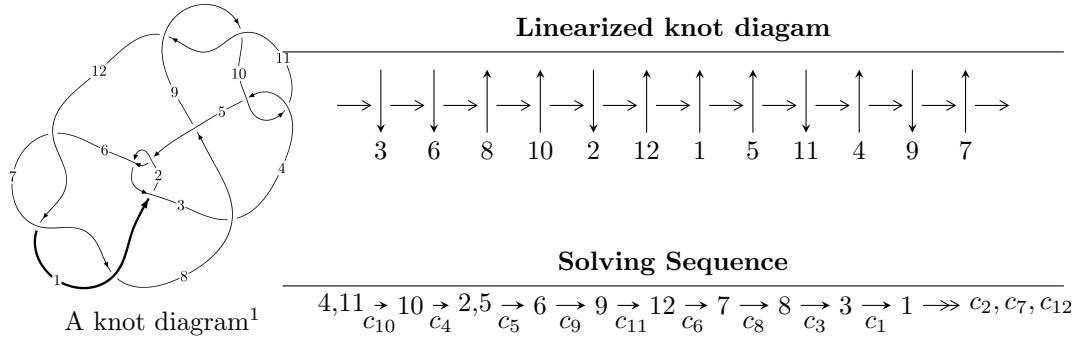


## $12a_{0298}$ ( $K12a_{0298}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -u^{66} - 10u^{64} + \dots + 4b - 4u, -u^{66} - 11u^{64} + \dots + 4a - 2, u^{69} + 2u^{68} + \dots - 2u^2 + 2 \rangle$$

$$I_2^u = \langle -412u^8a^2 + 444u^8a + \dots - 624a + 202, 2u^8a^2 - u^8a + \dots - a + 1,$$

$$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1 \rangle$$

$$I_3^u = \langle 2u^3 + u^2 + b + u + 1, u^3 + 2a + 3u + 2, u^4 + u^2 + 2 \rangle$$

$$I_4^u = \langle b + u, a + 2u - 1, u^2 + 1 \rangle$$

$$I_5^u = \langle -u^3 - u^2 + b - 2u + 1, u^3 - u^2 + a - u, u^4 + 1 \rangle$$

$$I_1^v = \langle a, b + 1, v - 1 \rangle$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 107 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^{66} - 10u^{64} + \dots + 4b - 4u, -u^{66} - 11u^{64} + \dots + 4a - 2, u^{69} + 2u^{68} + \dots - 2u^2 + 2 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{4}u^{66} + \frac{11}{4}u^{64} + \dots - \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{4}u^{66} + \frac{5}{2}u^{64} + \dots - \frac{9}{2}u^4 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^{68} + \frac{11}{2}u^{66} + \dots + u - \frac{3}{2} \\ u^{68} + u^{67} + \dots + \frac{1}{2}u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{4}u^{63} - \frac{5}{2}u^{61} + \dots + \frac{1}{2}u - 1 \\ -\frac{1}{4}u^{65} - \frac{11}{4}u^{63} + \dots - \frac{5}{2}u^2 + \frac{1}{2}u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^6 + u^4 + 2u^2 + 1 \\ u^8 + 2u^6 + 2u^4 + 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{13} - 2u^{11} - 5u^9 - 6u^7 - 6u^5 - 4u^3 - u \\ -u^{15} - 3u^{13} - 6u^{11} - 9u^9 - 8u^7 - 6u^5 - 2u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{4}u^{61} + \frac{5}{2}u^{59} + \dots - u^2 + 1 \\ \frac{1}{4}u^{61} + \frac{9}{4}u^{59} + \dots - \frac{1}{2}u^2 + \frac{1}{2}u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $2u^{68} + 4u^{67} + \dots - 10u + 8$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{69} + 26u^{68} + \cdots + 3481u + 256$
$c_2, c_5$	$u^{69} + 2u^{68} + \cdots - 5u - 16$
$c_3$	$u^{69} - 2u^{68} + \cdots - 188076u - 54322$
$c_4, c_{10}$	$u^{69} - 2u^{68} + \cdots + 2u^2 - 2$
$c_6, c_7, c_{12}$	$u^{69} - 2u^{68} + \cdots - 37u - 16$
$c_8$	$u^{69} + 10u^{68} + \cdots - 2116u - 86$
$c_9, c_{11}$	$u^{69} + 22u^{68} + \cdots + 8u - 4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{69} + 46y^{68} + \cdots - 2589327y - 65536$
$c_2, c_5$	$y^{69} - 26y^{68} + \cdots + 3481y - 256$
$c_3$	$y^{69} - 26y^{68} + \cdots + 15690417448y - 2950879684$
$c_4, c_{10}$	$y^{69} + 22y^{68} + \cdots + 8y - 4$
$c_6, c_7, c_{12}$	$y^{69} - 74y^{68} + \cdots - 10919y - 256$
$c_8$	$y^{69} - 2y^{68} + \cdots - 1189944y - 7396$
$c_9, c_{11}$	$y^{69} + 50y^{68} + \cdots + 768y - 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.735899 + 0.688576I$		
$a = -1.41058 - 0.11854I$	$-0.240515 + 0.033439I$	$-1.48136 + 0.I$
$b = -0.96277 + 2.11478I$		
$u = -0.735899 - 0.688576I$		
$a = -1.41058 + 0.11854I$	$-0.240515 - 0.033439I$	$-1.48136 + 0.I$
$b = -0.96277 - 2.11478I$		
$u = 0.338664 + 0.953969I$		
$a = 0.259722 + 0.602753I$	$5.18981 + 0.99757I$	$4.76342 - 3.46084I$
$b = 0.242668 + 1.080750I$		
$u = 0.338664 - 0.953969I$		
$a = 0.259722 - 0.602753I$	$5.18981 - 0.99757I$	$4.76342 + 3.46084I$
$b = 0.242668 - 1.080750I$		
$u = 0.484849 + 0.860276I$		
$a = 1.27015 + 0.75092I$	$-1.85693 - 1.13119I$	$-2.07731 + 1.47337I$
$b = -0.89181 + 2.10893I$		
$u = 0.484849 - 0.860276I$		
$a = 1.27015 - 0.75092I$	$-1.85693 + 1.13119I$	$-2.07731 - 1.47337I$
$b = -0.89181 - 2.10893I$		
$u = 0.058334 + 1.021690I$		
$a = 0.24060 - 2.11026I$	$-5.74447 - 0.01900I$	$-8.65927 + 0.I$
$b = 0.529272 - 0.918124I$		
$u = 0.058334 - 1.021690I$		
$a = 0.24060 + 2.11026I$	$-5.74447 + 0.01900I$	$-8.65927 + 0.I$
$b = 0.529272 + 0.918124I$		
$u = 0.154964 + 1.031240I$		
$a = -0.85296 + 1.99168I$	$-3.54966 + 6.72812I$	$-3.30535 - 7.86468I$
$b = -0.216276 + 0.724886I$		
$u = 0.154964 - 1.031240I$		
$a = -0.85296 - 1.99168I$	$-3.54966 - 6.72812I$	$-3.30535 + 7.86468I$
$b = -0.216276 - 0.724886I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.718154 + 0.761613I$		
$a = 0.040869 + 0.875751I$	$3.60394 - 0.19911I$	$9.90804 + 0.I$
$b = -0.531478 + 0.949465I$		
$u = 0.718154 - 0.761613I$		
$a = 0.040869 - 0.875751I$	$3.60394 + 0.19911I$	$9.90804 + 0.I$
$b = -0.531478 - 0.949465I$		
$u = -0.422383 + 0.968673I$		
$a = -0.599532 + 1.252790I$	$3.61056 + 4.51985I$	$0$
$b = 1.85369 + 1.47586I$		
$u = -0.422383 - 0.968673I$		
$a = -0.599532 - 1.252790I$	$3.61056 - 4.51985I$	$0$
$b = 1.85369 - 1.47586I$		
$u = 0.193872 + 1.039360I$		
$a = -0.624526 + 0.079575I$	$4.24263 + 5.04361I$	$0. - 4.03426I$
$b = -0.927525 - 0.005005I$		
$u = 0.193872 - 1.039360I$		
$a = -0.624526 - 0.079575I$	$4.24263 - 5.04361I$	$0. + 4.03426I$
$b = -0.927525 + 0.005005I$		
$u = 0.721986 + 0.582383I$		
$a = 1.020400 - 0.497911I$	$3.90829 + 1.18050I$	$7.40920 - 3.02522I$
$b = 1.35891 + 1.25471I$		
$u = 0.721986 - 0.582383I$		
$a = 1.020400 + 0.497911I$	$3.90829 - 1.18050I$	$7.40920 + 3.02522I$
$b = 1.35891 - 1.25471I$		
$u = -0.814686 + 0.705728I$		
$a = 2.39011 + 0.79666I$	$2.93810 + 6.44249I$	$0$
$b = 2.59506 - 2.01293I$		
$u = -0.814686 - 0.705728I$		
$a = 2.39011 - 0.79666I$	$2.93810 - 6.44249I$	$0$
$b = 2.59506 + 2.01293I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.028573 + 1.077810I$	$-1.60521 + 2.06429I$	0
$a = -0.61215 - 1.87207I$		
$b = -0.511359 - 0.452462I$		
$u = -0.028573 - 1.077810I$	$-1.60521 - 2.06429I$	0
$a = -0.61215 + 1.87207I$		
$b = -0.511359 + 0.452462I$		
$u = -0.170360 + 1.066470I$	$2.10642 - 10.83270I$	$0. + 7.91871I$
$a = 0.37501 + 2.28994I$		
$b = 0.350653 + 0.759401I$		
$u = -0.170360 - 1.066470I$	$2.10642 + 10.83270I$	$0. - 7.91871I$
$a = 0.37501 - 2.28994I$		
$b = 0.350653 - 0.759401I$		
$u = 0.836381 + 0.694622I$	$8.89008 - 10.76610I$	0
$a = -2.53666 + 0.36324I$		
$b = -2.27305 - 2.69677I$		
$u = 0.836381 - 0.694622I$	$8.89008 + 10.76610I$	0
$a = -2.53666 - 0.36324I$		
$b = -2.27305 + 2.69677I$		
$u = -0.833721 + 0.715169I$	$11.06750 + 4.64835I$	0
$a = -0.612597 + 0.721125I$		
$b = 0.402951 + 0.631456I$		
$u = -0.833721 - 0.715169I$	$11.06750 - 4.64835I$	0
$a = -0.612597 - 0.721125I$		
$b = 0.402951 - 0.631456I$		
$u = -0.788117 + 0.777559I$	$4.23303 - 3.52292I$	0
$a = -0.860399 - 0.145200I$		
$b = -1.208460 - 0.042361I$		
$u = -0.788117 - 0.777559I$	$4.23303 + 3.52292I$	0
$a = -0.860399 + 0.145200I$		
$b = -1.208460 + 0.042361I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.821959 + 0.782703I$		
$a = 1.141410 + 0.345243I$	$12.26590 - 0.79570I$	0
$b = 0.680996 - 0.881071I$		
$u = -0.821959 - 0.782703I$		
$a = 1.141410 - 0.345243I$	$12.26590 + 0.79570I$	0
$b = 0.680996 + 0.881071I$		
$u = 0.611116 + 0.956461I$		
$a = -0.49978 - 2.05095I$	$-2.54832 + 5.58402I$	0
$b = 2.42886 - 2.48221I$		
$u = 0.611116 - 0.956461I$		
$a = -0.49978 + 2.05095I$	$-2.54832 - 5.58402I$	0
$b = 2.42886 + 2.48221I$		
$u = 0.814707 + 0.809092I$		
$a = 0.295475 - 0.322981I$	$10.93290 + 7.02859I$	0
$b = 0.913082 - 1.062150I$		
$u = 0.814707 - 0.809092I$		
$a = 0.295475 + 0.322981I$	$10.93290 - 7.02859I$	0
$b = 0.913082 + 1.062150I$		
$u = 0.695607 + 0.941949I$		
$a = -0.886074 - 0.080146I$	$3.05990 + 5.61567I$	0
$b = -0.262992 - 0.787216I$		
$u = 0.695607 - 0.941949I$		
$a = -0.886074 + 0.080146I$	$3.05990 - 5.61567I$	0
$b = -0.262992 + 0.787216I$		
$u = -0.044024 + 0.818063I$		
$a = 0.652335 - 0.322162I$	$-1.27770 - 1.44146I$	$0.19549 + 5.54807I$
$b = -0.167905 + 0.623453I$		
$u = -0.044024 - 0.818063I$		
$a = 0.652335 + 0.322162I$	$-1.27770 + 1.44146I$	$0.19549 - 5.54807I$
$b = -0.167905 - 0.623453I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.613808 + 1.009340I$		
$a = 0.84248 - 1.87193I$	$1.96131 - 8.32605I$	0
$b = -2.04716 - 2.64513I$		
$u = -0.613808 - 1.009340I$		
$a = 0.84248 + 1.87193I$	$1.96131 + 8.32605I$	0
$b = -2.04716 + 2.64513I$		
$u = -0.662707 + 0.477450I$		
$a = -1.86190 + 0.54426I$	$3.39108 + 3.42806I$	$6.35256 - 3.02642I$
$b = -0.57360 + 1.90850I$		
$u = -0.662707 - 0.477450I$		
$a = -1.86190 - 0.54426I$	$3.39108 - 3.42806I$	$6.35256 + 3.02642I$
$b = -0.57360 - 1.90850I$		
$u = -0.737691 + 0.955567I$		
$a = -0.388118 - 0.820537I$	$3.68498 - 2.23055I$	0
$b = -0.573332 + 0.251331I$		
$u = -0.737691 - 0.955567I$		
$a = -0.388118 + 0.820537I$	$3.68498 + 2.23055I$	0
$b = -0.573332 - 0.251331I$		
$u = -0.689892 + 0.991018I$		
$a = 0.09117 - 1.66872I$	$-1.14588 - 5.49156I$	0
$b = -2.85026 - 1.61053I$		
$u = -0.689892 - 0.991018I$		
$a = 0.09117 + 1.66872I$	$-1.14588 + 5.49156I$	0
$b = -2.85026 + 1.61053I$		
$u = 0.659252 + 1.016190I$		
$a = 0.137976 - 1.363260I$	$2.66779 + 4.10740I$	0
$b = 2.56392 - 0.66959I$		
$u = 0.659252 - 1.016190I$		
$a = 0.137976 + 1.363260I$	$2.66779 - 4.10740I$	0
$b = 2.56392 + 0.66959I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.771414 + 0.943358I$		
$a = 0.552899 - 0.216552I$	$10.51840 - 1.09087I$	0
$b = -0.327428 + 0.913552I$		
$u = 0.771414 - 0.943358I$		
$a = 0.552899 + 0.216552I$	$10.51840 + 1.09087I$	0
$b = -0.327428 - 0.913552I$		
$u = -0.764178 + 0.965173I$		
$a = 0.412858 + 1.010290I$	$11.70390 - 5.14096I$	0
$b = 1.49440 + 0.94058I$		
$u = -0.764178 - 0.965173I$		
$a = 0.412858 - 1.010290I$	$11.70390 + 5.14096I$	0
$b = 1.49440 - 0.94058I$		
$u = -0.729127 + 1.006320I$		
$a = 0.85456 + 2.40770I$	$2.02182 - 12.24190I$	0
$b = 4.06882 + 0.97788I$		
$u = -0.729127 - 1.006320I$		
$a = 0.85456 - 2.40770I$	$2.02182 + 12.24190I$	0
$b = 4.06882 - 0.97788I$		
$u = -0.741771 + 1.008840I$		
$a = 0.545247 - 0.543242I$	$10.1674 - 10.5435I$	0
$b = 0.321004 - 1.292670I$		
$u = -0.741771 - 1.008840I$		
$a = 0.545247 + 0.543242I$	$10.1674 + 10.5435I$	0
$b = 0.321004 + 1.292670I$		
$u = 0.734769 + 1.019640I$		
$a = -0.36453 + 2.55787I$	$7.8960 + 16.6434I$	0
$b = -4.11635 + 1.81421I$		
$u = 0.734769 - 1.019640I$		
$a = -0.36453 - 2.55787I$	$7.8960 - 16.6434I$	0
$b = -4.11635 - 1.81421I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.670400 + 0.147828I$		
$a = 1.80229 + 0.50503I$	$6.05766 - 8.22168I$	$7.69702 + 5.92932I$
$b = 1.30651 - 0.96838I$		
$u = -0.670400 - 0.147828I$		
$a = 1.80229 - 0.50503I$	$6.05766 + 8.22168I$	$7.69702 - 5.92932I$
$b = 1.30651 + 0.96838I$		
$u = 0.656891 + 0.088355I$		
$a = -0.868107 - 1.024770I$	$7.87968 + 2.33195I$	$10.31373 - 1.18340I$
$b = -0.163464 - 0.301668I$		
$u = 0.656891 - 0.088355I$		
$a = -0.868107 + 1.024770I$	$7.87968 - 2.33195I$	$10.31373 + 1.18340I$
$b = -0.163464 + 0.301668I$		
$u = 0.412551 + 0.453150I$		
$a = 1.75896 - 0.29485I$	$-1.61119 - 1.13122I$	$-1.25895 + 1.21665I$
$b = 0.385319 + 1.182700I$		
$u = 0.412551 - 0.453150I$		
$a = 1.75896 + 0.29485I$	$-1.61119 + 1.13122I$	$-1.25895 - 1.21665I$
$b = 0.385319 - 1.182700I$		
$u = 0.591730 + 0.129745I$		
$a = -1.49243 + 0.30843I$	$0.12986 + 4.40376I$	$4.64576 - 6.38172I$
$b = -0.650903 - 1.070410I$		
$u = 0.591730 - 0.129745I$		
$a = -1.49243 - 0.30843I$	$0.12986 - 4.40376I$	$4.64576 + 6.38172I$
$b = -0.650903 + 1.070410I$		
$u = -0.371894$		
$a = 0.571634$	$0.931539$	$11.9680$
$b = -0.480013$		

$$\text{II. } I_2^u = \langle -412u^8a^2 + 444u^8a + \cdots - 624a + 202, 2u^8a^2 - u^8a + \cdots - a + 1, u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ 0.235026a^2u^8 - 0.253280au^8 + \cdots + 0.355961a - 0.115231 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.13862a^2u^8 + 0.287507au^8 + \cdots + 0.190531a - 0.247576 \\ 0.854535a^2u^8 + 1.25385au^8 + \cdots - 1.11352a + 0.309184 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.983457a^2u^8 - 0.108386au^8 + \cdots - 0.0638905a - 0.851112 \\ 0.826013a^2u^8 + 1.34284au^8 + \cdots - 1.29264a + 0.565887 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^6 + u^4 + 2u^2 + 1 \\ u^8 + 2u^6 + 2u^4 + 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.142042a^2u^8 + 0.483172au^8 + \cdots - 0.652025a + 0.278380 \\ 0.157444a^2u^8 - 0.451226au^8 + \cdots - 0.771249a - 1.41700 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^7 + 4u^6 - 4u^5 + 4u^4 - 8u^3 + 4u^2 + 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{27} + 18u^{26} + \cdots + u + 1$
$c_2, c_5, c_6$ $c_7, c_{12}$	$u^{27} - 9u^{25} + \cdots + u + 1$
$c_3$	$(u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)^3$
$c_4, c_{10}$	$(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)^3$
$c_8$	$(u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1)^3$
$c_9, c_{11}$	$(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)^3$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{27} - 18y^{26} + \cdots + y - 1$
$c_2, c_5, c_6$ $c_7, c_{12}$	$y^{27} - 18y^{26} + \cdots + y - 1$
$c_3$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3$
$c_4, c_{10}$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^3$
$c_8$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^3$
$c_9, c_{11}$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.140343 + 0.966856I$		
$a = 1.25673 + 1.05313I$	$-1.78344 - 2.09337I$	$-0.51499 + 4.16283I$
$b = 0.049646 + 0.706168I$		
$u = -0.140343 + 0.966856I$		
$a = 0.163898 - 0.278866I$	$-1.78344 - 2.09337I$	$-0.51499 + 4.16283I$
$b = 0.601292 + 0.256808I$		
$u = -0.140343 + 0.966856I$		
$a = -0.01736 - 2.34952I$	$-1.78344 - 2.09337I$	$-0.51499 + 4.16283I$
$b = -0.95932 - 1.47752I$		
$u = -0.140343 - 0.966856I$		
$a = 1.25673 - 1.05313I$	$-1.78344 + 2.09337I$	$-0.51499 - 4.16283I$
$b = 0.049646 - 0.706168I$		
$u = -0.140343 - 0.966856I$		
$a = 0.163898 + 0.278866I$	$-1.78344 + 2.09337I$	$-0.51499 - 4.16283I$
$b = 0.601292 - 0.256808I$		
$u = -0.140343 - 0.966856I$		
$a = -0.01736 + 2.34952I$	$-1.78344 + 2.09337I$	$-0.51499 - 4.16283I$
$b = -0.95932 + 1.47752I$		
$u = -0.628449 + 0.875112I$		
$a = 0.0738554 + 0.0112823I$	$0.61694 - 2.45442I$	$2.32792 + 2.91298I$
$b = -0.329184 + 0.287114I$		
$u = -0.628449 + 0.875112I$		
$a = -2.10033 + 0.25220I$	$0.61694 - 2.45442I$	$2.32792 + 2.91298I$
$b = -0.22682 + 3.11202I$		
$u = -0.628449 + 0.875112I$		
$a = 0.05733 - 2.33941I$	$0.61694 - 2.45442I$	$2.32792 + 2.91298I$
$b = -2.96621 - 2.53925I$		
$u = -0.628449 - 0.875112I$		
$a = 0.0738554 - 0.0112823I$	$0.61694 + 2.45442I$	$2.32792 - 2.91298I$
$b = -0.329184 - 0.287114I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.628449 - 0.875112I$		
$a = -2.10033 - 0.25220I$	$0.61694 + 2.45442I$	$2.32792 - 2.91298I$
$b = -0.22682 - 3.11202I$		
$u = -0.628449 - 0.875112I$		
$a = 0.05733 + 2.33941I$	$0.61694 + 2.45442I$	$2.32792 - 2.91298I$
$b = -2.96621 + 2.53925I$		
$u = 0.796005 + 0.733148I$		
$a = 0.897099 + 0.478488I$	$4.37135 - 1.33617I$	$7.28409 + 0.70175I$
$b = 0.366734 + 0.756648I$		
$u = 0.796005 + 0.733148I$		
$a = 1.64130 - 0.08440I$	$4.37135 - 1.33617I$	$7.28409 + 0.70175I$
$b = 1.01907 + 2.73861I$		
$u = 0.796005 + 0.733148I$		
$a = -1.69292 + 1.13699I$	$4.37135 - 1.33617I$	$7.28409 + 0.70175I$
$b = -2.24611 - 0.83019I$		
$u = 0.796005 - 0.733148I$		
$a = 0.897099 - 0.478488I$	$4.37135 + 1.33617I$	$7.28409 - 0.70175I$
$b = 0.366734 - 0.756648I$		
$u = 0.796005 - 0.733148I$		
$a = 1.64130 + 0.08440I$	$4.37135 + 1.33617I$	$7.28409 - 0.70175I$
$b = 1.01907 - 2.73861I$		
$u = 0.796005 - 0.733148I$		
$a = -1.69292 - 1.13699I$	$4.37135 + 1.33617I$	$7.28409 - 0.70175I$
$b = -2.24611 + 0.83019I$		
$u = 0.728966 + 0.986295I$		
$a = -0.280859 - 0.864363I$	$3.59813 + 7.08493I$	$5.57680 - 5.91335I$
$b = 0.366463 - 0.892237I$		
$u = 0.728966 + 0.986295I$		
$a = -0.12458 - 1.78606I$	$3.59813 + 7.08493I$	$5.57680 - 5.91335I$
$b = 3.23510 - 2.02570I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.728966 + 0.986295I$		
$a = -1.25383 + 1.67614I$	$3.59813 + 7.08493I$	$5.57680 - 5.91335I$
$b = -3.12748 - 0.01225I$		
$u = 0.728966 - 0.986295I$		
$a = -0.280859 + 0.864363I$	$3.59813 - 7.08493I$	$5.57680 + 5.91335I$
$b = 0.366463 + 0.892237I$		
$u = 0.728966 - 0.986295I$		
$a = -0.12458 + 1.78606I$	$3.59813 - 7.08493I$	$5.57680 + 5.91335I$
$b = 3.23510 + 2.02570I$		
$u = 0.728966 - 0.986295I$		
$a = -1.25383 - 1.67614I$	$3.59813 - 7.08493I$	$5.57680 + 5.91335I$
$b = -3.12748 + 0.01225I$		
$u = -0.512358$		
$a = 0.923120 + 0.394259I$	1.19845	8.65230
$b = -0.085863 - 0.444563I$		
$u = -0.512358$		
$a = 0.923120 - 0.394259I$	1.19845	8.65230
$b = -0.085863 + 0.444563I$		
$u = -0.512358$		
$a = -3.08692$	1.19845	8.65230
$b = -1.39464$		

$$\text{III. } I_3^u = \langle 2u^3 + u^2 + b + u + 1, \ u^3 + 2a + 3u + 2, \ u^4 + u^2 + 2 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u^3 - \frac{3}{2}u - 1 \\ -2u^3 - u^2 - u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}u^3 - \frac{1}{2}u - 1 \\ -u^3 - u^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -u^2 - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{2}u^3 - \frac{1}{2}u \\ -u^3 + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 + 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{2}u^3 - \frac{1}{2}u - 1 \\ -u^3 - u^2 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4u^2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$ $c_7$	$(u - 1)^4$
$c_2, c_{12}$	$(u + 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$u^4 + u^2 + 2$
$c_9$	$(u^2 - u + 2)^2$
$c_{11}$	$(u^2 + u + 2)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_7, c_{12}$	$(y - 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$(y^2 + y + 2)^2$
$c_9, c_{11}$	$(y^2 + 3y + 4)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.676097 + 0.978318I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.19802 - 1.67009I$	$0.82247 + 5.33349I$	$2.00000 - 5.29150I$
$b = 2.08839 - 3.11166I$		
$u = 0.676097 - 0.978318I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.19802 + 1.67009I$	$0.82247 - 5.33349I$	$2.00000 + 5.29150I$
$b = 2.08839 + 3.11166I$		
$u = -0.676097 + 0.978318I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.80198 - 1.67009I$	$0.82247 - 5.33349I$	$2.00000 + 5.29150I$
$b = -3.08839 - 0.46591I$		
$u = -0.676097 - 0.978318I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.80198 + 1.67009I$	$0.82247 + 5.33349I$	$2.00000 - 5.29150I$
$b = -3.08839 + 0.46591I$		

$$\text{IV. } I_4^u = \langle b + u, a + 2u - 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -2u + 1 \\ -u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u + 1 \\ -u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ -1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1 \\ 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ -u - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -1 \\ -1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u + 1 \\ -u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -4

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$ $c_7, c_9$	$(u - 1)^2$
$c_2, c_{11}, c_{12}$	$(u + 1)^2$
$c_3, c_4, c_8$ $c_{10}$	$u^2 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_7, c_9$ $c_{11}, c_{12}$	$(y - 1)^2$
$c_3, c_4, c_8$ $c_{10}$	$(y + 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$		
$a = 1.00000 - 2.00000I$	-3.28987	-4.00000
$b = -1.000000I$		
$u = -1.000000I$		
$a = 1.00000 + 2.00000I$	-3.28987	-4.00000
$b = 1.000000I$		

$$\mathbf{V. } I_5^u = \langle -u^3 - u^2 + b - 2u + 1, \ u^3 - u^2 + a - u, \ u^4 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^3 + u^2 + u \\ u^3 + u^2 + 2u - 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^3 - u^2 \\ -u^2 - u + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^2 \\ -1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^3 \\ -u^2 - u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^2 \\ -1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^3 + u^2 \\ u^2 + u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_{12}$	$(u - 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$u^4 + 1$
$c_5, c_6, c_7$	$(u + 1)^4$
$c_9, c_{11}$	$(u^2 + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_7, c_{12}$	$(y - 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$(y^2 + 1)^2$
$c_9, c_{11}$	$(y + 1)^4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.707107 + 0.707107I$		
$a = 1.41421 + 1.00000I$	1.64493	4.00000
$b = -0.29289 + 3.12132I$		
$u = 0.707107 - 0.707107I$		
$a = 1.41421 - 1.00000I$	1.64493	4.00000
$b = -0.29289 - 3.12132I$		
$u = -0.707107 + 0.707107I$		
$a = -1.41421 - 1.00000I$	1.64493	4.00000
$b = -1.70711 + 1.12132I$		
$u = -0.707107 - 0.707107I$		
$a = -1.41421 + 1.00000I$	1.64493	4.00000
$b = -1.70711 - 1.12132I$		

$$\text{VI. } I_1^v = \langle a, b+1, v-1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_{12}$	$u - 1$
$c_3, c_4, c_8$ $c_9, c_{10}, c_{11}$	$u$
$c_5, c_6, c_7$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_7, c_{12}$	$y - 1$
$c_3, c_4, c_8$ $c_9, c_{10}, c_{11}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$	0	0
$b = -1.00000$		

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^{11})(u^{27} + 18u^{26} + \dots + u + 1)(u^{69} + 26u^{68} + \dots + 3481u + 256)$
$c_2$	$((u - 1)^5)(u + 1)^6(u^{27} - 9u^{25} + \dots + u + 1)(u^{69} + 2u^{68} + \dots - 5u - 16)$
$c_3$	$u(u^2 + 1)(u^4 + 1)(u^4 + u^2 + 2)$ $\cdot (u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)^3$ $\cdot (u^{69} - 2u^{68} + \dots - 188076u - 54322)$
$c_4, c_{10}$	$u(u^2 + 1)(u^4 + 1)(u^4 + u^2 + 2)(u^9 + u^8 + \dots + u - 1)^3$ $\cdot (u^{69} - 2u^{68} + \dots + 2u^2 - 2)$
$c_5$	$((u - 1)^6)(u + 1)^5(u^{27} - 9u^{25} + \dots + u + 1)(u^{69} + 2u^{68} + \dots - 5u - 16)$
$c_6, c_7$	$((u - 1)^6)(u + 1)^5(u^{27} - 9u^{25} + \dots + u + 1)$ $\cdot (u^{69} - 2u^{68} + \dots - 37u - 16)$
$c_8$	$u(u^2 + 1)(u^4 + 1)(u^4 + u^2 + 2)$ $\cdot (u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1)^3$ $\cdot (u^{69} + 10u^{68} + \dots - 2116u - 86)$
$c_9$	$u(u - 1)^2(u^2 + 1)^2(u^2 - u + 2)^2$ $\cdot (u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)^3$ $\cdot (u^{69} + 22u^{68} + \dots + 8u - 4)$
$c_{11}$	$u(u + 1)^2(u^2 + 1)^2(u^2 + u + 2)^2$ $\cdot (u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)^3$ $\cdot (u^{69} + 22u^{68} + \dots + 8u - 4)$
$c_{12}$	$((u - 1)^5)(u + 1)^6(u^{27} - 9u^{25} + \dots + u + 1)$ $\cdot (u^{69} - 2u^{68} + \dots - 37u - 16)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^{11})(y^{27} - 18y^{26} + \dots + y - 1)$ $\cdot (y^{69} + 46y^{68} + \dots - 2589327y - 65536)$
$c_2, c_5$	$((y - 1)^{11})(y^{27} - 18y^{26} + \dots + y - 1)(y^{69} - 26y^{68} + \dots + 3481y - 256)$
$c_3$	$y(y + 1)^2(y^2 + 1)^2(y^2 + y + 2)^2$ $\cdot (y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3$ $\cdot (y^{69} - 26y^{68} + \dots + 15690417448y - 2950879684)$
$c_4, c_{10}$	$y(y + 1)^2(y^2 + 1)^2(y^2 + y + 2)^2$ $\cdot (y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^3$ $\cdot (y^{69} + 22y^{68} + \dots + 8y - 4)$
$c_6, c_7, c_{12}$	$((y - 1)^{11})(y^{27} - 18y^{26} + \dots + y - 1)$ $\cdot (y^{69} - 74y^{68} + \dots - 10919y - 256)$
$c_8$	$y(y + 1)^2(y^2 + 1)^2(y^2 + y + 2)^2$ $\cdot (y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^3$ $\cdot (y^{69} - 2y^{68} + \dots - 1189944y - 7396)$
$c_9, c_{11}$	$y(y - 1)^2(y + 1)^4(y^2 + 3y + 4)^2$ $\cdot (y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^3$ $\cdot (y^{69} + 50y^{68} + \dots + 768y - 16)$