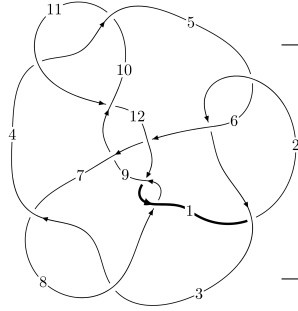
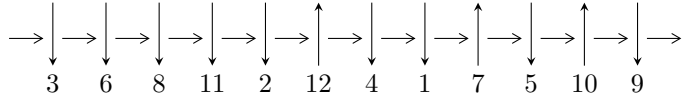


12a<sub>0326</sub> (K12a<sub>0326</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$1, 8 \xrightarrow{c_8} 4, 9 \xrightarrow{c_3} 3 \xrightarrow{c_1} 2 \xrightarrow{c_7} 7 \xrightarrow{c_9} 10 \xrightarrow{c_{12}} 12 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \xrightarrow{c_{11}} 11 \rightsquigarrow c_2, c_4, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2.14647 \times 10^{625} u^{136} - 1.57204 \times 10^{626} u^{135} + \dots + 5.04273 \times 10^{627} b + 2.01485 \times 10^{628}, \\ - 9.52837 \times 10^{628} u^{136} + 5.76897 \times 10^{629} u^{135} + \dots + 5.60247 \times 10^{630} a - 2.60191 \times 10^{633}, \\ u^{137} - 8u^{136} + \dots + 109806u + 32219 \rangle$$

$$I_2^u = \langle 969227805421u^{29} + 4997352190301u^{28} + \dots + 7614592375217b - 1781800267381, \\ - 8214623303611u^{29} - 14241638447196u^{28} + \dots + 7614592375217a - 12651568687672, \\ u^{30} + u^{29} + \dots + 2u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 167 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } J_1^u = \langle 2.15 \times 10^{625} u^{136} - 1.57 \times 10^{626} u^{135} + \dots + 5.04 \times 10^{627} b + 2.01 \times 10^{628}, -9.53 \times 10^{628} u^{136} + 5.77 \times 10^{629} u^{135} + \dots + 5.60 \times 10^{630} a - 2.60 \times 10^{633}, u^{137} - 8u^{136} + \dots + 109806u + 32219 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0170074u^{136} - 0.102972u^{135} + \dots + 1977.46u + 464.422 \\ -0.00425657u^{136} + 0.0311744u^{135} + \dots - 54.0695u - 3.99556 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0127509u^{136} - 0.0717974u^{135} + \dots + 1923.39u + 460.426 \\ -0.00425657u^{136} + 0.0311744u^{135} + \dots - 54.0695u - 3.99556 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.104079u^{136} - 0.731582u^{135} + \dots + 5658.43u + 962.800 \\ 0.0141435u^{136} - 0.160591u^{135} + \dots - 4271.95u - 1197.54 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0204806u^{136} - 0.164745u^{135} + \dots - 957.487u - 341.646 \\ 0.0166880u^{136} - 0.118460u^{135} + \dots + 830.580u + 151.032 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.154685u^{136} - 1.10541u^{135} + \dots + 7925.61u + 1193.45 \\ -0.0228178u^{136} + 0.0717336u^{135} + \dots - 8356.37u - 2109.51 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0414287u^{136} - 0.278536u^{135} + \dots + 3054.14u + 617.717 \\ 0.0316584u^{136} - 0.266647u^{135} + \dots - 1739.62u - 622.793 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.164628u^{136} + 1.24456u^{135} + \dots - 2428.11u + 289.540 \\ 0.0406849u^{136} - 0.234576u^{135} + \dots + 6901.62u + 1587.49 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.148430u^{136} + 0.926021u^{135} + \dots - 18759.7u - 4096.98 \\ -0.00521443u^{136} + 0.202164u^{135} + \dots + 12862.6u + 3478.39 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.0777998u^{136} - 0.574500u^{135} + \dots + 4442.71u + 535.291$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{137} + 51u^{136} + \dots + 28u + 1$
$c_2, c_5$	$u^{137} + 3u^{136} + \dots - 10u + 1$
$c_3, c_7$	$u^{137} + u^{136} + \dots - 450658u + 20477$
$c_4, c_{10}$	$u^{137} - u^{136} + \dots + 6u^2 + 1$
$c_6$	$u^{137} - 2u^{136} + \dots - 4683u + 2473$
$c_8, c_{12}$	$u^{137} - 8u^{136} + \dots + 109806u + 32219$
$c_9$	$u^{137} + 16u^{136} + \dots + 3863u + 251$
$c_{11}$	$u^{137} - 63u^{136} + \dots - 12u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{137} + 85y^{136} + \dots - 8004y - 1$
$c_2, c_5$	$y^{137} - 51y^{136} + \dots + 28y - 1$
$c_3, c_7$	$y^{137} + 115y^{136} + \dots - 17103469262y - 419307529$
$c_4, c_{10}$	$y^{137} + 63y^{136} + \dots - 12y - 1$
$c_6$	$y^{137} - 12y^{136} + \dots + 196459991y - 6115729$
$c_8, c_{12}$	$y^{137} + 118y^{136} + \dots + 87908229568y - 1038063961$
$c_9$	$y^{137} - 22y^{136} + \dots + 8590039y - 63001$
$c_{11}$	$y^{137} + 39y^{136} + \dots + 44y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.600215 + 0.825884I$ $a = 0.341214 + 0.182187I$ $b = 0.0429581 + 0.0446813I$	$-0.76985 + 2.36523I$	0
$u = -0.600215 - 0.825884I$ $a = 0.341214 - 0.182187I$ $b = 0.0429581 - 0.0446813I$	$-0.76985 - 2.36523I$	0
$u = 0.276628 + 0.934882I$ $a = 0.134951 + 0.863792I$ $b = -0.754988 - 0.080370I$	$0.027372 - 1.013400I$	0
$u = 0.276628 - 0.934882I$ $a = 0.134951 - 0.863792I$ $b = -0.754988 + 0.080370I$	$0.027372 + 1.013400I$	0
$u = 0.277443 + 1.042560I$ $a = -0.56568 + 1.72089I$ $b = 0.509378 - 0.961639I$	$2.76698 + 4.14223I$	0
$u = 0.277443 - 1.042560I$ $a = -0.56568 - 1.72089I$ $b = 0.509378 + 0.961639I$	$2.76698 - 4.14223I$	0
$u = -0.810726 + 0.376962I$ $a = 0.625383 + 0.386915I$ $b = 0.719560 - 0.588147I$	$-4.43117 + 3.80080I$	0
$u = -0.810726 - 0.376962I$ $a = 0.625383 - 0.386915I$ $b = 0.719560 + 0.588147I$	$-4.43117 - 3.80080I$	0
$u = 0.405570 + 0.762614I$ $a = -0.577183 - 0.645655I$ $b = 0.565672 + 0.632820I$	$2.17077 - 6.60754I$	0
$u = 0.405570 - 0.762614I$ $a = -0.577183 + 0.645655I$ $b = 0.565672 - 0.632820I$	$2.17077 + 6.60754I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.480617 + 0.678664I$		
$a = 0.319527 - 0.525767I$	$-0.09125 + 2.10745I$	0
$b = -0.342427 + 0.558103I$		
$u = -0.480617 - 0.678664I$		
$a = 0.319527 + 0.525767I$	$-0.09125 - 2.10745I$	0
$b = -0.342427 - 0.558103I$		
$u = 0.365595 + 1.115550I$		
$a = -0.320099 - 0.727207I$	$3.82283 + 0.95919I$	0
$b = -0.124434 + 0.427629I$		
$u = 0.365595 - 1.115550I$		
$a = -0.320099 + 0.727207I$	$3.82283 - 0.95919I$	0
$b = -0.124434 - 0.427629I$		
$u = 1.104240 + 0.401110I$		
$a = 0.113677 - 0.484296I$	$3.38915 - 7.43186I$	0
$b = 0.282562 + 1.184250I$		
$u = 1.104240 - 0.401110I$		
$a = 0.113677 + 0.484296I$	$3.38915 + 7.43186I$	0
$b = 0.282562 - 1.184250I$		
$u = 0.250630 + 1.162460I$		
$a = -0.58140 + 2.21392I$	$5.36671 - 3.68922I$	0
$b = 0.022548 - 1.349140I$		
$u = 0.250630 - 1.162460I$		
$a = -0.58140 - 2.21392I$	$5.36671 + 3.68922I$	0
$b = 0.022548 + 1.349140I$		
$u = 0.509415 + 1.076190I$		
$a = 0.524591 + 0.518478I$	$-1.57184 - 5.75032I$	0
$b = -0.886419 + 0.425051I$		
$u = 0.509415 - 1.076190I$		
$a = 0.524591 - 0.518478I$	$-1.57184 + 5.75032I$	0
$b = -0.886419 - 0.425051I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.584119 + 1.041150I$ $a = -0.460558 + 0.276017I$ $b = 0.676065 + 0.560471I$	$-2.46994 + 1.25079I$	0
$u = -0.584119 - 1.041150I$ $a = -0.460558 - 0.276017I$ $b = 0.676065 - 0.560471I$	$-2.46994 - 1.25079I$	0
$u = -0.144415 + 1.190800I$ $a = 0.457281 - 0.122460I$ $b = -1.212230 + 0.285741I$	$1.47034 + 1.58354I$	0
$u = -0.144415 - 1.190800I$ $a = 0.457281 + 0.122460I$ $b = -1.212230 - 0.285741I$	$1.47034 - 1.58354I$	0
$u = -0.753738 + 0.257933I$ $a = 0.795857 - 0.701646I$ $b = 0.576601 + 0.874596I$	$-3.62189 - 1.01410I$	0
$u = -0.753738 - 0.257933I$ $a = 0.795857 + 0.701646I$ $b = 0.576601 - 0.874596I$	$-3.62189 + 1.01410I$	0
$u = -0.335437 + 1.157330I$ $a = 0.25846 + 1.95888I$ $b = -0.141406 - 0.950478I$	$0.252574 + 1.080440I$	0
$u = -0.335437 - 1.157330I$ $a = 0.25846 - 1.95888I$ $b = -0.141406 + 0.950478I$	$0.252574 - 1.080440I$	0
$u = 0.173074 + 1.196750I$ $a = -0.613118 - 0.319995I$ $b = 1.36621 + 0.38306I$	$3.36982 - 6.59254I$	0
$u = 0.173074 - 1.196750I$ $a = -0.613118 + 0.319995I$ $b = 1.36621 - 0.38306I$	$3.36982 + 6.59254I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.252583 + 1.193810I$ $a = -0.48841 + 2.77901I$ $b = -0.325330 - 1.160690I$	$0.75973 - 9.92657I$	0
$u = 0.252583 - 1.193810I$ $a = -0.48841 - 2.77901I$ $b = -0.325330 + 1.160690I$	$0.75973 + 9.92657I$	0
$u = 0.401665 + 0.667335I$ $a = -0.191681 - 0.810457I$ $b = 0.128406 + 0.873969I$	$3.65193 + 0.66673I$	0
$u = 0.401665 - 0.667335I$ $a = -0.191681 + 0.810457I$ $b = 0.128406 - 0.873969I$	$3.65193 - 0.66673I$	0
$u = -0.259460 + 1.196040I$ $a = 0.33681 + 2.61041I$ $b = 0.245278 - 1.105050I$	$-0.75094 + 4.51996I$	0
$u = -0.259460 - 1.196040I$ $a = 0.33681 - 2.61041I$ $b = 0.245278 + 1.105050I$	$-0.75094 - 4.51996I$	0
$u = -0.043599 + 1.224900I$ $a = -0.081497 + 0.491243I$ $b = -0.773182 + 0.003155I$	$0.851004 - 0.795140I$	0
$u = -0.043599 - 1.224900I$ $a = -0.081497 - 0.491243I$ $b = -0.773182 - 0.003155I$	$0.851004 + 0.795140I$	0
$u = -0.272248 + 1.198580I$ $a = 1.73020 + 1.65034I$ $b = 0.246093 - 1.307720I$	$6.31626 + 8.78487I$	0
$u = -0.272248 - 1.198580I$ $a = 1.73020 - 1.65034I$ $b = 0.246093 + 1.307720I$	$6.31626 - 8.78487I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.258801 + 1.202340I$ $a = -1.24707 + 1.88429I$ $b = -0.356991 - 1.338480I$	$5.05012 - 5.03282I$	0
$u = 0.258801 - 1.202340I$ $a = -1.24707 - 1.88429I$ $b = -0.356991 + 1.338480I$	$5.05012 + 5.03282I$	0
$u = 0.721061 + 0.261174I$ $a = -0.765255 + 0.337826I$ $b = -0.857391 - 0.405574I$	$-3.95395 + 1.20522I$	0
$u = 0.721061 - 0.261174I$ $a = -0.765255 - 0.337826I$ $b = -0.857391 + 0.405574I$	$-3.95395 - 1.20522I$	0
$u = -0.212759 + 1.219960I$ $a = 0.39889 + 2.02793I$ $b = 0.61084 - 1.77061I$	$7.76381 + 1.99463I$	0
$u = -0.212759 - 1.219960I$ $a = 0.39889 - 2.02793I$ $b = 0.61084 + 1.77061I$	$7.76381 - 1.99463I$	0
$u = -0.286333 + 1.210290I$ $a = 1.61945 + 0.94113I$ $b = 0.169209 - 1.077120I$	$6.76255 + 2.94842I$	0
$u = -0.286333 - 1.210290I$ $a = 1.61945 - 0.94113I$ $b = 0.169209 + 1.077120I$	$6.76255 - 2.94842I$	0
$u = 0.243282 + 1.224860I$ $a = -0.64177 + 1.67068I$ $b = -0.60807 - 1.39180I$	$5.39433 - 5.32907I$	0
$u = 0.243282 - 1.224860I$ $a = -0.64177 - 1.67068I$ $b = -0.60807 + 1.39180I$	$5.39433 + 5.32907I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.699243 + 0.265046I$ $a = -0.902246 - 0.458831I$ $b = -0.627171 + 1.038880I$	$-2.08258 + 6.56291I$	0
$u = 0.699243 - 0.265046I$ $a = -0.902246 + 0.458831I$ $b = -0.627171 - 1.038880I$	$-2.08258 - 6.56291I$	0
$u = 0.133455 + 1.251360I$ $a = 0.084175 - 0.523657I$ $b = 0.895480 + 0.648314I$	$6.23673 + 0.17961I$	0
$u = 0.133455 - 1.251360I$ $a = 0.084175 + 0.523657I$ $b = 0.895480 - 0.648314I$	$6.23673 - 0.17961I$	0
$u = -0.221879 + 1.250790I$ $a = 0.11965 + 1.70945I$ $b = 1.01410 - 1.57896I$	$7.61960 + 8.66163I$	0
$u = -0.221879 - 1.250790I$ $a = 0.11965 - 1.70945I$ $b = 1.01410 + 1.57896I$	$7.61960 - 8.66163I$	0
$u = 0.301681 + 1.242530I$ $a = -0.725555 + 0.385722I$ $b = -0.484597 - 0.574971I$	$5.79279 - 5.78435I$	0
$u = 0.301681 - 1.242530I$ $a = -0.725555 - 0.385722I$ $b = -0.484597 + 0.574971I$	$5.79279 + 5.78435I$	0
$u = -0.063134 + 1.281760I$ $a = -1.23684 - 2.14792I$ $b = -0.011264 + 1.216080I$	$8.36571 - 4.84327I$	0
$u = -0.063134 - 1.281760I$ $a = -1.23684 + 2.14792I$ $b = -0.011264 - 1.216080I$	$8.36571 + 4.84327I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.134330 + 0.617531I$ $a = -0.127196 - 0.486382I$ $b = -0.126525 + 1.070720I$	$0.54578 + 1.90911I$	0
$u = -1.134330 - 0.617531I$ $a = -0.127196 + 0.486382I$ $b = -0.126525 - 1.070720I$	$0.54578 - 1.90911I$	0
$u = 0.275113 + 1.263970I$ $a = -0.281993 + 0.830321I$ $b = -0.913446 - 0.799643I$	$5.75402 - 5.70433I$	0
$u = 0.275113 - 1.263970I$ $a = -0.281993 - 0.830321I$ $b = -0.913446 + 0.799643I$	$5.75402 + 5.70433I$	0
$u = 0.069435 + 1.294050I$ $a = 0.579558 + 0.665158I$ $b = 0.445851 - 0.025283I$	$2.09940 + 6.03519I$	0
$u = 0.069435 - 1.294050I$ $a = 0.579558 - 0.665158I$ $b = 0.445851 + 0.025283I$	$2.09940 - 6.03519I$	0
$u = -0.026064 + 1.295990I$ $a = -0.48548 - 2.61453I$ $b = -0.008508 + 1.375680I$	$9.41866 + 1.21222I$	0
$u = -0.026064 - 1.295990I$ $a = -0.48548 + 2.61453I$ $b = -0.008508 - 1.375680I$	$9.41866 - 1.21222I$	0
$u = 0.081715 + 1.302440I$ $a = 0.81523 - 1.72233I$ $b = 0.201606 + 1.228170I$	$6.74367 + 0.78269I$	0
$u = 0.081715 - 1.302440I$ $a = 0.81523 + 1.72233I$ $b = 0.201606 - 1.228170I$	$6.74367 - 0.78269I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.297150 + 0.204185I$ $a = -0.219346 + 0.377698I$ $b = -0.388633 - 1.344330I$	$2.21246 - 12.85340I$	0
$u = 1.297150 - 0.204185I$ $a = -0.219346 - 0.377698I$ $b = -0.388633 + 1.344330I$	$2.21246 + 12.85340I$	0
$u = -0.677201 + 0.041589I$ $a = 0.80512 - 1.49239I$ $b = 0.677223 + 0.180341I$	$-3.72494 + 3.01705I$	$-13.21532 - 1.96138I$
$u = -0.677201 - 0.041589I$ $a = 0.80512 + 1.49239I$ $b = 0.677223 - 0.180341I$	$-3.72494 - 3.01705I$	$-13.21532 + 1.96138I$
$u = 0.117160 + 1.322660I$ $a = 0.37918 - 1.50554I$ $b = 0.49170 + 1.36391I$	$6.72024 + 0.53681I$	0
$u = 0.117160 - 1.322660I$ $a = 0.37918 + 1.50554I$ $b = 0.49170 - 1.36391I$	$6.72024 - 0.53681I$	0
$u = -0.161042 + 1.342350I$ $a = -0.05597 - 1.61600I$ $b = -0.80150 + 1.70452I$	$8.26014 + 3.01778I$	0
$u = -0.161042 - 1.342350I$ $a = -0.05597 + 1.61600I$ $b = -0.80150 - 1.70452I$	$8.26014 - 3.01778I$	0
$u = -0.407256 + 1.294530I$ $a = 0.026183 - 0.389081I$ $b = 0.680029 + 0.369673I$	$1.35104 + 3.81155I$	0
$u = -0.407256 - 1.294530I$ $a = 0.026183 + 0.389081I$ $b = 0.680029 - 0.369673I$	$1.35104 - 3.81155I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.610534 + 0.186046I$ $a = 0.445388 + 0.957310I$ $b = -0.03359 + 1.41643I$	$3.24778 - 5.49829I$	$-5.00006 + 6.13472I$
$u = -0.610534 - 0.186046I$ $a = 0.445388 - 0.957310I$ $b = -0.03359 - 1.41643I$	$3.24778 + 5.49829I$	$-5.00006 - 6.13472I$
$u = 0.286945 + 1.332370I$ $a = 0.527188 + 0.317971I$ $b = -1.57004 - 0.11173I$	$2.31371 - 11.85850I$	0
$u = 0.286945 - 1.332370I$ $a = 0.527188 - 0.317971I$ $b = -1.57004 + 0.11173I$	$2.31371 + 11.85850I$	0
$u = -0.306302 + 1.331350I$ $a = -0.395801 + 0.146440I$ $b = 1.368200 + 0.027238I$	$0.67456 + 6.63501I$	0
$u = -0.306302 - 1.331350I$ $a = -0.395801 - 0.146440I$ $b = 1.368200 - 0.027238I$	$0.67456 - 6.63501I$	0
$u = 0.626514 + 0.050151I$ $a = -0.84200 - 1.70554I$ $b = -0.811167 + 0.011205I$	$-2.10741 - 8.46095I$	$-10.29053 + 6.92192I$
$u = 0.626514 - 0.050151I$ $a = -0.84200 + 1.70554I$ $b = -0.811167 - 0.011205I$	$-2.10741 + 8.46095I$	$-10.29053 - 6.92192I$
$u = 0.583255 + 0.219848I$ $a = -0.316978 + 0.624569I$ $b = -0.166804 + 1.320420I$	$2.04697 + 1.89378I$	$-8.30712 + 0.I$
$u = 0.583255 - 0.219848I$ $a = -0.316978 - 0.624569I$ $b = -0.166804 - 1.320420I$	$2.04697 - 1.89378I$	$-8.30712 + 0.I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.606620 + 0.139527I$ $a = 0.267987 + 1.177840I$ $b = -0.266261 + 1.165630I$	$3.51581 + 0.39606I$	$-4.02934 - 2.78608I$
$u = -0.606620 - 0.139527I$ $a = 0.267987 - 1.177840I$ $b = -0.266261 - 1.165630I$	$3.51581 - 0.39606I$	$-4.02934 + 2.78608I$
$u = -0.157220 + 1.386930I$ $a = -0.20262 - 1.78566I$ $b = -0.43911 + 2.00856I$	$8.39206 - 2.84568I$	0
$u = -0.157220 - 1.386930I$ $a = -0.20262 + 1.78566I$ $b = -0.43911 - 2.00856I$	$8.39206 + 2.84568I$	0
$u = -1.365400 + 0.316476I$ $a = 0.260102 + 0.452500I$ $b = 0.343139 - 1.221160I$	$-0.43097 + 6.85078I$	0
$u = -1.365400 - 0.316476I$ $a = 0.260102 - 0.452500I$ $b = 0.343139 + 1.221160I$	$-0.43097 - 6.85078I$	0
$u = 0.583549 + 0.102512I$ $a = -0.136693 - 0.917007I$ $b = 0.696924 + 0.132143I$	$0.25747 + 3.83112I$	$-5.71601 - 2.49405I$
$u = 0.583549 - 0.102512I$ $a = -0.136693 + 0.917007I$ $b = 0.696924 - 0.132143I$	$0.25747 - 3.83112I$	$-5.71601 + 2.49405I$
$u = -0.531137 + 0.228329I$ $a = 0.154180 - 0.733272I$ $b = -0.525007 + 0.334915I$	$-1.23027 + 0.80713I$	$-8.01143 - 3.82200I$
$u = -0.531137 - 0.228329I$ $a = 0.154180 + 0.733272I$ $b = -0.525007 - 0.334915I$	$-1.23027 - 0.80713I$	$-8.01143 + 3.82200I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.13412 + 1.42109I$ $a = 0.27480 - 1.72876I$ $b = 0.12100 + 1.91232I$	$7.51590 - 0.56584I$	0
$u = 0.13412 - 1.42109I$ $a = 0.27480 + 1.72876I$ $b = 0.12100 - 1.91232I$	$7.51590 + 0.56584I$	0
$u = 0.562181 + 0.080157I$ $a = -0.292233 + 1.307150I$ $b = 0.176536 + 0.354661I$	$2.25523 + 2.39599I$	$-5.21005 - 3.82646I$
$u = 0.562181 - 0.080157I$ $a = -0.292233 - 1.307150I$ $b = 0.176536 - 0.354661I$	$2.25523 - 2.39599I$	$-5.21005 + 3.82646I$
$u = 0.528989 + 0.104664I$ $a = 0.091902 + 1.360790I$ $b = -0.204011 + 0.867265I$	$2.14967 + 2.60628I$	$-6.80056 - 4.70746I$
$u = 0.528989 - 0.104664I$ $a = 0.091902 - 1.360790I$ $b = -0.204011 - 0.867265I$	$2.14967 - 2.60628I$	$-6.80056 + 4.70746I$
$u = 0.488642 + 0.156091I$ $a = 0.419703 + 1.008160I$ $b = -0.258118 + 1.102630I$	$2.13489 + 2.49230I$	$-4.55425 - 3.52768I$
$u = 0.488642 - 0.156091I$ $a = 0.419703 - 1.008160I$ $b = -0.258118 - 1.102630I$	$2.13489 - 2.49230I$	$-4.55425 + 3.52768I$
$u = 0.41429 + 1.47620I$ $a = 0.42248 - 1.73952I$ $b = 0.47672 + 1.49807I$	$9.2931 - 12.6983I$	0
$u = 0.41429 - 1.47620I$ $a = 0.42248 + 1.73952I$ $b = 0.47672 - 1.49807I$	$9.2931 + 12.6983I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.39699 + 1.49928I$ $a = -0.36502 - 1.66962I$ $b = -0.43485 + 1.44199I$	$7.01641 + 7.09040I$	0
$u = -0.39699 - 1.49928I$ $a = -0.36502 + 1.66962I$ $b = -0.43485 - 1.44199I$	$7.01641 - 7.09040I$	0
$u = -0.355655 + 0.220235I$ $a = -1.377970 + 0.136306I$ $b = 0.278145 + 1.313290I$	$4.69066 + 0.36597I$	$-1.30932 - 2.96621I$
$u = -0.355655 - 0.220235I$ $a = -1.377970 - 0.136306I$ $b = 0.278145 - 1.313290I$	$4.69066 - 0.36597I$	$-1.30932 + 2.96621I$
$u = 0.53308 + 1.49033I$ $a = -0.57763 + 1.58115I$ $b = -0.61304 - 1.52807I$	$7.5580 - 19.2157I$	0
$u = 0.53308 - 1.49033I$ $a = -0.57763 - 1.58115I$ $b = -0.61304 + 1.52807I$	$7.5580 + 19.2157I$	0
$u = -0.401352 + 0.098657I$ $a = -1.27049 + 1.55407I$ $b = 0.491752 + 1.200300I$	$4.07486 - 6.17462I$	$-2.84721 + 7.18816I$
$u = -0.401352 - 0.098657I$ $a = -1.27049 - 1.55407I$ $b = 0.491752 - 1.200300I$	$4.07486 + 6.17462I$	$-2.84721 - 7.18816I$
$u = -0.53092 + 1.51520I$ $a = 0.53811 + 1.52732I$ $b = 0.59065 - 1.44238I$	$5.2569 + 13.3633I$	0
$u = -0.53092 - 1.51520I$ $a = 0.53811 - 1.52732I$ $b = 0.59065 + 1.44238I$	$5.2569 - 13.3633I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.45204 + 1.54813I$ $a = 0.47060 - 1.51549I$ $b = 0.30697 + 1.48878I$	$12.88360 - 4.10984I$	0
$u = 0.45204 - 1.54813I$ $a = 0.47060 + 1.51549I$ $b = 0.30697 - 1.48878I$	$12.88360 + 4.10984I$	0
$u = -0.01080 + 1.62519I$ $a = 0.022968 - 1.374860I$ $b = -0.182649 + 1.339380I$	$4.75904 + 2.79200I$	0
$u = -0.01080 - 1.62519I$ $a = 0.022968 + 1.374860I$ $b = -0.182649 - 1.339380I$	$4.75904 - 2.79200I$	0
$u = 0.59925 + 1.52996I$ $a = -0.61806 + 1.40369I$ $b = -0.40324 - 1.42797I$	$11.6217 - 10.1999I$	0
$u = 0.59925 - 1.52996I$ $a = -0.61806 - 1.40369I$ $b = -0.40324 + 1.42797I$	$11.6217 + 10.1999I$	0
$u = 1.63472 + 0.19652I$ $a = -0.021975 - 0.544479I$ $b = -0.059158 + 1.259790I$	$6.62314 + 2.60802I$	0
$u = 1.63472 - 0.19652I$ $a = -0.021975 + 0.544479I$ $b = -0.059158 - 1.259790I$	$6.62314 - 2.60802I$	0
$u = 1.05809 + 1.50494I$ $a = -0.539942 + 0.960179I$ $b = -0.113754 - 1.134000I$	$5.75951 - 0.22579I$	0
$u = 1.05809 - 1.50494I$ $a = -0.539942 - 0.960179I$ $b = -0.113754 + 1.134000I$	$5.75951 + 0.22579I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.136913$ $a = 3.87210$ $b = -0.411336$	-0.911004	-11.2840
$u = -0.15252 + 1.86735I$ $a = -0.106104 - 1.238710I$ $b = -0.232113 + 1.275320I$	$4.81891 + 2.74844I$	0
$u = -0.15252 - 1.86735I$ $a = -0.106104 + 1.238710I$ $b = -0.232113 - 1.275320I$	$4.81891 - 2.74844I$	0
$u = -0.62929 + 1.84278I$ $a = 0.401169 + 1.219110I$ $b = 0.321940 - 1.106760I$	$3.49212 + 7.61632I$	0
$u = -0.62929 - 1.84278I$ $a = 0.401169 - 1.219110I$ $b = 0.321940 + 1.106760I$	$3.49212 - 7.61632I$	0
$u = 0.89716 + 1.80883I$ $a = 0.373769 - 0.969692I$ $b = 0.023776 + 1.291180I$	$6.14734 + 4.75780I$	0
$u = 0.89716 - 1.80883I$ $a = 0.373769 + 0.969692I$ $b = 0.023776 - 1.291180I$	$6.14734 - 4.75780I$	0

**II.**

$$I_2^u = \langle 9.69 \times 10^{11} u^{29} + 5.00 \times 10^{12} u^{28} + \dots + 7.61 \times 10^{12} b - 1.78 \times 10^{12}, -8.21 \times 10^{12} u^{29} - 1.42 \times 10^{13} u^{28} + \dots + 7.61 \times 10^{12} a - 1.27 \times 10^{13}, u^{30} + u^{29} + \dots + 2u + 1 \rangle$$

**(i) Arc colorings**

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1.07880u^{29} + 1.87031u^{28} + \dots + 6.98066u + 1.66149 \\ -0.127286u^{29} - 0.656286u^{28} + \dots + 0.815661u + 0.233998 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.951515u^{29} + 1.21402u^{28} + \dots + 7.79632u + 1.89549 \\ -0.127286u^{29} - 0.656286u^{28} + \dots + 0.815661u + 0.233998 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1.44977u^{29} + 2.25417u^{28} + \dots + 1.57036u + 1.19725 \\ 0.562682u^{29} - 0.508894u^{28} + \dots + 1.00766u - 0.00613589 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.0685465u^{29} + 0.841396u^{28} + \dots - 3.15609u + 0.792779 \\ -0.0624106u^{29} - 0.272578u^{28} + \dots - 0.614245u + 0.227151 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1.11775u^{29} - 1.10749u^{28} + \dots + 2.05886u + 0.217486 \\ -0.950793u^{29} - 0.733908u^{28} + \dots + 0.0972228u - 0.0102653 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.00613589u^{29} + 0.568818u^{28} + \dots - 3.77033u + 0.0199295 \\ -0.133986u^{29} - 0.526835u^{28} + \dots - 0.745745u - 0.335531 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.674226u^{29} - 1.48426u^{28} + \dots - 2.30183u - 1.76154 \\ -1.13330u^{29} - 0.127945u^{28} + \dots + 1.56908u + 0.852693 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -2.15067u^{29} - 0.761822u^{28} + \dots + 0.354677u + 2.80358 \\ -0.875503u^{29} + 0.178922u^{28} + \dots + 2.30824u + 0.938891 \end{pmatrix} \end{aligned}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes**

$$= -\frac{26703140571941}{7614592375217} u^{29} - \frac{13681643041353}{7614592375217} u^{28} + \dots - \frac{89568892795504}{7614592375217} u - \frac{22427593702390}{7614592375217}$$

(iv)  $u$ -Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{30} - 14u^{29} + \dots - 14u + 1$
$c_2$	$u^{30} + 2u^{29} + \dots + 2u + 1$
$c_3$	$u^{30} + 16u^{28} + \dots - 4u + 1$
$c_4$	$u^{30} + 8u^{28} + \dots + 2u + 1$
$c_5$	$u^{30} - 2u^{29} + \dots - 2u + 1$
$c_6$	$u^{30} - u^{29} + \dots + 7u + 1$
$c_7$	$u^{30} + 16u^{28} + \dots + 4u + 1$
$c_8$	$u^{30} + u^{29} + \dots + 2u + 1$
$c_9$	$u^{30} - 3u^{29} + \dots + u + 1$
$c_{10}$	$u^{30} + 8u^{28} + \dots - 2u + 1$
$c_{11}$	$u^{30} - 16u^{29} + \dots - 18u + 1$
$c_{12}$	$u^{30} - u^{29} + \dots - 2u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{30} + 18y^{29} + \cdots + 2y + 1$
$c_2, c_5$	$y^{30} - 14y^{29} + \cdots - 14y + 1$
$c_3, c_7$	$y^{30} + 32y^{29} + \cdots + 12y + 1$
$c_4, c_{10}$	$y^{30} + 16y^{29} + \cdots + 18y + 1$
$c_6$	$y^{30} + y^{29} + \cdots - 9y + 1$
$c_8, c_{12}$	$y^{30} + 31y^{29} + \cdots + 14y + 1$
$c_9$	$y^{30} - 5y^{29} + \cdots - 9y + 1$
$c_{11}$	$y^{30} + 12y^{29} + \cdots - 38y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.522006 + 0.878409I$ $a = 0.174524 + 0.362277I$ $b = -0.522395 + 0.106070I$	$-1.12493 - 2.08959I$	$-12.37329 - 0.45284I$
$u = 0.522006 - 0.878409I$ $a = 0.174524 - 0.362277I$ $b = -0.522395 - 0.106070I$	$-1.12493 + 2.08959I$	$-12.37329 + 0.45284I$
$u = 0.580502 + 0.781634I$ $a = 0.079977 + 1.110490I$ $b = -0.285710 - 0.369681I$	$-1.07088 - 1.66964I$	$-11.34892 + 3.37717I$
$u = 0.580502 - 0.781634I$ $a = 0.079977 - 1.110490I$ $b = -0.285710 + 0.369681I$	$-1.07088 + 1.66964I$	$-11.34892 - 3.37717I$
$u = -0.658892 + 0.867526I$ $a = 0.885371 + 0.771691I$ $b = 0.202700 - 1.246440I$	$5.43916 + 1.20569I$	$-0.29178 - 2.33340I$
$u = -0.658892 - 0.867526I$ $a = 0.885371 - 0.771691I$ $b = 0.202700 + 1.246440I$	$5.43916 - 1.20569I$	$-0.29178 + 2.33340I$
$u = -0.254757 + 1.119880I$ $a = 1.13436 + 1.30510I$ $b = 0.498455 - 1.314340I$	$6.31642 + 7.63327I$	$-0.18303 - 5.98526I$
$u = -0.254757 - 1.119880I$ $a = 1.13436 - 1.30510I$ $b = 0.498455 + 1.314340I$	$6.31642 - 7.63327I$	$-0.18303 + 5.98526I$
$u = -0.396608 + 0.740773I$ $a = -0.716956 + 1.131870I$ $b = 0.700342 - 0.546826I$	$1.64081 + 6.14083I$	$-8.20173 - 4.13767I$
$u = -0.396608 - 0.740773I$ $a = -0.716956 - 1.131870I$ $b = 0.700342 + 0.546826I$	$1.64081 - 6.14083I$	$-8.20173 + 4.13767I$



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.346961 + 0.722605I$ $a = -1.44663 + 0.62621I$ $b = 0.239582 + 0.412642I$	$-2.17581 - 3.16922I$	$-7.99099 + 3.11007I$
$u = 0.346961 - 0.722605I$ $a = -1.44663 - 0.62621I$ $b = 0.239582 - 0.412642I$	$-2.17581 + 3.16922I$	$-7.99099 - 3.11007I$
$u = 0.201907 + 1.189600I$ $a = -1.05036 + 1.50279I$ $b = -0.569953 - 1.224480I$	$5.61608 - 4.26764I$	$-70.0956014 + 0.10I$
$u = 0.201907 - 1.189600I$ $a = -1.05036 - 1.50279I$ $b = -0.569953 + 1.224480I$	$5.61608 + 4.26764I$	$-70.0956014 + 0.10I$
$u = -0.217304 + 0.711721I$ $a = 1.93148 + 0.80426I$ $b = -0.405710 + 0.552639I$	$-0.49937 + 8.34773I$	$-4.55245 - 7.24511I$
$u = -0.217304 - 0.711721I$ $a = 1.93148 - 0.80426I$ $b = -0.405710 - 0.552639I$	$-0.49937 - 8.34773I$	$-4.55245 + 7.24511I$
$u = -0.115006 + 1.298860I$ $a = -0.43331 - 1.95090I$ $b = -0.12479 + 1.72136I$	$8.05808 + 1.30972I$	$1.85659 - 2.62857I$
$u = -0.115006 - 1.298860I$ $a = -0.43331 + 1.95090I$ $b = -0.12479 - 1.72136I$	$8.05808 - 1.30972I$	$1.85659 + 2.62857I$
$u = 0.035132 + 1.337570I$ $a = 0.11366 - 1.91500I$ $b = 0.29046 + 1.74271I$	$7.87534 + 1.73167I$	$0.51091 - 3.18280I$
$u = 0.035132 - 1.337570I$ $a = 0.11366 + 1.91500I$ $b = 0.29046 - 1.74271I$	$7.87534 - 1.73167I$	$0.51091 + 3.18280I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.62944 + 1.34305I$		
$a = -0.624614 - 1.011460I$	$5.89793 - 4.22625I$	$-1.34831 + 2.43844I$
$b = 0.021709 + 1.356000I$		
$u = -0.62944 - 1.34305I$		
$a = -0.624614 + 1.011460I$	$5.89793 + 4.22625I$	$-1.34831 - 2.43844I$
$b = 0.021709 - 1.356000I$		
$u = 0.259808 + 0.366084I$		
$a = 1.53491 + 1.37268I$	$3.03572 + 2.17126I$	$1.83066 - 2.11907I$
$b = -0.190414 + 1.069450I$		
$u = 0.259808 - 0.366084I$		
$a = 1.53491 - 1.37268I$	$3.03572 - 2.17126I$	$1.83066 + 2.11907I$
$b = -0.190414 - 1.069450I$		
$u = -0.319221 + 0.222101I$		
$a = -0.08687 + 2.98534I$	$3.51917 - 1.85555I$	$0.05388 + 3.21427I$
$b = 0.182935 - 0.889900I$		
$u = -0.319221 - 0.222101I$		
$a = -0.08687 - 2.98534I$	$3.51917 + 1.85555I$	$0.05388 - 3.21427I$
$b = 0.182935 + 0.889900I$		
$u = 0.29140 + 1.59039I$		
$a = -0.51828 + 1.34005I$	$3.45327 - 7.01722I$	0
$b = -0.370825 - 1.018460I$		
$u = 0.29140 - 1.59039I$		
$a = -0.51828 - 1.34005I$	$3.45327 + 7.01722I$	0
$b = -0.370825 + 1.018460I$		
$u = -0.14649 + 1.81277I$		
$a = 0.022740 - 1.200550I$	$5.01198 - 2.43840I$	0
$b = 0.333614 + 1.259170I$		
$u = -0.14649 - 1.81277I$		
$a = 0.022740 + 1.200550I$	$5.01198 + 2.43840I$	0
$b = 0.333614 - 1.259170I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{30} - 14u^{29} + \dots - 14u + 1)(u^{137} + 51u^{136} + \dots + 28u + 1)$
$c_2$	$(u^{30} + 2u^{29} + \dots + 2u + 1)(u^{137} + 3u^{136} + \dots - 10u + 1)$
$c_3$	$(u^{30} + 16u^{28} + \dots - 4u + 1)(u^{137} + u^{136} + \dots - 450658u + 20477)$
$c_4$	$(u^{30} + 8u^{28} + \dots + 2u + 1)(u^{137} - u^{136} + \dots + 6u^2 + 1)$
$c_5$	$(u^{30} - 2u^{29} + \dots - 2u + 1)(u^{137} + 3u^{136} + \dots - 10u + 1)$
$c_6$	$(u^{30} - u^{29} + \dots + 7u + 1)(u^{137} - 2u^{136} + \dots - 4683u + 2473)$
$c_7$	$(u^{30} + 16u^{28} + \dots + 4u + 1)(u^{137} + u^{136} + \dots - 450658u + 20477)$
$c_8$	$(u^{30} + u^{29} + \dots + 2u + 1)(u^{137} - 8u^{136} + \dots + 109806u + 32219)$
$c_9$	$(u^{30} - 3u^{29} + \dots + u + 1)(u^{137} + 16u^{136} + \dots + 3863u + 251)$
$c_{10}$	$(u^{30} + 8u^{28} + \dots - 2u + 1)(u^{137} - u^{136} + \dots + 6u^2 + 1)$
$c_{11}$	$(u^{30} - 16u^{29} + \dots - 18u + 1)(u^{137} - 63u^{136} + \dots - 12u + 1)$
$c_{12}$	$(u^{30} - u^{29} + \dots - 2u + 1)(u^{137} - 8u^{136} + \dots + 109806u + 32219)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{30} + 18y^{29} + \dots + 2y + 1)(y^{137} + 85y^{136} + \dots - 8004y - 1)$
$c_2, c_5$	$(y^{30} - 14y^{29} + \dots - 14y + 1)(y^{137} - 51y^{136} + \dots + 28y - 1)$
$c_3, c_7$	$(y^{30} + 32y^{29} + \dots + 12y + 1)$ $\cdot (y^{137} + 115y^{136} + \dots - 17103469262y - 419307529)$
$c_4, c_{10}$	$(y^{30} + 16y^{29} + \dots + 18y + 1)(y^{137} + 63y^{136} + \dots - 12y - 1)$
$c_6$	$(y^{30} + y^{29} + \dots - 9y + 1)$ $\cdot (y^{137} - 12y^{136} + \dots + 196459991y - 6115729)$
$c_8, c_{12}$	$(y^{30} + 31y^{29} + \dots + 14y + 1)$ $\cdot (y^{137} + 118y^{136} + \dots + 87908229568y - 1038063961)$
$c_9$	$(y^{30} - 5y^{29} + \dots - 9y + 1)(y^{137} - 22y^{136} + \dots + 8590039y - 63001)$
$c_{11}$	$(y^{30} + 12y^{29} + \dots - 38y + 1)(y^{137} + 39y^{136} + \dots + 44y - 1)$