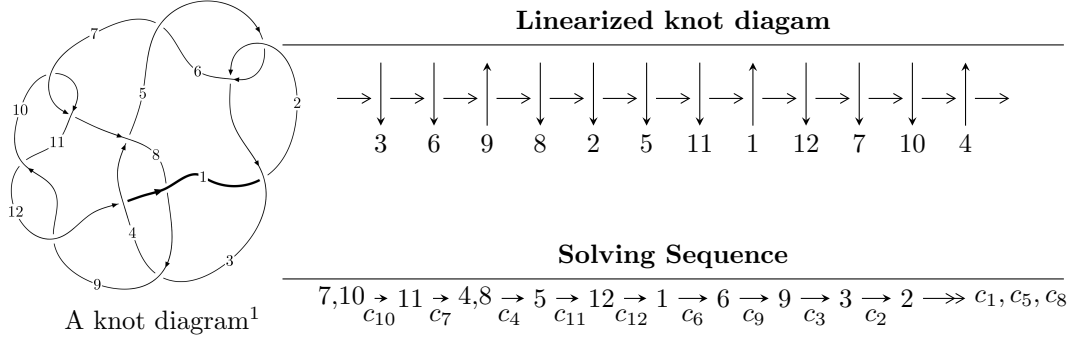


12a<sub>0353</sub> (K12a<sub>0353</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2u^{12} + 3u^{11} - 2u^{10} - 7u^9 + 3u^8 + 11u^7 - 13u^5 - 3u^4 + 6u^3 + 3u^2 + b + 3, \\ u^{12} + u^{11} - u^{10} - 3u^9 + u^8 + 4u^7 + u^6 - 5u^5 - 2u^4 + 2u^3 + 2u^2 + a + 1, \\ u^{13} + 2u^{12} - 4u^{10} - u^9 + 6u^8 + 4u^7 - 6u^6 - 6u^5 + 2u^4 + 4u^3 + u^2 + u + 1 \rangle$$

$$I_2^u = \langle -1.50748 \times 10^{77} u^{85} - 3.49171 \times 10^{77} u^{84} + \dots + 4.87932 \times 10^{75} b + 2.17543 \times 10^{77}, \\ -5.24953 \times 10^{76} u^{85} - 1.15851 \times 10^{77} u^{84} + \dots + 2.43966 \times 10^{75} a + 6.61885 \times 10^{76}, u^{86} + 3u^{85} + \dots - 9u \rangle$$

$$I_3^u = \langle -2u^2 + b, 2u^2 + a - u - 1, u^3 - u^2 + 1 \rangle$$

$$I_4^u = \langle b^3 - b^2 + 2b - 1, a, u + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 105 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle 2u^{12} + 3u^{11} + \dots + b + 3, u^{12} + u^{11} + \dots + a + 1, u^{13} + 2u^{12} + \dots + u + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{12} - u^{11} + u^{10} + 3u^9 - u^8 - 4u^7 - u^6 + 5u^5 + 2u^4 - 2u^3 - 2u^2 - 1 \\ -2u^{12} - 3u^{11} + 2u^{10} + 7u^9 - 3u^8 - 11u^7 + 13u^5 + 3u^4 - 6u^3 - 3u^2 - 3 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -2u^{12} - 3u^{11} + \dots + u - 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^6 + u^4 - 2u^2 + 1 \\ -u^{12} - u^{11} + u^{10} + 3u^9 - 2u^8 - 4u^7 + u^6 + 5u^5 - 2u^3 - u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3 \\ u^{12} + u^{11} - u^{10} - 3u^9 + u^8 + 4u^7 + u^6 - 4u^5 - 2u^4 + u^3 + 2u^2 + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^4 - u^2 + 1 \\ -3u^{12} - 4u^{11} + \dots - 4u^2 - 4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^2 + 1 \\ -2u^{12} - 3u^{11} + \dots - 3u^2 - 3 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 32u^{12} + 36u^{11} - 28u^{10} - 96u^9 + 52u^8 + 136u^7 + 8u^6 - 180u^5 - 24u^4 + 76u^3 + 48u^2 - 12u + 38$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_9$ $c_{11}$	$u^{13} + 4u^{12} + \dots - u + 1$
$c_2, c_5, c_7$ $c_{10}$	$u^{13} + 2u^{12} - 4u^{10} - u^9 + 6u^8 + 4u^7 - 6u^6 - 6u^5 + 2u^4 + 4u^3 + u^2 + u + 1$
$c_3$	$u^{13} - 19u^{12} + \dots + 208u - 32$
$c_4$	$u^{13} - 19u^{12} + \dots + 1920u - 256$
$c_8, c_{12}$	$u^{13} - 2u^{10} + 7u^9 + 8u^7 - 10u^6 + 8u^5 - 10u^4 + 14u^3 - 7u^2 + 5u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_9$ $c_{11}$	$y^{13} + 12y^{12} + \dots + 7y - 1$
$c_2, c_5, c_7$ $c_{10}$	$y^{13} - 4y^{12} + \dots - y - 1$
$c_3$	$y^{13} - 39y^{12} + \dots - 17664y - 1024$
$c_4$	$y^{13} - 33y^{12} + \dots + 49152y - 65536$
$c_8, c_{12}$	$y^{13} + 14y^{11} + \dots + 11y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.904846 + 0.518485I$ $a = -0.096373 - 0.132562I$ $b = -0.852642 - 0.464727I$	$-1.81047 + 4.05578I$	$-10.11630 - 6.00928I$
$u = -0.904846 - 0.518485I$ $a = -0.096373 + 0.132562I$ $b = -0.852642 + 0.464727I$	$-1.81047 - 4.05578I$	$-10.11630 + 6.00928I$
$u = 1.036990 + 0.250355I$ $a = -0.283354 + 0.764990I$ $b = 0.595552 + 0.354344I$	$-4.27978 - 7.04225I$	$-12.2400 + 9.0192I$
$u = 1.036990 - 0.250355I$ $a = -0.283354 - 0.764990I$ $b = 0.595552 - 0.354344I$	$-4.27978 + 7.04225I$	$-12.2400 - 9.0192I$
$u = 0.893443 + 0.777704I$ $a = 2.38786 + 1.96721I$ $b = -2.39968 - 0.31504I$	$6.69849 - 5.87553I$	$-15.0059 + 0.9974I$
$u = 0.893443 - 0.777704I$ $a = 2.38786 - 1.96721I$ $b = -2.39968 + 0.31504I$	$6.69849 + 5.87553I$	$-15.0059 - 0.9974I$
$u = -0.772869 + 0.915587I$ $a = -1.36740 - 1.45596I$ $b = 0.25765 + 2.33554I$	$11.49150 - 5.30654I$	$0.126296 + 1.125513I$
$u = -0.772869 - 0.915587I$ $a = -1.36740 + 1.45596I$ $b = 0.25765 - 2.33554I$	$11.49150 + 5.30654I$	$0.126296 - 1.125513I$
$u = -0.782810$ $a = -1.86558$ $b = -3.59947$	$-2.34512$	$76.3620$
$u = -1.031240 + 0.801398I$ $a = 1.18484 + 1.74923I$ $b = 0.77868 - 2.51426I$	$9.8415 + 18.0172I$	$-2.44507 - 10.27984I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.031240 - 0.801398I$		
$a = 1.18484 - 1.74923I$	$9.8415 - 18.0172I$	$-2.44507 + 10.27984I$
$b = 0.77868 + 2.51426I$		
$u = 0.169926 + 0.521088I$		
$a = 0.107226 - 0.405489I$	$1.43793 + 1.09121I$	$2.49987 - 1.33623I$
$b = -0.579822 - 0.331833I$		
$u = 0.169926 - 0.521088I$		
$a = 0.107226 + 0.405489I$	$1.43793 - 1.09121I$	$2.49987 + 1.33623I$
$b = -0.579822 + 0.331833I$		

**II.**

$$I_2^u = \langle -1.51 \times 10^{77} u^{85} - 3.49 \times 10^{77} u^{84} + \dots + 4.88 \times 10^{75} b + 2.18 \times 10^{77}, -5.25 \times 10^{76} u^{85} - 1.16 \times 10^{77} u^{84} + \dots + 2.44 \times 10^{75} a + 6.62 \times 10^{76}, u^{86} + 3u^{85} + \dots - 9u - 1 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 21.5175u^{85} + 47.4865u^{84} + \dots - 223.630u - 27.1302 \\ 30.8953u^{85} + 71.5614u^{84} + \dots - 332.611u - 44.5847 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.251807u^{85} - 1.22232u^{84} + \dots - 2.59267u + 1.81135 \\ 42.1634u^{85} + 96.0188u^{84} + \dots - 439.121u - 58.4380 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1.20192u^{85} - 4.20915u^{84} + \dots + 41.1638u + 11.5038 \\ 4.01802u^{85} + 8.63943u^{84} + \dots - 34.0326u - 2.81610 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -5.13993u^{85} - 10.2842u^{84} + \dots + 45.1346u + 7.41626 \\ -16.5884u^{85} - 40.3873u^{84} + \dots + 197.046u + 27.1217 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.405126u^{85} - 2.91912u^{84} + \dots + 7.79562u + 4.06769 \\ 37.1638u^{85} + 86.1844u^{84} + \dots - 402.124u - 53.8512 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2.39134u^{85} + 2.75645u^{84} + \dots + 9.79591u + 6.65558 \\ 15.1058u^{85} + 36.6780u^{84} + \dots - 177.568u - 23.1796 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =  $-58.8881u^{85} - 125.536u^{84} + \dots + 540.615u + 58.9944$**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_9$ $c_{11}$	$u^{86} + 25u^{85} + \dots + 77u + 1$
$c_2, c_5, c_7$ $c_{10}$	$u^{86} + 3u^{85} + \dots - 9u - 1$
$c_3$	$(u^{43} + 8u^{42} + \dots + 168u + 17)^2$
$c_4$	$(u^{43} + 7u^{42} + \dots + 736u - 47)^2$
$c_8, c_{12}$	$u^{86} + 10u^{85} + \dots - 12u - 8$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_9$ $c_{11}$	$y^{86} + 75y^{85} + \dots - 1501y + 1$
$c_2, c_5, c_7$ $c_{10}$	$y^{86} - 25y^{85} + \dots - 77y + 1$
$c_3$	$(y^{43} - 48y^{42} + \dots + 9150y - 289)^2$
$c_4$	$(y^{43} - 9y^{42} + \dots + 645754y - 2209)^2$
$c_8, c_{12}$	$y^{86} - 24y^{85} + \dots - 1872y + 64$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.917621 + 0.295314I$ $a = -0.040621 - 1.079690I$ $b = -0.333482 - 0.208136I$	$-0.79965 - 4.04123I$	0
$u = 0.917621 - 0.295314I$ $a = -0.040621 + 1.079690I$ $b = -0.333482 + 0.208136I$	$-0.79965 + 4.04123I$	0
$u = 0.717623 + 0.768123I$ $a = -0.054307 + 1.203790I$ $b = -0.77615 - 1.18911I$	$3.47079 + 0.34806I$	0
$u = 0.717623 - 0.768123I$ $a = -0.054307 - 1.203790I$ $b = -0.77615 + 1.18911I$	$3.47079 - 0.34806I$	0
$u = 0.876794 + 0.142275I$ $a = -0.48167 + 1.45763I$ $b = 0.571323 - 0.108452I$	$-3.83371 - 0.47604I$	$-14.5101 + 6.2522I$
$u = 0.876794 - 0.142275I$ $a = -0.48167 - 1.45763I$ $b = 0.571323 + 0.108452I$	$-3.83371 + 0.47604I$	$-14.5101 - 6.2522I$
$u = -1.060200 + 0.334825I$ $a = -0.274900 + 0.163237I$ $b = -0.332050 - 0.365366I$	$-3.83371 - 0.47604I$	0
$u = -1.060200 - 0.334825I$ $a = -0.274900 - 0.163237I$ $b = -0.332050 + 0.365366I$	$-3.83371 + 0.47604I$	0
$u = 0.048645 + 0.881375I$ $a = 0.613415 + 0.147896I$ $b = 0.246733 + 0.301746I$	$5.86063 + 7.97916I$	$0. - 7.01416I$
$u = 0.048645 - 0.881375I$ $a = 0.613415 - 0.147896I$ $b = 0.246733 - 0.301746I$	$5.86063 - 7.97916I$	$0. + 7.01416I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.821986 + 0.314452I$ $a = -1.25468 - 0.84044I$ $b = 1.235000 + 0.353410I$	$2.64548 - 6.03975I$	$-6.00000 + 8.80568I$
$u = 0.821986 - 0.314452I$ $a = -1.25468 + 0.84044I$ $b = 1.235000 - 0.353410I$	$2.64548 + 6.03975I$	$-6.00000 - 8.80568I$
$u = 0.094579 + 0.867631I$ $a = -0.556786 - 0.095510I$ $b = -0.266643 - 0.351424I$	$6.29916 + 1.89386I$	0
$u = 0.094579 - 0.867631I$ $a = -0.556786 + 0.095510I$ $b = -0.266643 + 0.351424I$	$6.29916 - 1.89386I$	0
$u = -1.12880$ $a = 0.312114$ $b = 0.0354189$	$-2.43233$	0
$u = 0.866972 + 0.726106I$ $a = -2.76658 - 0.35303I$ $b = 1.62157 - 1.38197I$	$1.75351 - 2.44365I$	0
$u = 0.866972 - 0.726106I$ $a = -2.76658 + 0.35303I$ $b = 1.62157 + 1.38197I$	$1.75351 + 2.44365I$	0
$u = -0.762384 + 0.840513I$ $a = 1.51688 + 1.40891I$ $b = -0.17717 - 2.46303I$	$2.89716 - 6.12343I$	0
$u = -0.762384 - 0.840513I$ $a = 1.51688 - 1.40891I$ $b = -0.17717 + 2.46303I$	$2.89716 + 6.12343I$	0
$u = 0.880885 + 0.729604I$ $a = 1.16854 + 2.90880I$ $b = -2.36887 - 1.57171I$	$1.71280 - 3.10788I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.880885 - 0.729604I$ $a = 1.16854 - 2.90880I$ $b = -2.36887 + 1.57171I$	$1.71280 + 3.10788I$	0
$u = 0.750808 + 0.405787I$ $a = 1.063390 + 0.813737I$ $b = -1.177760 - 0.479406I$	$3.47079 - 0.34806I$	$0. + 2.44010I$
$u = 0.750808 - 0.405787I$ $a = 1.063390 - 0.813737I$ $b = -1.177760 + 0.479406I$	$3.47079 + 0.34806I$	$0. - 2.44010I$
$u = -0.846576 + 0.783100I$ $a = 1.76856 + 1.13808I$ $b = -0.49787 - 2.92558I$	$1.70345 + 1.79198I$	0
$u = -0.846576 - 0.783100I$ $a = 1.76856 - 1.13808I$ $b = -0.49787 + 2.92558I$	$1.70345 - 1.79198I$	0
$u = 1.105160 + 0.366027I$ $a = 0.072699 - 0.394651I$ $b = -0.515812 - 0.642478I$	$2.89716 - 6.12343I$	0
$u = 1.105160 - 0.366027I$ $a = 0.072699 + 0.394651I$ $b = -0.515812 + 0.642478I$	$2.89716 + 6.12343I$	0
$u = -0.818643 + 0.838124I$ $a = -1.49455 - 1.26439I$ $b = 0.34626 + 2.52990I$	$6.29916 - 1.89386I$	0
$u = -0.818643 - 0.838124I$ $a = -1.49455 + 1.26439I$ $b = 0.34626 - 2.52990I$	$6.29916 + 1.89386I$	0
$u = -0.686110 + 0.456826I$ $a = 0.541999 + 0.343912I$ $b = 0.844191 + 0.091293I$	-1.05881	$-7.04899 + 0.I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.686110 - 0.456826I$ $a = 0.541999 - 0.343912I$ $b = 0.844191 - 0.091293I$	-1.05881	$-7.04899 + 0.I$
$u = 0.879564 + 0.782202I$ $a = -2.48262 - 1.84244I$ $b = 2.33766 + 0.15453I$	6.74222	0
$u = 0.879564 - 0.782202I$ $a = -2.48262 + 1.84244I$ $b = 2.33766 - 0.15453I$	6.74222	0
$u = 1.128620 + 0.339818I$ $a = -0.179591 + 0.381211I$ $b = 0.592065 + 0.635114I$	$2.19501 - 12.13950I$	0
$u = 1.128620 - 0.339818I$ $a = -0.179591 - 0.381211I$ $b = 0.592065 - 0.635114I$	$2.19501 + 12.13950I$	0
$u = 0.846457 + 0.825135I$ $a = 0.65254 - 1.45537I$ $b = 0.50726 + 1.67242I$	$4.38253 - 2.76075I$	0
$u = 0.846457 - 0.825135I$ $a = 0.65254 + 1.45537I$ $b = 0.50726 - 1.67242I$	$4.38253 + 2.76075I$	0
$u = -0.802208 + 0.140973I$ $a = 0.557150 - 0.373276I$ $b = 0.628483 - 0.240632I$	$-1.40474 + 0.34878I$	$-7.38819 - 0.48879I$
$u = -0.802208 - 0.140973I$ $a = 0.557150 + 0.373276I$ $b = 0.628483 + 0.240632I$	$-1.40474 - 0.34878I$	$-7.38819 + 0.48879I$
$u = -0.852796 + 0.826238I$ $a = 0.72480 + 1.58821I$ $b = 1.37042 - 1.46910I$	$9.40416 - 3.01245I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.852796 - 0.826238I$ $a = 0.72480 - 1.58821I$ $b = 1.37042 + 1.46910I$	$9.40416 + 3.01245I$	0
$u = -0.756346 + 0.920914I$ $a = 1.37912 + 1.48912I$ $b = -0.23915 - 2.32246I$	$10.7083 - 11.6657I$	0
$u = -0.756346 - 0.920914I$ $a = 1.37912 - 1.48912I$ $b = -0.23915 + 2.32246I$	$10.7083 + 11.6657I$	0
$u = -0.921144 + 0.766234I$ $a = 1.08970 + 1.99177I$ $b = 1.49532 - 2.56248I$	$1.47289 + 4.05110I$	0
$u = -0.921144 - 0.766234I$ $a = 1.08970 - 1.99177I$ $b = 1.49532 + 2.56248I$	$1.47289 - 4.05110I$	0
$u = -0.786752 + 0.107835I$ $a = -1.44543 - 0.59084I$ $b = -2.95462 + 1.12027I$	$1.71280 + 3.10788I$	$15.5620 + 5.8107I$
$u = -0.786752 - 0.107835I$ $a = -1.44543 + 0.59084I$ $b = -2.95462 - 1.12027I$	$1.71280 - 3.10788I$	$15.5620 - 5.8107I$
$u = -0.878782 + 0.827666I$ $a = -0.82029 - 1.67464I$ $b = -1.33935 + 1.71105I$	$10.31220 + 3.55575I$	0
$u = -0.878782 - 0.827666I$ $a = -0.82029 + 1.67464I$ $b = -1.33935 - 1.71105I$	$10.31220 - 3.55575I$	0
$u = 0.730111 + 0.963083I$ $a = -0.536660 + 1.024380I$ $b = -0.317022 - 1.266980I$	$10.20200 + 2.57833I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.730111 - 0.963083I$ $a = -0.536660 - 1.024380I$ $b = -0.317022 + 1.266980I$	$10.20200 - 2.57833I$	0
$u = 0.928153 + 0.792251I$ $a = 1.14740 - 1.16199I$ $b = 0.09332 + 1.78424I$	$4.12750 - 3.28305I$	0
$u = 0.928153 - 0.792251I$ $a = 1.14740 + 1.16199I$ $b = 0.09332 - 1.78424I$	$4.12750 + 3.28305I$	0
$u = -0.914373 + 0.816465I$ $a = -1.28901 - 0.79743I$ $b = 0.80994 + 2.29058I$	$10.20200 + 2.57833I$	0
$u = -0.914373 - 0.816465I$ $a = -1.28901 + 0.79743I$ $b = 0.80994 - 2.29058I$	$10.20200 - 2.57833I$	0
$u = 0.759578 + 0.962546I$ $a = 0.559992 - 1.061620I$ $b = 0.311745 + 1.317460I$	$10.31220 - 3.55575I$	0
$u = 0.759578 - 0.962546I$ $a = 0.559992 + 1.061620I$ $b = 0.311745 - 1.317460I$	$10.31220 + 3.55575I$	0
$u = -0.932557 + 0.800894I$ $a = 1.199860 + 0.650051I$ $b = -0.91908 - 2.15138I$	$9.15662 + 9.09299I$	0
$u = -0.932557 - 0.800894I$ $a = 1.199860 - 0.650051I$ $b = -0.91908 + 2.15138I$	$9.15662 - 9.09299I$	0
$u = 0.995053 + 0.728678I$ $a = -1.055620 + 0.564454I$ $b = 0.05946 - 1.44187I$	$2.64548 - 6.03975I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.995053 - 0.728678I$ $a = -1.055620 - 0.564454I$ $b = 0.05946 + 1.44187I$	$2.64548 + 6.03975I$	0
$u = -0.753137 + 0.142943I$ $a = 1.48723 + 0.69495I$ $b = 2.46674 - 1.23724I$	$1.75351 - 2.44365I$	$7.89478 + 9.66086I$
$u = -0.753137 - 0.142943I$ $a = 1.48723 - 0.69495I$ $b = 2.46674 + 1.23724I$	$1.75351 + 2.44365I$	$7.89478 - 9.66086I$
$u = -1.225610 + 0.208224I$ $a = 0.391824 - 0.174448I$ $b = -0.013628 + 0.275145I$	$1.70345 + 1.79198I$	0
$u = -1.225610 - 0.208224I$ $a = 0.391824 + 0.174448I$ $b = -0.013628 - 0.275145I$	$1.70345 - 1.79198I$	0
$u = -0.960073 + 0.791715I$ $a = -1.11430 - 1.81231I$ $b = -1.11043 + 2.41682I$	$5.86063 + 7.97916I$	0
$u = -0.960073 - 0.791715I$ $a = -1.11430 + 1.81231I$ $b = -1.11043 - 2.41682I$	$5.86063 - 7.97916I$	0
$u = -1.221170 + 0.248957I$ $a = -0.377952 + 0.202515I$ $b = -0.011493 - 0.335636I$	$1.47289 - 4.05110I$	0
$u = -1.221170 - 0.248957I$ $a = -0.377952 - 0.202515I$ $b = -0.011493 + 0.335636I$	$1.47289 + 4.05110I$	0
$u = -0.991388 + 0.769708I$ $a = 1.18009 + 1.79469I$ $b = 0.97907 - 2.57885I$	$2.19501 + 12.13950I$	0



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.991388 - 0.769708I$ $a = 1.18009 - 1.79469I$ $b = 0.97907 + 2.57885I$	$2.19501 - 12.13950I$	0
$u = -1.021020 + 0.807696I$ $a = -1.17604 - 1.74715I$ $b = -0.80186 + 2.47329I$	$10.7083 + 11.6657I$	0
$u = -1.021020 - 0.807696I$ $a = -1.17604 + 1.74715I$ $b = -0.80186 - 2.47329I$	$10.7083 - 11.6657I$	0
$u = -0.069448 + 0.675458I$ $a = 0.492940 + 0.490759I$ $b = 0.446685 + 0.191115I$	$-0.79965 + 4.04123I$	$-5.17521 - 7.54146I$
$u = -0.069448 - 0.675458I$ $a = 0.492940 - 0.490759I$ $b = 0.446685 - 0.191115I$	$-0.79965 - 4.04123I$	$-5.17521 + 7.54146I$
$u = 1.048440 + 0.831393I$ $a = 0.737106 - 0.872873I$ $b = 0.16449 + 1.52379I$	$9.40416 - 3.01245I$	0
$u = 1.048440 - 0.831393I$ $a = 0.737106 + 0.872873I$ $b = 0.16449 - 1.52379I$	$9.40416 + 3.01245I$	0
$u = 1.063500 + 0.815094I$ $a = -0.716411 + 0.821122I$ $b = -0.16567 - 1.50016I$	$9.15662 - 9.09299I$	0
$u = 1.063500 - 0.815094I$ $a = -0.716411 - 0.821122I$ $b = -0.16567 + 1.50016I$	$9.15662 + 9.09299I$	0
$u = 0.651510$ $a = -1.91887$ $b = 1.19129$	$-2.43233$	10.8950

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.425242 + 0.386203I$ $a = -1.28226 - 2.39252I$ $b = 0.230663 + 0.508900I$	$4.38253 - 2.76075I$	$-0.23115 + 5.66298I$
$u = 0.425242 - 0.386203I$ $a = -1.28226 + 2.39252I$ $b = 0.230663 - 0.508900I$	$4.38253 + 2.76075I$	$-0.23115 - 5.66298I$
$u = 0.291531 + 0.377070I$ $a = 1.62731 + 2.63950I$ $b = -0.180225 - 0.647686I$	$4.12750 + 3.28305I$	$-0.737032 - 0.421466I$
$u = 0.291531 - 0.377070I$ $a = 1.62731 - 2.63950I$ $b = -0.180225 + 0.647686I$	$4.12750 - 3.28305I$	$-0.737032 + 0.421466I$
$u = -0.177953 + 0.028058I$ $a = 3.73111 - 0.78030I$ $b = 0.526611 - 0.507482I$	$-1.40474 + 0.34878I$	$-7.38819 - 0.48879I$
$u = -0.177953 - 0.028058I$ $a = 3.73111 + 0.78030I$ $b = 0.526611 + 0.507482I$	$-1.40474 - 0.34878I$	$-7.38819 + 0.48879I$

$$\text{III. } I_3^u = \langle -2u^2 + b, 2u^2 + a - u - 1, u^3 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u^2 + u + 1 \\ 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 + u \\ u^2 - u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - u \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + u \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + u \\ u^2 - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-2u^2 + 7u - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_{12}$	$(u - 1)^3$
$c_3, c_4, c_{11}$	$u^3 + u^2 + 2u + 1$
$c_5, c_6$	$(u + 1)^3$
$c_7$	$u^3 + u^2 - 1$
$c_8$	$u^3$
$c_9$	$u^3 - u^2 + 2u - 1$
$c_{10}$	$u^3 - u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_{12}$	$(y - 1)^3$
$c_3, c_4, c_9$ $c_{11}$	$y^3 + 3y^2 + 2y - 1$
$c_7, c_{10}$	$y^3 - y^2 + 2y - 1$
$c_8$	$y^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 + 0.744862I$ $a = 1.44728 - 1.86942I$ $b = 0.43016 + 2.61428I$	$1.37919 - 2.82812I$	$-4.28809 + 2.59975I$
$u = 0.877439 - 0.744862I$ $a = 1.44728 + 1.86942I$ $b = 0.43016 - 2.61428I$	$1.37919 + 2.82812I$	$-4.28809 - 2.59975I$
$u = -0.754878$ $a = -0.894558$ $b = 1.13968$	$-2.75839$	$-16.4240$

$$\text{IV. } I_4^u = \langle b^3 - b^2 + 2b - 1, a, u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -b \\ b \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -b^2 \\ b^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -b \\ 2b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -b^2 \\ 2b^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-7b^2 + 5b - 17$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^3 - u^2 + 2u - 1$
$c_2$	$u^3 + u^2 - 1$
$c_3, c_4, c_6$	$u^3 + u^2 + 2u + 1$
$c_5$	$u^3 - u^2 + 1$
$c_7, c_8, c_9$	$(u - 1)^3$
$c_{10}, c_{11}$	$(u + 1)^3$
$c_{12}$	$u^3$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6$	$y^3 + 3y^2 + 2y - 1$
$c_2, c_5$	$y^3 - y^2 + 2y - 1$
$c_7, c_8, c_9$ $c_{10}, c_{11}$	$(y - 1)^3$
$c_{12}$	$y^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = 0$ $b = 0.215080 + 1.307140I$	$1.37919 - 2.82812I$	$-4.28809 + 2.59975I$
$u = -1.00000$ $a = 0$ $b = 0.215080 - 1.307140I$	$1.37919 + 2.82812I$	$-4.28809 - 2.59975I$
$u = -1.00000$ $a = 0$ $b = 0.569840$	$-2.75839$	$-16.4240$

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$((u-1)^3)(u^3 - u^2 + 2u - 1)(u^{13} + 4u^{12} + \dots - u + 1)$ $\cdot (u^{86} + 25u^{85} + \dots + 77u + 1)$
$c_2, c_7$	$(u-1)^3(u^3 + u^2 - 1)$ $\cdot (u^{13} + 2u^{12} - 4u^{10} - u^9 + 6u^8 + 4u^7 - 6u^6 - 6u^5 + 2u^4 + 4u^3 + u^2 + u + 1)$ $\cdot (u^{86} + 3u^{85} + \dots - 9u - 1)$
$c_3$	$((u^3 + u^2 + 2u + 1)^2)(u^{13} - 19u^{12} + \dots + 208u - 32)$ $\cdot (u^{43} + 8u^{42} + \dots + 168u + 17)^2$
$c_4$	$((u^3 + u^2 + 2u + 1)^2)(u^{13} - 19u^{12} + \dots + 1920u - 256)$ $\cdot (u^{43} + 7u^{42} + \dots + 736u - 47)^2$
$c_5, c_{10}$	$(u+1)^3(u^3 - u^2 + 1)$ $\cdot (u^{13} + 2u^{12} - 4u^{10} - u^9 + 6u^8 + 4u^7 - 6u^6 - 6u^5 + 2u^4 + 4u^3 + u^2 + u + 1)$ $\cdot (u^{86} + 3u^{85} + \dots - 9u - 1)$
$c_6, c_{11}$	$((u+1)^3)(u^3 + u^2 + 2u + 1)(u^{13} + 4u^{12} + \dots - u + 1)$ $\cdot (u^{86} + 25u^{85} + \dots + 77u + 1)$
$c_8, c_{12}$	$u^3(u-1)^3$ $\cdot (u^{13} - 2u^{10} + 7u^9 + 8u^7 - 10u^6 + 8u^5 - 10u^4 + 14u^3 - 7u^2 + 5u - 1)$ $\cdot (u^{86} + 10u^{85} + \dots - 12u - 8)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_9$ $c_{11}$	$((y-1)^3)(y^3 + 3y^2 + 2y - 1)(y^{13} + 12y^{12} + \dots + 7y - 1)$ $\cdot (y^{86} + 75y^{85} + \dots - 1501y + 1)$
$c_2, c_5, c_7$ $c_{10}$	$((y-1)^3)(y^3 - y^2 + 2y - 1)(y^{13} - 4y^{12} + \dots - y - 1)$ $\cdot (y^{86} - 25y^{85} + \dots - 77y + 1)$
$c_3$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{13} - 39y^{12} + \dots - 17664y - 1024)$ $\cdot (y^{43} - 48y^{42} + \dots + 9150y - 289)^2$
$c_4$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{13} - 33y^{12} + \dots + 49152y - 65536)$ $\cdot (y^{43} - 9y^{42} + \dots + 645754y - 2209)^2$
$c_8, c_{12}$	$y^3(y-1)^3(y^{13} + 14y^{11} + \dots + 11y - 1)$ $\cdot (y^{86} - 24y^{85} + \dots - 1872y + 64)$