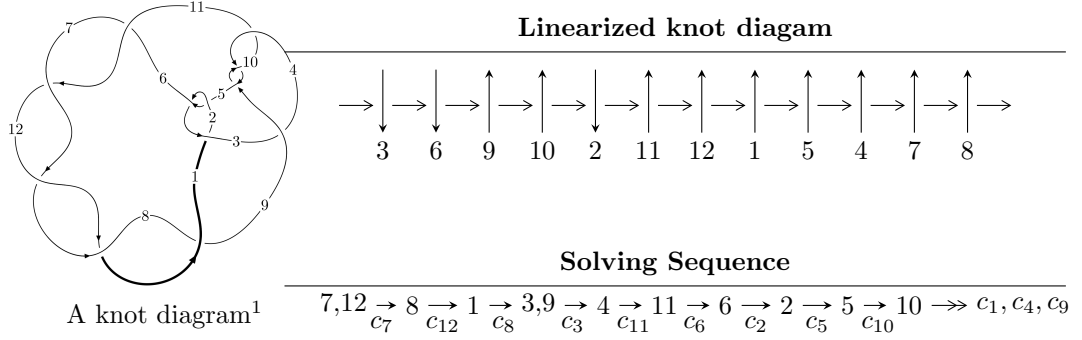


12a<sub>0371</sub> (K12a<sub>0371</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 6.22403 \times 10^{15} u^{53} - 2.16644 \times 10^{16} u^{52} + \dots + 1.15315 \times 10^{16} b + 1.86130 \times 10^{15}, \\ - 3.84141 \times 10^{15} u^{53} - 5.38285 \times 10^{15} u^{52} + \dots + 3.45944 \times 10^{16} a + 4.72334 \times 10^{16}, u^{54} - 2u^{53} + \dots - 9u \rangle$$

$$I_2^u = \langle b + 1, a - 1, u^2 - u - 1 \rangle$$

$$I_3^u = \langle -au + b - u - 1, a^2 + 2a + 3, u^2 + u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 60 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 6.22 \times 10^{15} u^{53} - 2.17 \times 10^{16} u^{52} + \dots + 1.15 \times 10^{16} b + 1.86 \times 10^{15}, -3.84 \times 10^{15} u^{53} - 5.38 \times 10^{15} u^{52} + \dots + 3.46 \times 10^{16} a + 4.72 \times 10^{16}, u^{54} - 2u^{53} + \dots - 9u + 3 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.111041u^{53} + 0.155599u^{52} + \dots + 4.11220u - 1.36535 \\ -0.539742u^{53} + 1.87871u^{52} + \dots + 3.32643u - 0.161411 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.607017u^{53} + 0.0379752u^{52} + \dots + 3.56687u - 1.29746 \\ -1.30686u^{53} + 2.07232u^{52} + \dots - 0.567204u + 1.29954 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.874650u^{53} + 0.540026u^{52} + \dots + 6.16049u - 2.08423 \\ -1.85817u^{53} + 1.24119u^{52} + \dots - 7.27374u + 3.92680 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.818828u^{53} - 1.31508u^{52} + \dots - 12.3614u + 1.51037 \\ -1.22880u^{53} + 1.80213u^{52} + \dots + 3.71901u - 0.853328 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.287418u^{53} - 0.715155u^{52} + \dots - 7.57410u + 3.47537 \\ 0.496261u^{53} + 1.55979u^{52} + \dots + 11.6363u - 3.00772 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{1362927332552725}{5765740254433699} u^{53} - \frac{23381515261364111}{5765740254433699} u^{52} + \dots - \frac{315387112075661492}{5765740254433699} u + \frac{81812943695667795}{5765740254433699}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{54} + 25u^{53} + \dots + 4038u + 121$
$c_2, c_5$	$u^{54} + 3u^{53} + \dots - 12u + 11$
$c_3$	$u^{54} - u^{53} + \dots - 1064u + 212$
$c_4, c_9, c_{10}$	$u^{54} + u^{53} + \dots - 36u^2 + 4$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$u^{54} + 2u^{53} + \dots + 9u + 3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{54} + 15y^{53} + \dots - 5943246y + 14641$
$c_2, c_5$	$y^{54} - 25y^{53} + \dots - 4038y + 121$
$c_3$	$y^{54} - 11y^{53} + \dots - 679264y + 44944$
$c_4, c_9, c_{10}$	$y^{54} + 49y^{53} + \dots - 288y + 16$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^{54} - 72y^{53} + \dots + 15y + 9$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.033200 + 0.205031I$ $a = -0.154928 - 0.608627I$ $b = 0.043531 - 1.156360I$	$2.48098 - 2.65644I$	0
$u = -1.033200 - 0.205031I$ $a = -0.154928 + 0.608627I$ $b = 0.043531 + 1.156360I$	$2.48098 + 2.65644I$	0
$u = -0.909027 + 0.201496I$ $a = 1.133080 - 0.239512I$ $b = -1.44506 + 0.44518I$	$-4.31420 - 2.29321I$	$6.00000 + 3.97838I$
$u = -0.909027 - 0.201496I$ $a = 1.133080 + 0.239512I$ $b = -1.44506 - 0.44518I$	$-4.31420 + 2.29321I$	$6.00000 - 3.97838I$
$u = -1.002340 + 0.391017I$ $a = 0.373522 - 0.490684I$ $b = 0.159427 - 1.337780I$	$-0.92608 - 10.90870I$	0
$u = -1.002340 - 0.391017I$ $a = 0.373522 + 0.490684I$ $b = 0.159427 + 1.337780I$	$-0.92608 + 10.90870I$	0
$u = -1.035390 + 0.306908I$ $a = -0.826876 + 0.402579I$ $b = 0.073409 + 0.249362I$	$1.28679 - 5.35006I$	0
$u = -1.035390 - 0.306908I$ $a = -0.826876 - 0.402579I$ $b = 0.073409 - 0.249362I$	$1.28679 + 5.35006I$	0
$u = 1.035020 + 0.327197I$ $a = -0.175793 - 0.504243I$ $b = -0.136856 - 1.285110I$	$4.34470 + 6.91339I$	0
$u = 1.035020 - 0.327197I$ $a = -0.175793 + 0.504243I$ $b = -0.136856 + 1.285110I$	$4.34470 - 6.91339I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.084440 + 0.195251I$ $a = 0.775059 + 0.381941I$ $b = -0.098656 + 0.410716I$	$5.85353 + 1.52576I$	0
$u = 1.084440 - 0.195251I$ $a = 0.775059 - 0.381941I$ $b = -0.098656 - 0.410716I$	$5.85353 - 1.52576I$	0
$u = -1.120580 + 0.004894I$ $a = -0.589724 + 0.389273I$ $b = 0.128535 + 0.742200I$	$3.05827 + 2.30358I$	0
$u = -1.120580 - 0.004894I$ $a = -0.589724 - 0.389273I$ $b = 0.128535 - 0.742200I$	$3.05827 - 2.30358I$	0
$u = 0.849728 + 0.155769I$ $a = 0.39360 - 1.41513I$ $b = 0.39372 - 1.40393I$	$-4.89459 + 1.45597I$	$7.23813 - 5.57336I$
$u = 0.849728 - 0.155769I$ $a = 0.39360 + 1.41513I$ $b = 0.39372 + 1.40393I$	$-4.89459 - 1.45597I$	$7.23813 + 5.57336I$
$u = 0.824308$ $a = -1.10776$ $b = 1.34525$	$-0.0557748$	15.4170
$u = 0.611997 + 0.492090I$ $a = -0.641324 - 0.317061I$ $b = 0.772587 + 0.690967I$	$-3.28887 - 3.64964I$	$5.12459 + 1.94620I$
$u = 0.611997 - 0.492090I$ $a = -0.641324 + 0.317061I$ $b = 0.772587 - 0.690967I$	$-3.28887 + 3.64964I$	$5.12459 - 1.94620I$
$u = 0.184324 + 0.638362I$ $a = 1.16880 + 1.08855I$ $b = 0.356445 - 0.466281I$	$-4.58312 + 7.42689I$	$2.31046 - 6.99724I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.184324 - 0.638362I$ $a = 1.16880 - 1.08855I$ $b = 0.356445 + 0.466281I$	$-4.58312 - 7.42689I$	$2.31046 + 6.99724I$
$u = 0.454241 + 0.453212I$ $a = 0.661574 + 0.833835I$ $b = 0.301434 - 0.167958I$	$-2.14560 + 0.88769I$	$6.18591 - 4.35554I$
$u = 0.454241 - 0.453212I$ $a = 0.661574 - 0.833835I$ $b = 0.301434 + 0.167958I$	$-2.14560 - 0.88769I$	$6.18591 + 4.35554I$
$u = -0.455135 + 0.442932I$ $a = 0.490955 - 0.173110I$ $b = -0.587686 + 0.546971I$	$1.046370 + 0.494844I$	$10.64023 + 0.18722I$
$u = -0.455135 - 0.442932I$ $a = 0.490955 + 0.173110I$ $b = -0.587686 - 0.546971I$	$1.046370 - 0.494844I$	$10.64023 - 0.18722I$
$u = -0.248292 + 0.564754I$ $a = -0.98947 + 1.14172I$ $b = -0.374122 - 0.374831I$	$0.36246 - 3.88016I$	$7.34275 + 7.06872I$
$u = -0.248292 - 0.564754I$ $a = -0.98947 - 1.14172I$ $b = -0.374122 + 0.374831I$	$0.36246 + 3.88016I$	$7.34275 - 7.06872I$
$u = 0.260818 + 0.544636I$ $a = -0.240106 - 0.253128I$ $b = 0.306471 + 0.627052I$	$-2.73742 + 2.46050I$	$4.87493 - 3.38491I$
$u = 0.260818 - 0.544636I$ $a = -0.240106 + 0.253128I$ $b = 0.306471 - 0.627052I$	$-2.73742 - 2.46050I$	$4.87493 + 3.38491I$
$u = -1.54880 + 0.05145I$ $a = -0.928695 - 0.013670I$ $b = 0.951552 + 0.345464I$	$3.71593 + 1.81884I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.54880 - 0.05145I$ $a = -0.928695 + 0.013670I$ $b = 0.951552 - 0.345464I$	$3.71593 - 1.81884I$	0
$u = -0.421997$ $a = -0.252936$ $b = -0.323293$	0.611710	16.5140
$u = 1.59012$ $a = 1.01605$ $b = -1.17062$	7.70118	0
$u = 0.209460 + 0.318057I$ $a = 0.26966 + 1.81111I$ $b = 0.598382 - 0.217505I$	$-1.44891 + 0.87205I$	$-0.45042 - 2.57700I$
$u = 0.209460 - 0.318057I$ $a = 0.26966 - 1.81111I$ $b = 0.598382 + 0.217505I$	$-1.44891 - 0.87205I$	$-0.45042 + 2.57700I$
$u = 0.052280 + 0.369852I$ $a = -2.16277 + 2.09624I$ $b = -0.774037 - 0.521212I$	$-7.25657 + 0.32248I$	$-3.59043 - 0.24507I$
$u = 0.052280 - 0.369852I$ $a = -2.16277 - 2.09624I$ $b = -0.774037 + 0.521212I$	$-7.25657 - 0.32248I$	$-3.59043 + 0.24507I$
$u = -1.68847 + 0.03150I$ $a = -0.90904 - 3.14347I$ $b = 1.74981 + 5.17567I$	$4.15513 - 2.12237I$	0
$u = -1.68847 - 0.03150I$ $a = -0.90904 + 3.14347I$ $b = 1.74981 - 5.17567I$	$4.15513 + 2.12237I$	0
$u = -1.69091$ $a = -1.02001$ $b = 0.854840$	8.98922	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.69828 + 0.04672I$		
$a = 1.022170 + 0.018668I$	$4.95768 + 3.23508I$	0
$b = -0.834861 + 0.045952I$		
$u = 1.69828 - 0.04672I$		
$a = 1.022170 - 0.018668I$	$4.95768 - 3.23508I$	0
$b = -0.834861 - 0.045952I$		
$u = 1.71944 + 0.10562I$		
$a = -0.42831 - 2.69040I$	$8.6699 + 12.9219I$	0
$b = 0.36112 + 4.43030I$		
$u = 1.71944 - 0.10562I$		
$a = -0.42831 + 2.69040I$	$8.6699 - 12.9219I$	0
$b = 0.36112 - 4.43030I$		
$u = 1.72963 + 0.05599I$		
$a = 0.14187 - 2.61907I$	$12.36250 + 3.74731I$	0
$b = -0.54631 + 4.33951I$		
$u = 1.72963 - 0.05599I$		
$a = 0.14187 + 2.61907I$	$12.36250 - 3.74731I$	0
$b = -0.54631 - 4.33951I$		
$u = 1.72946 + 0.07949I$		
$a = 0.62410 + 1.44096I$	$11.12150 + 6.92662I$	0
$b = -1.29088 - 2.56923I$		
$u = 1.72946 - 0.07949I$		
$a = 0.62410 - 1.44096I$	$11.12150 - 6.92662I$	0
$b = -1.29088 + 2.56923I$		
$u = -1.72986 + 0.08588I$		
$a = 0.19966 - 2.64199I$	$14.1686 - 8.6037I$	0
$b = 0.00573 + 4.36280I$		
$u = -1.72986 - 0.08588I$		
$a = 0.19966 + 2.64199I$	$14.1686 + 8.6037I$	0
$b = 0.00573 - 4.36280I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.73989 + 0.05063I$ $a = -0.61741 + 1.65827I$ $b = 1.29019 - 2.88401I$	$15.9719 - 2.5529I$	0
$u = -1.73989 - 0.05063I$ $a = -0.61741 - 1.65827I$ $b = 1.29019 + 2.88401I$	$15.9719 + 2.5529I$	0
$u = 1.74111 + 0.01390I$ $a = 0.59275 + 1.97467I$ $b = -1.25696 - 3.35550I$	$13.30770 - 2.12200I$	0
$u = 1.74111 - 0.01390I$ $a = 0.59275 - 1.97467I$ $b = -1.25696 + 3.35550I$	$13.30770 + 2.12200I$	0

$$\text{II. } I_2^u = \langle b + 1, a - 1, u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u + 1 \\ -u - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 2

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_4, c_9$ $c_{10}$	$u^2$
$c_5$	$(u + 1)^2$
$c_6, c_7, c_8$	$u^2 - u - 1$
$c_{11}, c_{12}$	$u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^2$
$c_3, c_4, c_9$ $c_{10}$	$y^2$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^2 - 3y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$ $a = 1.00000$ $b = -1.00000$	-0.657974	2.00000
$u = 1.61803$ $a = 1.00000$ $b = -1.00000$	7.23771	2.00000

$$\text{III. } I_3^u = \langle -au + b - u - 1, a^2 + 2a + 3, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ au + u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} au + a + u \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + u \\ au + 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a \\ -au - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a + u + 3 \\ -a + u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u - 1)^4$
$c_2$	$(u + 1)^4$
$c_3, c_4, c_9$ $c_{10}$	$(u^2 + 2)^2$
$c_6, c_7, c_8$	$(u^2 + u - 1)^2$
$c_{11}, c_{12}$	$(u^2 - u - 1)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^4$
$c_3, c_4, c_9$ $c_{10}$	$(y + 2)^4$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = -1.00000 + 1.41421I$ $b = 1.000000 + 0.874032I$	-5.59278	4.00000
$u = 0.618034$ $a = -1.00000 - 1.41421I$ $b = 1.000000 - 0.874032I$	-5.59278	4.00000
$u = -1.61803$ $a = -1.00000 + 1.41421I$ $b = 1.00000 - 2.28825I$	2.30291	4.00000
$u = -1.61803$ $a = -1.00000 - 1.41421I$ $b = 1.00000 + 2.28825I$	2.30291	4.00000

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^6)(u^{54} + 25u^{53} + \dots + 4038u + 121)$
$c_2$	$((u - 1)^2)(u + 1)^4(u^{54} + 3u^{53} + \dots - 12u + 11)$
$c_3$	$u^2(u^2 + 2)^2(u^{54} - u^{53} + \dots - 1064u + 212)$
$c_4, c_9, c_{10}$	$u^2(u^2 + 2)^2(u^{54} + u^{53} + \dots - 36u^2 + 4)$
$c_5$	$((u - 1)^4)(u + 1)^2(u^{54} + 3u^{53} + \dots - 12u + 11)$
$c_6, c_7, c_8$	$(u^2 - u - 1)(u^2 + u - 1)^2(u^{54} + 2u^{53} + \dots + 9u + 3)$
$c_{11}, c_{12}$	$((u^2 - u - 1)^2)(u^2 + u - 1)(u^{54} + 2u^{53} + \dots + 9u + 3)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^6)(y^{54} + 15y^{53} + \dots - 5943246y + 14641)$
$c_2, c_5$	$((y - 1)^6)(y^{54} - 25y^{53} + \dots - 4038y + 121)$
$c_3$	$y^2(y + 2)^4(y^{54} - 11y^{53} + \dots - 679264y + 44944)$
$c_4, c_9, c_{10}$	$y^2(y + 2)^4(y^{54} + 49y^{53} + \dots - 288y + 16)$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$((y^2 - 3y + 1)^3)(y^{54} - 72y^{53} + \dots + 15y + 9)$