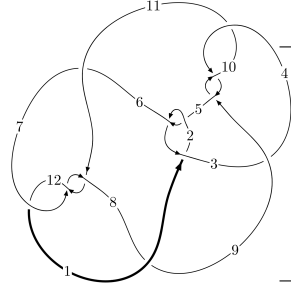
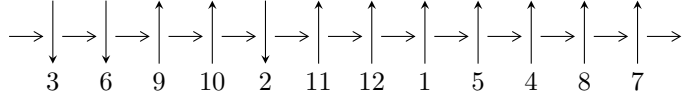


12a<sub>0372</sub> (K12a<sub>0372</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,5 \xrightarrow{c_5} 6 \xrightarrow{c_2} 3 \xrightarrow{c_1} 1,10 \xrightarrow{c_4} 4 \xrightarrow{c_{10}} 11 \xrightarrow{c_6} 7 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \Rightarrow c_3, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -4.00775 \times 10^{87} u^{85} - 2.48507 \times 10^{88} u^{84} + \dots + 1.44535 \times 10^{88} b + 2.76929 \times 10^{89}, \\ -3.45221 \times 10^{89} u^{85} - 1.15168 \times 10^{90} u^{84} + \dots + 4.91419 \times 10^{89} a + 4.17969 \times 10^{90}, \\ u^{86} + 4u^{85} + \dots - 20u - 17 \rangle$$

$$I_2^u = \langle -194a^5 - 315a^4 - 5270a^3 - 4555a^2 + 69650b - 64279a - 26651, \\ a^6 + 2a^5 + 25a^4 + 30a^3 + 206a^2 + 176a + 593, u - 1 \rangle$$

$$I_3^u = \langle b, a^3 + a^2 - 1, u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 95 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -4.01 \times 10^{87} u^{85} - 2.49 \times 10^{88} u^{84} + \dots + 1.45 \times 10^{88} b + 2.77 \times 10^{89}, -3.45 \times 10^{89} u^{85} - 1.15 \times 10^{90} u^{84} + \dots + 4.91 \times 10^{89} a + 4.18 \times 10^{90}, u^{86} + 4u^{85} + \dots - 20u - 17 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.702499u^{85} + 2.34358u^{84} + \dots - 17.6252u - 8.50536 \\ 0.277286u^{85} + 1.71936u^{84} + \dots + 8.31636u - 19.1600 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.504301u^{85} + 1.30510u^{84} + \dots - 13.8214u - 5.82459 \\ 0.0137884u^{85} + 0.0233804u^{84} + \dots + 1.94469u - 3.22686 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.294534u^{85} + 1.15575u^{84} + \dots + 5.28585u - 19.1152 \\ 0.244106u^{85} + 0.263311u^{84} + \dots - 4.48711u + 4.51370 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1.36374u^{85} - 4.50519u^{84} + \dots + 9.32384u + 28.0444 \\ 0.448009u^{85} + 1.37637u^{84} + \dots - 4.79587u - 5.94786 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.425213u^{85} + 0.624223u^{84} + \dots - 25.9416u + 10.6546 \\ 0.277286u^{85} + 1.71936u^{84} + \dots + 8.31636u - 19.1600 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.00970161u^{85} - 0.280717u^{84} + \dots - 21.0594u + 11.2096 \\ 0.0519514u^{85} + 0.807957u^{84} + \dots + 2.49003u - 10.0728 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1.53639u^{85} - 4.66319u^{84} + \dots + 30.2188u + 12.1772 \\ 0.253558u^{85} + 0.199433u^{84} + \dots - 14.9224u + 12.1204 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.907710u^{85} - 2.76373u^{84} + \dots + 58.7556u + 7.47521$

(iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing             |
|-----------------------|--------------------------------------------|
| $c_1$                 | $u^{86} + 42u^{85} + \dots + 8016u + 289$  |
| $c_2, c_5$            | $u^{86} + 4u^{85} + \dots - 20u - 17$      |
| $c_3$                 | $u^{86} - u^{85} + \dots - 8992u + 16424$  |
| $c_4, c_9, c_{10}$    | $u^{86} + u^{85} + \dots + 16u + 8$        |
| $c_6, c_8$            | $u^{86} + 2u^{85} + \dots - 11367u - 2391$ |
| $c_7, c_{11}, c_{12}$ | $u^{86} - 2u^{85} + \dots - 3u - 3$        |

(v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing                   |
|-----------------------|------------------------------------------------------|
| $c_1$                 | $y^{86} + 14y^{85} + \dots - 19463568y + 83521$      |
| $c_2, c_5$            | $y^{86} - 42y^{85} + \dots - 8016y + 289$            |
| $c_3$                 | $y^{86} - 5y^{85} + \dots - 1234215040y + 269747776$ |
| $c_4, c_9, c_{10}$    | $y^{86} + 79y^{85} + \dots - 1280y + 64$             |
| $c_6, c_8$            | $y^{86} - 56y^{85} + \dots + 68087067y + 5716881$    |
| $c_7, c_{11}, c_{12}$ | $y^{86} + 72y^{85} + \dots + 51y + 9$                |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.509248 + 0.852642I$  | $6.59236 + 1.97479I$                  | 0          |
| $a = 0.322825 + 0.048607I$  |                                       |            |
| $b = -0.789445 - 0.160402I$ |                                       |            |
| $u = 0.509248 - 0.852642I$  | $6.59236 - 1.97479I$                  | 0          |
| $a = 0.322825 - 0.048607I$  |                                       |            |
| $b = -0.789445 + 0.160402I$ |                                       |            |
| $u = 0.584122 + 0.824498I$  | $3.13486 - 2.30297I$                  | 0          |
| $a = -0.334198 - 0.153374I$ |                                       |            |
| $b = 0.790561 + 0.106022I$  |                                       |            |
| $u = 0.584122 - 0.824498I$  | $3.13486 + 2.30297I$                  | 0          |
| $a = -0.334198 + 0.153374I$ |                                       |            |
| $b = 0.790561 - 0.106022I$  |                                       |            |
| $u = -0.329631 + 0.932362I$ | $-2.75721 - 10.22800I$                | 0          |
| $a = -0.451079 - 0.979419I$ |                                       |            |
| $b = 0.32373 - 1.38168I$    |                                       |            |
| $u = -0.329631 - 0.932362I$ | $-2.75721 + 10.22800I$                | 0          |
| $a = -0.451079 + 0.979419I$ |                                       |            |
| $b = 0.32373 + 1.38168I$    |                                       |            |
| $u = 0.896991 + 0.410818I$  | $-4.54753 - 1.67750I$                 | 0          |
| $a = 0.53853 + 2.78692I$    |                                       |            |
| $b = 0.06533 + 1.51526I$    |                                       |            |
| $u = 0.896991 - 0.410818I$  | $-4.54753 + 1.67750I$                 | 0          |
| $a = 0.53853 - 2.78692I$    |                                       |            |
| $b = 0.06533 - 1.51526I$    |                                       |            |
| $u = -0.371807 + 0.912630I$ | $1.81661 - 5.99490I$                  | 0          |
| $a = 0.399618 + 0.904183I$  |                                       |            |
| $b = -0.326539 + 1.355580I$ |                                       |            |
| $u = -0.371807 - 0.912630I$ | $1.81661 + 5.99490I$                  | 0          |
| $a = 0.399618 - 0.904183I$  |                                       |            |
| $b = -0.326539 - 1.355580I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.447851 + 0.874871I$  | $2.26451 + 6.21660I$                  | 0          |
| $a = -0.312467 + 0.033097I$ |                                       |            |
| $b = 0.787438 + 0.204817I$  |                                       |            |
| $u = 0.447851 - 0.874871I$  | $2.26451 - 6.21660I$                  | 0          |
| $a = -0.312467 - 0.033097I$ |                                       |            |
| $b = 0.787438 - 0.204817I$  |                                       |            |
| $u = -0.608566 + 0.769255I$ | $-0.04968 - 1.95533I$                 | 0          |
| $a = -0.650245 + 0.848054I$ |                                       |            |
| $b = 0.384469 + 0.945216I$  |                                       |            |
| $u = -0.608566 - 0.769255I$ | $-0.04968 + 1.95533I$                 | 0          |
| $a = -0.650245 - 0.848054I$ |                                       |            |
| $b = 0.384469 - 0.945216I$  |                                       |            |
| $u = -0.428356 + 0.876203I$ | $-1.30715 - 1.70626I$                 | 0          |
| $a = -0.326362 - 0.791803I$ |                                       |            |
| $b = 0.324167 - 1.315440I$  |                                       |            |
| $u = -0.428356 - 0.876203I$ | $-1.30715 + 1.70626I$                 | 0          |
| $a = -0.326362 + 0.791803I$ |                                       |            |
| $b = 0.324167 + 1.315440I$  |                                       |            |
| $u = -0.686031 + 0.768487I$ | $3.93150 + 2.25304I$                  | 0          |
| $a = 0.752897 - 0.902852I$  |                                       |            |
| $b = -0.373726 - 1.024720I$ |                                       |            |
| $u = -0.686031 - 0.768487I$ | $3.93150 - 2.25304I$                  | 0          |
| $a = 0.752897 + 0.902852I$  |                                       |            |
| $b = -0.373726 + 1.024720I$ |                                       |            |
| $u = 0.924737 + 0.534530I$  | $0.27137 - 3.73444I$                  | 0          |
| $a = 0.575892 + 0.848478I$  |                                       |            |
| $b = -0.665118 + 0.182466I$ |                                       |            |
| $u = 0.924737 - 0.534530I$  | $0.27137 + 3.73444I$                  | 0          |
| $a = 0.575892 - 0.848478I$  |                                       |            |
| $b = -0.665118 - 0.182466I$ |                                       |            |

| Solutions to $I_1^u$                                                                      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape      |
|-------------------------------------------------------------------------------------------|---------------------------------------|-----------------|
| $u = 0.966175 + 0.460720I$<br>$a = -0.52607 - 2.70537I$<br>$b = -0.09038 - 1.52749I$      | $-8.90441 - 5.42664I$                 | 0               |
| $u = 0.966175 - 0.460720I$<br>$a = -0.52607 + 2.70537I$<br>$b = -0.09038 + 1.52749I$      | $-8.90441 + 5.42664I$                 | 0               |
| $u = -0.756050 + 0.766739I$<br>$a = -0.861234 + 0.982031I$<br>$b = 0.371400 + 1.094440I$  | $0.10136 + 6.51112I$                  | 0               |
| $u = -0.756050 - 0.766739I$<br>$a = -0.861234 - 0.982031I$<br>$b = 0.371400 - 1.094440I$  | $0.10136 - 6.51112I$                  | 0               |
| $u = -0.986156 + 0.463423I$<br>$a = 2.45774 - 1.20507I$<br>$b = -0.189677 - 1.345070I$    | $-8.83115 + 0.16688I$                 | 0               |
| $u = -0.986156 - 0.463423I$<br>$a = 2.45774 + 1.20507I$<br>$b = -0.189677 + 1.345070I$    | $-8.83115 - 0.16688I$                 | 0               |
| $u = -0.871820 + 0.230790I$<br>$a = -0.264628 + 0.427871I$<br>$b = -0.187263 + 0.458115I$ | $-1.46632 + 0.85886I$                 | $0. - 2.31420I$ |
| $u = -0.871820 - 0.230790I$<br>$a = -0.264628 - 0.427871I$<br>$b = -0.187263 - 0.458115I$ | $-1.46632 - 0.85886I$                 | $0. + 2.31420I$ |
| $u = -0.879504 + 0.671225I$<br>$a = -0.360993 + 0.571062I$<br>$b = -0.418022 + 0.882634I$ | $-0.283252 - 1.079100I$               | 0               |
| $u = -0.879504 - 0.671225I$<br>$a = -0.360993 - 0.571062I$<br>$b = -0.418022 - 0.882634I$ | $-0.283252 + 1.079100I$               | 0               |

| Solutions to $I_1^u$                                                                    | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------------------------------------------------------------------|---------------------------------------|----------------------|
| $u = 1.100000 + 0.189928I$<br>$a = -0.23593 - 2.68382I$<br>$b = -0.089636 - 1.408420I$  | $-7.23808 + 0.30916I$                 | 0                    |
| $u = 1.100000 - 0.189928I$<br>$a = -0.23593 + 2.68382I$<br>$b = -0.089636 + 1.408420I$  | $-7.23808 - 0.30916I$                 | 0                    |
| $u = -0.981639 + 0.534063I$<br>$a = -2.00458 + 1.26234I$<br>$b = 0.229804 + 1.325390I$  | $-3.48232 + 3.39964I$                 | 0                    |
| $u = -0.981639 - 0.534063I$<br>$a = -2.00458 - 1.26234I$<br>$b = 0.229804 - 1.325390I$  | $-3.48232 - 3.39964I$                 | 0                    |
| $u = 0.742085 + 0.454046I$<br>$a = -0.864160 - 0.546861I$<br>$b = 0.587415 - 0.064260I$ | $0.916106 - 0.421753I$                | $10.41879 + 0.I$     |
| $u = 0.742085 - 0.454046I$<br>$a = -0.864160 + 0.546861I$<br>$b = 0.587415 + 0.064260I$ | $0.916106 + 0.421753I$                | $10.41879 + 0.I$     |
| $u = 0.830940 + 0.240284I$<br>$a = 1.41644 + 0.82559I$<br>$b = -0.448531 + 0.114261I$   | $-4.18135 + 2.25158I$                 | $7.13926 + 2.78271I$ |
| $u = 0.830940 - 0.240284I$<br>$a = 1.41644 - 0.82559I$<br>$b = -0.448531 - 0.114261I$   | $-4.18135 - 2.25158I$                 | $7.13926 - 2.78271I$ |
| $u = 1.047320 + 0.468070I$<br>$a = -0.536699 - 1.151690I$<br>$b = 0.631147 - 0.292577I$ | $-5.75601 - 5.20754I$                 | 0                    |
| $u = 1.047320 - 0.468070I$<br>$a = -0.536699 + 1.151690I$<br>$b = 0.631147 + 0.292577I$ | $-5.75601 + 5.20754I$                 | 0                    |



| Solutions to $I_1^u$                                                                      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-------------------------------------------------------------------------------------------|---------------------------------------|----------------------|
| $u = -1.095810 + 0.344023I$<br>$a = 0.450668 - 0.368225I$<br>$b = 0.464015 - 0.457806I$   | $-6.48632 + 1.75628I$                 | 0                    |
| $u = -1.095810 - 0.344023I$<br>$a = 0.450668 + 0.368225I$<br>$b = 0.464015 + 0.457806I$   | $-6.48632 - 1.75628I$                 | 0                    |
| $u = -0.958955 + 0.647599I$<br>$a = 0.414297 - 0.568075I$<br>$b = 0.474434 - 0.815046I$   | $3.10357 + 3.09687I$                  | 0                    |
| $u = -0.958955 - 0.647599I$<br>$a = 0.414297 + 0.568075I$<br>$b = 0.474434 + 0.815046I$   | $3.10357 - 3.09687I$                  | 0                    |
| $u = 0.753237 + 0.364190I$<br>$a = -0.64318 - 2.95965I$<br>$b = -0.02689 - 1.50940I$      | $-8.07669 + 1.87059I$                 | $2.84516 + 0.42953I$ |
| $u = 0.753237 - 0.364190I$<br>$a = -0.64318 + 2.95965I$<br>$b = -0.02689 + 1.50940I$      | $-8.07669 - 1.87059I$                 | $2.84516 - 0.42953I$ |
| $u = -1.016700 + 0.633935I$<br>$a = -0.451131 + 0.561079I$<br>$b = -0.518692 + 0.772841I$ | $-1.29006 + 7.25611I$                 | 0                    |
| $u = -1.016700 - 0.633935I$<br>$a = -0.451131 - 0.561079I$<br>$b = -0.518692 - 0.772841I$ | $-1.29006 - 7.25611I$                 | 0                    |
| $u = -1.054830 + 0.577809I$<br>$a = 1.81540 - 1.65430I$<br>$b = -0.271885 - 1.362200I$    | $-4.61406 + 7.15880I$                 | 0                    |
| $u = -1.054830 - 0.577809I$<br>$a = 1.81540 + 1.65430I$<br>$b = -0.271885 + 1.362200I$    | $-4.61406 - 7.15880I$                 | 0                    |

| Solutions to $I_1^u$                                                                      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-------------------------------------------------------------------------------------------|---------------------------------------|----------------------|
| $u = -0.426091 + 0.660797I$<br>$a = -0.467482 - 0.247485I$<br>$b = 0.196765 - 1.275150I$  | $-2.83344 - 2.33982I$                 | $4.51071 + 3.69455I$ |
| $u = -0.426091 - 0.660797I$<br>$a = -0.467482 + 0.247485I$<br>$b = 0.196765 + 1.275150I$  | $-2.83344 + 2.33982I$                 | $4.51071 - 3.69455I$ |
| $u = 1.171760 + 0.330721I$<br>$a = 0.36279 + 2.60051I$<br>$b = 0.15928 + 1.45009I$        | $-12.60960 + 0.53188I$                | 0                    |
| $u = 1.171760 - 0.330721I$<br>$a = 0.36279 - 2.60051I$<br>$b = 0.15928 - 1.45009I$        | $-12.60960 - 0.53188I$                | 0                    |
| $u = -0.561224 + 0.536687I$<br>$a = -0.130904 - 0.198541I$<br>$b = -0.091191 + 1.196000I$ | $-2.28991 + 0.95503I$                 | $5.78427 - 4.47037I$ |
| $u = -0.561224 - 0.536687I$<br>$a = -0.130904 + 0.198541I$<br>$b = -0.091191 - 1.196000I$ | $-2.28991 - 0.95503I$                 | $5.78427 + 4.47037I$ |
| $u = -1.23000$<br>$a = 0.487096$<br>$b = 0.526354$                                        | 0.302978                              | 0                    |
| $u = 1.033160 + 0.672308I$<br>$a = 0.249124 + 0.871946I$<br>$b = -0.792360 + 0.236164I$   | $1.77987 - 3.27789I$                  | 0                    |
| $u = 1.033160 - 0.672308I$<br>$a = 0.249124 - 0.871946I$<br>$b = -0.792360 - 0.236164I$   | $1.77987 + 3.27789I$                  | 0                    |
| $u = -1.120250 + 0.532355I$<br>$a = -1.98299 + 2.00595I$<br>$b = 0.25455 + 1.40909I$      | $-11.17690 + 8.47102I$                | 0                    |

| Solutions to $I_1^u$                                                                      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-------------------------------------------------------------------------------------------|---------------------------------------|----------------------|
| $u = -1.120250 - 0.532355I$<br>$a = -1.98299 - 2.00595I$<br>$b = 0.25455 - 1.40909I$      | $-11.17690 - 8.47102I$                | 0                    |
| $u = -1.253150 + 0.085853I$<br>$a = -0.518095 + 0.091265I$<br>$b = -0.562417 + 0.108346I$ | $-3.71512 - 3.61639I$                 | 0                    |
| $u = -1.253150 - 0.085853I$<br>$a = -0.518095 - 0.091265I$<br>$b = -0.562417 - 0.108346I$ | $-3.71512 + 3.61639I$                 | 0                    |
| $u = 1.087850 + 0.663273I$<br>$a = -0.201529 - 0.952587I$<br>$b = 0.799806 - 0.280258I$   | $4.84791 - 7.60111I$                  | 0                    |
| $u = 1.087850 - 0.663273I$<br>$a = -0.201529 + 0.952587I$<br>$b = 0.799806 + 0.280258I$   | $4.84791 + 7.60111I$                  | 0                    |
| $u = -0.226176 + 0.670392I$<br>$a = 1.092930 + 0.581518I$<br>$b = -0.183977 + 1.375540I$  | $-8.69537 - 3.85336I$                 | $0.06507 + 3.00079I$ |
| $u = -0.226176 - 0.670392I$<br>$a = 1.092930 - 0.581518I$<br>$b = -0.183977 - 1.375540I$  | $-8.69537 + 3.85336I$                 | $0.06507 - 3.00079I$ |
| $u = 1.122620 + 0.650698I$<br>$a = 0.176872 + 1.009790I$<br>$b = -0.799739 + 0.310768I$   | $0.23048 - 11.85200I$                 | 0                    |
| $u = 1.122620 - 0.650698I$<br>$a = 0.176872 - 1.009790I$<br>$b = -0.799739 - 0.310768I$   | $0.23048 + 11.85200I$                 | 0                    |
| $u = -1.126730 + 0.643608I$<br>$a = 1.51181 - 1.91377I$<br>$b = -0.32382 - 1.39843I$      | $-3.40709 + 7.31230I$                 | 0                    |

| Solutions to $I_1^u$                                                                    | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------------------------------------------------------------------|---------------------------------------|----------------------|
| $u = -1.126730 - 0.643608I$<br>$a = 1.51181 + 1.91377I$<br>$b = -0.32382 + 1.39843I$    | $-3.40709 - 7.31230I$                 | 0                    |
| $u = 1.292600 + 0.117096I$<br>$a = -0.17327 - 2.45986I$<br>$b = -0.156978 - 1.269640I$  | $-7.24729 - 1.14255I$                 | 0                    |
| $u = 1.292600 - 0.117096I$<br>$a = -0.17327 + 2.45986I$<br>$b = -0.156978 + 1.269640I$  | $-7.24729 + 1.14255I$                 | 0                    |
| $u = -0.590405 + 0.374886I$<br>$a = 0.544712 + 1.162400I$<br>$b = 0.011567 - 1.267360I$ | $-7.59821 + 3.51299I$                 | $1.50213 - 4.82756I$ |
| $u = -0.590405 - 0.374886I$<br>$a = 0.544712 - 1.162400I$<br>$b = 0.011567 + 1.267360I$ | $-7.59821 - 3.51299I$                 | $1.50213 + 4.82756I$ |
| $u = 1.305650 + 0.179739I$<br>$a = 0.24358 + 2.46781I$<br>$b = 0.200042 + 1.317550I$    | $-3.91048 + 2.62248I$                 | 0                    |
| $u = 1.305650 - 0.179739I$<br>$a = 0.24358 - 2.46781I$<br>$b = 0.200042 - 1.317550I$    | $-3.91048 - 2.62248I$                 | 0                    |
| $u = -1.165480 + 0.637891I$<br>$a = -1.49482 + 2.05321I$<br>$b = 0.32450 + 1.42352I$    | $-0.57989 + 11.67450I$                | 0                    |
| $u = -1.165480 - 0.637891I$<br>$a = -1.49482 - 2.05321I$<br>$b = 0.32450 - 1.42352I$    | $-0.57989 - 11.67450I$                | 0                    |
| $u = 1.322240 + 0.219958I$<br>$a = -0.28506 - 2.46512I$<br>$b = -0.226534 - 1.344900I$  | $-8.34294 + 6.52071I$                 | 0                    |

| Solutions to $I_1^u$                                                                    | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------------------------------------------------------------------|---------------------------------------|----------------------|
| $u = 1.322240 - 0.219958I$<br>$a = -0.28506 + 2.46512I$<br>$b = -0.226534 + 1.344900I$  | $-8.34294 - 6.52071I$                 | 0                    |
| $u = -1.188080 + 0.627308I$<br>$a = 1.50177 - 2.14199I$<br>$b = -0.32023 - 1.43864I$    | $-5.3572 + 15.9154I$                  | 0                    |
| $u = -1.188080 - 0.627308I$<br>$a = 1.50177 + 2.14199I$<br>$b = -0.32023 + 1.43864I$    | $-5.3572 - 15.9154I$                  | 0                    |
| $u = 0.032159 + 0.548639I$<br>$a = 0.683294 - 0.535532I$<br>$b = -0.458589 - 0.358951I$ | $-3.33000 + 1.53573I$                 | $4.91213 - 4.32886I$ |
| $u = 0.032159 - 0.548639I$<br>$a = 0.683294 + 0.535532I$<br>$b = -0.458589 + 0.358951I$ | $-3.33000 - 1.53573I$                 | $4.91213 + 4.32886I$ |
| $u = 0.255360$<br>$a = -1.59057$<br>$b = 0.336114$                                      | 0.640620                              | 15.8240              |

**II.**

$$I_2^u = \langle -194a^5 + 69650b + \dots - 64279a - 26651, a^6 + 2a^5 + \dots + 176a + 593, u - 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 0.00278536a^5 + 0.00452261a^4 + \dots + 0.922886a + 0.382642 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.00104810a^5 + 0.00603015a^4 + \dots - 0.107581a - 0.651716 \\ -2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.00278536a^5 + 0.00452261a^4 + \dots - 0.0771141a + 0.382642 \\ -0.00278536a^5 - 0.00452261a^4 + \dots - 0.922886a - 0.382642 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.00314429a^5 - 0.0180905a^4 + \dots + 0.322742a + 1.95515 \\ -0.00104810a^5 + 0.00603015a^4 + \dots - 0.107581a + 3.34828 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.00278536a^5 - 0.00452261a^4 + \dots + 0.0771141a - 0.382642 \\ 0.00278536a^5 + 0.00452261a^4 + \dots + 0.922886a + 0.382642 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.00835607a^5 - 0.0135678a^4 + \dots - 0.768658a - 1.14793 \\ -0.00278536a^5 - 0.00452261a^4 + \dots + 0.0771141a - 0.382642 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0197559a^5 + 0.0246231a^4 + \dots - 1.78810a + 2.72930 \\ -0.0211342a^5 - 0.00854271a^4 + \dots - 2.20355a - 0.429117 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes** =  $-\frac{776}{34825}a^5 - \frac{36}{995}a^4 - \frac{4216}{6965}a^3 - \frac{3644}{6965}a^2 - \frac{117816}{34825}a - \frac{106604}{34825}$

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| $c_1, c_5$                  | $(u - 1)^6$                    |
| $c_2$                       | $(u + 1)^6$                    |
| $c_3, c_4, c_9$<br>$c_{10}$ | $(u^2 + 2)^3$                  |
| $c_6, c_8$                  | $(u^3 + u^2 - 1)^2$            |
| $c_7$                       | $(u^3 - u^2 + 2u - 1)^2$       |
| $c_{11}, c_{12}$            | $(u^3 + u^2 + 2u + 1)^2$       |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing |
|-----------------------------|------------------------------------|
| $c_1, c_2, c_5$             | $(y - 1)^6$                        |
| $c_3, c_4, c_9$<br>$c_{10}$ | $(y + 2)^6$                        |
| $c_6, c_8$                  | $(y^3 - y^2 + 2y - 1)^2$           |
| $c_7, c_{11}, c_{12}$       | $(y^3 + 3y^2 + 2y - 1)^2$          |



(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$                                           | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|----------------------------------------------------------------|---------------------------------------|-----------------------|
| $u = 1.00000$<br>$a = -0.87744 + 2.08357I$<br>$b = 1.414210I$  | $-9.60386 + 2.82812I$                 | $-3.50976 - 2.97945I$ |
| $u = 1.00000$<br>$a = -0.87744 - 2.08357I$<br>$b = -1.414210I$ | $-9.60386 - 2.82812I$                 | $-3.50976 + 2.97945I$ |
| $u = 1.00000$<br>$a = 0.75488 + 2.82843I$<br>$b = 1.414210I$   | $-5.46628$                            | $3.01951 + 0.I$       |
| $u = 1.00000$<br>$a = 0.75488 - 2.82843I$<br>$b = -1.414210I$  | $-5.46628$                            | $3.01951 + 0.I$       |
| $u = 1.00000$<br>$a = -0.87744 + 3.57329I$<br>$b = 1.414210I$  | $-9.60386 - 2.82812I$                 | $-3.50976 + 2.97945I$ |
| $u = 1.00000$<br>$a = -0.87744 - 3.57329I$<br>$b = -1.414210I$ | $-9.60386 + 2.82812I$                 | $-3.50976 - 2.97945I$ |

$$\text{III. } I_3^u = \langle b, a^3 + a^2 - 1, u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a^2 + 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 2a \\ a \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2a^2 + a - 2 \\ a^2 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-2a^2 + 2a + 2$

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| $c_1, c_2$                  | $(u - 1)^3$                    |
| $c_3, c_4, c_9$<br>$c_{10}$ | $u^3$                          |
| $c_5$                       | $(u + 1)^3$                    |
| $c_6, c_8$                  | $u^3 - u^2 + 1$                |
| $c_7$                       | $u^3 + u^2 + 2u + 1$           |
| $c_{11}, c_{12}$            | $u^3 - u^2 + 2u - 1$           |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing |
|-----------------------------|------------------------------------|
| $c_1, c_2, c_5$             | $(y - 1)^3$                        |
| $c_3, c_4, c_9$<br>$c_{10}$ | $y^3$                              |
| $c_6, c_8$                  | $y^3 - y^2 + 2y - 1$               |
| $c_7, c_{11}, c_{12}$       | $y^3 + 3y^2 + 2y - 1$              |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$                                     | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|----------------------------------------------------------|---------------------------------------|-----------------------|
| $u = -1.00000$<br>$a = -0.877439 + 0.744862I$<br>$b = 0$ | $-4.66906 - 2.82812I$                 | $-0.18504 + 4.10401I$ |
| $u = -1.00000$<br>$a = -0.877439 - 0.744862I$<br>$b = 0$ | $-4.66906 + 2.82812I$                 | $-0.18504 - 4.10401I$ |
| $u = -1.00000$<br>$a = 0.754878$<br>$b = 0$              | $-0.531480$                           | $2.37010$             |

#### IV. u-Polynomials

| Crossings          | u-Polynomials at each crossing                                                    |
|--------------------|-----------------------------------------------------------------------------------|
| $c_1$              | $((u - 1)^9)(u^{86} + 42u^{85} + \dots + 8016u + 289)$                            |
| $c_2$              | $((u - 1)^3)(u + 1)^6(u^{86} + 4u^{85} + \dots - 20u - 17)$                       |
| $c_3$              | $u^3(u^2 + 2)^3(u^{86} - u^{85} + \dots - 8992u + 16424)$                         |
| $c_4, c_9, c_{10}$ | $u^3(u^2 + 2)^3(u^{86} + u^{85} + \dots + 16u + 8)$                               |
| $c_5$              | $((u - 1)^6)(u + 1)^3(u^{86} + 4u^{85} + \dots - 20u - 17)$                       |
| $c_6, c_8$         | $(u^3 - u^2 + 1)(u^3 + u^2 - 1)^2(u^{86} + 2u^{85} + \dots - 11367u - 2391)$      |
| $c_7$              | $((u^3 - u^2 + 2u - 1)^2)(u^3 + u^2 + 2u + 1)(u^{86} - 2u^{85} + \dots - 3u - 3)$ |
| $c_{11}, c_{12}$   | $(u^3 - u^2 + 2u - 1)(u^3 + u^2 + 2u + 1)^2(u^{86} - 2u^{85} + \dots - 3u - 3)$   |

### V. Riley Polynomials

| Crossings             | Riley Polynomials at each crossing                                                      |
|-----------------------|-----------------------------------------------------------------------------------------|
| $c_1$                 | $((y-1)^9)(y^{86} + 14y^{85} + \dots - 1.94636 \times 10^7 y + 83521)$                  |
| $c_2, c_5$            | $((y-1)^9)(y^{86} - 42y^{85} + \dots - 8016y + 289)$                                    |
| $c_3$                 | $y^3(y+2)^6(y^{86} - 5y^{85} + \dots - 1.23422 \times 10^9 y + 2.69748 \times 10^8)$    |
| $c_4, c_9, c_{10}$    | $y^3(y+2)^6(y^{86} + 79y^{85} + \dots - 1280y + 64)$                                    |
| $c_6, c_8$            | $((y^3 - y^2 + 2y - 1)^3)(y^{86} - 56y^{85} + \dots + 6.80871 \times 10^7 y + 5716881)$ |
| $c_7, c_{11}, c_{12}$ | $((y^3 + 3y^2 + 2y - 1)^3)(y^{86} + 72y^{85} + \dots + 51y + 9)$                        |