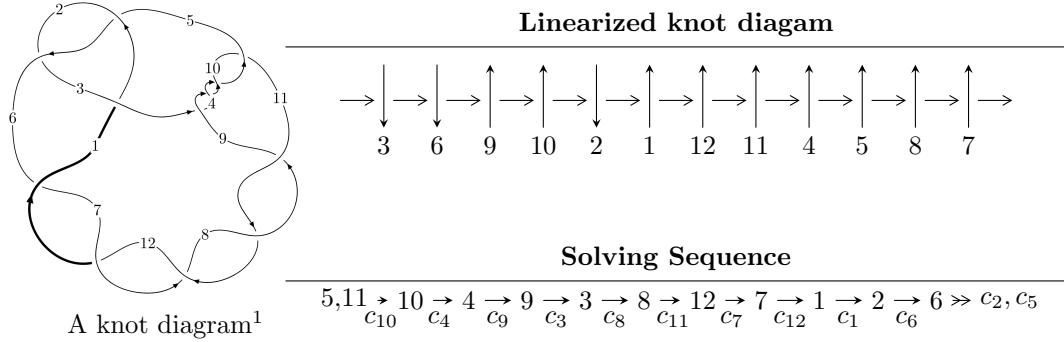


12a<sub>0379</sub> (K12a<sub>0379</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{35} - u^{34} + \dots + 3u^2 - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 35 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle u^{35} - u^{34} + \dots + 3u^2 - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 - 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 - 3u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^8 - 5u^6 + 7u^4 - 2u^2 + 1 \\ -u^8 + 4u^6 - 4u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^{12} - 7u^{10} + 17u^8 - 16u^6 + 6u^4 - 5u^2 + 1 \\ -u^{12} + 6u^{10} - 12u^8 + 8u^6 - u^4 + 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^{16} - 9u^{14} + 31u^{12} - 50u^{10} + 39u^8 - 22u^6 + 18u^4 - 4u^2 + 1 \\ -u^{16} + 8u^{14} - 24u^{12} + 32u^{10} - 18u^8 + 8u^6 - 8u^4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{24} - 13u^{22} + \dots - 6u^2 + 1 \\ u^{26} - 14u^{24} + \dots - 18u^4 + u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{20} - 11u^{18} + \dots - 7u^2 + 1 \\ -u^{20} + 10u^{18} + \dots - u^4 + 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -4u^{32} + 68u^{30} + 4u^{29} - 508u^{28} - 64u^{27} + 2184u^{26} + 444u^{25} - \\ &5960u^{24} - 1744u^{23} + 10836u^{22} + 4264u^{21} - 13756u^{20} - 6804u^{19} + 13416u^{18} + 7508u^{17} - \\ &11532u^{16} - 6528u^{15} + 8700u^{14} + 5128u^{13} - 5028u^{12} - 3288u^{11} + 2552u^{10} + 1528u^9 - \\ &1288u^8 - 704u^7 + 328u^6 + 240u^5 - 120u^4 - 44u^3 + 16u^2 + 20u + 6 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{35} + 21u^{34} + \dots + 6u + 1$
$c_2, c_5$	$u^{35} + u^{34} + \dots + 3u^2 - 1$
$c_3, c_4, c_9$ $c_{10}$	$u^{35} - u^{34} + \dots + 3u^2 - 1$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$u^{35} + 3u^{34} + \dots + 12u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{35} - 13y^{34} + \dots + 10y - 1$
$c_2, c_5$	$y^{35} - 21y^{34} + \dots + 6y - 1$
$c_3, c_4, c_9$ $c_{10}$	$y^{35} - 37y^{34} + \dots + 6y - 1$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^{35} + 47y^{34} + \dots + 90y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.525071 + 0.695031I$	$-15.9587 - 7.3230I$	$-0.50203 + 5.74720I$
$u = -0.525071 - 0.695031I$	$-15.9587 + 7.3230I$	$-0.50203 - 5.74720I$
$u = -0.503644 + 0.700836I$	$-16.0231 + 2.6486I$	$-0.693389 - 0.151455I$
$u = -0.503644 - 0.700836I$	$-16.0231 - 2.6486I$	$-0.693389 + 0.151455I$
$u = 0.512719 + 0.691106I$	$-12.06160 + 2.31682I$	$2.54987 - 2.83092I$
$u = 0.512719 - 0.691106I$	$-12.06160 - 2.31682I$	$2.54987 + 2.83092I$
$u = 0.522839 + 0.541402I$	$-5.47274 + 5.77937I$	$0.47146 - 7.85052I$
$u = 0.522839 - 0.541402I$	$-5.47274 - 5.77937I$	$0.47146 + 7.85052I$
$u = 0.408454 + 0.569281I$	$-5.82031 - 1.98611I$	$-1.101715 + 0.333068I$
$u = 0.408454 - 0.569281I$	$-5.82031 + 1.98611I$	$-1.101715 - 0.333068I$
$u = -0.459588 + 0.502405I$	$-2.40665 - 1.73767I$	$3.44724 + 4.36626I$
$u = -0.459588 - 0.502405I$	$-2.40665 + 1.73767I$	$3.44724 - 4.36626I$
$u = -0.549002 + 0.276756I$	$-0.34953 - 3.08643I$	$6.48319 + 9.61199I$
$u = -0.549002 - 0.276756I$	$-0.34953 + 3.08643I$	$6.48319 - 9.61199I$
$u = 1.43209$	$3.32584$	$2.08830$
$u = -1.46088 + 0.14870I$	$0.217823 - 0.520687I$	$0$
$u = -1.46088 - 0.14870I$	$0.217823 + 0.520687I$	$0$
$u = 0.495921 + 0.057416I$	$0.779355 + 0.040720I$	$13.22367 - 0.76931I$
$u = 0.495921 - 0.057416I$	$0.779355 - 0.040720I$	$13.22367 + 0.76931I$
$u = 1.49978 + 0.13102I$	$4.04258 + 3.93448I$	$6.00000 + 0.I$
$u = 1.49978 - 0.13102I$	$4.04258 - 3.93448I$	$6.00000 + 0.I$
$u = -1.51928 + 0.02326I$	$7.54181 - 0.38720I$	$12.42967 + 0.I$
$u = -1.51928 - 0.02326I$	$7.54181 + 0.38720I$	$12.42967 + 0.I$
$u = -1.51926 + 0.15290I$	$1.26876 - 8.24991I$	$0. + 7.12333I$
$u = -1.51926 - 0.15290I$	$1.26876 + 8.24991I$	$0. - 7.12333I$
$u = 1.52643 + 0.06311I$	$6.56659 + 4.22789I$	$0. - 6.71857I$
$u = 1.52643 - 0.06311I$	$6.56659 - 4.22789I$	$0. + 6.71857I$
$u = 1.50999 + 0.23245I$	$-9.45605 + 0.74325I$	$0$
$u = 1.50999 - 0.23245I$	$-9.45605 - 0.74325I$	$0$
$u = -1.51605 + 0.22648I$	$-5.43016 - 5.65254I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.51605 - 0.22648I$	$-5.43016 + 5.65254I$	0
$u = 1.52333 + 0.22907I$	$-9.25340 + 10.69110I$	0
$u = 1.52333 - 0.22907I$	$-9.25340 - 10.69110I$	0
$u = -0.162727 + 0.381338I$	$-1.53270 + 0.77833I$	$-1.99796 - 0.53208I$
$u = -0.162727 - 0.381338I$	$-1.53270 - 0.77833I$	$-1.99796 + 0.53208I$

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^{35} + 21u^{34} + \dots + 6u + 1$
$c_2, c_5$	$u^{35} + u^{34} + \dots + 3u^2 - 1$
$c_3, c_4, c_9$ $c_{10}$	$u^{35} - u^{34} + \dots + 3u^2 - 1$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$u^{35} + 3u^{34} + \dots + 12u + 1$

### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{35} - 13y^{34} + \dots + 10y - 1$
$c_2, c_5$	$y^{35} - 21y^{34} + \dots + 6y - 1$
$c_3, c_4, c_9$ $c_{10}$	$y^{35} - 37y^{34} + \dots + 6y - 1$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^{35} + 47y^{34} + \dots + 90y - 1$