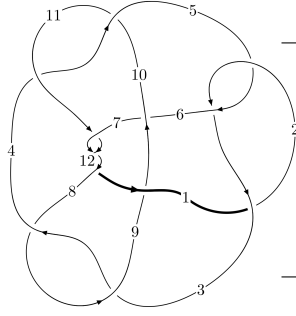
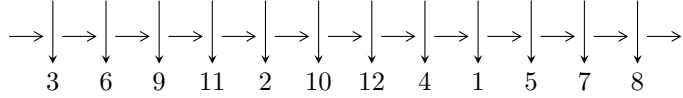


12a<sub>0391</sub> (K12a<sub>0391</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,5 \xrightarrow{c_5} 6 \xrightarrow{c_2} 3,10 \xrightarrow{c_6} 7 \xrightarrow{c_{10}} 11 \xrightarrow{c_{11}} 12 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \rightsquigarrow c_3, c_7, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 544u^{36} + 6427u^{35} + \dots + 4b + 11548, 1863u^{36} + 20659u^{35} + \dots + 32a + 23056, \\ u^{37} + 13u^{36} + \dots + 416u + 32 \rangle$$

$$I_2^u = \langle -1.94716 \times 10^{15} a^9 u^7 - 3.59875 \times 10^{15} a^8 u^7 + \dots + 1.27159 \times 10^{14} a + 2.70520 \times 10^{14}, \\ 2a^9 u^7 + 21a^8 u^7 + \dots - 2134a + 3278, u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1 \rangle$$

$$I_3^u = \langle -2u^{23} + 2u^{22} + \dots + b - 1, -u^{23} + 2u^{22} + \dots + a - 4, u^{24} - 2u^{23} + \dots - 2u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 141 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 544u^{36} + 6427u^{35} + \dots + 4b + 11548, 1863u^{36} + 20659u^{35} + \dots + 32a + 23056, u^{37} + 13u^{36} + \dots + 416u + 32 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -58.2188u^{36} - 645.594u^{35} + \dots - 9423u - 720.500 \\ -136u^{36} - \frac{6427}{4}u^{35} + \dots - \frac{72311}{2}u - 2887 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{205}{32}u^{36} + \frac{2379}{32}u^{35} + \dots + 9u - 19 \\ -\frac{11}{16}u^{36} - \frac{301}{16}u^{35} + \dots - 2628u - 225 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 77.7813u^{36} + 961.156u^{35} + \dots + 26732.5u + 2166.50 \\ -136u^{36} - \frac{6427}{4}u^{35} + \dots - \frac{72311}{2}u - 2887 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{479}{8}u^{36} - 599u^{35} + \dots + 11117u + 1067 \\ -\frac{851}{8}u^{36} - \frac{5439}{4}u^{35} + \dots - 50186u - 4130 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{541}{32}u^{36} - \frac{6235}{32}u^{35} + \dots - 3157u - 243 \\ -\frac{27}{16}u^{36} - \frac{509}{16}u^{35} + \dots - 3043u - 257 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -140.219u^{36} - 1723.59u^{35} + \dots - 47943u - 3864.50 \\ \frac{147}{2}u^{36} + 771u^{35} + \dots - \frac{13221}{2}u - 687 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 30.2500u^{36} + 180.688u^{35} + \dots - 37250.8u - 3265.50 \\ 126.313u^{36} + 1576.19u^{35} + \dots + 47332.5u + 3836 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $51u^{36} + 733u^{35} + \dots + 41316u + 3454$

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing              |
|-----------------------------|---|
| $c_1$                       | $u^{37} + 11u^{36} + \dots + 26112u + 1024$ |
| $c_2, c_5$                  | $u^{37} + 13u^{36} + \dots + 416u + 32$     |
| $c_3, c_4, c_8$<br>$c_{10}$ | $u^{37} + 11u^{35} + \dots + 4u + 1$        |
| $c_6, c_9$                  | $u^{37} - u^{36} + \dots + 6u + 1$          |
| $c_7, c_{11}, c_{12}$       | $u^{37} - 18u^{36} + \dots + 512u + 256$    |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing                 |
|-----------------------------|--|
| $c_1$                       | $y^{37} + 17y^{36} + \dots + 387842048y - 1048576$ |
| $c_2, c_5$                  | $y^{37} - 11y^{36} + \dots + 26112y - 1024$        |
| $c_3, c_4, c_8$<br>$c_{10}$ | $y^{37} + 22y^{36} + \dots + 8y - 1$               |
| $c_6, c_9$                  | $y^{37} - 9y^{36} + \dots + 10y - 1$               |
| $c_7, c_{11}, c_{12}$       | $y^{37} - 32y^{36} + \dots + 720896y - 65536$      |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|---|---------------------------------------|------------------------|
| $u = 0.957322 + 0.313722I$<br>$a = -1.37747 + 0.35388I$<br>$b = -0.371748 - 0.629257I$    | $-2.42925 - 1.37778I$                 | $-15.2263 + 4.5212I$   |
| $u = 0.957322 - 0.313722I$<br>$a = -1.37747 - 0.35388I$<br>$b = -0.371748 + 0.629257I$    | $-2.42925 + 1.37778I$                 | $-15.2263 - 4.5212I$   |
| $u = -0.212937 + 1.010140I$<br>$a = 0.105717 + 0.341356I$<br>$b = 0.417230 - 1.057270I$   | $0.06787 + 6.99887I$                  | $-9.49176 - 9.04622I$  |
| $u = -0.212937 - 1.010140I$<br>$a = 0.105717 - 0.341356I$<br>$b = 0.417230 + 1.057270I$   | $0.06787 - 6.99887I$                  | $-9.49176 + 9.04622I$  |
| $u = -0.808608 + 0.468821I$<br>$a = 0.794637 + 0.373997I$<br>$b = 0.652472 + 0.162568I$   | $-0.382992 + 0.607426I$               | $-13.17243 + 1.65752I$ |
| $u = -0.808608 - 0.468821I$<br>$a = 0.794637 - 0.373997I$<br>$b = 0.652472 - 0.162568I$   | $-0.382992 - 0.607426I$               | $-13.17243 - 1.65752I$ |
| $u = 0.930819 + 0.078146I$<br>$a = 2.43124 - 0.30243I$<br>$b = 0.561271 + 0.218932I$      | $-10.40420 - 0.06262I$                | $-27.5972 + 8.6345I$   |
| $u = 0.930819 - 0.078146I$<br>$a = 2.43124 + 0.30243I$<br>$b = 0.561271 - 0.218932I$      | $-10.40420 + 0.06262I$                | $-27.5972 - 8.6345I$   |
| $u = -0.926437 + 0.557113I$<br>$a = -1.031580 - 0.740190I$<br>$b = -0.770583 - 0.153074I$ | $-0.87598 + 3.63195I$                 | $-14.6770 - 6.3220I$   |
| $u = -0.926437 - 0.557113I$<br>$a = -1.031580 + 0.740190I$<br>$b = -0.770583 + 0.153074I$ | $-0.87598 - 3.63195I$                 | $-14.6770 + 6.3220I$   |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|---|---------------------------------------|------------------------|
| $u = -0.614591 + 0.927505I$<br>$a = 0.101554 - 0.338395I$<br>$b = 0.59999 + 1.38292I$     | $2.35753 - 12.00730I$                 | $-10.01703 + 5.56781I$ |
| $u = -0.614591 - 0.927505I$<br>$a = 0.101554 + 0.338395I$<br>$b = 0.59999 - 1.38292I$     | $2.35753 + 12.00730I$                 | $-10.01703 - 5.56781I$ |
| $u = -0.630557 + 0.967163I$<br>$a = -0.048373 + 0.373479I$<br>$b = -0.405525 - 1.330510I$ | $8.47416 - 7.17337I$                  | 0                      |
| $u = -0.630557 - 0.967163I$<br>$a = -0.048373 - 0.373479I$<br>$b = -0.405525 + 1.330510I$ | $8.47416 + 7.17337I$                  | 0                      |
| $u = -0.990193 + 0.597141I$<br>$a = 1.12308 + 1.13131I$<br>$b = 0.981847 + 0.092937I$     | $-7.29602 + 5.47264I$                 | $-18.3738 + 0.I$       |
| $u = -0.990193 - 0.597141I$<br>$a = 1.12308 - 1.13131I$<br>$b = 0.981847 - 0.092937I$     | $-7.29602 - 5.47264I$                 | $-18.3738 + 0.I$       |
| $u = -0.536542 + 0.602236I$<br>$a = -0.573017 - 0.130584I$<br>$b = -0.886654 + 0.014064I$ | $-6.05184 - 0.72046I$                 | $-16.3757 - 0.2379I$   |
| $u = -0.536542 - 0.602236I$<br>$a = -0.573017 + 0.130584I$<br>$b = -0.886654 - 0.014064I$ | $-6.05184 + 0.72046I$                 | $-16.3757 + 0.2379I$   |
| $u = 1.221810 + 0.174233I$<br>$a = -1.37712 - 0.86239I$<br>$b = -0.670944 - 1.153860I$    | $-5.18126 - 10.69840I$                | 0                      |
| $u = 1.221810 - 0.174233I$<br>$a = -1.37712 + 0.86239I$<br>$b = -0.670944 + 1.153860I$    | $-5.18126 + 10.69840I$                | 0                      |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 0.215278 + 1.228850I$<br>$a = 0.054876 - 0.356628I$<br>$b = -0.149731 + 0.905170I$  | $4.52184 + 0.80776I$                  | 0          |
| $u = 0.215278 - 1.228850I$<br>$a = 0.054876 + 0.356628I$<br>$b = -0.149731 - 0.905170I$  | $4.52184 - 0.80776I$                  | 0          |
| $u = -0.694901 + 1.046620I$<br>$a = -0.055254 - 0.424345I$<br>$b = 0.200354 + 1.178170I$ | $7.14912 - 0.88155I$                  | 0          |
| $u = -0.694901 - 1.046620I$<br>$a = -0.055254 + 0.424345I$<br>$b = 0.200354 - 1.178170I$ | $7.14912 + 0.88155I$                  | 0          |
| $u = 1.226760 + 0.280486I$<br>$a = 1.109360 + 0.476558I$<br>$b = 0.460985 + 1.013230I$   | $0.19290 - 5.94150I$                  | 0          |
| $u = 1.226760 - 0.280486I$<br>$a = 1.109360 - 0.476558I$<br>$b = 0.460985 - 1.013230I$   | $0.19290 + 5.94150I$                  | 0          |
| $u = -1.257750 + 0.369372I$<br>$a = 0.003296 - 0.634264I$<br>$b = -0.379654 - 0.721501I$ | $-3.74392 - 1.77689I$                 | 0          |
| $u = -1.257750 - 0.369372I$<br>$a = 0.003296 + 0.634264I$<br>$b = -0.379654 + 0.721501I$ | $-3.74392 + 1.77689I$                 | 0          |
| $u = -1.087090 + 0.734376I$<br>$a = -1.92634 - 0.43812I$<br>$b = -0.66863 + 1.42209I$    | $0.8899 + 18.1180I$                   | 0          |
| $u = -1.087090 - 0.734376I$<br>$a = -1.92634 + 0.43812I$<br>$b = -0.66863 - 1.42209I$    | $0.8899 - 18.1180I$                   | 0          |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -1.095130 + 0.752809I$<br>$a = 1.70277 + 0.33196I$<br>$b = 0.48754 - 1.36862I$       | $7.0104 + 13.4550I$                   | 0          |
| $u = -1.095130 - 0.752809I$<br>$a = 1.70277 - 0.33196I$<br>$b = 0.48754 + 1.36862I$       | $7.0104 - 13.4550I$                   | 0          |
| $u = -0.983113 + 0.905356I$<br>$a = 0.658309 + 0.731201I$<br>$b = 0.068498 - 0.917485I$   | $-3.94428 + 3.41322I$                 | 0          |
| $u = -0.983113 - 0.905356I$<br>$a = 0.658309 - 0.731201I$<br>$b = 0.068498 + 0.917485I$   | $-3.94428 - 3.41322I$                 | 0          |
| $u = -1.100530 + 0.794275I$<br>$a = -1.344770 - 0.325865I$<br>$b = -0.298478 + 1.225560I$ | $5.79816 + 7.52421I$                  | 0          |
| $u = -1.100530 - 0.794275I$<br>$a = -1.344770 + 0.325865I$<br>$b = -0.298478 - 1.225560I$ | $5.79816 - 7.52421I$                  | 0          |
| $u = -0.227221$<br>$a = 1.29817$<br>$b = 0.343523$  | $-0.528764$                           | $-18.5960$ |



$$\text{II. } I_2^u = \langle -1.95 \times 10^{15} a^9 u^7 - 3.60 \times 10^{15} a^8 u^7 + \dots + 1.27 \times 10^{14} a + 2.71 \times 10^{14}, 2a^9 u^7 + 21a^8 u^7 + \dots - 2134a + 3278, u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 11.1056a^9 u^7 + 20.5255a^8 u^7 + \dots - 0.725251a - 1.54291 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 3.98131a^9 u^7 - 2.65272a^8 u^7 + \dots - 0.325728a - 0.746886 \\ 1.02326a^2 u^7 - 0.511628u^7 + \dots + 0.139535a^2 - 1.06977 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -11.1056a^9 u^7 - 20.5255a^8 u^7 + \dots + 1.72525a + 1.54291 \\ 11.1056a^9 u^7 + 20.5255a^8 u^7 + \dots - 0.725251a - 1.54291 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -20.1671a^9 u^7 - 27.8400a^8 u^7 + \dots + 1.73758a - 0.272610 \\ 11.1859a^9 u^7 + 29.1048a^8 u^7 + \dots - 0.552681a + 1.07179 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1.02730a^9 u^7 + 3.91889a^8 u^7 + \dots + 0.758648a + 1.50660 \\ -2.95401a^9 u^7 - 1.26617a^8 u^7 + \dots - 0.432919a + 1.24029 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.906309a^9 u^7 + 1.79884a^8 u^7 + \dots + 2.18676a + 1.25107 \\ 9.35107a^9 u^7 + 13.2623a^8 u^7 + \dots + 0.466900a - 1.73564 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -8.72539a^9 u^7 - 15.3608a^8 u^7 + \dots + 1.00957a - 1.08501 \\ 2.09106a^9 u^7 + 10.0259a^8 u^7 + \dots + 0.977705a - 0.181873 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{3312696866563328}{175330710141469} a^9 u^7 - \frac{10860915930820932}{175330710141469} a^8 u^7 + \dots - \frac{524784750398904}{175330710141469} a - \frac{3778793332341578}{175330710141469}$$

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing                                     |
|-----------------------------|--|
| $c_1$                       | $(u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1)^{10}$ |
| $c_2, c_5$                  | $(u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1)^{10}$              |
| $c_3, c_4, c_8$<br>$c_{10}$ | $u^{80} - u^{79} + \dots + 3548u + 1579$                           |
| $c_6, c_9$                  | $u^{80} + 9u^{79} + \dots + 6422u + 569$                           |
| $c_7, c_{11}, c_{12}$       | $(u^5 + u^4 - 2u^3 - u^2 + u - 1)^{16}$                            |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing                                  |
|-----------------------------|---|
| $c_1$                       | $(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1)^{10}$ |
| $c_2, c_5$                  | $(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)^{10}$  |
| $c_3, c_4, c_8$<br>$c_{10}$ | $y^{80} + 63y^{79} + \dots + 269522152y + 2493241$                  |
| $c_6, c_9$                  | $y^{80} + 27y^{79} + \dots + 120888776y + 323761$                   |
| $c_7, c_{11}, c_{12}$       | $(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^{16}$                           |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = 0.570868 + 0.730671I$<br>$a = 0.317717 - 0.891415I$<br>$b = 1.305780 - 0.021800I$   | $-1.97842 + 5.53207I$                 | $-12.15954 - 4.00938I$ |
| $u = 0.570868 + 0.730671I$<br>$a = -0.372527 + 0.813712I$<br>$b = 0.473970 - 0.367837I$  | $-1.97842 - 3.26960I$                 | $-12.15954 + 2.98779I$ |
| $u = 0.570868 + 0.730671I$<br>$a = -0.472750 - 0.641845I$<br>$b = -0.445650 + 1.315720I$ | $-1.97842 + 5.53207I$                 | $-12.15954 - 4.00938I$ |
| $u = 0.570868 + 0.730671I$<br>$a = 0.453598 - 0.633400I$<br>$b = 0.0442048 - 0.1093490I$ | $3.56505 - 0.39935I$                  | $-7.93034 + 3.91986I$  |
| $u = 0.570868 + 0.730671I$<br>$a = -0.242021 + 0.721707I$<br>$b = -0.914022 + 0.321383I$ | $3.56505 + 2.66181I$                  | $-7.93034 - 4.94144I$  |
| $u = 0.570868 + 0.730671I$<br>$a = -0.701722 + 0.223215I$<br>$b = 0.118471 + 0.985556I$  | $1.49307 + 1.13123I$                  | $-8.89637 - 0.51079I$  |
| $u = 0.570868 + 0.730671I$<br>$a = -0.529151 + 0.436048I$<br>$b = -0.258551 - 1.170880I$ | $-1.97842 - 3.26960I$                 | $-12.15954 + 2.98779I$ |
| $u = 0.570868 + 0.730671I$<br>$a = 0.379390 + 0.337276I$<br>$b = 0.292944 - 1.200800I$   | $3.56505 + 2.66181I$                  | $-7.93034 - 4.94144I$  |
| $u = 0.570868 + 0.730671I$<br>$a = -0.187370 - 0.461746I$<br>$b = 0.78647 - 1.19152I$    | $1.49307 + 1.13123I$                  | $-8.89637 - 0.51079I$  |
| $u = 0.570868 + 0.730671I$<br>$a = 0.195391 - 0.214615I$<br>$b = -0.223507 + 1.170930I$  | $3.56505 - 0.39935I$                  | $-7.93034 + 3.91986I$  |

| Solutions to $I_2^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|------------------------------|---------------------------------------|------------------------|
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = 0.317717 + 0.891415I$   | $-1.97842 - 5.53207I$                 | $-12.15954 + 4.00938I$ |
| $b = 1.305780 + 0.021800I$   |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = -0.372527 - 0.813712I$  | $-1.97842 + 3.26960I$                 | $-12.15954 - 2.98779I$ |
| $b = 0.473970 + 0.367837I$   |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = -0.472750 + 0.641845I$  | $-1.97842 - 5.53207I$                 | $-12.15954 + 4.00938I$ |
| $b = -0.445650 - 1.315720I$  |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = 0.453598 + 0.633400I$   | $3.56505 + 0.39935I$                  | $-7.93034 - 3.91986I$  |
| $b = 0.0442048 + 0.1093490I$ |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = -0.242021 - 0.721707I$  | $3.56505 - 2.66181I$                  | $-7.93034 + 4.94144I$  |
| $b = -0.914022 - 0.321383I$  |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = -0.701722 - 0.223215I$  | $1.49307 - 1.13123I$                  | $-8.89637 + 0.51079I$  |
| $b = 0.118471 - 0.985556I$   |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = -0.529151 - 0.436048I$  | $-1.97842 + 3.26960I$                 | $-12.15954 - 2.98779I$ |
| $b = -0.258551 + 1.170880I$  |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = 0.379390 - 0.337276I$   | $3.56505 - 2.66181I$                  | $-7.93034 + 4.94144I$  |
| $b = 0.292944 + 1.200800I$   |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = -0.187370 + 0.461746I$  | $1.49307 - 1.13123I$                  | $-8.89637 + 0.51079I$  |
| $b = 0.78647 + 1.19152I$     |                                       |                        |
| $u = 0.570868 - 0.730671I$   |                                       |                        |
| $a = 0.195391 + 0.214615I$   | $3.56505 + 0.39935I$                  | $-7.93034 - 3.91986I$  |
| $b = -0.223507 - 1.170930I$  |                                       |                        |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.855237 + 0.665892I$<br>$a = 0.184288 + 1.123720I$<br>$b = -0.049819 - 1.318620I$ | $6.76512 + 4.10907I$                  | $-4.79219 - 7.99861I$ |
| $u = -0.855237 + 0.665892I$<br>$a = -0.000369 - 0.558136I$<br>$b = -0.89941 - 1.42516I$  | $1.22165 - 1.82234I$                  | $-9.02139 - 0.06937I$ |
| $u = -0.855237 + 0.665892I$<br>$a = 0.55671 - 1.37754I$<br>$b = -0.094640 + 1.087870I$   | $1.22165 + 6.97933I$                  | $-9.02139 - 7.06654I$ |
| $u = -0.855237 + 0.665892I$<br>$a = -0.461095 + 0.026790I$<br>$b = 0.46574 + 1.57218I$   | $6.76512 + 1.04791I$                  | $-4.79219 + 0.86269I$ |
| $u = -0.855237 + 0.665892I$<br>$a = 1.67042 - 0.02563I$<br>$b = 0.09310 - 2.08054I$      | $4.69313 + 2.57849I$                  | $-5.75822 - 3.56796I$ |
| $u = -0.855237 + 0.665892I$<br>$a = -2.07727 - 0.57527I$<br>$b = -0.60157 + 1.48322I$    | $6.76512 + 4.10907I$                  | $-4.79219 - 7.99861I$ |
| $u = -0.855237 + 0.665892I$<br>$a = -1.48542 - 1.66320I$<br>$b = -0.01022 + 1.50733I$    | $4.69313 + 2.57849I$                  | $-5.75822 - 3.56796I$ |
| $u = -0.855237 + 0.665892I$<br>$a = 2.19641 + 0.66346I$<br>$b = 1.04102 - 1.29878I$      | $1.22165 + 6.97933I$                  | $-9.02139 - 7.06654I$ |
| $u = -0.855237 + 0.665892I$<br>$a = 2.19046 + 0.91845I$<br>$b = 0.112336 - 1.229800I$    | $6.76512 + 1.04791I$                  | $-4.79219 + 0.86269I$ |
| $u = -0.855237 + 0.665892I$<br>$a = -2.53287 - 0.73501I$<br>$b = 0.051544 + 0.954798I$   | $1.22165 - 1.82234I$                  | $-9.02139 - 0.06937I$ |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.855237 - 0.665892I$<br>$a = 0.184288 - 1.123720I$<br>$b = -0.049819 + 1.318620I$ | $6.76512 - 4.10907I$                  | $-4.79219 + 7.99861I$ |
| $u = -0.855237 - 0.665892I$<br>$a = -0.000369 + 0.558136I$<br>$b = -0.89941 + 1.42516I$  | $1.22165 + 1.82234I$                  | $-9.02139 + 0.06937I$ |
| $u = -0.855237 - 0.665892I$<br>$a = 0.55671 + 1.37754I$<br>$b = -0.094640 - 1.087870I$   | $1.22165 - 6.97933I$                  | $-9.02139 + 7.06654I$ |
| $u = -0.855237 - 0.665892I$<br>$a = -0.461095 - 0.026790I$<br>$b = 0.46574 - 1.57218I$   | $6.76512 - 1.04791I$                  | $-4.79219 - 0.86269I$ |
| $u = -0.855237 - 0.665892I$<br>$a = 1.67042 + 0.02563I$<br>$b = 0.09310 + 2.08054I$      | $4.69313 - 2.57849I$                  | $-5.75822 + 3.56796I$ |
| $u = -0.855237 - 0.665892I$<br>$a = -2.07727 + 0.57527I$<br>$b = -0.60157 - 1.48322I$    | $6.76512 - 4.10907I$                  | $-4.79219 + 7.99861I$ |
| $u = -0.855237 - 0.665892I$<br>$a = -1.48542 + 1.66320I$<br>$b = -0.01022 - 1.50733I$    | $4.69313 - 2.57849I$                  | $-5.75822 + 3.56796I$ |
| $u = -0.855237 - 0.665892I$<br>$a = 2.19641 - 0.66346I$<br>$b = 1.04102 + 1.29878I$      | $1.22165 - 6.97933I$                  | $-9.02139 + 7.06654I$ |
| $u = -0.855237 - 0.665892I$<br>$a = 2.19046 - 0.91845I$<br>$b = 0.112336 + 1.229800I$    | $6.76512 - 1.04791I$                  | $-4.79219 - 0.86269I$ |
| $u = -0.855237 - 0.665892I$<br>$a = -2.53287 + 0.73501I$<br>$b = 0.051544 - 0.954798I$   | $1.22165 + 1.82234I$                  | $-9.02139 + 0.06937I$ |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = -1.09818$<br>$a = 1.213950 + 0.060472I$<br>$b = 0.743281 - 0.274344I$   | $-1.89703 - 1.53058I$                 | $-14.3792 + 4.4306I$ |
| $u = -1.09818$<br>$a = 1.213950 - 0.060472I$<br>$b = 0.743281 + 0.274344I$   | $-1.89703 + 1.53058I$                 | $-14.3792 - 4.4306I$ |
| $u = -1.09818$<br>$a = -0.794603 + 1.077430I$<br>$b = -0.278360 + 0.853134I$ | $-1.89703 + 1.53058I$                 | $-14.3792 - 4.4306I$ |
| $u = -1.09818$<br>$a = -0.794603 - 1.077430I$<br>$b = -0.278360 - 0.853134I$ | $-1.89703 - 1.53058I$                 | $-14.3792 + 4.4306I$ |
| $u = -1.09818$<br>$a = -0.474135 + 1.292280I$<br>$b = -0.525660 + 0.657310I$ | $-3.96901$                            | $-15.3452 + 0.I$     |
| $u = -1.09818$<br>$a = -0.474135 - 1.292280I$<br>$b = -0.525660 - 0.657310I$ | $-3.96901$                            | $-15.3452 + 0.I$     |
| $u = -1.09818$<br>$a = -1.87939 + 0.04068I$<br>$b = -1.125010 + 0.465951I$   | $-7.44049 - 4.40083I$                 | $-18.6084 + 3.4986I$ |
| $u = -1.09818$<br>$a = -1.87939 - 0.04068I$<br>$b = -1.125010 - 0.465951I$   | $-7.44049 + 4.40083I$                 | $-18.6084 - 3.4986I$ |
| $u = -1.09818$<br>$a = 1.31587 + 1.44345I$<br>$b = 0.500246 + 1.179460I$     | $-7.44049 - 4.40083I$                 | $-18.6084 + 3.4986I$ |
| $u = -1.09818$<br>$a = 1.31587 - 1.44345I$<br>$b = 0.500246 - 1.179460I$     | $-7.44049 + 4.40083I$                 | $-18.6084 - 3.4986I$ |



| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = 1.031810 + 0.655470I$<br>$a = -0.999846 + 0.759611I$<br>$b = -0.518695 - 0.817196I$ | $-3.31744 - 2.04270I$                 | $-14.1728 + 1.7956I$   |
| $u = 1.031810 + 0.655470I$<br>$a = 1.117550 - 0.688666I$<br>$b = 1.127550 + 0.190536I$   | $2.22602 - 7.97412I$                  | $-9.94356 + 9.72482I$  |
| $u = 1.031810 + 0.655470I$<br>$a = -0.452863 - 0.411616I$<br>$b = 0.293319 - 0.929775I$  | $-3.31744 - 2.04270I$                 | $-14.1728 + 1.7956I$   |
| $u = 1.031810 + 0.655470I$<br>$a = -0.523882 - 0.058026I$<br>$b = -0.298543 + 0.084388I$ | $2.22602 - 4.91296I$                  | $-9.94356 + 0.86352I$  |
| $u = 1.031810 + 0.655470I$<br>$a = -1.00804 + 1.15213I$<br>$b = -1.49599 + 0.11672I$     | $-3.31744 - 10.84440I$                | $-14.1728 + 8.7928I$   |
| $u = 1.031810 + 0.655470I$<br>$a = 1.52330 - 0.21142I$<br>$b = 0.488814 + 1.121250I$     | $2.22602 - 4.91296I$                  | $-9.94356 + 0.86352I$  |
| $u = 1.031810 + 0.655470I$<br>$a = 1.64924 + 0.59159I$<br>$b = -0.002912 + 0.837279I$    | $0.15404 - 6.44354I$                  | $-10.90959 + 5.29417I$ |
| $u = 1.031810 + 0.655470I$<br>$a = -1.76293 + 0.29343I$<br>$b = -1.02044 - 1.08184I$     | $0.15404 - 6.44354I$                  | $-10.90959 + 5.29417I$ |
| $u = 1.031810 + 0.655470I$<br>$a = -2.01641 + 0.17535I$<br>$b = -0.412717 - 1.179870I$   | $2.22602 - 7.97412I$                  | $-9.94356 + 9.72482I$  |
| $u = 1.031810 + 0.655470I$<br>$a = 2.32562 - 0.44824I$<br>$b = 0.50508 + 1.33958I$       | $-3.31744 - 10.84440I$                | $-14.1728 + 8.7928I$   |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = 1.031810 - 0.655470I$<br>$a = -0.999846 - 0.759611I$<br>$b = -0.518695 + 0.817196I$ | $-3.31744 + 2.04270I$                 | $-14.1728 - 1.7956I$   |
| $u = 1.031810 - 0.655470I$<br>$a = 1.117550 + 0.688666I$<br>$b = 1.127550 - 0.190536I$   | $2.22602 + 7.97412I$                  | $-9.94356 - 9.72482I$  |
| $u = 1.031810 - 0.655470I$<br>$a = -0.452863 + 0.411616I$<br>$b = 0.293319 + 0.929775I$  | $-3.31744 + 2.04270I$                 | $-14.1728 - 1.7956I$   |
| $u = 1.031810 - 0.655470I$<br>$a = -0.523882 + 0.058026I$<br>$b = -0.298543 - 0.084388I$ | $2.22602 + 4.91296I$                  | $-9.94356 - 0.86352I$  |
| $u = 1.031810 - 0.655470I$<br>$a = -1.00804 - 1.15213I$<br>$b = -1.49599 - 0.11672I$     | $-3.31744 + 10.84440I$                | $-14.1728 - 8.7928I$   |
| $u = 1.031810 - 0.655470I$<br>$a = 1.52330 + 0.21142I$<br>$b = 0.488814 - 1.121250I$     | $2.22602 + 4.91296I$                  | $-9.94356 - 0.86352I$  |
| $u = 1.031810 - 0.655470I$<br>$a = 1.64924 - 0.59159I$<br>$b = -0.002912 - 0.837279I$    | $0.15404 + 6.44354I$                  | $-10.90959 - 5.29417I$ |
| $u = 1.031810 - 0.655470I$<br>$a = -1.76293 - 0.29343I$<br>$b = -1.02044 + 1.08184I$     | $0.15404 + 6.44354I$                  | $-10.90959 - 5.29417I$ |
| $u = 1.031810 - 0.655470I$<br>$a = -2.01641 - 0.17535I$<br>$b = -0.412717 + 1.179870I$   | $2.22602 + 7.97412I$                  | $-9.94356 - 9.72482I$  |
| $u = 1.031810 - 0.655470I$<br>$a = 2.32562 + 0.44824I$<br>$b = 0.50508 - 1.33958I$       | $-3.31744 + 10.84440I$                | $-14.1728 - 8.7928I$   |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = 0.603304$<br>$a = 0.955688 + 0.192007I$<br>$b = 0.152198 + 1.333960I$ | $3.76067 - 1.53058I$                  | $-12.40958 + 4.43065I$ |
| $u = 0.603304$<br>$a = 0.955688 - 0.192007I$<br>$b = 0.152198 - 1.333960I$ | $3.76067 + 1.53058I$                  | $-12.40958 - 4.43065I$ |
| $u = 0.603304$<br>$a = -1.62568 + 0.77113I$<br>$b = -0.436213 - 1.233300I$ | $-1.78280 - 4.40083I$                 | $-16.6388 + 3.4986I$   |
| $u = 0.603304$<br>$a = -1.62568 - 0.77113I$<br>$b = -0.436213 + 1.233300I$ | $-1.78280 + 4.40083I$                 | $-16.6388 - 3.4986I$   |
| $u = 0.603304$<br>$a = -1.39197 + 2.25490I$<br>$b = 0.17777 + 1.53018I$    | $1.68869$                             | $-13.37561 + 0.I$      |
| $u = 0.603304$<br>$a = -1.39197 - 2.25490I$<br>$b = 0.17777 - 1.53018I$    | $1.68869$                             | $-13.37561 + 0.I$      |
| $u = 0.603304$<br>$a = 0.27544 + 3.17761I$<br>$b = -0.309423 + 0.952672I$  | $3.76067 + 1.53058I$                  | $-12.40958 - 4.43065I$ |
| $u = 0.603304$<br>$a = 0.27544 - 3.17761I$<br>$b = -0.309423 - 0.952672I$  | $3.76067 - 1.53058I$                  | $-12.40958 + 4.43065I$ |
| $u = 0.603304$<br>$a = -0.02871 + 3.58598I$<br>$b = 0.647493 + 0.676864I$  | $-1.78280 - 4.40083I$                 | $-16.6388 + 3.4986I$   |
| $u = 0.603304$<br>$a = -0.02871 - 3.58598I$<br>$b = 0.647493 - 0.676864I$  | $-1.78280 + 4.40083I$                 | $-16.6388 - 3.4986I$   |

III.

$$I_3^u = \langle -2u^{23} + 2u^{22} + \dots + b - 1, -u^{23} + 2u^{22} + \dots + a - 4, u^{24} - 2u^{23} + \dots - 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^{23} - 2u^{22} + \dots - 3u + 4 \\ 2u^{23} - 2u^{22} + \dots + 3u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -4u^{23} + 7u^{22} + \dots + 3u - 1 \\ -2u^{23} + 2u^{22} + \dots - 3u + 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^{23} + 6u^{21} + \dots - 6u + 3 \\ 2u^{23} - 2u^{22} + \dots + 3u + 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^{23} + 5u^{22} + \dots + 5u + 1 \\ 3u^{23} - 2u^{22} + \dots + 2u + 2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^{20} + u^{19} + \dots + 3u + 1 \\ -u^{22} + 4u^{20} + \dots + 4u^2 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^{23} - 3u^{21} + \dots - u + 4 \\ u^{23} - u^{22} + \dots + 4u - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 2u^{23} - 4u^{22} + \dots + 2u^2 - 2u \\ -2u^{23} + 3u^{22} + \dots - 3u^2 - 3u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= 22u^{23} - 38u^{22} - 42u^{21} + 159u^{20} + 11u^{19} - 320u^{18} + 155u^{17} + \\ &435u^{16} - 413u^{15} - 315u^{14} + 694u^{13} - 11u^{12} - 699u^{11} + 324u^{10} + 595u^9 - 454u^8 - \\ &311u^7 + 354u^6 + 145u^5 - 165u^4 - 58u^3 + 75u^2 + 2u - 16 \end{aligned}$$

(iv) u-Polynomials at the component

| Crossings        | u-Polynomials at each crossing      |
|------------------|-------------------------------------|
| $c_1$            | $u^{24} - 8u^{23} + \dots - 8u + 1$ |
| $c_2$            | $u^{24} + 2u^{23} + \dots + 2u + 1$ |
| $c_3, c_{10}$    | $u^{24} + 13u^{22} + \dots - u - 1$ |
| $c_4, c_8$       | $u^{24} + 13u^{22} + \dots + u - 1$ |
| $c_5$            | $u^{24} - 2u^{23} + \dots - 2u + 1$ |
| $c_6, c_9$       | $u^{24} - u^{23} + \dots + 9u - 3$  |
| $c_7$            | $u^{24} - u^{23} + \dots - u - 1$   |
| $c_{11}, c_{12}$ | $u^{24} + u^{23} + \dots + u - 1$   |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing    |
|-----------------------------|---------------------------------------|
| $c_1$                       | $y^{24} + 12y^{23} + \dots + 16y + 1$ |
| $c_2, c_5$                  | $y^{24} - 8y^{23} + \dots - 8y + 1$   |
| $c_3, c_4, c_8$<br>$c_{10}$ | $y^{24} + 26y^{23} + \dots - 21y + 1$ |
| $c_6, c_9$                  | $y^{24} + 3y^{23} + \dots + 69y + 9$  |
| $c_7, c_{11}, c_{12}$       | $y^{24} - 27y^{23} + \dots - 9y + 1$  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape              |
|--|---------------------------------------|-------------------------|
| $u = -0.859104 + 0.619061I$<br>$a = -1.77700 - 0.81550I$<br>$b = -0.05224 + 1.79614I$    | $3.64574 + 2.43004I$                  | $-15.3160 - 2.5325I$    |
| $u = -0.859104 - 0.619061I$<br>$a = -1.77700 + 0.81550I$<br>$b = -0.05224 - 1.79614I$    | $3.64574 - 2.43004I$                  | $-15.3160 + 2.5325I$    |
| $u = -0.921806$<br>$a = -1.13142$<br>$b = -0.238208$                                     | $-2.48108$                            | $-16.6080$              |
| $u = 0.274672 + 1.053350I$<br>$a = -0.186811 + 0.192436I$<br>$b = 0.163662 - 0.961355I$  | $4.89050 + 0.67182I$                  | $-0.331093 - 0.291966I$ |
| $u = 0.274672 - 1.053350I$<br>$a = -0.186811 - 0.192436I$<br>$b = 0.163662 + 0.961355I$  | $4.89050 - 0.67182I$                  | $-0.331093 + 0.291966I$ |
| $u = -0.847989 + 0.693024I$<br>$a = 1.23905 + 0.72068I$<br>$b = 0.06183 - 1.51814I$      | $6.81902 + 2.66285I$                  | $-3.87424 - 2.89541I$   |
| $u = -0.847989 - 0.693024I$<br>$a = 1.23905 - 0.72068I$<br>$b = 0.06183 + 1.51814I$      | $6.81902 - 2.66285I$                  | $-3.87424 + 2.89541I$   |
| $u = 0.694510 + 0.572688I$<br>$a = -0.830889 + 1.076290I$<br>$b = -0.698566 + 1.033420I$ | $-0.25743 + 3.41207I$                 | $-11.71453 - 2.05195I$  |
| $u = 0.694510 - 0.572688I$<br>$a = -0.830889 - 1.076290I$<br>$b = -0.698566 - 1.033420I$ | $-0.25743 - 3.41207I$                 | $-11.71453 + 2.05195I$  |
| $u = 0.998881 + 0.595015I$<br>$a = 1.82392 + 0.25160I$<br>$b = 0.776391 + 0.880199I$     | $-1.25649 - 8.10140I$                 | $-14.1033 + 8.4780I$    |

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 0.998881 - 0.595015I$<br>$a = 1.82392 - 0.25160I$<br>$b = 0.776391 - 0.880199I$     | $-1.25649 + 8.10140I$                 | $-14.1033 - 8.4780I$  |
| $u = -0.829372$<br>$a = 2.78344$<br>$b = 0.236926$                                       | $-10.1589$                            | $5.82770$             |
| $u = 0.772444 + 0.266120I$<br>$a = 0.21598 + 1.86268I$<br>$b = -0.13292 + 1.53643I$      | $1.73546 - 1.04679I$                  | $-12.7704 + 7.1412I$  |
| $u = 0.772444 - 0.266120I$<br>$a = 0.21598 - 1.86268I$<br>$b = -0.13292 - 1.53643I$      | $1.73546 + 1.04679I$                  | $-12.7704 - 7.1412I$  |
| $u = -1.196510 + 0.259459I$<br>$a = -0.231267 + 0.835819I$<br>$b = 0.318802 + 0.654164I$ | $-3.32815 - 1.41217I$                 | $-8.36483 + 0.95661I$ |
| $u = -1.196510 - 0.259459I$<br>$a = -0.231267 - 0.835819I$<br>$b = 0.318802 - 0.654164I$ | $-3.32815 + 1.41217I$                 | $-8.36483 - 0.95661I$ |
| $u = -0.535643 + 0.545861I$<br>$a = -0.12086 - 1.74579I$<br>$b = -0.401964 + 1.059050I$  | $-0.55694 + 5.07983I$                 | $-9.81409 - 5.66090I$ |
| $u = -0.535643 - 0.545861I$<br>$a = -0.12086 + 1.74579I$<br>$b = -0.401964 - 1.059050I$  | $-0.55694 - 5.07983I$                 | $-9.81409 + 5.66090I$ |
| $u = 1.069460 + 0.653928I$<br>$a = -1.328700 - 0.042768I$<br>$b = -0.478932 - 0.857563I$ | $2.77511 - 6.09098I$                  | $-6.24923 + 6.46782I$ |
| $u = 1.069460 - 0.653928I$<br>$a = -1.328700 + 0.042768I$<br>$b = -0.478932 + 0.857563I$ | $2.77511 + 6.09098I$                  | $-6.24923 - 6.46782I$ |



| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.510957 + 0.450721I$  | $4.69210 + 1.06045I$                  | $-2.95845 - 0.15547I$ |
| $a = -0.220431 - 1.219110I$ |                                       |                       |
| $b = 0.326073 - 1.173880I$  |                                       |                       |
| $u = 0.510957 - 0.450721I$  | $4.69210 - 1.06045I$                  | $-2.95845 + 0.15547I$ |
| $a = -0.220431 + 1.219110I$ |                                       |                       |
| $b = 0.326073 + 1.173880I$  |                                       |                       |
| $u = 0.993906 + 0.876026I$  | $-4.61425 - 3.36496I$                 | $-21.1138 + 3.8610I$  |
| $a = 0.591000 - 0.624229I$  |                                       |                       |
| $b = 0.118504 + 0.699899I$  |                                       |                       |
| $u = 0.993906 - 0.876026I$  | $-4.61425 + 3.36496I$                 | $-21.1138 - 3.8610I$  |
| $a = 0.591000 + 0.624229I$  |                                       |                       |
| $b = 0.118504 - 0.699899I$  |                                       |                       |

#### IV. u-Polynomials

| Crossings        | u-Polynomials at each crossing  |
|------------------|---|
| $c_1$            | $(u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1)^{10}$ $\cdot (u^{24} - 8u^{23} + \dots - 8u + 1)(u^{37} + 11u^{36} + \dots + 26112u + 1024)$ |
| $c_2$            | $((u^8 - u^7 + \dots + 2u - 1)^{10})(u^{24} + 2u^{23} + \dots + 2u + 1)$ $\cdot (u^{37} + 13u^{36} + \dots + 416u + 32)$                                  |
| $c_3, c_{10}$    | $(u^{24} + 13u^{22} + \dots - u - 1)(u^{37} + 11u^{35} + \dots + 4u + 1)$ $\cdot (u^{80} - u^{79} + \dots + 3548u + 1579)$                                |
| $c_4, c_8$       | $(u^{24} + 13u^{22} + \dots + u - 1)(u^{37} + 11u^{35} + \dots + 4u + 1)$ $\cdot (u^{80} - u^{79} + \dots + 3548u + 1579)$                                |
| $c_5$            | $((u^8 - u^7 + \dots + 2u - 1)^{10})(u^{24} - 2u^{23} + \dots - 2u + 1)$ $\cdot (u^{37} + 13u^{36} + \dots + 416u + 32)$                                  |
| $c_6, c_9$       | $(u^{24} - u^{23} + \dots + 9u - 3)(u^{37} - u^{36} + \dots + 6u + 1)$ $\cdot (u^{80} + 9u^{79} + \dots + 6422u + 569)$                                   |
| $c_7$            | $((u^5 + u^4 - 2u^3 - u^2 + u - 1)^{16})(u^{24} - u^{23} + \dots - u - 1)$ $\cdot (u^{37} - 18u^{36} + \dots + 512u + 256)$                               |
| $c_{11}, c_{12}$ | $((u^5 + u^4 - 2u^3 - u^2 + u - 1)^{16})(u^{24} + u^{23} + \dots + u - 1)$ $\cdot (u^{37} - 18u^{36} + \dots + 512u + 256)$                               |

## V. Riley Polynomials

| Crossings                   | Riley Polynomials at each crossing   |
|-----------------------------|--|
| $c_1$                       | $(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1)^{10}$ $\cdot (y^{24} + 12y^{23} + \dots + 16y + 1)$ $\cdot (y^{37} + 17y^{36} + \dots + 387842048y - 1048576)$ |
| $c_2, c_5$                  | $(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)^{10}$ $\cdot (y^{24} - 8y^{23} + \dots - 8y + 1)(y^{37} - 11y^{36} + \dots + 26112y - 1024)$                    |
| $c_3, c_4, c_8$<br>$c_{10}$ | $(y^{24} + 26y^{23} + \dots - 21y + 1)(y^{37} + 22y^{36} + \dots + 8y - 1)$ $\cdot (y^{80} + 63y^{79} + \dots + 269522152y + 2493241)$                                       |
| $c_6, c_9$                  | $(y^{24} + 3y^{23} + \dots + 69y + 9)(y^{37} - 9y^{36} + \dots + 10y - 1)$ $\cdot (y^{80} + 27y^{79} + \dots + 120888776y + 323761)$   |
| $c_7, c_{11}, c_{12}$       | $((y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^{16})(y^{24} - 27y^{23} + \dots - 9y + 1)$ $\cdot (y^{37} - 32y^{36} + \dots + 720896y - 65536)$  |