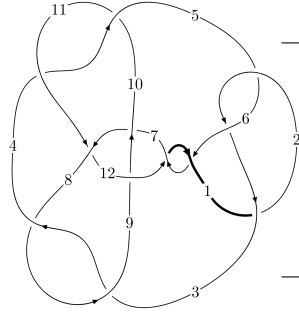
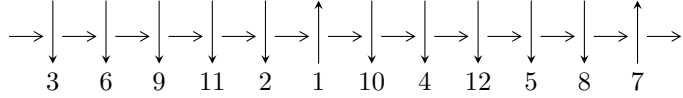


12a<sub>0397</sub> (K12a<sub>0397</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$8,11 \xrightarrow{c_{11}} 5,12 \xrightarrow{c_4} 4 \xrightarrow{c_8} 9 \xrightarrow{c_3} 3 \xrightarrow{c_{10}} 10 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 1 \xrightarrow{c_6} 6 \xrightarrow{c_2} 2 \rightsquigarrow c_1, c_5, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1908269u^{44} + 69257295u^{43} + \dots + 524288b - 1459838517248, \\ -6600959u^{44} - 250923547u^{43} + \dots + 1048576a - 5495160045568, \\ u^{45} + 39u^{44} + \dots + 23068672u + 1048576 \rangle$$

$$I_2^u = \langle -4.69815 \times 10^{233} a^{39} u - 6.24002 \times 10^{233} a^{38} u + \dots - 1.03893 \times 10^{237} a + 1.05559 \times 10^{236}, \\ 2a^{39}u + 21a^{38}u + \dots + 142a - 33, u^2 - u + 1 \rangle$$

$$I_3^u = \langle -11u^{22} - 8u^{21} + \dots + b + 40, -29u^{22} - 83u^{21} + \dots + a + 3, u^{23} + 2u^{22} + \dots - u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 148 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 1.91 \times 10^6 u^{44} + 6.93 \times 10^7 u^{43} + \dots + 5.24 \times 10^5 b - 1.46 \times 10^{12}, -6.60 \times 10^6 u^{44} - 2.51 \times 10^8 u^{43} + \dots + 1.05 \times 10^6 a - 5.50 \times 10^{12}, u^{45} + 39u^{44} + \dots + 23068672u + 1048576 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 6.29517u^{44} + 239.299u^{43} + \dots + 1.12427 \times 10^8 u + 5240593 \\ -3.63973u^{44} - 132.098u^{43} + \dots + 5.32322 \times 10^7 u + 2784421 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 2.65543u^{44} + 107.202u^{43} + \dots + 1.65659 \times 10^8 u + 8025014 \\ -3.63973u^{44} - 132.098u^{43} + \dots + 5.32322 \times 10^7 u + 2784421 \end{pmatrix} \\ a_9 &= \begin{pmatrix} \frac{1}{1024}u^{43} + \frac{37}{1024}u^{42} + \dots + 10752u + \frac{1025}{2} \\ -0.000976563u^{44} - 0.0361328u^{43} + \dots - 10752u^2 - 511.500u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 10.3764u^{44} + 403.507u^{43} + \dots + 3.53442 \times 10^8 u + 1.68991 \times 10^7 \\ 11.0232u^{44} + 424.937u^{43} + \dots + 3.09218 \times 10^8 u + 1.46969 \times 10^7 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.000976563u^{44} - 0.0371094u^{43} + \dots - 11264.5u - 511.500 \\ \frac{1}{1024}u^{44} + \frac{37}{1024}u^{43} + \dots + 10752u^2 + \frac{1025}{2}u \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{1}{1024}u^{44} + \frac{45}{1024}u^{43} + \dots + \frac{388097}{4}u + 4608 \\ -\frac{7}{1024}u^{44} - \frac{17}{64}u^{43} + \dots - 154111u - 7168 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.0998535u^{44} + 3.81567u^{43} + \dots + 1630976u + 75265 \\ -0.0717773u^{44} - 2.68408u^{43} + \dots - 383232u - 16128 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.245605u^{44} + 8.91406u^{43} + \dots - 2.76384 \times 10^6 u - 142464 \\ 0.267578u^{44} + 10.4087u^{43} + \dots + 7706241u + 364032 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -1.21094u^{44} - 46.2363u^{43} + \dots - 2.15274 \times 10^7 u - 998527. \\ -1.38721u^{44} - 52.9595u^{43} + \dots - 2.50382 \times 10^7 u - 1163264 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{1487947}{65536}u^{44} + \frac{6940087}{8192}u^{43} + \dots + 108839472u + 4370874$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{45} + 24u^{44} + \dots + 172u + 16$
$c_2, c_5$	$u^{45} + 6u^{44} + \dots + 38u + 4$
$c_3, c_4, c_8$ $c_{10}$	$u^{45} + 15u^{43} + \dots + 2u + 1$
$c_6, c_{12}$	$u^{45} + 18u^{44} + \dots + 2834u + 188$
$c_7, c_9$	$u^{45} + u^{44} + \dots - 7u + 1$
$c_{11}$	$u^{45} + 39u^{44} + \dots + 23068672u + 1048576$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{45} - 4y^{44} + \dots + 11504y - 256$
$c_2, c_5$	$y^{45} - 24y^{44} + \dots + 172y - 16$
$c_3, c_4, c_8$ $c_{10}$	$y^{45} + 30y^{44} + \dots + 2y - 1$
$c_6, c_{12}$	$y^{45} + 32y^{44} + \dots + 315660y - 35344$
$c_7, c_9$	$y^{45} - 21y^{44} + \dots + 65y - 1$
$c_{11}$	$y^{45} - 3y^{44} + \dots + 9345848836096y - 1099511627776$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.298816 + 0.989953I$ $a = -0.117552 - 1.073810I$ $b = -0.660784 + 0.641263I$	$-5.72982 - 2.27070I$	0
$u = -0.298816 - 0.989953I$ $a = -0.117552 + 1.073810I$ $b = -0.660784 - 0.641263I$	$-5.72982 + 2.27070I$	0
$u = -0.926262 + 0.495766I$ $a = 0.273491 - 0.286793I$ $b = -0.759181 - 0.337100I$	$-4.38180 + 2.50542I$	0
$u = -0.926262 - 0.495766I$ $a = 0.273491 + 0.286793I$ $b = -0.759181 + 0.337100I$	$-4.38180 - 2.50542I$	0
$u = -0.919385 + 0.529264I$ $a = -0.306815 + 0.321928I$ $b = 0.814984 + 0.335175I$	$-7.68302 + 7.12344I$	0
$u = -0.919385 - 0.529264I$ $a = -0.306815 - 0.321928I$ $b = 0.814984 - 0.335175I$	$-7.68302 - 7.12344I$	0
$u = -0.967769 + 0.504465I$ $a = -0.313757 + 0.244824I$ $b = 0.757522 + 0.405488I$	$-8.11430 - 1.70581I$	0
$u = -0.967769 - 0.504465I$ $a = -0.313757 - 0.244824I$ $b = 0.757522 - 0.405488I$	$-8.11430 + 1.70581I$	0
$u = -1.088800 + 0.239432I$ $a = 0.1243660 - 0.0152569I$ $b = -0.349735 - 0.420577I$	$-3.24070 - 0.55670I$	0
$u = -1.088800 - 0.239432I$ $a = 0.1243660 + 0.0152569I$ $b = -0.349735 + 0.420577I$	$-3.24070 + 0.55670I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.198202 + 1.097100I$		
$a = 0.142561 + 1.104920I$	$-2.07839 + 2.22551I$	0
$b = 0.575831 - 0.709841I$		
$u = -0.198202 - 1.097100I$		
$a = 0.142561 - 1.104920I$	$-2.07839 - 2.22551I$	0
$b = 0.575831 + 0.709841I$		
$u = -0.748453 + 0.420636I$		
$a = 0.044813 - 0.385321I$	$-1.42425 + 3.31805I$	0
$b = -0.672626 - 0.096659I$		
$u = -0.748453 - 0.420636I$		
$a = 0.044813 + 0.385321I$	$-1.42425 - 3.31805I$	0
$b = -0.672626 + 0.096659I$		
$u = 1.137450 + 0.415999I$		
$a = 0.056535 + 1.223700I$	$1.92192 + 2.39939I$	0
$b = 0.076306 - 0.677052I$		
$u = 1.137450 - 0.415999I$		
$a = 0.056535 - 1.223700I$	$1.92192 - 2.39939I$	0
$b = 0.076306 + 0.677052I$		
$u = -0.316288 + 1.178330I$		
$a = -0.124276 - 1.126580I$	$-5.70018 + 6.82908I$	0
$b = -0.636773 + 0.790453I$		
$u = -0.316288 - 1.178330I$		
$a = -0.124276 + 1.126580I$	$-5.70018 - 6.82908I$	0
$b = -0.636773 - 0.790453I$		
$u = -0.489115 + 0.309548I$		
$a = 0.313689 + 0.454525I$	$-0.730208 - 0.083656I$	0
$b = 0.529742 - 0.075882I$		
$u = -0.489115 - 0.309548I$		
$a = 0.313689 - 0.454525I$	$-0.730208 + 0.083656I$	0
$b = 0.529742 + 0.075882I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.497869$ $a = 0.450653$ $b = 0.446828$	$-0.768321$	0
$u = -0.87680 + 1.39604I$ $a = -0.302809 - 1.259470I$ $b = -0.61138 + 1.39569I$	$-1.64377 + 9.31582I$	0
$u = -0.87680 - 1.39604I$ $a = -0.302809 + 1.259470I$ $b = -0.61138 - 1.39569I$	$-1.64377 - 9.31582I$	0
$u = -0.90557 + 1.38569I$ $a = -0.325344 - 1.265460I$ $b = -0.59960 + 1.43721I$	$-0.4610 + 18.4165I$	0
$u = -0.90557 - 1.38569I$ $a = -0.325344 + 1.265460I$ $b = -0.59960 - 1.43721I$	$-0.4610 - 18.4165I$	0
$u = -0.89990 + 1.39988I$ $a = 0.319514 + 1.255210I$ $b = 0.58882 - 1.41851I$	$2.67201 + 13.38930I$	0
$u = -0.89990 - 1.39988I$ $a = 0.319514 - 1.255210I$ $b = 0.58882 + 1.41851I$	$2.67201 - 13.38930I$	0
$u = -1.66275 + 0.46895I$ $a = -0.248878 - 0.405451I$ $b = 0.210659 + 0.990181I$	$-4.73342 - 0.73218I$	0
$u = -1.66275 - 0.46895I$ $a = -0.248878 + 0.405451I$ $b = 0.210659 - 0.990181I$	$-4.73342 + 0.73218I$	0
$u = -0.77091 + 1.54748I$ $a = 0.250065 + 1.181600I$ $b = 0.520537 - 1.229120I$	$1.55549 + 7.27021I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.77091 - 1.54748I$		
$a = 0.250065 - 1.181600I$	$1.55549 - 7.27021I$	0
$b = 0.520537 + 1.229120I$		
$u = -0.93055 + 1.47612I$		
$a = 0.326629 + 1.202060I$	$6.74317 + 12.42830I$	0
$b = 0.49630 - 1.38462I$		
$u = -0.93055 - 1.47612I$		
$a = 0.326629 - 1.202060I$	$6.74317 - 12.42830I$	0
$b = 0.49630 + 1.38462I$		
$u = -0.92821 + 1.52975I$		
$a = -0.314902 - 1.176640I$	$7.57419 + 7.55749I$	0
$b = -0.46221 + 1.34602I$		
$u = -0.92821 - 1.52975I$		
$a = -0.314902 + 1.176640I$	$7.57419 - 7.55749I$	0
$b = -0.46221 - 1.34602I$		
$u = -1.75215 + 0.63639I$		
$a = -0.297374 - 0.502556I$	$-3.21485 - 9.54783I$	0
$b = 0.198323 + 1.086910I$		
$u = -1.75215 - 0.63639I$		
$a = -0.297374 + 0.502556I$	$-3.21485 + 9.54783I$	0
$b = 0.198323 - 1.086910I$		
$u = -1.80049 + 0.55270I$		
$a = 0.247640 + 0.493732I$	$-0.29405 - 4.47039I$	0
$b = -0.168749 - 1.056050I$		
$u = -1.80049 - 0.55270I$		
$a = 0.247640 - 0.493732I$	$-0.29405 + 4.47039I$	0
$b = -0.168749 + 1.056050I$		
$u = -0.87811 + 1.69637I$		
$a = -0.272990 - 1.129230I$	$6.69869 + 5.23471I$	0
$b = -0.400769 + 1.241740I$		



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.87811 - 1.69637I$ $a = -0.272990 + 1.129230I$ $b = -0.400769 - 1.241740I$	$6.69869 - 5.23471I$	0
$u = -0.84113 + 1.84473I$ $a = 0.248866 + 1.102950I$ $b = 0.356157 - 1.185750I$	$4.90627 + 0.20772I$	0
$u = -0.84113 - 1.84473I$ $a = 0.248866 - 1.102950I$ $b = 0.356157 + 1.185750I$	$4.90627 - 0.20772I$	0
$u = -2.18886 + 0.16892I$ $a = 0.051200 + 0.568765I$ $b = -0.026784 - 1.043710I$	$2.93772 - 2.57806I$	0
$u = -2.18886 - 0.16892I$ $a = 0.051200 - 0.568765I$ $b = -0.026784 + 1.043710I$	$2.93772 + 2.57806I$	0

$$\text{II. } I_2^u = \langle -4.70 \times 10^{233} a^{39} u - 6.24 \times 10^{233} a^{38} u + \dots - 1.04 \times 10^{237} a + 1.06 \times 10^{236}, 2a^{39} u + 21a^{38} u + \dots + 142a - 33, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ 0.00205561a^{39}u + 0.00273024a^{38}u + \dots + 4.54569a - 0.461858 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.00205561a^{39}u + 0.00273024a^{38}u + \dots + 5.54569a - 0.461858 \\ 0.00205561a^{39}u + 0.00273024a^{38}u + \dots + 4.54569a - 0.461858 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.000862208a^{39}u + 0.000899759a^{38}u + \dots - 0.242076a + 0.813630 \\ -0.000364350a^{39}u + 0.00216092a^{38}u + \dots + 0.166117a + 0.454919 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.000192689a^{39}u - 0.00330351a^{38}u + \dots + 4.35116a + 0.103482 \\ -0.00192222a^{39}u + 0.000432146a^{38}u + \dots + 1.19703a - 0.0456529 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.000862208a^{39}u - 0.000899759a^{38}u + \dots + 0.242076a + 1.18637 \\ -0.00308448a^{39}u + 0.00143811a^{38}u + \dots - 1.13442a - 1.20040 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.000354572a^{39}u - 0.000538750a^{38}u + \dots - 0.171861a + 0.357600 \\ 0.000286009a^{39}u + 0.000105031a^{38}u + \dots + 0.617988a + 0.351373 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0000706296a^{39}u - 0.000562200a^{38}u + \dots + 0.412914a - 0.859285 \\ 0.00181884a^{39}u + 0.00345821a^{38}u + \dots - 0.844918a - 0.506231 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.00463429a^{39}u - 0.00244524a^{38}u + \dots + 1.18427a + 2.37145 \\ 0.00370820a^{39}u + 0.00576929a^{38}u + \dots - 1.20106a - 2.81103 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.00374070a^{39}u + 0.00316369a^{38}u + \dots - 8.66531a - 1.32879 \\ -0.00721432a^{39}u + 0.00732931a^{38}u + \dots - 5.27593a + 1.01325 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.0241933a^{39}u + 0.0327742a^{38}u + \dots + 13.1336a - 21.3800$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{20} + 11u^{19} + \dots + 2u + 1)^4$
$c_2, c_5$	$(u^{20} - u^{19} + \dots + 2u - 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$u^{80} - u^{79} + \dots + 35792u + 15097$
$c_6, c_{12}$	$(u^{20} - 3u^{19} + \dots - 12u + 1)^4$
$c_7, c_9$	$u^{80} - 21u^{79} + \dots + 36u + 169$
$c_{11}$	$(u^2 - u + 1)^{40}$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{20} - 3y^{19} + \dots - 6y + 1)^4$
$c_2, c_5$	$(y^{20} - 11y^{19} + \dots - 2y + 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$y^{80} + 63y^{79} + \dots + 4240509516y + 227919409$
$c_6, c_{12}$	$(y^{20} + 17y^{19} + \dots - 62y + 1)^4$
$c_7, c_9$	$y^{80} + 11y^{79} + \dots - 716504y + 28561$
$c_{11}$	$(y^2 + y + 1)^{40}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = 0.223301 - 0.984504I$ $b = -0.721069 + 0.935523I$	$-5.08534 + 7.61442I$	$-9.65468 - 2.74133I$
$u = 0.500000 + 0.866025I$ $a = -0.161727 + 0.977147I$ $b = 0.679884 - 0.852689I$	$-1.84893 + 2.76931I$	$-6.69810 + 0.36946I$
$u = 0.500000 + 0.866025I$ $a = -0.872992 + 0.525012I$ $b = -0.450422 - 1.018540I$	$3.95796 - 2.02988I$	$-8.93879 + 3.46410I$
$u = 0.500000 + 0.866025I$ $a = 0.521612 + 0.826124I$ $b = 0.311528 - 0.160068I$	$1.94981 + 2.81121I$	$-5.63163 - 2.91571I$
$u = 0.500000 + 0.866025I$ $a = -0.499155 + 0.940951I$ $b = -0.65006 - 1.49725I$	$6.19099 - 3.97633I$	$0.94680 + 8.28286I$
$u = 0.500000 + 0.866025I$ $a = 0.171118 - 0.891526I$ $b = -0.788373 + 0.790387I$	$-5.88315 - 1.39328I$	$-10.96035 + 3.63399I$
$u = 0.500000 + 0.866025I$ $a = -0.417061 + 0.760824I$ $b = -0.83097 - 1.32637I$	$4.01885 - 3.83436I$	$-2.82463 + 7.16468I$
$u = 0.500000 + 0.866025I$ $a = 0.355095 - 0.780475I$ $b = 0.90175 + 1.37031I$	$0.92426 - 8.30305I$	$-6.10015 + 10.00758I$
$u = 0.500000 + 0.866025I$ $a = 0.531113 - 1.032670I$ $b = 0.54401 + 1.57078I$	$6.19099 - 0.08344I$	$0.94680 - 1.35465I$
$u = 0.500000 + 0.866025I$ $a = 0.375110 - 0.675074I$ $b = 0.90343 + 1.23362I$	$0.496471 + 0.114015I$	$-7.45592 + 3.22103I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = -0.528289 + 1.180870I$ $b = -0.35513 - 1.72050I$	$0.92426 + 4.24328I$	$-8.00000 + 0.I$
$u = 0.500000 + 0.866025I$ $a = 0.560866 - 1.168870I$ $b = 0.35123 + 1.65493I$	$4.01885 - 0.22541I$	0
$u = 0.500000 + 0.866025I$ $a = -0.455734 - 0.521331I$ $b = -0.539610 - 0.030941I$	$2.99206 - 1.44519I$	$-3.20205 + 3.45501I$
$u = 0.500000 + 0.866025I$ $a = -0.565033 + 1.216060I$ $b = -0.26427 - 1.66859I$	$0.49647 - 4.17378I$	0
$u = 0.500000 + 0.866025I$ $a = -0.17739 + 1.40437I$ $b = 0.160251 - 1.054550I$	$1.94981 + 2.81121I$	0
$u = 0.500000 + 0.866025I$ $a = 0.043628 + 0.507114I$ $b = 0.928213 - 0.215774I$	$-1.59840 - 2.02988I$	$-11.89977 + 3.46410I$
$u = 0.500000 + 0.866025I$ $a = 0.87299 - 1.27368I$ $b = 0.234300 + 1.392880I$	$3.95796 - 2.02988I$	0
$u = 0.500000 + 0.866025I$ $a = 1.55443 - 0.33903I$ $b = 0.022743 + 0.944463I$	$0.49647 - 4.17378I$	0
$u = 0.500000 + 0.866025I$ $a = 0.27721 - 1.58998I$ $b = 0.019390 + 1.138130I$	$2.99206 - 1.44519I$	0
$u = 0.500000 + 0.866025I$ $a = 0.54980 + 1.52611I$ $b = -0.151295 - 0.510966I$	$-1.84893 + 2.76931I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = -1.57372 + 0.50963I$ $b = -0.035102 - 1.032930I$	$4.01885 - 0.22541I$	0
$u = 0.500000 + 0.866025I$ $a = -0.223415 - 0.228493I$ $b = -0.909375 - 0.182307I$	$2.99206 - 2.61458I$	$-3.20205 + 3.47320I$
$u = 0.500000 + 0.866025I$ $a = -0.65612 - 1.54780I$ $b = 0.206465 + 0.455571I$	$-5.08534 + 7.61442I$	0
$u = 0.500000 + 0.866025I$ $a = 0.157128 - 0.259381I$ $b = -1.328830 + 0.069336I$	$-5.88315 - 2.66649I$	$-10.96035 + 3.29421I$
$u = 0.500000 + 0.866025I$ $a = -0.511135 - 1.66307I$ $b = 0.221039 + 0.585128I$	$-5.88315 - 1.39328I$	0
$u = 0.500000 + 0.866025I$ $a = -0.132043 + 0.215117I$ $b = 1.324980 + 0.002145I$	$-1.84893 - 6.82908I$	$-6.69810 + 6.55874I$
$u = 0.500000 + 0.866025I$ $a = 0.161659 - 0.191649I$ $b = -1.376880 - 0.014061I$	$-5.08534 - 11.67420I$	$-9.65468 + 9.66953I$
$u = 0.500000 + 0.866025I$ $a = 1.69318 - 0.48218I$ $b = -0.025625 + 1.034880I$	$0.92426 + 4.24328I$	0
$u = 0.500000 + 0.866025I$ $a = -1.56080 + 0.88587I$ $b = -0.071541 - 1.200140I$	$6.19099 - 0.08344I$	0
$u = 0.500000 + 0.866025I$ $a = 0.068505 + 0.163465I$ $b = 1.111960 + 0.176330I$	$1.94981 - 6.87098I$	$-5.63163 + 9.84391I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = 1.52884 - 1.08774I$ $b = 0.092842 + 1.273400I$	$6.19099 - 3.97633I$	0
$u = 0.500000 + 0.866025I$ $a = -0.04363 + 1.89905I$ $b = -0.233613 - 0.987309I$	$-1.59840 - 2.02988I$	0
$u = 0.500000 + 0.866025I$ $a = 0.40194 - 1.88281I$ $b = 0.210631 + 1.186430I$	$2.99206 - 2.61458I$	0
$u = 0.500000 + 0.866025I$ $a = 1.42992 - 1.42006I$ $b = 0.134239 + 1.363600I$	$4.01885 - 3.83436I$	0
$u = 0.500000 + 0.866025I$ $a = -1.36451 + 1.55210I$ $b = -0.155551 - 1.386520I$	$0.496471 + 0.114015I$	0
$u = 0.500000 + 0.866025I$ $a = -0.41272 + 2.06703I$ $b = -0.295962 - 1.192210I$	$1.94981 - 6.87098I$	0
$u = 0.500000 + 0.866025I$ $a = -1.51999 + 1.47916I$ $b = -0.117609 - 1.383380I$	$0.92426 - 8.30305I$	0
$u = 0.500000 + 0.866025I$ $a = -0.25603 + 2.28814I$ $b = -0.408313 - 1.141740I$	$-1.84893 - 6.82908I$	0
$u = 0.500000 + 0.866025I$ $a = 0.18310 - 2.29522I$ $b = 0.421267 + 1.109750I$	$-5.88315 - 2.66649I$	0
$u = 0.500000 + 0.866025I$ $a = 0.27116 - 2.34065I$ $b = 0.429461 + 1.155270I$	$-5.08534 - 11.67420I$	0



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 - 0.866025I$ $a = 0.223301 + 0.984504I$ $b = -0.721069 - 0.935523I$	$-5.08534 - 7.61442I$	$-9.65468 + 2.74133I$
$u = 0.500000 - 0.866025I$ $a = -0.161727 - 0.977147I$ $b = 0.679884 + 0.852689I$	$-1.84893 - 2.76931I$	$-6.69810 - 0.36946I$
$u = 0.500000 - 0.866025I$ $a = -0.872992 - 0.525012I$ $b = -0.450422 + 1.018540I$	$3.95796 + 2.02988I$	$-8.93879 - 3.46410I$
$u = 0.500000 - 0.866025I$ $a = 0.521612 - 0.826124I$ $b = 0.311528 + 0.160068I$	$1.94981 - 2.81121I$	$-5.63163 + 2.91571I$
$u = 0.500000 - 0.866025I$ $a = -0.499155 - 0.940951I$ $b = -0.65006 + 1.49725I$	$6.19099 + 3.97633I$	$0.94680 - 8.28286I$
$u = 0.500000 - 0.866025I$ $a = 0.171118 + 0.891526I$ $b = -0.788373 - 0.790387I$	$-5.88315 + 1.39328I$	$-10.96035 - 3.63399I$
$u = 0.500000 - 0.866025I$ $a = -0.417061 - 0.760824I$ $b = -0.83097 + 1.32637I$	$4.01885 + 3.83436I$	$-2.82463 - 7.16468I$
$u = 0.500000 - 0.866025I$ $a = 0.355095 + 0.780475I$ $b = 0.90175 - 1.37031I$	$0.92426 + 8.30305I$	$-6.10015 - 10.00758I$
$u = 0.500000 - 0.866025I$ $a = 0.531113 + 1.032670I$ $b = 0.54401 - 1.57078I$	$6.19099 + 0.08344I$	$0.94680 + 1.35465I$
$u = 0.500000 - 0.866025I$ $a = 0.375110 + 0.675074I$ $b = 0.90343 - 1.23362I$	$0.496471 - 0.114015I$	$-7.45592 - 3.22103I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 - 0.866025I$ $a = -0.528289 - 1.180870I$ $b = -0.35513 + 1.72050I$	$0.92426 - 4.24328I$	$-8.00000 + 0.I$
$u = 0.500000 - 0.866025I$ $a = 0.560866 + 1.168870I$ $b = 0.35123 - 1.65493I$	$4.01885 + 0.22541I$	0
$u = 0.500000 - 0.866025I$ $a = -0.455734 + 0.521331I$ $b = -0.539610 + 0.030941I$	$2.99206 + 1.44519I$	$-3.20205 - 3.45501I$
$u = 0.500000 - 0.866025I$ $a = -0.565033 - 1.216060I$ $b = -0.26427 + 1.66859I$	$0.49647 + 4.17378I$	0
$u = 0.500000 - 0.866025I$ $a = -0.17739 - 1.40437I$ $b = 0.160251 + 1.054550I$	$1.94981 - 2.81121I$	0
$u = 0.500000 - 0.866025I$ $a = 0.043628 - 0.507114I$ $b = 0.928213 + 0.215774I$	$-1.59840 + 2.02988I$	$-11.89977 - 3.46410I$
$u = 0.500000 - 0.866025I$ $a = 0.87299 + 1.27368I$ $b = 0.234300 - 1.392880I$	$3.95796 + 2.02988I$	0
$u = 0.500000 - 0.866025I$ $a = 1.55443 + 0.33903I$ $b = 0.022743 - 0.944463I$	$0.49647 + 4.17378I$	0
$u = 0.500000 - 0.866025I$ $a = 0.27721 + 1.58998I$ $b = 0.019390 - 1.138130I$	$2.99206 + 1.44519I$	0
$u = 0.500000 - 0.866025I$ $a = 0.54980 - 1.52611I$ $b = -0.151295 + 0.510966I$	$-1.84893 - 2.76931I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 - 0.866025I$ $a = -1.57372 - 0.50963I$ $b = -0.035102 + 1.032930I$	$4.01885 + 0.22541I$	0
$u = 0.500000 - 0.866025I$ $a = -0.223415 + 0.228493I$ $b = -0.909375 + 0.182307I$	$2.99206 + 2.61458I$	$-3.20205 - 3.47320I$
$u = 0.500000 - 0.866025I$ $a = -0.65612 + 1.54780I$ $b = 0.206465 - 0.455571I$	$-5.08534 - 7.61442I$	0
$u = 0.500000 - 0.866025I$ $a = 0.157128 + 0.259381I$ $b = -1.328830 - 0.069336I$	$-5.88315 + 2.66649I$	$-10.96035 - 3.29421I$
$u = 0.500000 - 0.866025I$ $a = -0.51135 + 1.66307I$ $b = 0.221039 - 0.585128I$	$-5.88315 + 1.39328I$	0
$u = 0.500000 - 0.866025I$ $a = -0.132043 - 0.215117I$ $b = 1.324980 - 0.002145I$	$-1.84893 + 6.82908I$	$-6.69810 - 6.55874I$
$u = 0.500000 - 0.866025I$ $a = 0.161659 + 0.191649I$ $b = -1.376880 + 0.014061I$	$-5.08534 + 11.67420I$	$-9.65468 - 9.66953I$
$u = 0.500000 - 0.866025I$ $a = 1.69318 + 0.48218I$ $b = -0.025625 - 1.034880I$	$0.92426 - 4.24328I$	0
$u = 0.500000 - 0.866025I$ $a = -1.56080 - 0.88587I$ $b = -0.071541 + 1.200140I$	$6.19099 + 0.08344I$	0
$u = 0.500000 - 0.866025I$ $a = 0.068505 - 0.163465I$ $b = 1.111960 - 0.176330I$	$1.94981 + 6.87098I$	$-5.63163 - 9.84391I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 - 0.866025I$ $a = 1.52884 + 1.08774I$ $b = 0.092842 - 1.273400I$	$6.19099 + 3.97633I$	0
$u = 0.500000 - 0.866025I$ $a = -0.04363 - 1.89905I$ $b = -0.233613 + 0.987309I$	$-1.59840 + 2.02988I$	0
$u = 0.500000 - 0.866025I$ $a = 0.40194 + 1.88281I$ $b = 0.210631 - 1.186430I$	$2.99206 + 2.61458I$	0
$u = 0.500000 - 0.866025I$ $a = 1.42992 + 1.42006I$ $b = 0.134239 - 1.363600I$	$4.01885 + 3.83436I$	0
$u = 0.500000 - 0.866025I$ $a = -1.36451 - 1.55210I$ $b = -0.155551 + 1.386520I$	$0.496471 - 0.114015I$	0
$u = 0.500000 - 0.866025I$ $a = -0.41272 - 2.06703I$ $b = -0.295962 + 1.192210I$	$1.94981 + 6.87098I$	0
$u = 0.500000 - 0.866025I$ $a = -1.51999 - 1.47916I$ $b = -0.117609 + 1.383380I$	$0.92426 + 8.30305I$	0
$u = 0.500000 - 0.866025I$ $a = -0.25603 - 2.28814I$ $b = -0.408313 + 1.141740I$	$-1.84893 + 6.82908I$	0
$u = 0.500000 - 0.866025I$ $a = 0.18310 + 2.29522I$ $b = 0.421267 - 1.109750I$	$-5.88315 + 2.66649I$	0
$u = 0.500000 - 0.866025I$ $a = 0.27116 + 2.34065I$ $b = 0.429461 - 1.155270I$	$-5.08534 + 11.67420I$	0

$$\text{III. } I_3^u = \langle -11u^{22} - 8u^{21} + \dots + b + 40, -29u^{22} - 83u^{21} + \dots + a + 3, u^{23} + 2u^{22} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 29u^{22} + 83u^{21} + \dots + 45u - 3 \\ 11u^{22} + 8u^{21} + \dots - 3u - 40 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 40u^{22} + 91u^{21} + \dots + 42u - 43 \\ 11u^{22} + 8u^{21} + \dots - 3u - 40 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^{22} - 5u^{21} + \dots - 8u + 1 \\ -u^{22} - 2u^{21} + \dots - 6u^2 + 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -43u^{22} - 126u^{21} + \dots - 67u + 1 \\ -26u^{22} - 43u^{21} + \dots - 13u + 54 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{22} - 3u^{21} + \dots - 5u^2 - 7u \\ -u^{22} - 2u^{21} + \dots - u + 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{21} - 3u^{20} + \dots - 5u - 7 \\ -2u^{22} - 5u^{21} + \dots - 7u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -11u^{22} - 28u^{21} + \dots - 26u + 6 \\ -5u^{22} - 9u^{21} + \dots - 9u^2 + 16 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -14u^{22} - 23u^{21} + \dots + 3u + 40 \\ 13u^{22} + 39u^{21} + \dots + 40u + 5 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 30u^{22} + 69u^{21} + \dots + 35u - 32 \\ u^{22} - 6u^{21} + \dots - 16u - 21 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -101u^{22} - 241u^{21} - 63u^{20} - 438u^{19} - 1512u^{18} - 929u^{17} - 817u^{16} - 3145u^{15} - 2707u^{14} - 726u^{13} - 3279u^{12} - 3820u^{11} - 319u^{10} - 1123u^9 - 2832u^8 - 256u^7 + 468u^6 - 1028u^5 - 293u^4 + 427u^3 - 102u^2 - 118u + 87$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{23} - 13u^{22} + \dots + 5u - 1$
$c_2$	$u^{23} + u^{22} + \dots - u - 1$
$c_3, c_{10}$	$u^{23} + 12u^{21} + \dots + 3u - 1$
$c_4, c_8$	$u^{23} + 12u^{21} + \dots + 3u + 1$
$c_5$	$u^{23} - u^{22} + \dots - u + 1$
$c_6$	$u^{23} - 3u^{22} + \dots + 3u + 1$
$c_7, c_9$	$u^{23} + u^{22} + \dots + 2u - 1$
$c_{11}$	$u^{23} + 2u^{22} + \dots - u + 1$
$c_{12}$	$u^{23} + 3u^{22} + \dots + 3u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{23} - y^{22} + \dots + 9y - 1$
$c_2, c_5$	$y^{23} - 13y^{22} + \dots + 5y - 1$
$c_3, c_4, c_8$ $c_{10}$	$y^{23} + 24y^{22} + \dots + 5y - 1$
$c_6, c_{12}$	$y^{23} + 15y^{22} + \dots + 43y - 1$
$c_7, c_9$	$y^{23} + y^{22} + \dots + 4y - 1$
$c_{11}$	$y^{23} - 4y^{22} + \dots - y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.891523 + 0.539467I$ $a = -0.465440 - 1.290310I$ $b = 0.417800 + 0.594568I$	$-2.06437 - 3.95440I$	$-8.63156 + 6.09948I$
$u = -0.891523 - 0.539467I$ $a = -0.465440 + 1.290310I$ $b = 0.417800 - 0.594568I$	$-2.06437 + 3.95440I$	$-8.63156 - 6.09948I$
$u = -0.772619 + 0.561019I$ $a = 0.52054 + 1.46048I$ $b = -0.490640 - 0.627106I$	$-5.20691 - 8.91486I$	$-10.68690 + 8.90274I$
$u = -0.772619 - 0.561019I$ $a = 0.52054 - 1.46048I$ $b = -0.490640 + 0.627106I$	$-5.20691 + 8.91486I$	$-10.68690 - 8.90274I$
$u = -0.948923$ $a = -0.476498$ $b = 0.232005$	$-3.06830$	$-9.64660$
$u = -0.853358 + 0.383068I$ $a = 0.687818 + 1.149760I$ $b = -0.454872 - 0.481247I$	$-6.25538 + 0.06461I$	$-13.33134 + 1.68019I$
$u = -0.853358 - 0.383068I$ $a = 0.687818 - 1.149760I$ $b = -0.454872 + 0.481247I$	$-6.25538 - 0.06461I$	$-13.33134 - 1.68019I$
$u = 0.260940 + 1.058470I$ $a = 0.74302 - 1.25125I$ $b = 0.381175 + 1.168270I$	$3.61187 - 4.35423I$	$-4.17455 + 6.43852I$
$u = 0.260940 - 1.058470I$ $a = 0.74302 + 1.25125I$ $b = 0.381175 - 1.168270I$	$3.61187 + 4.35423I$	$-4.17455 - 6.43852I$
$u = 0.755052 + 0.791973I$ $a = -0.767365 + 0.648951I$ $b = -0.254019 - 1.301980I$	$5.36340 - 2.81228I$	$-2.58785 + 3.59508I$



Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.755052 - 0.791973I$ $a = -0.767365 - 0.648951I$ $b = -0.254019 + 1.301980I$	$5.36340 + 2.81228I$	$-2.58785 - 3.59508I$
$u = 0.357379 + 0.820793I$ $a = -1.07541 + 1.11627I$ $b = -0.403716 - 1.268430I$	$4.71667 - 1.35723I$	$-1.00741 - 1.61688I$
$u = 0.357379 - 0.820793I$ $a = -1.07541 - 1.11627I$ $b = -0.403716 + 1.268430I$	$4.71667 + 1.35723I$	$-1.00741 + 1.61688I$
$u = 0.487371 + 0.607807I$ $a = -1.32119 + 0.63458I$ $b = -0.36016 - 1.39021I$	$3.92488 - 2.52107I$	$-3.55346 + 0.94577I$
$u = 0.487371 - 0.607807I$ $a = -1.32119 - 0.63458I$ $b = -0.36016 + 1.39021I$	$3.92488 + 2.52107I$	$-3.55346 - 0.94577I$
$u = 0.493262 + 0.533153I$ $a = 1.42724 - 0.44917I$ $b = 0.35215 + 1.43492I$	$0.80414 - 6.84512I$	$-6.80922 + 4.56757I$
$u = 0.493262 - 0.533153I$ $a = 1.42724 + 0.44917I$ $b = 0.35215 - 1.43492I$	$0.80414 + 6.84512I$	$-6.80922 - 4.56757I$
$u = 0.412195 + 0.581577I$ $a = 1.53236 - 0.73131I$ $b = 0.40701 + 1.40600I$	$0.56415 + 1.51972I$	$-7.03913 - 2.65885I$
$u = 0.412195 - 0.581577I$ $a = 1.53236 + 0.73131I$ $b = 0.40701 - 1.40600I$	$0.56415 - 1.51972I$	$-7.03913 + 2.65885I$
$u = 0.91123 + 1.19260I$ $a = 0.507332 - 0.834010I$ $b = 0.219623 + 1.205300I$	$4.37259 + 1.11056I$	$-5.33341 - 2.98849I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.91123 - 1.19260I$		
$a = 0.507332 + 0.834010I$	$4.37259 - 1.11056I$	$-5.33341 + 2.98849I$
$b = 0.219623 - 1.205300I$		
$u = -1.68547 + 0.26457I$		
$a = -0.050661 - 1.036720I$	$1.57271 - 2.56456I$	$-19.0218 + 7.7387I$
$b = 0.069646 + 0.652543I$		
$u = -1.68547 - 0.26457I$		
$a = -0.050661 + 1.036720I$	$1.57271 + 2.56456I$	$-19.0218 - 7.7387I$
$b = 0.069646 - 0.652543I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^{20} + 11u^{19} + \dots + 2u + 1)^4)(u^{23} - 13u^{22} + \dots + 5u - 1)$ $\cdot (u^{45} + 24u^{44} + \dots + 172u + 16)$
$c_2$	$((u^{20} - u^{19} + \dots + 2u - 1)^4)(u^{23} + u^{22} + \dots - u - 1)$ $\cdot (u^{45} + 6u^{44} + \dots + 38u + 4)$
$c_3, c_{10}$	$(u^{23} + 12u^{21} + \dots + 3u - 1)(u^{45} + 15u^{43} + \dots + 2u + 1)$ $\cdot (u^{80} - u^{79} + \dots + 35792u + 15097)$
$c_4, c_8$	$(u^{23} + 12u^{21} + \dots + 3u + 1)(u^{45} + 15u^{43} + \dots + 2u + 1)$ $\cdot (u^{80} - u^{79} + \dots + 35792u + 15097)$
$c_5$	$((u^{20} - u^{19} + \dots + 2u - 1)^4)(u^{23} - u^{22} + \dots - u + 1)$ $\cdot (u^{45} + 6u^{44} + \dots + 38u + 4)$
$c_6$	$((u^{20} - 3u^{19} + \dots - 12u + 1)^4)(u^{23} - 3u^{22} + \dots + 3u + 1)$ $\cdot (u^{45} + 18u^{44} + \dots + 2834u + 188)$
$c_7, c_9$	$(u^{23} + u^{22} + \dots + 2u - 1)(u^{45} + u^{44} + \dots - 7u + 1)$ $\cdot (u^{80} - 21u^{79} + \dots + 36u + 169)$
$c_{11}$	$((u^2 - u + 1)^{40})(u^{23} + 2u^{22} + \dots - u + 1)$ $\cdot (u^{45} + 39u^{44} + \dots + 23068672u + 1048576)$
$c_{12}$	$((u^{20} - 3u^{19} + \dots - 12u + 1)^4)(u^{23} + 3u^{22} + \dots + 3u - 1)$ $\cdot (u^{45} + 18u^{44} + \dots + 2834u + 188)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^{20} - 3y^{19} + \dots - 6y + 1)^4)(y^{23} - y^{22} + \dots + 9y - 1)$ $\cdot (y^{45} - 4y^{44} + \dots + 11504y - 256)$
$c_2, c_5$	$((y^{20} - 11y^{19} + \dots - 2y + 1)^4)(y^{23} - 13y^{22} + \dots + 5y - 1)$ $\cdot (y^{45} - 24y^{44} + \dots + 172y - 16)$
$c_3, c_4, c_8$ $c_{10}$	$(y^{23} + 24y^{22} + \dots + 5y - 1)(y^{45} + 30y^{44} + \dots + 2y - 1)$ $\cdot (y^{80} + 63y^{79} + \dots + 4240509516y + 227919409)$
$c_6, c_{12}$	$((y^{20} + 17y^{19} + \dots - 62y + 1)^4)(y^{23} + 15y^{22} + \dots + 43y - 1)$ $\cdot (y^{45} + 32y^{44} + \dots + 315660y - 35344)$
$c_7, c_9$	$(y^{23} + y^{22} + \dots + 4y - 1)(y^{45} - 21y^{44} + \dots + 65y - 1)$ $\cdot (y^{80} + 11y^{79} + \dots - 716504y + 28561)$
$c_{11}$	$((y^2 + y + 1)^{40})(y^{23} - 4y^{22} + \dots - y - 1)$ $\cdot (y^{45} - 3y^{44} + \dots + 9345848836096y - 1099511627776)$