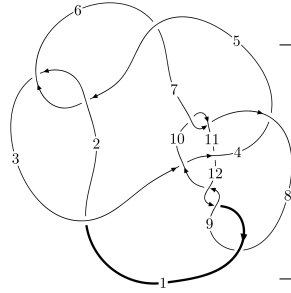
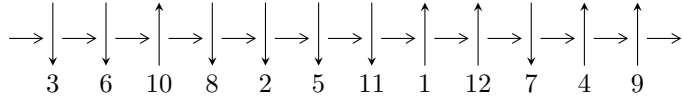


12a<sub>0429</sub> (K12a<sub>0429</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$9,12 \xrightarrow{c_9} 10 \xrightarrow{c_{12}} 1,4 \xrightarrow{c_3} 3 \xrightarrow{c_1} 2 \xrightarrow{c_8} 8 \xrightarrow{c_4} 5 \xrightarrow{c_{11}} 11 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \rightsquigarrow c_2, c_5, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.05234 \times 10^{155} u^{99} + 7.99874 \times 10^{155} u^{98} + \dots + 1.26559 \times 10^{156} b - 4.31298 \times 10^{155}, \\ -6.46036 \times 10^{154} u^{99} + 2.42368 \times 10^{155} u^{98} + \dots + 4.21862 \times 10^{155} a - 2.87887 \times 10^{155}, \\ u^{100} - 4u^{99} + \dots - 2u + 2 \rangle$$

$$I_2^u = \langle 9b^3 + 6b^2u + 3b^2 - 6b - 2u - 1, a, u^2 + u + 1 \rangle$$

$$I_3^u = \langle b + 1, 2a + u, u^2 + 2 \rangle$$

$$I_1^v = \langle a, b - 1, v - 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 109 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -2.05 \times 10^{155} u^{99} + 8.00 \times 10^{155} u^{98} + \dots + 1.27 \times 10^{156} b - 4.31 \times 10^{155}, -6.46 \times 10^{154} u^{99} + 2.42 \times 10^{155} u^{98} + \dots + 4.22 \times 10^{155} a - 2.88 \times 10^{155}, u^{100} - 4u^{99} + \dots - 2u + 2 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.153139u^{99} - 0.574519u^{98} + \dots - 8.03232u + 0.682420 \\ 0.162165u^{99} - 0.632019u^{98} + \dots - 5.73442u + 0.340789 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.0302022u^{99} + 0.163017u^{98} + \dots - 2.06770u + 0.417704 \\ 0.179404u^{99} - 0.709755u^{98} + \dots - 6.10945u + 0.349133 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.173099u^{99} + 0.676163u^{98} + \dots + 4.89191u + 0.906950 \\ 0.0182730u^{99} - 0.0469571u^{98} + \dots + 4.00425u - 1.14662 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0703189u^{99} - 0.177839u^{98} + \dots - 1.91494u + 0.223572 \\ 0.202770u^{99} - 0.766671u^{98} + \dots - 5.41230u + 0.265518 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0494285u^{99} - 0.0313702u^{98} + \dots + 1.20145u + 0.366829 \\ 0.00688276u^{99} + 0.0220776u^{98} + \dots - 2.07197u + 0.512273 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0425457u^{99} - 0.0534478u^{98} + \dots + 3.27342u - 0.145444 \\ -0.00688276u^{99} - 0.0220776u^{98} + \dots + 2.07197u - 0.512273 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.138863u^{99} - 0.465578u^{98} + \dots - 1.24267u - 0.857682 \\ -0.0184998u^{99} + 0.0344608u^{98} + \dots - 0.833055u + 0.461735 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $1.15224u^{99} - 4.78283u^{98} + \dots - 86.7199u + 10.7919$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{100} + 34u^{99} + \dots + 925u + 81$
$c_2, c_5$	$u^{100} + 6u^{99} + \dots + 59u + 9$
$c_3$	$27(27u^{100} - 234u^{99} + \dots - 3357967u - 461099)$
$c_4$	$27(27u^{100} + 45u^{99} + \dots - 4549965u + 518603)$
$c_7, c_{10}$	$u^{100} + 5u^{99} + \dots - 38u - 3$
$c_8, c_9, c_{12}$	$u^{100} + 4u^{99} + \dots + 2u + 2$
$c_{11}$	$u^{100} - 4u^{99} + \dots - 12960u - 5184$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{100} + 70y^{99} + \dots - 377077y + 6561$
$c_2, c_5$	$y^{100} - 34y^{99} + \dots - 925y + 81$
$c_3$	$729$ $\cdot (729y^{100} + 11502y^{99} + \dots - 1559280610721y + 212612287801)$
$c_4$	$729$ $\cdot (729y^{100} - 27135y^{99} + \dots - 3345262023807y + 268949071609)$
$c_7, c_{10}$	$y^{100} - 53y^{99} + \dots - 658y + 9$
$c_8, c_9, c_{12}$	$y^{100} + 94y^{99} + \dots - 60y + 4$
$c_{11}$	$y^{100} + 32y^{99} + \dots + 414305280y + 26873856$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.679869 + 0.748107I$ $a = -0.295432 - 1.043560I$ $b = -0.528057 - 0.396540I$	$0.57702 - 2.41824I$	0
$u = 0.679869 - 0.748107I$ $a = -0.295432 + 1.043560I$ $b = -0.528057 + 0.396540I$	$0.57702 + 2.41824I$	0
$u = -0.936181 + 0.398524I$ $a = -0.806021 + 0.540723I$ $b = -0.497698 - 0.087674I$	$3.87531 - 7.09723I$	0
$u = -0.936181 - 0.398524I$ $a = -0.806021 - 0.540723I$ $b = -0.497698 + 0.087674I$	$3.87531 + 7.09723I$	0
$u = -0.344981 + 0.919122I$ $a = -0.224263 - 0.488787I$ $b = -0.173178 - 0.412785I$	$-0.77026 - 2.23336I$	0
$u = -0.344981 - 0.919122I$ $a = -0.224263 + 0.488787I$ $b = -0.173178 + 0.412785I$	$-0.77026 + 2.23336I$	0
$u = 0.849871 + 0.454924I$ $a = 1.30719 + 0.64935I$ $b = 0.877707 - 0.222614I$	$0.55952 + 13.49860I$	0
$u = 0.849871 - 0.454924I$ $a = 1.30719 - 0.64935I$ $b = 0.877707 + 0.222614I$	$0.55952 - 13.49860I$	0
$u = -0.898112 + 0.334651I$ $a = 0.868301 - 0.554620I$ $b = 0.482624 + 0.101398I$	$4.50393 - 1.41421I$	0
$u = -0.898112 - 0.334651I$ $a = 0.868301 + 0.554620I$ $b = 0.482624 - 0.101398I$	$4.50393 + 1.41421I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.732409 + 0.617249I$		
$a = -0.681387 + 0.294463I$	$-1.18132 - 2.64358I$	0
$b = -0.437220 - 0.022316I$		
$u = -0.732409 - 0.617249I$		
$a = -0.681387 - 0.294463I$	$-1.18132 + 2.64358I$	0
$b = -0.437220 + 0.022316I$		
$u = 0.758120 + 0.731071I$		
$a = 0.266524 + 1.044920I$	$-0.23831 - 8.08349I$	0
$b = 0.488342 + 0.372478I$		
$u = 0.758120 - 0.731071I$		
$a = 0.266524 - 1.044920I$	$-0.23831 + 8.08349I$	0
$b = 0.488342 - 0.372478I$		
$u = 0.820796 + 0.415357I$		
$a = -1.33445 - 0.70691I$	$1.56962 + 7.53478I$	0
$b = -0.838028 + 0.244297I$		
$u = 0.820796 - 0.415357I$		
$a = -1.33445 + 0.70691I$	$1.56962 - 7.53478I$	0
$b = -0.838028 - 0.244297I$		
$u = 0.739811 + 0.488405I$		
$a = 0.236103 + 1.139040I$	$-5.36950 - 2.86567I$	0
$b = 0.383295 + 0.485386I$		
$u = 0.739811 - 0.488405I$		
$a = 0.236103 - 1.139040I$	$-5.36950 + 2.86567I$	0
$b = 0.383295 - 0.485386I$		
$u = 0.685574 + 0.521881I$		
$a = 1.54529 + 0.54023I$	$-5.53789 + 7.57635I$	0
$b = 0.773480 - 0.091899I$		
$u = 0.685574 - 0.521881I$		
$a = 1.54529 - 0.54023I$	$-5.53789 - 7.57635I$	0
$b = 0.773480 + 0.091899I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.773853 + 0.126658I$	$-2.85478 + 2.28442I$	0
$a = 0.073723 + 1.239840I$		
$b = 0.112212 + 0.588993I$		
$u = 0.773853 - 0.126658I$	$-2.85478 - 2.28442I$	0
$a = 0.073723 - 1.239840I$		
$b = 0.112212 - 0.588993I$		
$u = -0.742950 + 0.971442I$	$2.25943 + 1.26483I$	0
$a = -0.379885 + 0.450207I$		
$b = -0.443297 + 0.208112I$		
$u = -0.742950 - 0.971442I$	$2.25943 - 1.26483I$	0
$a = -0.379885 - 0.450207I$		
$b = -0.443297 - 0.208112I$		
$u = 0.021499 + 1.227650I$	$0.82547 - 1.32524I$	0
$a = -0.999611 - 0.389930I$		
$b = -2.86921 - 0.22184I$		
$u = 0.021499 - 1.227650I$	$0.82547 + 1.32524I$	0
$a = -0.999611 + 0.389930I$		
$b = -2.86921 + 0.22184I$		
$u = -0.682650 + 1.028010I$	$2.53530 - 4.11578I$	0
$a = 0.314081 - 0.478465I$		
$b = 0.411579 - 0.285935I$		
$u = -0.682650 - 1.028010I$	$2.53530 + 4.11578I$	0
$a = 0.314081 + 0.478465I$		
$b = 0.411579 + 0.285935I$		
$u = 0.089185 + 1.254450I$	$0.54484 + 5.05920I$	0
$a = 1.090420 + 0.281507I$		
$b = 3.13638 + 0.17745I$		
$u = 0.089185 - 1.254450I$	$0.54484 - 5.05920I$	0
$a = 1.090420 - 0.281507I$		
$b = 3.13638 - 0.17745I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.129409 + 1.287930I$ $a = -0.441936 - 0.858037I$ $b = -1.209260 - 0.582559I$	$0.097636 - 0.577860I$	0
$u = 0.129409 - 1.287930I$ $a = -0.441936 + 0.858037I$ $b = -1.209260 + 0.582559I$	$0.097636 + 0.577860I$	0
$u = 0.591401 + 0.372296I$ $a = -1.78322 - 0.87172I$ $b = -0.608394 + 0.173490I$	$-1.51260 + 4.59124I$	$-1.18190 - 7.08838I$
$u = 0.591401 - 0.372296I$ $a = -1.78322 + 0.87172I$ $b = -0.608394 - 0.173490I$	$-1.51260 - 4.59124I$	$-1.18190 + 7.08838I$
$u = -0.188206 + 1.312440I$ $a = -0.000149 - 1.118010I$ $b = 0.03449 - 1.53600I$	$-1.31735 - 3.54814I$	0
$u = -0.188206 - 1.312440I$ $a = -0.000149 + 1.118010I$ $b = 0.03449 + 1.53600I$	$-1.31735 + 3.54814I$	0
$u = -0.049713 + 1.345270I$ $a = 0.51133 + 1.49541I$ $b = 1.17296 + 2.41695I$	$-7.10395 - 1.14182I$	0
$u = -0.049713 - 1.345270I$ $a = 0.51133 - 1.49541I$ $b = 1.17296 - 2.41695I$	$-7.10395 + 1.14182I$	0
$u = 0.136745 + 1.361250I$ $a = 0.439945 + 0.800424I$ $b = 1.351600 + 0.407360I$	$-0.81482 + 5.24891I$	0
$u = 0.136745 - 1.361250I$ $a = 0.439945 - 0.800424I$ $b = 1.351600 - 0.407360I$	$-0.81482 - 5.24891I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.277514 + 1.363830I$ $a = 0.760070 - 0.073241I$ $b = 1.46420 + 0.87101I$	$-6.81470 + 1.22350I$	0
$u = 0.277514 - 1.363830I$ $a = 0.760070 + 0.073241I$ $b = 1.46420 - 0.87101I$	$-6.81470 - 1.22350I$	0
$u = -0.089485 + 1.389530I$ $a = 0.090696 - 0.485921I$ $b = -0.94839 + 2.04503I$	$-4.19619 + 2.34737I$	0
$u = -0.089485 - 1.389530I$ $a = 0.090696 + 0.485921I$ $b = -0.94839 - 2.04503I$	$-4.19619 - 2.34737I$	0
$u = -0.548947 + 0.259031I$ $a = -1.30165 - 1.81150I$ $b = -0.262516 + 0.230241I$	$2.18117 - 6.47618I$	$-0.36986 + 8.71363I$
$u = -0.548947 - 0.259031I$ $a = -1.30165 + 1.81150I$ $b = -0.262516 - 0.230241I$	$2.18117 + 6.47618I$	$-0.36986 - 8.71363I$
$u = -0.583366 + 0.156368I$ $a = 1.51729 + 1.42250I$ $b = 0.302065 - 0.186011I$	$3.23926 - 0.72911I$	$2.75290 + 2.73531I$
$u = -0.583366 - 0.156368I$ $a = 1.51729 - 1.42250I$ $b = 0.302065 + 0.186011I$	$3.23926 + 0.72911I$	$2.75290 - 2.73531I$
$u = -0.188664 + 1.389350I$ $a = -0.177107 + 1.219500I$ $b = -0.42888 + 1.77705I$	$-3.06032 - 9.15441I$	0
$u = -0.188664 - 1.389350I$ $a = -0.177107 - 1.219500I$ $b = -0.42888 - 1.77705I$	$-3.06032 + 9.15441I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.526193 + 0.244659I$		
$a = 1.331340 - 0.219705I$	$1.090210 - 0.801985I$	$5.31856 + 2.50411I$
$b = 0.414062 + 0.073402I$		
$u = -0.526193 - 0.244659I$		
$a = 1.331340 + 0.219705I$	$1.090210 + 0.801985I$	$5.31856 - 2.50411I$
$b = 0.414062 - 0.073402I$		
$u = 0.406757 + 0.405711I$		
$a = -0.429280 - 1.280950I$	$-1.89883 - 1.20494I$	$-2.45244 - 0.57004I$
$b = -0.568191 - 0.723482I$		
$u = 0.406757 - 0.405711I$		
$a = -0.429280 + 1.280950I$	$-1.89883 + 1.20494I$	$-2.45244 + 0.57004I$
$b = -0.568191 + 0.723482I$		
$u = -0.17361 + 1.42113I$		
$a = -0.773205 - 0.392754I$	$-4.31361 - 3.27424I$	0
$b = -2.26968 - 0.26907I$		
$u = -0.17361 - 1.42113I$		
$a = -0.773205 + 0.392754I$	$-4.31361 + 3.27424I$	0
$b = -2.26968 + 0.26907I$		
$u = -0.08217 + 1.43290I$		
$a = 0.012161 + 0.479575I$	$-4.33040 - 2.95362I$	0
$b = 1.47788 - 1.81226I$		
$u = -0.08217 - 1.43290I$		
$a = 0.012161 - 0.479575I$	$-4.33040 + 2.95362I$	0
$b = 1.47788 + 1.81226I$		
$u = 0.369359 + 0.423465I$		
$a = 2.63371 + 0.41174I$	$-4.52529 + 0.64236I$	$-8.88416 - 5.33505I$
$b = 0.439230 + 0.012251I$		
$u = 0.369359 - 0.423465I$		
$a = 2.63371 - 0.41174I$	$-4.52529 - 0.64236I$	$-8.88416 + 5.33505I$
$b = 0.439230 - 0.012251I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.04013 + 1.43787I$		
$a = 0.368603 + 0.074688I$	$-7.42832 + 0.17125I$	0
$b = 3.17675 + 1.32808I$		
$u = 0.04013 - 1.43787I$		
$a = 0.368603 - 0.074688I$	$-7.42832 - 0.17125I$	0
$b = 3.17675 - 1.32808I$		
$u = 0.34785 + 1.41208I$		
$a = -0.798393 + 0.009874I$	$-7.81342 + 6.46103I$	0
$b = -1.51058 - 0.70211I$		
$u = 0.34785 - 1.41208I$		
$a = -0.798393 - 0.009874I$	$-7.81342 - 6.46103I$	0
$b = -1.51058 + 0.70211I$		
$u = 0.15166 + 1.45394I$		
$a = -1.341240 + 0.389661I$	$-10.59050 + 2.67643I$	0
$b = -3.44448 + 0.51105I$		
$u = 0.15166 - 1.45394I$		
$a = -1.341240 - 0.389661I$	$-10.59050 - 2.67643I$	0
$b = -3.44448 - 0.51105I$		
$u = 0.21401 + 1.44731I$		
$a = 1.165350 - 0.332979I$	$-7.38327 + 7.53531I$	0
$b = 3.24423 - 0.33629I$		
$u = 0.21401 - 1.44731I$		
$a = 1.165350 + 0.332979I$	$-7.38327 - 7.53531I$	0
$b = 3.24423 + 0.33629I$		
$u = -0.04327 + 1.46569I$		
$a = 0.612952 + 0.425075I$	$-7.08799 + 0.13600I$	0
$b = 2.22983 + 0.27823I$		
$u = -0.04327 - 1.46569I$		
$a = 0.612952 - 0.425075I$	$-7.08799 - 0.13600I$	0
$b = 2.22983 - 0.27823I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.514435 + 0.029790I$ $a = -0.62541 + 1.82321I$ $b = -0.248771 - 0.638119I$	$4.13023 - 2.87256I$	$2.80596 + 5.41221I$
$u = 0.514435 - 0.029790I$ $a = -0.62541 - 1.82321I$ $b = -0.248771 + 0.638119I$	$4.13023 + 2.87256I$	$2.80596 - 5.41221I$
$u = -0.189126 + 0.472524I$ $a = -1.170830 - 0.682908I$ $b = -1.90042 - 0.09678I$	$1.62783 - 1.86935I$	$-4.71859 + 9.09029I$
$u = -0.189126 - 0.472524I$ $a = -1.170830 + 0.682908I$ $b = -1.90042 + 0.09678I$	$1.62783 + 1.86935I$	$-4.71859 - 9.09029I$
$u = -0.33202 + 1.46447I$ $a = -0.812027 - 0.326676I$ $b = -2.22023 - 0.19560I$	$-1.27736 - 5.80994I$	0
$u = -0.33202 - 1.46447I$ $a = -0.812027 + 0.326676I$ $b = -2.22023 + 0.19560I$	$-1.27736 + 5.80994I$	0
$u = -0.282682 + 0.397129I$ $a = 1.30656 + 0.57839I$ $b = 2.05135 + 0.16180I$	$1.30774 + 3.73013I$	$-2.74021 + 5.37610I$
$u = -0.282682 - 0.397129I$ $a = 1.30656 - 0.57839I$ $b = 2.05135 - 0.16180I$	$1.30774 - 3.73013I$	$-2.74021 - 5.37610I$
$u = 0.30445 + 1.48923I$ $a = 0.995764 - 0.381668I$ $b = 3.00560 - 0.23025I$	$-4.57444 + 11.61720I$	0
$u = 0.30445 - 1.48923I$ $a = 0.995764 + 0.381668I$ $b = 3.00560 + 0.23025I$	$-4.57444 - 11.61720I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.464839 + 0.113252I$ $a = 0.27220 - 1.70926I$ $b = 0.123712 + 0.765459I$	$3.88141 + 3.13960I$	$1.64371 - 0.37863I$
$u = 0.464839 - 0.113252I$ $a = 0.27220 + 1.70926I$ $b = 0.123712 - 0.765459I$	$3.88141 - 3.13960I$	$1.64371 + 0.37863I$
$u = 0.23746 + 1.50791I$ $a = -1.085810 + 0.439549I$ $b = -3.05401 + 0.40388I$	$-12.1325 + 10.9448I$	0
$u = 0.23746 - 1.50791I$ $a = -1.085810 - 0.439549I$ $b = -3.05401 - 0.40388I$	$-12.1325 - 10.9448I$	0
$u = 0.08480 + 1.53234I$ $a = 0.596803 + 0.147459I$ $b = 2.21447 + 0.68075I$	$-7.40992 - 0.00114I$	0
$u = 0.08480 - 1.53234I$ $a = 0.596803 - 0.147459I$ $b = 2.21447 - 0.68075I$	$-7.40992 + 0.00114I$	0
$u = -0.22585 + 1.52169I$ $a = 0.765917 + 0.329597I$ $b = 2.21047 + 0.25037I$	$-8.11266 - 6.00339I$	0
$u = -0.22585 - 1.52169I$ $a = 0.765917 - 0.329597I$ $b = 2.21047 - 0.25037I$	$-8.11266 + 6.00339I$	0
$u = -0.34530 + 1.50016I$ $a = 0.808150 + 0.315217I$ $b = 2.20445 + 0.19663I$	$-2.24324 - 11.70050I$	0
$u = -0.34530 - 1.50016I$ $a = 0.808150 - 0.315217I$ $b = 2.20445 - 0.19663I$	$-2.24324 + 11.70050I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.31293 + 1.51066I$ $a = -0.979232 + 0.406327I$ $b = -2.95400 + 0.23722I$	$-5.7917 + 17.7278I$	0
$u = 0.31293 - 1.51066I$ $a = -0.979232 - 0.406327I$ $b = -2.95400 - 0.23722I$	$-5.7917 - 17.7278I$	0
$u = 0.24997 + 1.52779I$ $a = -0.716417 - 0.060866I$ $b = -1.78953 - 0.69898I$	$-11.99200 + 0.79354I$	0
$u = 0.24997 - 1.52779I$ $a = -0.716417 + 0.060866I$ $b = -1.78953 + 0.69898I$	$-11.99200 - 0.79354I$	0
$u = 0.13806 + 1.60905I$ $a = -0.679385 - 0.144169I$ $b = -2.01284 - 0.57418I$	$-8.37514 - 4.86967I$	0
$u = 0.13806 - 1.60905I$ $a = -0.679385 + 0.144169I$ $b = -2.01284 + 0.57418I$	$-8.37514 + 4.86967I$	0
$u = -0.313657$ $a = -5.14324$ $b = -0.161887$	$-2.86791$	11.2900
$u = 0.054224 + 0.273579I$ $a = -1.10118 - 1.39810I$ $b = -0.515038 + 0.369932I$	$-1.295400 + 0.319885I$	$-8.06448 + 0.00737I$
$u = 0.054224 - 0.273579I$ $a = -1.10118 + 1.39810I$ $b = -0.515038 - 0.369932I$	$-1.295400 - 0.319885I$	$-8.06448 - 0.00737I$
$u = -0.203756$ $a = 2.23736$ $b = 2.72642$	$-3.01291$	42.4150

$$\text{II. } I_2^u = \langle 9b^3 + 6b^2u + 3b^2 - 6b - 2u - 1, a, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -b \\ -bu \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2b^2u - b^2 + u \\ b^2u + 2b^2 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} bu + b \\ 2b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b^2u - b^2 - u \\ 4b^2u + 2b^2 - u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $17b^2u + 30b^2 + 11bu + b - 5u - 15$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_3$	$27(27u^6 - 27u^4 + 6u^2 + 1)$
$c_4$	$27(27u^6 - 27u^5 + 27u^4 - 18u^3 + 15u^2 - 6u + 1)$
$c_5$	$(u^3 - u^2 + 1)^2$
$c_6$	$(u^3 + u^2 + 2u + 1)^2$
$c_7, c_{12}$	$(u^2 - u + 1)^3$
$c_8, c_9, c_{10}$	$(u^2 + u + 1)^3$
$c_{11}$	$u^6$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_5$	$(y^3 - y^2 + 2y - 1)^2$
$c_3$	$729(27y^3 - 27y^2 + 6y + 1)^2$
$c_4$	$729(729y^6 + 729y^5 + 567y^4 + 216y^3 + 63y^2 - 6y + 1)$
$c_7, c_8, c_9$ $c_{10}, c_{12}$	$(y^2 + y + 1)^3$
$c_{11}$	$y^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$ $a = 0$ $b = 0.754678 - 0.124176I$	$3.02413 - 4.85801I$	$-0.04017 + 7.54626I$
$u = -0.500000 + 0.866025I$ $a = 0$ $b = -0.754678 - 0.124176I$	$3.02413 + 0.79824I$	$1.23319 + 1.22705I$
$u = -0.500000 + 0.866025I$ $a = 0$ $b = -0.328997I$	$-1.11345 - 2.02988I$	$-11.69302 - 4.44318I$
$u = -0.500000 - 0.866025I$ $a = 0$ $b = 0.754678 + 0.124176I$	$3.02413 + 4.85801I$	$-0.04017 - 7.54626I$
$u = -0.500000 - 0.866025I$ $a = 0$ $b = -0.754678 + 0.124176I$	$3.02413 - 0.79824I$	$1.23319 - 1.22705I$
$u = -0.500000 - 0.866025I$ $a = 0$ $b = 0.328997I$	$-1.11345 + 2.02988I$	$-11.69302 + 4.44318I$

$$\text{III. } I_3^u = \langle b + 1, 2a + u, u^2 + 2 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{2}u \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{3}{2}u + 1 \\ -2u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u + 1 \\ -u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{3}{2}u + 1 \\ -2u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{2}u \\ u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{2}u - 1 \\ u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_{10}$	$(u - 1)^2$
$c_3$	$u^2 - 2u + 3$
$c_4$	$u^2 + 2u + 3$
$c_5, c_6, c_7$ $c_{11}$	$(u + 1)^2$
$c_8, c_9, c_{12}$	$u^2 + 2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_7, c_{10}$ $c_{11}$	$(y - 1)^2$
$c_3, c_4$	$y^2 + 2y + 9$
$c_8, c_9, c_{12}$	$(y + 2)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$		$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$1.414210I$		
$a =$	$-0.707107I$	$-8.22467$	$-12.0000$
$b =$	$-1.00000$		
$u =$	$-1.414210I$		
$a =$	$0.707107I$	$-8.22467$	$-12.0000$
$b =$	$-1.00000$		

$$\text{IV. } I_1^v = \langle a, b - 1, v - 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_7$ $c_{11}$	$u - 1$
$c_3, c_4, c_5$ $c_6, c_{10}$	$u + 1$
$c_8, c_9, c_{12}$	$u$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_6$ $c_7, c_{10}, c_{11}$	$y - 1$
$c_8, c_9, c_{12}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$	-3.28987	-12.0000
$b = 1.00000$		

### V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^3)(u^3 - u^2 + 2u - 1)^2(u^{100} + 34u^{99} + \dots + 925u + 81)$
$c_2$	$((u-1)^3)(u^3 + u^2 - 1)^2(u^{100} + 6u^{99} + \dots + 59u + 9)$
$c_3$	$729(u+1)(u^2 - 2u + 3)(27u^6 - 27u^4 + 6u^2 + 1)$ $\cdot (27u^{100} - 234u^{99} + \dots - 3357967u - 461099)$
$c_4$	$729(u+1)(u^2 + 2u + 3)(27u^6 - 27u^5 + \dots - 6u + 1)$ $\cdot (27u^{100} + 45u^{99} + \dots - 4549965u + 518603)$
$c_5$	$((u+1)^3)(u^3 - u^2 + 1)^2(u^{100} + 6u^{99} + \dots + 59u + 9)$
$c_6$	$((u+1)^3)(u^3 + u^2 + 2u + 1)^2(u^{100} + 34u^{99} + \dots + 925u + 81)$
$c_7$	$(u-1)(u+1)^2(u^2 - u + 1)^3(u^{100} + 5u^{99} + \dots - 38u - 3)$
$c_8, c_9$	$u(u^2 + 2)(u^2 + u + 1)^3(u^{100} + 4u^{99} + \dots + 2u + 2)$
$c_{10}$	$((u-1)^2)(u+1)(u^2 + u + 1)^3(u^{100} + 5u^{99} + \dots - 38u - 3)$
$c_{11}$	$u^6(u-1)(u+1)^2(u^{100} - 4u^{99} + \dots - 12960u - 5184)$
$c_{12}$	$u(u^2 + 2)(u^2 - u + 1)^3(u^{100} + 4u^{99} + \dots + 2u + 2)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$((y-1)^3)(y^3 + 3y^2 + 2y - 1)^2(y^{100} + 70y^{99} + \dots - 377077y + 6561)$
$c_2, c_5$	$((y-1)^3)(y^3 - y^2 + 2y - 1)^2(y^{100} - 34y^{99} + \dots - 925y + 81)$
$c_3$	$531441(y-1)(y^2 + 2y + 9)(27y^3 - 27y^2 + 6y + 1)^2$ $\cdot (729y^{100} + 11502y^{99} + \dots - 1559280610721y + 212612287801)$
$c_4$	$531441(y-1)(y^2 + 2y + 9)$ $\cdot (729y^6 + 729y^5 + 567y^4 + 216y^3 + 63y^2 - 6y + 1)$ $\cdot (729y^{100} - 27135y^{99} + \dots - 3345262023807y + 268949071609)$
$c_7, c_{10}$	$((y-1)^3)(y^2 + y + 1)^3(y^{100} - 53y^{99} + \dots - 658y + 9)$
$c_8, c_9, c_{12}$	$y(y+2)^2(y^2 + y + 1)^3(y^{100} + 94y^{99} + \dots - 60y + 4)$
$c_{11}$	$y^6(y-1)^3(y^{100} + 32y^{99} + \dots + 4.14305 \times 10^8 y + 2.68739 \times 10^7)$