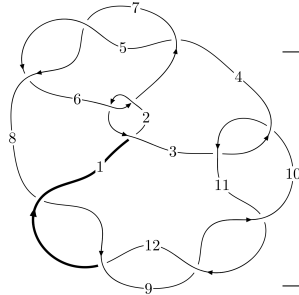
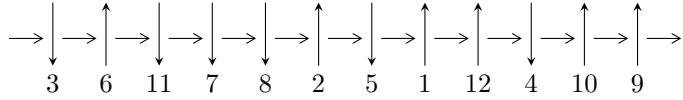


12a₀₄₆₃ (K12a₀₄₆₃)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3, 11 \xrightarrow{c_3} 4, 6 \xrightarrow{c_2} 2 \xrightarrow{c_6} 7 \xrightarrow{c_4} 5 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 10 \xrightarrow{c_{11}} 12 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \rightsquigarrow c_5, c_7, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{58} + 2u^{57} + \dots + b - 1, -u^{57} - u^{56} + \dots + a + 1, u^{59} + 2u^{58} + \dots - 2u - 1 \rangle$$

$$I_2^u = \langle b, -u^2 + a + u - 1, u^4 - u^3 + u^2 + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 63 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{58} + 2u^{57} + \dots + b - 1, -u^{57} - u^{56} + \dots + a + 1, u^{59} + 2u^{58} + \dots - 2u - 1 \rangle \quad \mathbf{I.}$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{57} + u^{56} + \dots + u - 1 \\ -u^{58} - 2u^{57} + \dots + u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^9 - 3u^5 - u \\ u^9 + u^7 + 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{57} - u^{56} + \dots + 3u^2 + 2u \\ u^{58} + 2u^{57} + \dots - 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{55} - u^{54} + \dots - u + 1 \\ u^{29} + 3u^{27} + \dots + 4u^2 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^7 + 2u^3 \\ u^9 + u^7 + 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 + u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^9 + 3u^5 + u \\ u^{11} + u^9 + 4u^7 + 3u^5 + 3u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $4u^{58} + 8u^{57} + \dots - 13u - 5$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|---|
| c_1 | $u^{59} + 27u^{58} + \dots - 1984u - 256$ |
| c_2, c_6 | $u^{59} - u^{58} + \dots - 56u + 16$ |
| c_3, c_{10} | $u^{59} + 2u^{58} + \dots - 2u - 1$ |
| c_4, c_5, c_7 | $u^{59} - 5u^{58} + \dots + 24u^2 + 1$ |
| c_8, c_9, c_{11} c_{12} | $u^{59} - 12u^{58} + \dots + 2u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1 | $y^{59} + 3y^{58} + \dots - 2207744y - 65536$ |
| c_2, c_6 | $y^{59} + 27y^{58} + \dots - 1984y - 256$ |
| c_3, c_{10} | $y^{59} + 12y^{58} + \dots + 2y - 1$ |
| c_4, c_5, c_7 | $y^{59} - 53y^{58} + \dots - 48y - 1$ |
| c_8, c_9, c_{11} c_{12} | $y^{59} + 72y^{58} + \dots + 50y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.343246 + 0.929430I$ | | |
| $a = 0.23393 + 2.03837I$ | $-2.90400 - 0.48534I$ | $-3.04622 - 0.93099I$ |
| $b = 0.385366 - 0.992201I$ | | |
| $u = -0.343246 - 0.929430I$ | | |
| $a = 0.23393 - 2.03837I$ | $-2.90400 + 0.48534I$ | $-3.04622 + 0.93099I$ |
| $b = 0.385366 + 0.992201I$ | | |
| $u = -0.530651 + 0.868709I$ | | |
| $a = -1.04989 + 1.47863I$ | $-3.01197 + 4.86238I$ | $-3.57054 - 6.43781I$ |
| $b = 0.958742 - 0.452365I$ | | |
| $u = -0.530651 - 0.868709I$ | | |
| $a = -1.04989 - 1.47863I$ | $-3.01197 - 4.86238I$ | $-3.57054 + 6.43781I$ |
| $b = 0.958742 + 0.452365I$ | | |
| $u = 0.512834 + 0.819534I$ | | |
| $a = -2.07477 - 1.14802I$ | $-2.20006 - 2.45590I$ | $-5.34282 + 5.82388I$ |
| $b = 0.344806 - 0.832765I$ | | |
| $u = 0.512834 - 0.819534I$ | | |
| $a = -2.07477 + 1.14802I$ | $-2.20006 + 2.45590I$ | $-5.34282 - 5.82388I$ |
| $b = 0.344806 + 0.832765I$ | | |
| $u = 0.517835 + 0.901720I$ | | |
| $a = 2.57194 + 0.49149I$ | $-0.05687 - 6.75762I$ | $0. + 9.22820I$ |
| $b = -0.571645 + 0.989887I$ | | |
| $u = 0.517835 - 0.901720I$ | | |
| $a = 2.57194 - 0.49149I$ | $-0.05687 + 6.75762I$ | $0. - 9.22820I$ |
| $b = -0.571645 - 0.989887I$ | | |
| $u = -0.431886 + 0.855275I$ | | |
| $a = 0.42205 - 1.46717I$ | $1.17445 + 2.04675I$ | $3.24024 - 3.82120I$ |
| $b = -0.622029 + 0.574005I$ | | |
| $u = -0.431886 - 0.855275I$ | | |
| $a = 0.42205 + 1.46717I$ | $1.17445 - 2.04675I$ | $3.24024 + 3.82120I$ |
| $b = -0.622029 - 0.574005I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.104023 + 0.946889I$ $a = -2.13002 - 1.92768I$ $b = 0.550439 + 1.057570I$ | $-1.60171 + 5.75877I$ | $0.24744 - 6.03089I$ |
| $u = -0.104023 - 0.946889I$ $a = -2.13002 + 1.92768I$ $b = 0.550439 - 1.057570I$ | $-1.60171 - 5.75877I$ | $0.24744 + 6.03089I$ |
| $u = 0.731988 + 0.763169I$ $a = 0.800342 + 0.062233I$ $b = -0.112548 + 1.197950I$ | $-9.65537 - 2.66883I$ | $-9.83468 + 3.25272I$ |
| $u = 0.731988 - 0.763169I$ $a = 0.800342 - 0.062233I$ $b = -0.112548 - 1.197950I$ | $-9.65537 + 2.66883I$ | $-9.83468 - 3.25272I$ |
| $u = 0.537997 + 0.944744I$ $a = -2.66911 - 0.07381I$ $b = 0.647369 - 1.158890I$ | $-5.25013 - 10.71760I$ | $-4.54465 + 9.45987I$ |
| $u = 0.537997 - 0.944744I$ $a = -2.66911 + 0.07381I$ $b = 0.647369 + 1.158890I$ | $-5.25013 + 10.71760I$ | $-4.54465 - 9.45987I$ |
| $u = -0.057586 + 0.882777I$ $a = 2.31101 + 1.39500I$ $b = -0.592455 - 0.810374I$ | $3.06980 + 2.34027I$ | $6.64897 - 4.48405I$ |
| $u = -0.057586 - 0.882777I$ $a = 2.31101 - 1.39500I$ $b = -0.592455 + 0.810374I$ | $3.06980 - 2.34027I$ | $6.64897 + 4.48405I$ |
| $u = 0.714820 + 0.495375I$ $a = 0.447234 - 0.136210I$ $b = -0.585668 - 1.188170I$ | $-6.70702 + 6.08853I$ | $-8.24622 - 3.55476I$ |
| $u = 0.714820 - 0.495375I$ $a = 0.447234 + 0.136210I$ $b = -0.585668 + 1.188170I$ | $-6.70702 - 6.08853I$ | $-8.24622 + 3.55476I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.566605 + 0.649388I$ $a = -0.266615 - 1.188520I$ $b = -0.124692 - 0.867050I$ | $-2.75909 - 1.65966I$ | $-8.41788 + 3.66504I$ |
| $u = 0.566605 - 0.649388I$ $a = -0.266615 + 1.188520I$ $b = -0.124692 + 0.867050I$ | $-2.75909 + 1.65966I$ | $-8.41788 - 3.66504I$ |
| $u = -0.611622 + 0.577390I$ $a = 1.131410 - 0.440626I$ $b = -0.956464 - 0.308436I$ | $-3.94508 - 0.54490I$ | $-6.77151 - 0.50771I$ |
| $u = -0.611622 - 0.577390I$ $a = 1.131410 + 0.440626I$ $b = -0.956464 + 0.308436I$ | $-3.94508 + 0.54490I$ | $-6.77151 + 0.50771I$ |
| $u = 0.629823 + 0.513947I$ $a = -0.474587 + 0.552020I$ $b = 0.472585 + 0.971110I$ | $-1.28323 + 2.43963I$ | $-4.50558 - 3.22204I$ |
| $u = 0.629823 - 0.513947I$ $a = -0.474587 - 0.552020I$ $b = 0.472585 - 0.971110I$ | $-1.28323 - 2.43963I$ | $-4.50558 + 3.22204I$ |
| $u = 0.050655 + 0.809073I$ $a = -2.80210 - 0.73123I$ $b = 0.654760 + 0.520162I$ | $0.057074 - 1.043030I$ | $3.86720 + 0.46567I$ |
| $u = 0.050655 - 0.809073I$ $a = -2.80210 + 0.73123I$ $b = 0.654760 - 0.520162I$ | $0.057074 + 1.043030I$ | $3.86720 - 0.46567I$ |
| $u = 0.802556 + 0.909873I$ $a = 0.645306 - 0.524552I$ $b = 0.073782 + 0.922649I$ | $-9.57681 - 3.00894I$ | 0 |
| $u = 0.802556 - 0.909873I$ $a = 0.645306 + 0.524552I$ $b = 0.073782 - 0.922649I$ | $-9.57681 + 3.00894I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $u = 0.878048 + 0.900066I$ $a = -0.608654 - 0.248494I$ $b = 0.743403 - 0.349469I$ | $-6.92983 - 1.93819I$ | 0 |
| $u = 0.878048 - 0.900066I$ $a = -0.608654 + 0.248494I$ $b = 0.743403 + 0.349469I$ | $-6.92983 + 1.93819I$ | 0 |
| $u = -0.908427 + 0.893152I$ $a = -0.394230 - 0.515132I$ $b = 0.548605 - 1.127370I$ | $-9.26800 - 2.97267I$ | 0 |
| $u = -0.908427 - 0.893152I$ $a = -0.394230 + 0.515132I$ $b = 0.548605 + 1.127370I$ | $-9.26800 + 2.97267I$ | 0 |
| $u = 0.862553 + 0.938272I$ $a = 0.210045 + 0.711663I$ $b = -0.759924 - 0.382114I$ | $-6.80919 - 4.50807I$ | 0 |
| $u = 0.862553 - 0.938272I$ $a = 0.210045 - 0.711663I$ $b = -0.759924 + 0.382114I$ | $-6.80919 + 4.50807I$ | 0 |
| $u = -0.350516 + 0.631281I$ $a = -0.830854 + 0.196340I$ $b = 0.379823 + 0.257914I$ | $0.162716 + 1.132970I$ | $2.90169 - 5.38040I$ |
| $u = -0.350516 - 0.631281I$ $a = -0.830854 - 0.196340I$ $b = 0.379823 - 0.257914I$ | $0.162716 - 1.132970I$ | $2.90169 + 5.38040I$ |
| $u = -0.922367 + 0.885921I$ $a = 0.414846 + 0.164365I$ $b = -0.69639 + 1.25575I$ | $-14.8968 - 7.2841I$ | 0 |
| $u = -0.922367 - 0.885921I$ $a = 0.414846 - 0.164365I$ $b = -0.69639 - 1.25575I$ | $-14.8968 + 7.2841I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.906516 + 0.902473I$ | | |
| $a = 0.880104 + 0.387890I$ | $-12.19390 + 0.69942I$ | 0 |
| $b = -1.146010 + 0.424597I$ | | |
| $u = 0.906516 - 0.902473I$ | | |
| $a = 0.880104 - 0.387890I$ | $-12.19390 - 0.69942I$ | 0 |
| $b = -1.146010 - 0.424597I$ | | |
| $u = -0.899151 + 0.910017I$ | | |
| $a = 0.012912 + 0.933912I$ | $-11.05620 + 2.06484I$ | 0 |
| $b = -0.290358 + 1.086540I$ | | |
| $u = -0.899151 - 0.910017I$ | | |
| $a = 0.012912 - 0.933912I$ | $-11.05620 - 2.06484I$ | 0 |
| $b = -0.290358 - 1.086540I$ | | |
| $u = -0.881614 + 0.946166I$ | | |
| $a = -1.35992 + 1.22851I$ | $-10.93940 + 4.50938I$ | 0 |
| $b = 0.320527 + 1.080930I$ | | |
| $u = -0.881614 - 0.946166I$ | | |
| $a = -1.35992 - 1.22851I$ | $-10.93940 - 4.50938I$ | 0 |
| $b = 0.320527 - 1.080930I$ | | |
| $u = 0.880655 + 0.955668I$ | | |
| $a = -0.445587 - 0.984412I$ | $-12.02220 - 7.29324I$ | 0 |
| $b = 1.141580 + 0.449582I$ | | |
| $u = 0.880655 - 0.955668I$ | | |
| $a = -0.445587 + 0.984412I$ | $-12.02220 + 7.29324I$ | 0 |
| $b = 1.141580 - 0.449582I$ | | |
| $u = -0.875312 + 0.962071I$ | | |
| $a = 1.78278 - 1.05080I$ | $-9.04599 + 9.55430I$ | 0 |
| $b = -0.569196 - 1.124490I$ | | |
| $u = -0.875312 - 0.962071I$ | | |
| $a = 1.78278 + 1.05080I$ | $-9.04599 - 9.55430I$ | 0 |
| $b = -0.569196 + 1.124490I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.913352 + 0.939543I$ $a = 0.829208 - 0.487224I$ $b = -0.01243 - 1.44915I$ | $-19.6434 + 3.3613I$ | 0 |
| $u = -0.913352 - 0.939543I$ $a = 0.829208 + 0.487224I$ $b = -0.01243 + 1.44915I$ | $-19.6434 - 3.3613I$ | 0 |
| $u = -0.877468 + 0.975151I$ $a = -1.93743 + 0.83023I$ $b = 0.71000 + 1.24590I$ | $-14.6076 + 13.9156I$ | 0 |
| $u = -0.877468 - 0.975151I$ $a = -1.93743 - 0.83023I$ $b = 0.71000 - 1.24590I$ | $-14.6076 - 13.9156I$ | 0 |
| $u = -0.626785 + 0.171888I$ $a = 0.501490 - 0.081895I$ $b = -0.432777 - 1.116070I$ | $-5.26927 + 3.82540I$ | $-8.88049 - 3.82555I$ |
| $u = -0.626785 - 0.171888I$ $a = 0.501490 + 0.081895I$ $b = -0.432777 + 1.116070I$ | $-5.26927 - 3.82540I$ | $-8.88049 + 3.82555I$ |
| $u = -0.424302 + 0.237848I$ $a = -0.692243 + 0.560199I$ $b = 0.363149 + 0.700644I$ | $-0.194105 + 1.203550I$ | $-3.60543 - 5.01021I$ |
| $u = -0.424302 - 0.237848I$ $a = -0.692243 - 0.560199I$ $b = 0.363149 - 0.700644I$ | $-0.194105 - 1.203550I$ | $-3.60543 + 5.01021I$ |
| $u = 0.330842$ $a = 2.08280$ $b = -0.644701$ | -2.22425 | -4.28740 |

$$\text{II. } I_2^u = \langle b, -u^2 + a + u - 1, u^4 - u^3 + u^2 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 - u + 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 - u + 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 - u + 2 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 \\ u^3 - u^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ -u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $3u^2 - 2u - 1$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------|--------------------------------|
| c_1, c_2, c_6 | u^4 |
| c_3 | $u^4 - u^3 + u^2 + 1$ |
| c_4, c_5 | $(u - 1)^4$ |
| c_7 | $(u + 1)^4$ |
| c_8, c_9 | $u^4 + u^3 + 3u^2 + 2u + 1$ |
| c_{10} | $u^4 + u^3 + u^2 + 1$ |
| c_{11}, c_{12} | $u^4 - u^3 + 3u^2 - 2u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|------------------------------------|
| c_1, c_2, c_6 | y^4 |
| c_3, c_{10} | $y^4 + y^3 + 3y^2 + 2y + 1$ |
| c_4, c_5, c_7 | $(y - 1)^4$ |
| c_8, c_9, c_{11} c_{12} | $y^4 + 5y^3 + 7y^2 + 2y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.351808 + 0.720342I$ | | |
| $a = 0.95668 - 1.22719I$ | $-1.43393 + 1.41510I$ | $-1.48175 - 2.96122I$ |
| $b = 0$ | | |
| $u = -0.351808 - 0.720342I$ | | |
| $a = 0.95668 + 1.22719I$ | $-1.43393 - 1.41510I$ | $-1.48175 + 2.96122I$ |
| $b = 0$ | | |
| $u = 0.851808 + 0.911292I$ | | |
| $a = 0.043315 + 0.641200I$ | $-8.43568 - 3.16396I$ | $-3.01825 + 2.83489I$ |
| $b = 0$ | | |
| $u = 0.851808 - 0.911292I$ | | |
| $a = 0.043315 - 0.641200I$ | $-8.43568 + 3.16396I$ | $-3.01825 - 2.83489I$ |
| $b = 0$ | | |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------------|---|
| c_1 | $u^4(u^{59} + 27u^{58} + \dots - 1984u - 256)$ |
| c_2, c_6 | $u^4(u^{59} - u^{58} + \dots - 56u + 16)$ |
| c_3 | $(u^4 - u^3 + u^2 + 1)(u^{59} + 2u^{58} + \dots - 2u - 1)$ |
| c_4, c_5 | $((u - 1)^4)(u^{59} - 5u^{58} + \dots + 24u^2 + 1)$ |
| c_7 | $((u + 1)^4)(u^{59} - 5u^{58} + \dots + 24u^2 + 1)$ |
| c_8, c_9 | $(u^4 + u^3 + 3u^2 + 2u + 1)(u^{59} - 12u^{58} + \dots + 2u + 1)$ |
| c_{10} | $(u^4 + u^3 + u^2 + 1)(u^{59} + 2u^{58} + \dots - 2u - 1)$ |
| c_{11}, c_{12} | $(u^4 - u^3 + 3u^2 - 2u + 1)(u^{59} - 12u^{58} + \dots + 2u + 1)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1 | $y^4(y^{59} + 3y^{58} + \dots - 2207744y - 65536)$ |
| c_2, c_6 | $y^4(y^{59} + 27y^{58} + \dots - 1984y - 256)$ |
| c_3, c_{10} | $(y^4 + y^3 + 3y^2 + 2y + 1)(y^{59} + 12y^{58} + \dots + 2y - 1)$ |
| c_4, c_5, c_7 | $((y - 1)^4)(y^{59} - 53y^{58} + \dots - 48y - 1)$ |
| c_8, c_9, c_{11} c_{12} | $(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^{59} + 72y^{58} + \dots + 50y - 1)$ |