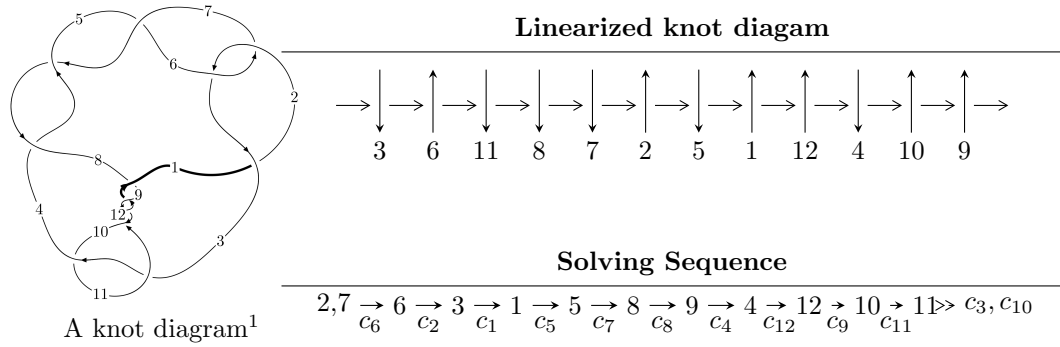


12a₀₄₇₁ (K12a₀₄₇₁)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{40} + 2u^{39} + \dots + 4u + 1 \rangle$$

$$I_2^u = \langle u^2 - u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 42 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{40} + 2u^{39} + \dots + 4u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{12} - u^{10} - 3u^8 - 2u^6 + u^2 + 1 \\ -u^{14} - 2u^{12} - 5u^{10} - 6u^8 - 6u^6 - 2u^4 - u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^6 + u^4 + 2u^2 + 1 \\ u^6 + u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{21} + 2u^{19} + 7u^{17} + 10u^{15} + 14u^{13} + 12u^{11} + 5u^9 - 2u^7 - 5u^5 - 2u^3 - u \\ u^{23} + 3u^{21} + \dots + 2u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{30} - 3u^{28} + \dots + 2u^2 + 1 \\ -u^{32} - 4u^{30} + \dots - 6u^4 - 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{39} + 4u^{37} + \dots - 6u^3 - 2u \\ 3u^{39} + 4u^{38} + \dots + 8u + 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $8u^{39} + 12u^{38} + \dots + 48u + 14$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|-------------------------------------|
| c_1, c_4, c_5 c_7 | $u^{40} + 8u^{39} + \dots + 4u + 1$ |
| c_2, c_6 | $u^{40} - 2u^{39} + \dots - 4u + 1$ |
| c_3, c_{10} | $u^{40} + 2u^{39} + \dots + 4u + 1$ |
| c_8, c_9, c_{11} c_{12} | $u^{40} - 8u^{39} + \dots - 4u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--|---------------------------------------|
| c_1, c_4, c_5 c_7, c_8, c_9 c_{11}, c_{12} | $y^{40} + 48y^{39} + \dots + 52y + 1$ |
| c_2, c_3, c_6 c_{10} | $y^{40} + 8y^{39} + \dots + 4y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.007642 + 0.966456I$ | $-11.28980 - 3.26800I$ | $-8.22072 + 2.51230I$ |
| $u = -0.007642 - 0.966456I$ | $-11.28980 + 3.26800I$ | $-8.22072 - 2.51230I$ |
| $u = -0.455339 + 0.953830I$ | $-8.76382 - 2.08770I$ | $-4.31619 + 3.32105I$ |
| $u = -0.455339 - 0.953830I$ | $-8.76382 + 2.08770I$ | $-4.31619 - 3.32105I$ |
| $u = -0.424765 + 0.837410I$ | $-1.06965 - 2.01513I$ | $-4.12618 + 3.84559I$ |
| $u = -0.424765 - 0.837410I$ | $-1.06965 + 2.01513I$ | $-4.12618 - 3.84559I$ |
| $u = 0.468864 + 0.955282I$ | $-8.59119 + 8.60337I$ | $-3.84612 - 8.10725I$ |
| $u = 0.468864 - 0.955282I$ | $-8.59119 - 8.60337I$ | $-3.84612 + 8.10725I$ |
| $u = 0.547826 + 0.720762I$ | $2.87673 + 2.07761I$ | $8.03109 - 4.87367I$ |
| $u = 0.547826 - 0.720762I$ | $2.87673 - 2.07761I$ | $8.03109 + 4.87367I$ |
| $u = -0.054899 + 0.842893I$ | $-2.87673 - 2.07761I$ | $-8.03109 + 4.87367I$ |
| $u = -0.054899 - 0.842893I$ | $-2.87673 + 2.07761I$ | $-8.03109 - 4.87367I$ |
| $u = 0.675982 + 0.376953I$ | $-6.76036 - 4.39632I$ | $0.35650 + 2.56566I$ |
| $u = 0.675982 - 0.376953I$ | $-6.76036 + 4.39632I$ | $0.35650 - 2.56566I$ |
| $u = 0.570879 + 0.520043I$ | $1.06965 - 2.01513I$ | $4.12618 + 3.84559I$ |
| $u = 0.570879 - 0.520043I$ | $1.06965 + 2.01513I$ | $4.12618 - 3.84559I$ |
| $u = 0.897344 + 0.861664I$ | $0.784836I$ | $0. - 2.11264I$ |
| $u = 0.897344 - 0.861664I$ | $- 0.784836I$ | $0. + 2.11264I$ |
| $u = -0.666629 + 0.352689I$ | $-6.87304 - 2.02249I$ | $0.14883 + 2.38441I$ |
| $u = -0.666629 - 0.352689I$ | $-6.87304 + 2.02249I$ | $0.14883 - 2.38441I$ |
| $u = -0.903766 + 0.864696I$ | $0.34673 + 5.67431I$ | $0.59636 - 2.67543I$ |
| $u = -0.903766 - 0.864696I$ | $0.34673 - 5.67431I$ | $0.59636 + 2.67543I$ |
| $u = 0.873303 + 0.899277I$ | $6.87304 + 2.02249I$ | $0. - 2.38441I$ |
| $u = 0.873303 - 0.899277I$ | $6.87304 - 2.02249I$ | $0. + 2.38441I$ |
| $u = -0.893753 + 0.895948I$ | $8.76382 + 2.08770I$ | $4.31619 - 3.32105I$ |
| $u = -0.893753 - 0.895948I$ | $8.76382 - 2.08770I$ | $4.31619 + 3.32105I$ |
| $u = 0.858890 + 0.934946I$ | $6.76036 + 4.39632I$ | $0. - 2.56566I$ |
| $u = 0.858890 - 0.934946I$ | $6.76036 - 4.39632I$ | $0. + 2.56566I$ |
| $u = -0.350675 + 0.633429I$ | $-0.162533 - 1.134740I$ | $-3.04903 + 5.46701I$ |
| $u = -0.350675 - 0.633429I$ | $-0.162533 + 1.134740I$ | $-3.04903 - 5.46701I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.884538 + 0.925182I$ | $11.28980 - 3.26800I$ | $8.22072 + 2.51230I$ |
| $u = -0.884538 - 0.925182I$ | $11.28980 + 3.26800I$ | $8.22072 - 2.51230I$ |
| $u = -0.869391 + 0.950001I$ | $8.59119 - 8.60337I$ | $3.84612 + 8.10725I$ |
| $u = -0.869391 - 0.950001I$ | $8.59119 + 8.60337I$ | $3.84612 - 8.10725I$ |
| $u = 0.849710 + 0.970863I$ | $-0.34673 + 5.67431I$ | $0. - 2.67543I$ |
| $u = 0.849710 - 0.970863I$ | $-0.34673 - 5.67431I$ | $0. + 2.67543I$ |
| $u = -0.854577 + 0.973346I$ | $-12.1697I$ | $0. + 7.37185I$ |
| $u = -0.854577 - 0.973346I$ | $12.1697I$ | $0. - 7.37185I$ |
| $u = -0.376823 + 0.254532I$ | $0.162533 - 1.134740I$ | $3.04903 + 5.46701I$ |
| $u = -0.376823 - 0.254532I$ | $0.162533 + 1.134740I$ | $3.04903 - 5.46701I$ |

$$\text{II. } I_2^u = \langle u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2u + 1 \\ -u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2u + 2 \\ -u + 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-12u + 6$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---|--------------------------------|
| c_1, c_2, c_4 c_5, c_6, c_7 | $u^2 + u + 1$ |
| c_3, c_8, c_9 c_{10}, c_{11}, c_{12} | $u^2 - u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|------------------------------------|
| c_1, c_2, c_3 | |
| c_4, c_5, c_6 | $y^2 + y + 1$ |
| c_7, c_8, c_9 | |
| c_{10}, c_{11}, c_{12} | |

(vi) Complex Volumes and Cusp Shapes

| | Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------|------------------------|---------------------------------------|------------------|
| $u =$ | $0.500000 + 0.866025I$ | $6.08965I$ | $0. - 10.39230I$ |
| $u =$ | $0.500000 - 0.866025I$ | $- 6.08965I$ | $0. + 10.39230I$ |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_4, c_5 c_7 | $(u^2 + u + 1)(u^{40} + 8u^{39} + \dots + 4u + 1)$ |
| c_2, c_6 | $(u^2 + u + 1)(u^{40} - 2u^{39} + \dots - 4u + 1)$ |
| c_3, c_{10} | $(u^2 - u + 1)(u^{40} + 2u^{39} + \dots + 4u + 1)$ |
| c_8, c_9, c_{11} c_{12} | $(u^2 - u + 1)(u^{40} - 8u^{39} + \dots - 4u + 1)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--|---|
| c_1, c_4, c_5 c_7, c_8, c_9 c_{11}, c_{12} | $(y^2 + y + 1)(y^{40} + 48y^{39} + \cdots + 52y + 1)$ |
| c_2, c_3, c_6 c_{10} | $(y^2 + y + 1)(y^{40} + 8y^{39} + \cdots + 4y + 1)$ |