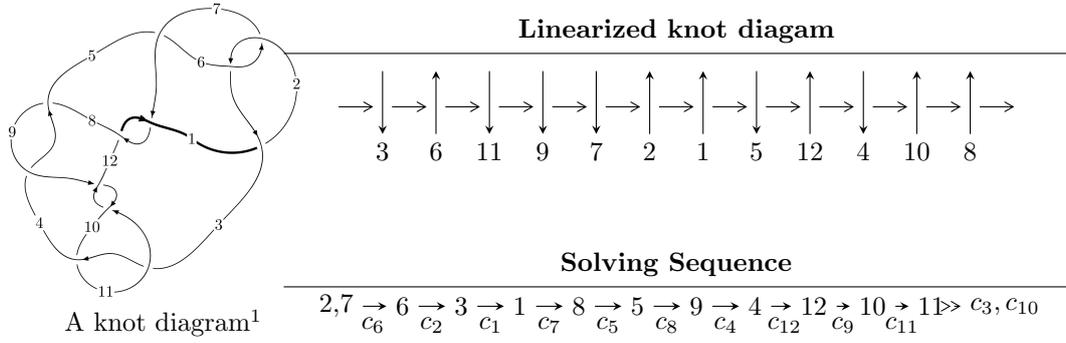


12a<sub>0477</sub> (K12a<sub>0477</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{84} + u^{83} + \dots + 2u + 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 84 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle u^{84} + u^{83} + \cdots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ -u^{10} - 2u^8 - 3u^6 - 2u^4 - u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{14} + 3u^{12} + 6u^{10} + 7u^8 + 6u^6 + 4u^4 + 2u^2 + 1 \\ u^{14} + 2u^{12} + 3u^{10} + 2u^8 - u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{26} + 5u^{24} + \cdots + 3u^2 + 1 \\ u^{26} + 4u^{24} + \cdots - 2u^4 + u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{13} + 2u^{11} + 3u^9 + 2u^7 - u \\ u^{15} + 3u^{13} + 6u^{11} + 7u^9 + 6u^7 + 4u^5 + 2u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{42} - 7u^{40} + \cdots + 3u^2 + 1 \\ -u^{44} - 8u^{42} + \cdots - 5u^4 - 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{71} + 12u^{69} + \cdots - 6u^3 - 2u \\ u^{73} + 13u^{71} + \cdots + 4u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^{83} + 56u^{81} + \cdots + 16u + 2$

(iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing       |
|---------------|--------------------------------------|
| $c_1, c_5$    | $u^{84} + 29u^{83} + \dots + 6u + 1$ |
| $c_2, c_6$    | $u^{84} - u^{83} + \dots - 2u + 1$   |
| $c_3, c_{10}$ | $u^{84} + u^{83} + \dots + 2u + 1$   |
| $c_4, c_8$    | $u^{84} - 5u^{83} + \dots - 4u + 1$  |
| $c_7, c_{12}$ | $u^{84} + 5u^{83} + \dots + 4u + 1$  |
| $c_9, c_{11}$ | $u^{84} - 29u^{83} + \dots - 6u + 1$ |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing     |
|-----------------------------|--|
| $c_1, c_5, c_9$<br>$c_{11}$ | $y^{84} + 53y^{83} + \cdots + 66y + 1$ |
| $c_2, c_3, c_6$<br>$c_{10}$ | $y^{84} + 29y^{83} + \cdots + 6y + 1$  |
| $c_4, c_7, c_8$<br>$c_{12}$ | $y^{84} + 49y^{83} + \cdots - 62y + 1$ |

(vi) Complex Volumes and Cusp Shapes

|       | Solutions to $I_1^u$    | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-------|-------------------------|---------------------------------------|-----------------------|
| $u =$ | $0.763893 + 0.642507I$  | $1.33433 - 2.60412I$                  | 0                     |
| $u =$ | $0.763893 - 0.642507I$  | $1.33433 + 2.60412I$                  | 0                     |
| $u =$ | $0.792082 + 0.624713I$  | $-5.01747I$                           | 0                     |
| $u =$ | $0.792082 - 0.624713I$  | $5.01747I$                            | 0                     |
| $u =$ | $0.710184 + 0.689350I$  | $1.67480 - 2.05474I$                  | 0                     |
| $u =$ | $0.710184 - 0.689350I$  | $1.67480 + 2.05474I$                  | 0                     |
| $u =$ | $0.476640 + 0.893687I$  | $-0.79843 + 7.36772I$                 | 0                     |
| $u =$ | $0.476640 - 0.893687I$  | $-0.79843 - 7.36772I$                 | 0                     |
| $u =$ | $-0.798874 + 0.626987I$ | $1.22047 + 10.61460I$                 | 0                     |
| $u =$ | $-0.798874 - 0.626987I$ | $1.22047 - 10.61460I$                 | 0                     |
| $u =$ | $0.072967 + 1.014750I$  | $-2.95072 - 2.15409I$                 | 0                     |
| $u =$ | $0.072967 - 1.014750I$  | $-2.95072 + 2.15409I$                 | 0                     |
| $u =$ | $-0.789993 + 0.643641I$ | $6.04939 + 4.33772I$                  | 0                     |
| $u =$ | $-0.789993 - 0.643641I$ | $6.04939 - 4.33772I$                  | 0                     |
| $u =$ | $-0.773008 + 0.666465I$ | $2.86621 - 2.05200I$                  | 0                     |
| $u =$ | $-0.773008 - 0.666465I$ | $2.86621 + 2.05200I$                  | 0                     |
| $u =$ | $-0.454631 + 0.853158I$ | $-1.67480 - 2.05474I$                 | 0                     |
| $u =$ | $-0.454631 - 0.853158I$ | $-1.67480 + 2.05474I$                 | 0                     |
| $u =$ | $0.643313 + 0.822859I$  | $3.24509 + 2.47363I$                  | 0                     |
| $u =$ | $0.643313 - 0.822859I$  | $3.24509 - 2.47363I$                  | 0                     |
| $u =$ | $-0.047485 + 1.060200I$ | $-4.39822 - 2.11638I$                 | 0                     |
| $u =$ | $-0.047485 - 1.060200I$ | $-4.39822 + 2.11638I$                 | 0                     |
| $u =$ | $0.079203 + 1.069310I$  | $3.88417I$                            | 0                     |
| $u =$ | $0.079203 - 1.069310I$  | $-3.88417I$                           | 0                     |
| $u =$ | $0.731757 + 0.564908I$  | $-4.05942 - 3.96631I$                 | $-2.91590 + 3.49131I$ |
| $u =$ | $0.731757 - 0.564908I$  | $-4.05942 + 3.96631I$                 | $-2.91590 - 3.49131I$ |
| $u =$ | $-0.067639 + 1.089980I$ | $-6.04939 - 4.33772I$                 | 0                     |
| $u =$ | $-0.067639 - 1.089980I$ | $-6.04939 + 4.33772I$                 | 0                     |
| $u =$ | $0.074978 + 1.092560I$  | $-4.90631 + 9.94933I$                 | 0                     |
| $u =$ | $0.074978 - 1.092560I$  | $-4.90631 - 9.94933I$                 | 0                     |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.716193 + 0.552263I$ | $-4.16451 - 1.63916I$                 | $-3.30737 + 2.61534I$ |
| $u = -0.716193 - 0.552263I$ | $-4.16451 + 1.63916I$                 | $-3.30737 - 2.61534I$ |
| $u = -0.005011 + 1.096860I$ | $-9.54569 - 2.83875I$                 | 0                     |
| $u = -0.005011 - 1.096860I$ | $-9.54569 + 2.83875I$                 | 0                     |
| $u = -0.587223 + 0.661375I$ | $0.139076 - 1.080380I$                | $-2.54390 + 3.63061I$ |
| $u = -0.587223 - 0.661375I$ | $0.139076 + 1.080380I$                | $-2.54390 - 3.63061I$ |
| $u = 0.741950 + 0.844828I$  | $4.16451 + 1.63916I$                  | 0                     |
| $u = 0.741950 - 0.844828I$  | $4.16451 - 1.63916I$                  | 0                     |
| $u = 0.588860 + 0.964530I$  | $2.95072 + 2.15409I$                  | 0                     |
| $u = 0.588860 - 0.964530I$  | $2.95072 - 2.15409I$                  | 0                     |
| $u = -0.754193 + 0.844225I$ | $5.52875 + 3.59746I$                  | 0                     |
| $u = -0.754193 - 0.844225I$ | $5.52875 - 3.59746I$                  | 0                     |
| $u = -0.082243 + 0.852291I$ | $-3.24509 - 2.47363I$                 | $-6.54650 + 4.35842I$ |
| $u = -0.082243 - 0.852291I$ | $-3.24509 + 2.47363I$                 | $-6.54650 - 4.35842I$ |
| $u = -0.751026 + 0.864969I$ | $9.54569 - 2.83875I$                  | 0                     |
| $u = -0.751026 - 0.864969I$ | $9.54569 + 2.83875I$                  | 0                     |
| $u = 0.736347 + 0.879595I$  | $4.05942 + 3.96631I$                  | 0                     |
| $u = 0.736347 - 0.879595I$  | $4.05942 - 3.96631I$                  | 0                     |
| $u = -0.745804 + 0.884079I$ | $5.40777 - 9.26844I$                  | 0                     |
| $u = -0.745804 - 0.884079I$ | $5.40777 + 9.26844I$                  | 0                     |
| $u = 0.585015 + 1.007660I$  | $-1.83509 - 3.51182I$                 | 0                     |
| $u = 0.585015 - 1.007660I$  | $-1.83509 + 3.51182I$                 | 0                     |
| $u = -0.595485 + 1.007220I$ | $-2.86621 - 2.05200I$                 | 0                     |
| $u = -0.595485 - 1.007220I$ | $-2.86621 + 2.05200I$                 | 0                     |
| $u = -0.632358 + 0.991826I$ | $-0.88505 - 3.85213I$                 | 0                     |
| $u = -0.632358 - 0.991826I$ | $-0.88505 + 3.85213I$                 | 0                     |
| $u = 0.669522 + 0.981184I$  | $0.79843 + 7.36772I$                  | 0                     |
| $u = 0.669522 - 0.981184I$  | $0.79843 - 7.36772I$                  | 0                     |
| $u = -0.647306 + 1.029130I$ | $-5.52875 - 3.59746I$                 | 0                     |
| $u = -0.647306 - 1.029130I$ | $-5.52875 + 3.59746I$                 | 0                     |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.654058 + 1.030900I$  | $-5.40777 + 9.26844I$                 | 0                     |
| $u = 0.654058 - 1.030900I$  | $-5.40777 - 9.26844I$                 | 0                     |
| $u = -0.694389 + 1.008940I$ | $1.83509 - 3.51182I$                  | 0                     |
| $u = -0.694389 - 1.008940I$ | $1.83509 + 3.51182I$                  | 0                     |
| $u = 0.685026 + 1.017620I$  | $0.21279 + 8.11285I$                  | 0                     |
| $u = 0.685026 - 1.017620I$  | $0.21279 - 8.11285I$                  | 0                     |
| $u = -0.695652 + 1.024070I$ | $4.90631 - 9.94933I$                  | 0                     |
| $u = -0.695652 - 1.024070I$ | $4.90631 + 9.94933I$                  | 0                     |
| $u = 0.690563 + 1.032180I$  | $-1.22047 + 10.61460I$                | 0                     |
| $u = 0.690563 - 1.032180I$  | $-1.22047 - 10.61460I$                | 0                     |
| $u = -0.693816 + 1.033570I$ | $-16.2411I$                           | 0                     |
| $u = -0.693816 - 1.033570I$ | $16.2411I$                            | 0                     |
| $u = 0.638274 + 0.365821I$  | $-0.21279 + 8.11285I$                 | $1.45002 - 7.51274I$  |
| $u = 0.638274 - 0.365821I$  | $-0.21279 - 8.11285I$                 | $1.45002 + 7.51274I$  |
| $u = -0.623404 + 0.388000I$ | $-1.33433 - 2.60412I$                 | $-0.71892 + 2.81283I$ |
| $u = -0.623404 - 0.388000I$ | $-1.33433 + 2.60412I$                 | $-0.71892 - 2.81283I$ |
| $u = 0.585335 + 0.317246I$  | $4.39822 + 2.11638I$                  | $7.22959 - 3.54257I$  |
| $u = 0.585335 - 0.317246I$  | $4.39822 - 2.11638I$                  | $7.22959 + 3.54257I$  |
| $u = 0.540814 + 0.224283I$  | $0.88505 - 3.85213I$                  | $3.84909 + 2.49398I$  |
| $u = 0.540814 - 0.224283I$  | $0.88505 + 3.85213I$                  | $3.84909 - 2.49398I$  |
| $u = -0.353189 + 0.381764I$ | $-0.971383I$                          | $0. + 6.39452I$       |
| $u = -0.353189 - 0.381764I$ | $0.971383I$                           | $0. - 6.39452I$       |
| $u = -0.451862 + 0.205211I$ | $-0.139076 - 1.080380I$               | $2.54390 + 3.63061I$  |
| $u = -0.451862 - 0.205211I$ | $-0.139076 + 1.080380I$               | $2.54390 - 3.63061I$  |

## II. u-Polynomials

| Crossings     | u-Polynomials at each crossing       |
|---------------|--------------------------------------|
| $c_1, c_5$    | $u^{84} + 29u^{83} + \dots + 6u + 1$ |
| $c_2, c_6$    | $u^{84} - u^{83} + \dots - 2u + 1$   |
| $c_3, c_{10}$ | $u^{84} + u^{83} + \dots + 2u + 1$   |
| $c_4, c_8$    | $u^{84} - 5u^{83} + \dots - 4u + 1$  |
| $c_7, c_{12}$ | $u^{84} + 5u^{83} + \dots + 4u + 1$  |
| $c_9, c_{11}$ | $u^{84} - 29u^{83} + \dots - 6u + 1$ |

### III. Riley Polynomials

| Crossings                   | Riley Polynomials at each crossing    |
|-----------------------------|---------------------------------------|
| $c_1, c_5, c_9$<br>$c_{11}$ | $y^{84} + 53y^{83} + \dots + 66y + 1$ |
| $c_2, c_3, c_6$<br>$c_{10}$ | $y^{84} + 29y^{83} + \dots + 6y + 1$  |
| $c_4, c_7, c_8$<br>$c_{12}$ | $y^{84} + 49y^{83} + \dots - 62y + 1$ |