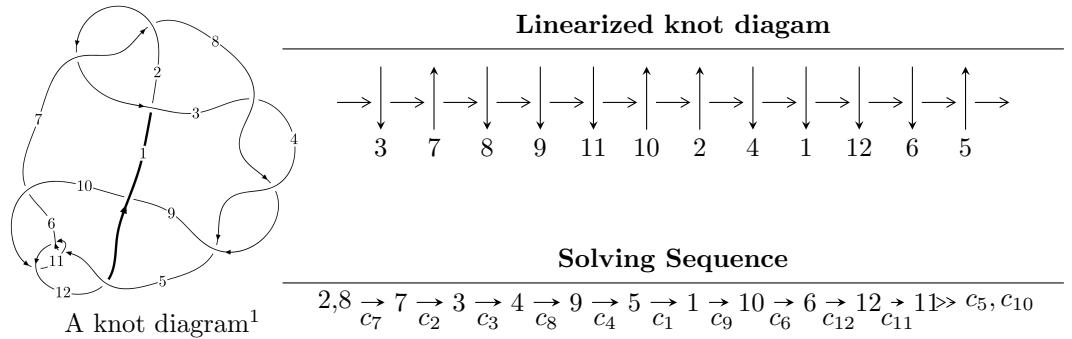


$12a_{0517}$  ( $K12a_{0517}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$I_1^u = \langle u^{72} - u^{71} + \cdots + 2u - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 72 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I.} \quad I_1^u = \langle u^{72} - u^{71} + \cdots + 2u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned}
a_2 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\
a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\
a_4 &= \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix} \\
a_9 &= \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix} \\
a_5 &= \begin{pmatrix} u^9 + 2u^7 + u^5 - 2u^3 - u \\ -u^9 - 3u^7 - 3u^5 + u \end{pmatrix} \\
a_1 &= \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix} \\
a_{10} &= \begin{pmatrix} -u^{14} - 3u^{12} - 4u^{10} - u^8 + 1 \\ -u^{16} - 4u^{14} - 8u^{12} - 8u^{10} - 4u^8 + 2u^6 + 4u^4 + 2u^2 \end{pmatrix} \\
a_6 &= \begin{pmatrix} u^{28} + 7u^{26} + \cdots + u^2 + 1 \\ u^{30} + 8u^{28} + \cdots + 2u^4 + u^2 \end{pmatrix} \\
a_{12} &= \begin{pmatrix} -u^{23} - 6u^{21} - 16u^{19} - 20u^{17} - 4u^{15} + 22u^{13} + 26u^{11} + 6u^9 - 9u^7 - 6u^5 \\ u^{23} + 7u^{21} + \cdots + 2u^3 + u \end{pmatrix} \\
a_{11} &= \begin{pmatrix} u^{62} + 17u^{60} + \cdots - 6u^6 + 1 \\ -u^{62} - 18u^{60} + \cdots + 8u^4 + 3u^2 \end{pmatrix}
\end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $4u^{70} - 4u^{69} + \cdots + 8u - 10$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{72} + 41u^{71} + \cdots - 10u^2 + 1$
$c_2, c_7$	$u^{72} + u^{71} + \cdots - 2u - 1$
$c_3, c_4, c_8$	$u^{72} - u^{71} + \cdots + 42u - 17$
$c_5, c_{11}$	$u^{72} - u^{71} + \cdots + 2u^3 - 1$
$c_6, c_{12}$	$u^{72} - 3u^{71} + \cdots - 18u + 3$
$c_9$	$u^{72} - 11u^{71} + \cdots - 18764u + 1889$
$c_{10}$	$u^{72} + 39u^{71} + \cdots - 2u^2 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{72} - 19y^{71} + \cdots - 20y + 1$
$c_2, c_7$	$y^{72} + 41y^{71} + \cdots - 10y^2 + 1$
$c_3, c_4, c_8$	$y^{72} - 79y^{71} + \cdots - 10740y + 289$
$c_5, c_{11}$	$y^{72} - 39y^{71} + \cdots - 2y^2 + 1$
$c_6, c_{12}$	$y^{72} + 61y^{71} + \cdots - 624y + 9$
$c_9$	$y^{72} - 31y^{71} + \cdots - 2222228y + 3568321$
$c_{10}$	$y^{72} - 11y^{71} + \cdots - 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.439849 + 0.927313I$	$0.59296 - 2.15388I$	$0. + 3.34635I$
$u = -0.439849 - 0.927313I$	$0.59296 + 2.15388I$	$0. - 3.34635I$
$u = 0.127748 + 0.947194I$	$-2.02452 - 1.35976I$	$-10.77685 + 3.46053I$
$u = 0.127748 - 0.947194I$	$-2.02452 + 1.35976I$	$-10.77685 - 3.46053I$
$u = -0.351185 + 0.866043I$	$-0.38120 - 1.62589I$	$-2.66925 + 4.11942I$
$u = -0.351185 - 0.866043I$	$-0.38120 + 1.62589I$	$-2.66925 - 4.11942I$
$u = 0.461087 + 0.962460I$	$0.08467 + 6.28501I$	0
$u = 0.461087 - 0.962460I$	$0.08467 - 6.28501I$	0
$u = 0.344819 + 1.019280I$	$-3.62015 + 2.92141I$	0
$u = 0.344819 - 1.019280I$	$-3.62015 - 2.92141I$	0
$u = 0.206282 + 1.082360I$	$-4.82312 - 0.17742I$	0
$u = 0.206282 - 1.082360I$	$-4.82312 + 0.17742I$	0
$u = 0.456210 + 0.765907I$	$-3.17229 - 2.09595I$	$-5.70344 - 0.42832I$
$u = 0.456210 - 0.765907I$	$-3.17229 + 2.09595I$	$-5.70344 + 0.42832I$
$u = -0.189472 + 1.099100I$	$-8.15714 + 4.74025I$	0
$u = -0.189472 - 1.099100I$	$-8.15714 - 4.74025I$	0
$u = 0.882022 + 0.044279I$	$-11.98020 - 0.80891I$	$-10.79930 - 0.35413I$
$u = 0.882022 - 0.044279I$	$-11.98020 + 0.80891I$	$-10.79930 + 0.35413I$
$u = 0.879727 + 0.056445I$	$-11.1703 - 9.8634I$	$-9.53343 + 5.93137I$
$u = 0.879727 - 0.056445I$	$-11.1703 + 9.8634I$	$-9.53343 - 5.93137I$
$u = -0.875707 + 0.050791I$	$-7.91972 + 4.99528I$	$-6.55693 - 2.82964I$
$u = -0.875707 - 0.050791I$	$-7.91972 - 4.99528I$	$-6.55693 + 2.82964I$
$u = -0.225561 + 1.101690I$	$-8.49214 - 4.06217I$	0
$u = -0.225561 - 1.101690I$	$-8.49214 + 4.06217I$	0
$u = 0.474807 + 1.020050I$	$-2.88869 + 6.40679I$	0
$u = 0.474807 - 1.020050I$	$-2.88869 - 6.40679I$	0
$u = -0.489288 + 1.023920I$	$-5.98929 - 11.10170I$	0
$u = -0.489288 - 1.023920I$	$-5.98929 + 11.10170I$	0
$u = -0.862003$	$-7.62273$	$-11.5620$
$u = -0.467805 + 1.041330I$	$-6.73822 - 2.46906I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.467805 - 1.041330I$	$-6.73822 + 2.46906I$	0
$u = -0.838828 + 0.044532I$	$-3.98379 + 5.00843I$	$-5.49188 - 6.00077I$
$u = -0.838828 - 0.044532I$	$-3.98379 - 5.00843I$	$-5.49188 + 6.00077I$
$u = 0.474990 + 0.690912I$	$-2.96171 + 6.03372I$	$-4.87395 - 7.35313I$
$u = 0.474990 - 0.690912I$	$-2.96171 - 6.03372I$	$-4.87395 + 7.35313I$
$u = 0.825126 + 0.022311I$	$-2.88998 - 0.66859I$	$-2.98851 - 0.14329I$
$u = 0.825126 - 0.022311I$	$-2.88998 + 0.66859I$	$-2.98851 + 0.14329I$
$u = -0.413409 + 0.683683I$	$0.00742 - 1.75216I$	$-1.16689 + 4.43589I$
$u = -0.413409 - 0.683683I$	$0.00742 + 1.75216I$	$-1.16689 - 4.43589I$
$u = 0.450918 + 1.227690I$	$-6.60070 + 3.85865I$	0
$u = 0.450918 - 1.227690I$	$-6.60070 - 3.85865I$	0
$u = -0.438765 + 1.234300I$	$-7.81587 + 0.51539I$	0
$u = -0.438765 - 1.234300I$	$-7.81587 - 0.51539I$	0
$u = 0.470711 + 1.225250I$	$-6.45782 + 5.32632I$	0
$u = 0.470711 - 1.225250I$	$-6.45782 - 5.32632I$	0
$u = -0.442364 + 0.520924I$	$1.71123 - 1.63055I$	$1.63060 + 4.27651I$
$u = -0.442364 - 0.520924I$	$1.71123 + 1.63055I$	$1.63060 - 4.27651I$
$u = -0.481138 + 1.227880I$	$-7.51183 - 9.76537I$	0
$u = -0.481138 - 1.227880I$	$-7.51183 + 9.76537I$	0
$u = -0.590261 + 0.336282I$	$-4.08423 + 6.85269I$	$-6.08983 - 5.98107I$
$u = -0.590261 - 0.336282I$	$-4.08423 - 6.85269I$	$-6.08983 + 5.98107I$
$u = -0.463776 + 1.244240I$	$-11.37070 - 4.72051I$	0
$u = -0.463776 - 1.244240I$	$-11.37070 + 4.72051I$	0
$u = -0.436607 + 1.257510I$	$-11.90830 + 0.38192I$	0
$u = -0.436607 - 1.257510I$	$-11.90830 - 0.38192I$	0
$u = 0.433445 + 1.260510I$	$-15.1956 - 5.2532I$	0
$u = 0.433445 - 1.260510I$	$-15.1956 + 5.2532I$	0
$u = 0.441141 + 1.260650I$	$-15.9636 + 3.8514I$	0
$u = 0.441141 - 1.260650I$	$-15.9636 - 3.8514I$	0
$u = -0.490825 + 1.242560I$	$-11.5116 - 9.9029I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.490825 - 1.242560I$	$-11.5116 + 9.9029I$	0
$u = 0.494249 + 1.243290I$	$-14.7502 + 14.8001I$	0
$u = 0.494249 - 1.243290I$	$-14.7502 - 14.8001I$	0
$u = 0.488923 + 1.246820I$	$-15.6129 + 5.7245I$	0
$u = 0.488923 - 1.246820I$	$-15.6129 - 5.7245I$	0
$u = 0.477316 + 0.439878I$	$1.50816 - 2.35510I$	$0.54892 + 4.70586I$
$u = 0.477316 - 0.439878I$	$1.50816 + 2.35510I$	$0.54892 - 4.70586I$
$u = -0.586128 + 0.275072I$	$-4.62644 - 1.65735I$	$-7.50243 + 0.63837I$
$u = -0.586128 - 0.275072I$	$-4.62644 + 1.65735I$	$-7.50243 - 0.63837I$
$u = 0.556736 + 0.320665I$	$-0.97920 - 2.29313I$	$-2.83779 + 3.07654I$
$u = 0.556736 - 0.320665I$	$-0.97920 + 2.29313I$	$-2.83779 - 3.07654I$
$u = 0.411425$	-1.15550	-8.76440

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^{72} + 41u^{71} + \cdots - 10u^2 + 1$
$c_2, c_7$	$u^{72} + u^{71} + \cdots - 2u - 1$
$c_3, c_4, c_8$	$u^{72} - u^{71} + \cdots + 42u - 17$
$c_5, c_{11}$	$u^{72} - u^{71} + \cdots + 2u^3 - 1$
$c_6, c_{12}$	$u^{72} - 3u^{71} + \cdots - 18u + 3$
$c_9$	$u^{72} - 11u^{71} + \cdots - 18764u + 1889$
$c_{10}$	$u^{72} + 39u^{71} + \cdots - 2u^2 + 1$

### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{72} - 19y^{71} + \cdots - 20y + 1$
$c_2, c_7$	$y^{72} + 41y^{71} + \cdots - 10y^2 + 1$
$c_3, c_4, c_8$	$y^{72} - 79y^{71} + \cdots - 10740y + 289$
$c_5, c_{11}$	$y^{72} - 39y^{71} + \cdots - 2y^2 + 1$
$c_6, c_{12}$	$y^{72} + 61y^{71} + \cdots - 624y + 9$
$c_9$	$y^{72} - 31y^{71} + \cdots - 222228y + 3568321$
$c_{10}$	$y^{72} - 11y^{71} + \cdots - 4y + 1$