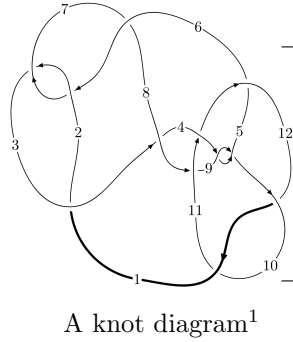
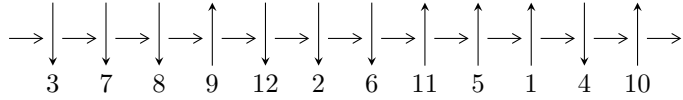


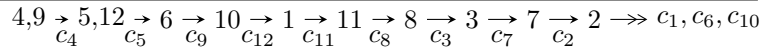
12a<sub>0523</sub> (K12a<sub>0523</sub>)



**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -6.53596 \times 10^{293} u^{104} + 7.87917 \times 10^{293} u^{103} + \dots + 2.51893 \times 10^{295} b + 4.10389 \times 10^{293}, \\ 5.19190 \times 10^{296} u^{104} - 1.30156 \times 10^{297} u^{103} + \dots + 7.80867 \times 10^{296} a + 2.98862 \times 10^{296}, \\ u^{105} - 2u^{104} + \dots + 3u^2 + 1 \rangle$$

$$I_2^u = \langle b, a + 1, u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 106 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -6.54 \times 10^{293} u^{104} + 7.88 \times 10^{293} u^{103} + \dots + 2.52 \times 10^{295} b + 4.10 \times 10^{293}, 5.19 \times 10^{296} u^{104} - 1.30 \times 10^{297} u^{103} + \dots + 7.81 \times 10^{296} a + 2.99 \times 10^{296}, u^{105} - 2u^{104} + \dots + 3u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.664889u^{104} + 1.66681u^{103} + \dots + 1.49798u - 0.382731 \\ 0.0259474u^{104} - 0.0312799u^{103} + \dots + 2.02082u - 0.0162922 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -4.30965u^{104} + 4.08364u^{103} + \dots + 3.79930u + 8.10925 \\ 0.0507263u^{104} - 0.0723374u^{103} + \dots - 0.0688675u - 0.0910713 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.675206u^{104} + 1.69171u^{103} + \dots + 0.487482u - 0.370705 \\ -u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.638941u^{104} + 1.63553u^{103} + \dots + 3.51880u - 0.399023 \\ 0.0259474u^{104} - 0.0312799u^{103} + \dots + 2.02082u - 0.0162922 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 5.02213u^{104} - 5.76629u^{103} + \dots - 14.5025u - 3.74387 \\ -0.0685443u^{104} + 0.0806585u^{103} + \dots - 0.927508u + 0.0754778 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1.84791u^{104} - 1.44973u^{103} + \dots - 1.12604u - 1.51565 \\ -0.104549u^{104} + 0.0699046u^{103} + \dots + 0.0417599u + 0.0704983 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 5.89546u^{104} - 6.94305u^{103} + \dots - 11.8346u - 4.93404 \\ -0.278081u^{104} + 0.312953u^{103} + \dots - 0.771699u + 0.279228 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.53539u^{104} - 0.555872u^{103} + \dots - 2.03889u - 2.74853 \\ -0.0668628u^{104} + 0.0559341u^{103} + \dots + 0.951702u + 0.0225999 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 3.59047u^{104} - 1.27532u^{103} + \dots + 8.64459u - 8.12545$$

(iv) u-Polynomials at the component

| Crossings        | u-Polynomials at each crossing   |
|------------------|--|
| $c_1, c_7$       | $u^{105} + 34u^{104} + \dots - 6u + 1$                                 |
| $c_2, c_6$       | $u^{105} - 2u^{104} + \dots + 2u - 1$                                  |
| $c_3$            | $u^{105} + 4u^{104} + \dots - 317390u - 19141$                         |
| $c_4, c_9$       | $u^{105} - 2u^{104} + \dots + 3u^2 + 1$                                |
| $c_5$            | $31(31u^{105} + 196u^{104} + \dots + 3.96866 \times 10^7 u + 4806371)$ |
| $c_8$            | $31(31u^{105} - 196u^{104} + \dots - 554872u - 22063)$                 |
| $c_{10}, c_{12}$ | $u^{105} + 3u^{104} + \dots + 1098u - 81$                              |
| $c_{11}$         | $u^{105} + 3u^{104} + \dots + 1440u + 279$                             |

(v) Riley Polynomials at the component

| Crossings        | Riley Polynomials at each crossing  |
|------------------|---|
| $c_1, c_7$       | $y^{105} + 74y^{104} + \dots + 18y - 1$   |
| $c_2, c_6$       | $y^{105} - 34y^{104} + \dots - 6y - 1$  |
| $c_3$            | $y^{105} - 22y^{104} + \dots + 16340336002y - 366377881$                                  |
| $c_4, c_9$       | $y^{105} - 78y^{104} + \dots - 6y - 1$  |
| $c_5$            | $961$<br>$\cdot (961y^{105} + 107098y^{104} + \dots - 351460639183822y - 23101202189641)$ |
| $c_8$            | $961(961y^{105} + 31830y^{104} + \dots + 2.58328 \times 10^{10}y - 4.86776 \times 10^8)$  |
| $c_{10}, c_{12}$ | $y^{105} - 75y^{104} + \dots + 599886y - 6561$  |
| $c_{11}$         | $y^{105} + 9y^{104} + \dots - 4365162y - 77841$   |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -1.001250 + 0.088635I$<br>$a = -2.64914 + 5.35272I$<br>$b = -0.038011 - 0.343487I$ | $4.00760 - 5.28754I$                  | 0          |
| $u = -1.001250 - 0.088635I$<br>$a = -2.64914 - 5.35272I$<br>$b = -0.038011 + 0.343487I$ | $4.00760 + 5.28754I$                  | 0          |
| $u = 1.037460 + 0.104080I$<br>$a = 1.02767 + 3.93015I$<br>$b = -0.075087 - 0.439132I$   | $4.74875 + 0.03581I$                  | 0          |
| $u = 1.037460 - 0.104080I$<br>$a = 1.02767 - 3.93015I$<br>$b = -0.075087 + 0.439132I$   | $4.74875 - 0.03581I$                  | 0          |
| $u = 1.047450 + 0.159162I$<br>$a = 1.32246 + 0.67047I$<br>$b = -0.040020 - 0.427091I$   | $3.59853 - 0.03988I$                  | 0          |
| $u = 1.047450 - 0.159162I$<br>$a = 1.32246 - 0.67047I$<br>$b = -0.040020 + 0.427091I$   | $3.59853 + 0.03988I$                  | 0          |
| $u = 1.029210 + 0.252615I$<br>$a = 0.504533 + 1.067150I$<br>$b = 0.348579 - 0.558726I$  | $1.77503 + 1.08366I$                  | 0          |
| $u = 1.029210 - 0.252615I$<br>$a = 0.504533 - 1.067150I$<br>$b = 0.348579 + 0.558726I$  | $1.77503 - 1.08366I$                  | 0          |
| $u = -1.066080 + 0.143000I$<br>$a = -1.39931 + 0.46826I$<br>$b = 0.123128 - 0.376700I$  | $2.65966 + 5.47007I$                  | 0          |
| $u = -1.066080 - 0.143000I$<br>$a = -1.39931 - 0.46826I$<br>$b = 0.123128 + 0.376700I$  | $2.65966 - 5.47007I$                  | 0          |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -0.183896 + 1.081830I$<br>$a = -0.119743 + 0.157510I$<br>$b = -0.891981 - 0.657983I$ | $-3.14658 - 6.82487I$                 | 0          |
| $u = -0.183896 - 1.081830I$<br>$a = -0.119743 - 0.157510I$<br>$b = -0.891981 + 0.657983I$ | $-3.14658 + 6.82487I$                 | 0          |
| $u = -0.138219 + 1.094920I$<br>$a = -0.147917 + 0.115663I$<br>$b = -0.905202 - 0.860589I$ | $2.52804 - 12.97190I$                 | 0          |
| $u = -0.138219 - 1.094920I$<br>$a = -0.147917 - 0.115663I$<br>$b = -0.905202 + 0.860589I$ | $2.52804 + 12.97190I$                 | 0          |
| $u = 0.143059 + 1.107000I$<br>$a = 0.133437 + 0.111080I$<br>$b = 0.843222 - 0.849587I$    | $3.64054 + 7.10836I$                  | 0          |
| $u = 0.143059 - 1.107000I$<br>$a = 0.133437 - 0.111080I$<br>$b = 0.843222 + 0.849587I$    | $3.64054 - 7.10836I$                  | 0          |
| $u = -0.351677 + 1.075110I$<br>$a = -0.023335 + 0.193334I$<br>$b = -0.702928 - 0.316022I$ | $-1.404440 - 0.105905I$               | 0          |
| $u = -0.351677 - 1.075110I$<br>$a = -0.023335 - 0.193334I$<br>$b = -0.702928 + 0.316022I$ | $-1.404440 + 0.105905I$               | 0          |
| $u = 1.14082$<br>$a = -1.00687$<br>$b = -0.761997$  | 3.91618                               | 0          |
| $u = -1.080450 + 0.395669I$<br>$a = 0.151530 + 1.044050I$<br>$b = -0.877507 - 0.498572I$  | $0.58128 - 4.51844I$                  | 0          |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -1.080450 - 0.395669I$<br>$a = 0.151530 - 1.044050I$<br>$b = -0.877507 + 0.498572I$ | $0.58128 + 4.51844I$                  | 0                     |
| $u = 0.216903 + 1.144560I$<br>$a = 0.071825 + 0.135759I$<br>$b = 0.677532 - 0.614095I$   | $1.14640 + 4.18416I$                  | 0                     |
| $u = 0.216903 - 1.144560I$<br>$a = 0.071825 - 0.135759I$<br>$b = 0.677532 + 0.614095I$   | $1.14640 - 4.18416I$                  | 0                     |
| $u = -0.604422 + 0.510373I$<br>$a = 0.001363 + 0.303028I$<br>$b = -0.557423 + 0.021591I$ | $-1.294600 + 0.266261I$               | $-9.33366 + 0.I$      |
| $u = -0.604422 - 0.510373I$<br>$a = 0.001363 - 0.303028I$<br>$b = -0.557423 - 0.021591I$ | $-1.294600 - 0.266261I$               | $-9.33366 + 0.I$      |
| $u = 1.21149$<br>$a = 0.364379$<br>$b = -1.43398$  | 3.79413                               | 0                     |
| $u = 0.186143 + 0.758490I$<br>$a = -0.041179 + 0.402886I$<br>$b = 1.023650 + 0.274246I$  | $-2.75964 + 3.82456I$                 | $-7.69394 - 5.15963I$ |
| $u = 0.186143 - 0.758490I$<br>$a = -0.041179 - 0.402886I$<br>$b = 1.023650 - 0.274246I$  | $-2.75964 - 3.82456I$                 | $-7.69394 + 5.15963I$ |
| $u = -1.175660 + 0.322718I$<br>$a = 0.13151 + 1.62525I$<br>$b = -0.95555 - 1.17209I$     | $1.64381 - 4.37178I$                  | 0                     |
| $u = -1.175660 - 0.322718I$<br>$a = 0.13151 - 1.62525I$<br>$b = -0.95555 + 1.17209I$     | $1.64381 + 4.37178I$                  | 0                     |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.199780 + 0.219409I$<br>$a = 0.34279 + 1.87081I$<br>$b = 0.09902 - 1.60939I$     | $5.55471 - 0.56979I$                  | 0          |
| $u = 1.199780 - 0.219409I$<br>$a = 0.34279 - 1.87081I$<br>$b = 0.09902 + 1.60939I$     | $5.55471 + 0.56979I$                  | 0          |
| $u = 1.162080 + 0.371487I$<br>$a = -0.31585 + 1.40380I$<br>$b = 1.14678 - 0.84513I$    | $0.238755 + 0.320365I$                | 0          |
| $u = 1.162080 - 0.371487I$<br>$a = -0.31585 - 1.40380I$<br>$b = 1.14678 + 0.84513I$    | $0.238755 - 0.320365I$                | 0          |
| $u = -1.197630 + 0.242815I$<br>$a = -0.24103 + 1.86816I$<br>$b = -0.33800 - 1.59119I$  | $5.86921 - 4.87500I$                  | 0          |
| $u = -1.197630 - 0.242815I$<br>$a = -0.24103 - 1.86816I$<br>$b = -0.33800 + 1.59119I$  | $5.86921 + 4.87500I$                  | 0          |
| $u = -1.222500 + 0.093211I$<br>$a = -0.618978 + 1.252910I$<br>$b = 1.22271 - 1.10340I$ | $5.71349 - 1.89041I$                  | 0          |
| $u = -1.222500 - 0.093211I$<br>$a = -0.618978 - 1.252910I$<br>$b = 1.22271 + 1.10340I$ | $5.71349 + 1.89041I$                  | 0          |
| $u = 1.227930 + 0.136503I$<br>$a = 0.65931 + 1.63245I$<br>$b = -0.89616 - 1.54631I$    | $2.52130 + 3.67820I$                  | 0          |
| $u = 1.227930 - 0.136503I$<br>$a = 0.65931 - 1.63245I$<br>$b = -0.89616 + 1.54631I$    | $2.52130 - 3.67820I$                  | 0          |



| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.202250 + 0.346653I$<br>$a = -0.34406 + 1.69024I$<br>$b = 1.26890 - 1.21120I$    | $-2.45776 + 6.16809I$                 | 0          |
| $u = 1.202250 - 0.346653I$<br>$a = -0.34406 - 1.69024I$<br>$b = 1.26890 + 1.21120I$    | $-2.45776 - 6.16809I$                 | 0          |
| $u = -1.255710 + 0.057159I$<br>$a = -1.016010 + 0.818544I$<br>$b = 1.87080 - 0.87723I$ | $9.02776 - 1.33183I$                  | 0          |
| $u = -1.255710 - 0.057159I$<br>$a = -1.016010 - 0.818544I$<br>$b = 1.87080 + 0.87723I$ | $9.02776 + 1.33183I$                  | 0          |
| $u = 1.258390 + 0.046924I$<br>$a = 1.058200 + 0.680510I$<br>$b = -1.96530 - 0.73898I$  | $8.40796 - 4.25540I$                  | 0          |
| $u = 1.258390 - 0.046924I$<br>$a = 1.058200 - 0.680510I$<br>$b = -1.96530 + 0.73898I$  | $8.40796 + 4.25540I$                  | 0          |
| $u = -1.217260 + 0.325928I$<br>$a = 0.27210 + 1.85122I$<br>$b = -1.21658 - 1.46883I$   | $3.61544 - 6.31212I$                  | 0          |
| $u = -1.217260 - 0.325928I$<br>$a = 0.27210 - 1.85122I$<br>$b = -1.21658 + 1.46883I$   | $3.61544 + 6.31212I$                  | 0          |
| $u = -1.255260 + 0.117370I$<br>$a = -0.92722 + 1.52083I$<br>$b = 1.35471 - 1.65467I$   | $8.36985 - 3.15222I$                  | 0          |
| $u = -1.255260 - 0.117370I$<br>$a = -0.92722 - 1.52083I$<br>$b = 1.35471 + 1.65467I$   | $8.36985 + 3.15222I$                  | 0          |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = 1.257520 + 0.125339I$<br>$a = 0.92754 + 1.60282I$<br>$b = -1.28893 - 1.76611I$      | $7.54940 + 8.78410I$                  | 0                      |
| $u = 1.257520 - 0.125339I$<br>$a = 0.92754 - 1.60282I$<br>$b = -1.28893 + 1.76611I$      | $7.54940 - 8.78410I$                  | 0                      |
| $u = 1.222260 + 0.332374I$<br>$a = -0.33002 + 1.86212I$<br>$b = 1.30750 - 1.46504I$      | $2.59147 + 11.95360I$                 | 0                      |
| $u = 1.222260 - 0.332374I$<br>$a = -0.33002 - 1.86212I$<br>$b = 1.30750 + 1.46504I$      | $2.59147 - 11.95360I$                 | 0                      |
| $u = 0.110022 + 0.709216I$<br>$a = -0.132806 + 0.485406I$<br>$b = 1.023330 + 0.544364I$  | $-5.80400 - 2.26364I$                 | $-10.97921 + 2.02009I$ |
| $u = 0.110022 - 0.709216I$<br>$a = -0.132806 - 0.485406I$<br>$b = 1.023330 - 0.544364I$  | $-5.80400 + 2.26364I$                 | $-10.97921 - 2.02009I$ |
| $u = 0.029234 + 1.290430I$<br>$a = 0.0082975 + 0.0595641I$<br>$b = 0.073881 - 0.793429I$ | $7.30962 + 3.06464I$                  | 0                      |
| $u = 0.029234 - 1.290430I$<br>$a = 0.0082975 - 0.0595641I$<br>$b = 0.073881 + 0.793429I$ | $7.30962 - 3.06464I$                  | 0                      |
| $u = 0.058274 + 0.684355I$<br>$a = -0.225911 + 0.552452I$<br>$b = 0.988094 + 0.748338I$  | $-0.96466 - 8.18446I$                 | $-5.29812 + 6.41381I$  |
| $u = 0.058274 - 0.684355I$<br>$a = -0.225911 - 0.552452I$<br>$b = 0.988094 - 0.748338I$  | $-0.96466 + 8.18446I$                 | $-5.29812 - 6.41381I$  |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.198391 + 0.656872I$<br>$a = 0.128951 + 0.351468I$<br>$b = -0.807130 + 0.376578I$ | $-1.37508 + 0.69491I$                 | $-5.30659 - 1.43743I$ |
| $u = -0.198391 - 0.656872I$<br>$a = 0.128951 - 0.351468I$<br>$b = -0.807130 - 0.376578I$ | $-1.37508 - 0.69491I$                 | $-5.30659 + 1.43743I$ |
| $u = -0.066609 + 0.664501I$<br>$a = 0.251170 + 0.510908I$<br>$b = -0.910547 + 0.727872I$ | $0.10737 + 2.61763I$                  | $-3.53159 - 1.71174I$ |
| $u = -0.066609 - 0.664501I$<br>$a = 0.251170 - 0.510908I$<br>$b = -0.910547 - 0.727872I$ | $0.10737 - 2.61763I$                  | $-3.53159 + 1.71174I$ |
| $u = 1.40362 + 0.48950I$<br>$a = 0.00883 - 1.60449I$<br>$b = -1.16869 + 1.20887I$        | $7.3598 + 18.5471I$                   | 0                     |
| $u = 1.40362 - 0.48950I$<br>$a = 0.00883 + 1.60449I$<br>$b = -1.16869 - 1.20887I$        | $7.3598 - 18.5471I$                   | 0                     |
| $u = -1.40671 + 0.49098I$<br>$a = 0.01328 - 1.57139I$<br>$b = 1.12578 + 1.21228I$        | $8.4984 - 12.7188I$                   | 0                     |
| $u = -1.40671 - 0.49098I$<br>$a = 0.01328 + 1.57139I$<br>$b = 1.12578 - 1.21228I$        | $8.4984 + 12.7188I$                   | 0                     |
| $u = 1.41075 + 0.48080I$<br>$a = 0.08806 - 1.51090I$<br>$b = -1.12260 + 1.08649I$        | $1.82215 + 12.33280I$                 | 0                     |
| $u = 1.41075 - 0.48080I$<br>$a = 0.08806 + 1.51090I$<br>$b = -1.12260 - 1.08649I$        | $1.82215 - 12.33280I$                 | 0                     |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -1.42223 + 0.48655I$<br>$a = -0.018088 - 1.406970I$<br>$b = 0.99133 + 1.09509I$    | $6.23656 - 9.84835I$                  | 0                     |
| $u = -1.42223 - 0.48655I$<br>$a = -0.018088 + 1.406970I$<br>$b = 0.99133 - 1.09509I$    | $6.23656 + 9.84835I$                  | 0                     |
| $u = 1.43045 + 0.47266I$<br>$a = 0.129535 - 1.323860I$<br>$b = -0.977552 + 0.952506I$   | $3.94876 + 5.59214I$                  | 0                     |
| $u = 1.43045 - 0.47266I$<br>$a = 0.129535 + 1.323860I$<br>$b = -0.977552 - 0.952506I$   | $3.94876 - 5.59214I$                  | 0                     |
| $u = -1.43719 + 0.51844I$<br>$a = 0.246826 - 1.221380I$<br>$b = 0.669947 + 1.223210I$   | $12.1930 - 9.2857I$                   | 0                     |
| $u = -1.43719 - 0.51844I$<br>$a = 0.246826 + 1.221380I$<br>$b = 0.669947 - 1.223210I$   | $12.1930 + 9.2857I$                   | 0                     |
| $u = 1.44374 + 0.52482I$<br>$a = -0.270248 - 1.146870I$<br>$b = -0.588875 + 1.196410I$  | $12.12610 + 3.28595I$                 | 0                     |
| $u = 1.44374 - 0.52482I$<br>$a = -0.270248 + 1.146870I$<br>$b = -0.588875 - 1.196410I$  | $12.12610 - 3.28595I$                 | 0                     |
| $u = 0.045808 + 0.458306I$<br>$a = 0.818270 - 0.034288I$<br>$b = -0.155246 + 0.850670I$ | $2.32263 + 2.17537I$                  | $-1.25483 - 4.43451I$ |
| $u = 0.045808 - 0.458306I$<br>$a = 0.818270 + 0.034288I$<br>$b = -0.155246 - 0.850670I$ | $2.32263 - 2.17537I$                  | $-1.25483 + 4.43451I$ |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.095860 + 0.444326I$<br>$a = -1.149790 - 0.090487I$<br>$b = 0.012329 + 0.925237I$ | $1.86071 + 3.04955I$                  | $-2.34350 - 1.80734I$ |
| $u = -0.095860 - 0.444326I$<br>$a = -1.149790 + 0.090487I$<br>$b = 0.012329 - 0.925237I$ | $1.86071 - 3.04955I$                  | $-2.34350 + 1.80734I$ |
| $u = -0.256720 + 0.364302I$<br>$a = -2.57277 - 0.09048I$<br>$b = -0.566482 + 0.850730I$  | $3.11999 - 7.09682I$                  | $-1.22727 + 6.68806I$ |
| $u = -0.256720 - 0.364302I$<br>$a = -2.57277 + 0.09048I$<br>$b = -0.566482 - 0.850730I$  | $3.11999 + 7.09682I$                  | $-1.22727 - 6.68806I$ |
| $u = 0.259161 + 0.341076I$<br>$a = 2.70653 - 0.22007I$<br>$b = 0.575046 + 0.774355I$     | $3.95977 + 1.57224I$                  | $0.72765 - 1.22976I$  |
| $u = 0.259161 - 0.341076I$<br>$a = 2.70653 + 0.22007I$<br>$b = 0.575046 - 0.774355I$     | $3.95977 - 1.57224I$                  | $0.72765 + 1.22976I$  |
| $u = -0.185439 + 0.373872I$<br>$a = -2.03610 - 0.36458I$<br>$b = -0.333036 + 0.850412I$  | $-1.55602 - 1.86353I$                 | $-7.04309 + 3.50475I$ |
| $u = -0.185439 - 0.373872I$<br>$a = -2.03610 + 0.36458I$<br>$b = -0.333036 - 0.850412I$  | $-1.55602 + 1.86353I$                 | $-7.04309 - 3.50475I$ |
| $u = -0.384548 + 0.144143I$<br>$a = -4.17541 - 0.15190I$<br>$b = -0.771056 + 0.219016I$  | $3.79007 + 4.86557I$                  | $-3.91765 - 5.78099I$ |
| $u = -0.384548 - 0.144143I$<br>$a = -4.17541 + 0.15190I$<br>$b = -0.771056 - 0.219016I$  | $3.79007 - 4.86557I$                  | $-3.91765 + 5.78099I$ |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -1.54081 + 0.44876I$<br>$a = -0.198025 - 0.762752I$<br>$b = 0.581214 + 0.586799I$ | $3.16248 - 7.87070I$                  | 0                     |
| $u = -1.54081 - 0.44876I$<br>$a = -0.198025 + 0.762752I$<br>$b = 0.581214 - 0.586799I$ | $3.16248 + 7.87070I$                  | 0                     |
| $u = 0.352843 + 0.170127I$<br>$a = 4.04123 - 0.28066I$<br>$b = 0.730822 + 0.288597I$   | $4.48313 + 0.58245I$                  | $-1.56702 + 0.71193I$ |
| $u = 0.352843 - 0.170127I$<br>$a = 4.04123 + 0.28066I$<br>$b = 0.730822 - 0.288597I$   | $4.48313 - 0.58245I$                  | $-1.56702 - 0.71193I$ |
| $u = -1.45640 + 0.72941I$<br>$a = 0.412409 - 0.298435I$<br>$b = -0.225627 + 0.675899I$ | $6.15662 + 6.42755I$                  | 0                     |
| $u = -1.45640 - 0.72941I$<br>$a = 0.412409 + 0.298435I$<br>$b = -0.225627 - 0.675899I$ | $6.15662 - 6.42755I$                  | 0                     |
| $u = 1.55729 + 0.52982I$<br>$a = -0.030593 - 0.671169I$<br>$b = -0.367899 + 0.684184I$ | $5.35803 + 3.08361I$                  | 0                     |
| $u = 1.55729 - 0.52982I$<br>$a = -0.030593 + 0.671169I$<br>$b = -0.367899 - 0.684184I$ | $5.35803 - 3.08361I$                  | 0                     |
| $u = 1.49683 + 0.69386I$<br>$a = -0.355902 - 0.391949I$<br>$b = 0.100044 + 0.709134I$  | $7.37741 - 0.45511I$                  | 0                     |
| $u = 1.49683 - 0.69386I$<br>$a = -0.355902 + 0.391949I$<br>$b = 0.100044 - 0.709134I$  | $7.37741 + 0.45511I$                  | 0                     |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = -0.347632$<br>$a = -4.59360$<br>$b = -0.664125$                                   | -0.447801                             | -12.5780             |
| $u = 0.170027 + 0.238840I$<br>$a = 2.84527 - 1.60576I$<br>$b = 0.343400 + 0.495146I$   | $1.76251 + 0.66899I$                  | $4.46975 + 0.53128I$ |
| $u = 0.170027 - 0.238840I$<br>$a = 2.84527 + 1.60576I$<br>$b = 0.343400 - 0.495146I$   | $1.76251 - 0.66899I$                  | $4.46975 - 0.53128I$ |
| $u = -1.75988 + 0.61452I$<br>$a = -0.006746 - 0.326907I$<br>$b = 0.171742 + 0.388574I$ | $0.283122 - 0.464056I$                | 0                    |
| $u = -1.75988 - 0.61452I$<br>$a = -0.006746 + 0.326907I$<br>$b = 0.171742 - 0.388574I$ | $0.283122 + 0.464056I$                | 0                    |

$$\text{II. } I_2^u = \langle b, a + 1, u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class =  $-1$

(iii) Cusp Shapes =  $-6$



(iv) **u**-Polynomials at the component

| Crossings  | <b>u</b> -Polynomials at each crossing |
|--|--|
| $c_1, c_2, c_3$<br>$c_4, c_5, c_6$<br>$c_7, c_9$ | $u + 1$                                |
| $c_8$  | $u - 1$                                |
| $c_{10}, c_{11}, c_{12}$                         | $u$                                    |

(v) Riley Polynomials at the component

| Crossings   | Riley Polynomials at each crossing |
|---|------------------------------------|
| $c_1, c_2, c_3$<br>$c_4, c_5, c_6$<br>$c_7, c_8, c_9$ | $y - 1$                            |
| $c_{10}, c_{11}, c_{12}$                              | $y$                                |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = -1.00000$       |                                       |            |
| $a = -1.00000$       | -1.64493                              | -6.00000   |
| $b = 0$              |                                       |            |

### III. u-Polynomials

| Crossings        | u-Polynomials at each crossing   |
|------------------|--|
| $c_1, c_7$       | $(u + 1)(u^{105} + 34u^{104} + \dots - 6u + 1)$                              |
| $c_2, c_6$       | $(u + 1)(u^{105} - 2u^{104} + \dots + 2u - 1)$                               |
| $c_3$            | $(u + 1)(u^{105} + 4u^{104} + \dots - 317390u - 19141)$                      |
| $c_4, c_9$       | $(u + 1)(u^{105} - 2u^{104} + \dots + 3u^2 + 1)$                             |
| $c_5$            | $31(u + 1)(31u^{105} + 196u^{104} + \dots + 3.96866 \times 10^7u + 4806371)$ |
| $c_8$            | $31(u - 1)(31u^{105} - 196u^{104} + \dots - 554872u - 22063)$                |
| $c_{10}, c_{12}$ | $u(u^{105} + 3u^{104} + \dots + 1098u - 81)$                                 |
| $c_{11}$         | $u(u^{105} + 3u^{104} + \dots + 1440u + 279)$                                |

#### IV. Riley Polynomials

| Crossings        | Riley Polynomials at each crossing   |
|------------------|--|
| $c_1, c_7$       | $(y - 1)(y^{105} + 74y^{104} + \dots + 18y - 1)$   |
| $c_2, c_6$       | $(y - 1)(y^{105} - 34y^{104} + \dots - 6y - 1)$  |
| $c_3$            | $(y - 1)(y^{105} - 22y^{104} + \dots + 1.63403 \times 10^{10}y - 3.66378 \times 10^8)$           |
| $c_4, c_9$       | $(y - 1)(y^{105} - 78y^{104} + \dots - 6y - 1)$  |
| $c_5$            | $961(y - 1)$<br>$\cdot (961y^{105} + 107098y^{104} + \dots - 351460639183822y - 23101202189641)$ |
| $c_8$            | $961(y - 1)$<br>$\cdot (961y^{105} + 31830y^{104} + \dots + 25832765582y - 486775969)$           |
| $c_{10}, c_{12}$ | $y(y^{105} - 75y^{104} + \dots + 599886y - 6561)$  |
| $c_{11}$         | $y(y^{105} + 9y^{104} + \dots - 4365162y - 77841)$   |