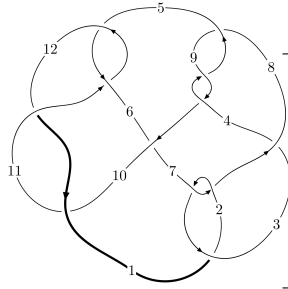
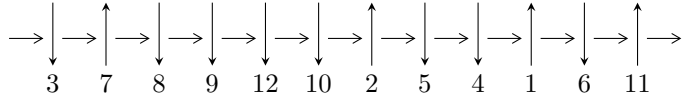


12a<sub>0524</sub> (K12a<sub>0524</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,8 \xrightarrow{c_7} 7 \xrightarrow{c_2} 3 \xrightarrow{c_3} 4 \xrightarrow{c_1} 1,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_6} 6 \xrightarrow{c_9} 9 \xrightarrow{c_4} 5 \xrightarrow{c_{12}} 12 \Rightarrow c_5, c_8, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1.19165 \times 10^{29} u^{63} + 7.17172 \times 10^{28} u^{62} + \dots + 8.78717 \times 10^{29} b + 1.18770 \times 10^{30}, \\ 1.42661 \times 10^{31} u^{63} - 8.31260 \times 10^{30} u^{62} + \dots + 7.02973 \times 10^{30} a + 1.31917 \times 10^{31}, u^{64} - u^{63} + \dots - 2u + 1 \rangle$$

$$I_2^u = \langle -u^4 - 2u^2 + b, u^4 + u^2 + a - 1, u^{27} + 9u^{25} + \dots - u - 1 \rangle$$

$$I_3^u = \langle b + 1, a^3 - a^2 u - 3a^2 + 2au + a + 1, u^2 + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 97 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.19 \times 10^{29} u^{63} + 7.17 \times 10^{28} u^{62} + \dots + 8.79 \times 10^{29} b + 1.19 \times 10^{30}, 1.43 \times 10^{31} u^{63} - 8.31 \times 10^{30} u^{62} + \dots + 7.03 \times 10^{30} a + 1.32 \times 10^{31}, u^{64} - u^{63} + \dots - 2u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2.02940u^{63} + 1.18249u^{62} + \dots - 2.99982u - 1.87655 \\ -0.135612u^{63} - 0.0816158u^{62} + \dots + 0.389219u - 1.35163 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2.09643u^{63} + 1.12088u^{62} + \dots - 3.17116u - 1.64675 \\ -0.314315u^{63} - 0.0337323u^{62} + \dots - 0.348072u - 1.64704 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1.85442u^{63} + 0.738976u^{62} + \dots - 1.32676u - 3.25750 \\ -0.355484u^{63} + 0.0412247u^{62} + \dots - 0.0480554u - 2.11408 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2.16501u^{63} + 1.10088u^{62} + \dots - 2.61060u - 2.22819 \\ -0.314049u^{63} - 0.0375849u^{62} + \dots - 0.543961u - 1.53479 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2.41577u^{63} + 2.96723u^{62} + \dots - 13.7211u + 4.47906 \\ -0.534793u^{63} + 0.848842u^{62} + \dots - 4.03951u + 1.61355 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2.57675u^{63} + 2.92049u^{62} + \dots - 15.0731u + 4.77964 \\ -0.807524u^{63} + 1.17773u^{62} + \dots - 5.99028u + 1.80950 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-2.60252u^{63} + 1.80827u^{62} + \dots - 15.4271u + 3.07685$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{64} + 31u^{63} + \dots + 8u + 1$
$c_2, c_7$	$u^{64} + u^{63} + \dots + 2u + 1$
$c_3$	$u^{64} + 2u^{63} + \dots + 1984u + 128$
$c_4, c_8, c_9$	$u^{64} + u^{63} + \dots + 16u + 1$
$c_5, c_{11}$	$u^{64} + 2u^{63} + \dots + u + 2$
$c_6$	$u^{64} - 10u^{63} + \dots - 14873u + 1862$
$c_{10}, c_{12}$	$u^{64} - 20u^{63} + \dots - 19u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{64} + 11y^{63} + \dots - 40y + 1$
$c_2, c_7$	$y^{64} + 31y^{63} + \dots + 8y + 1$
$c_3$	$y^{64} - 30y^{63} + \dots + 1945600y + 16384$
$c_4, c_8, c_9$	$y^{64} + 59y^{63} + \dots + 104y + 1$
$c_5, c_{11}$	$y^{64} + 20y^{63} + \dots + 19y + 4$
$c_6$	$y^{64} - 12y^{63} + \dots - 37020813y + 3467044$
$c_{10}, c_{12}$	$y^{64} + 48y^{63} + \dots + 879y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.740864 + 0.662784I$ $a = -1.076250 + 0.014411I$ $b = 0.049744 + 0.197245I$	$6.16267 + 3.38539I$	$2.09489 - 2.71260I$
$u = -0.740864 - 0.662784I$ $a = -1.076250 - 0.014411I$ $b = 0.049744 - 0.197245I$	$6.16267 - 3.38539I$	$2.09489 + 2.71260I$
$u = -0.445418 + 0.865420I$ $a = -0.339938 - 0.644967I$ $b = 0.121992 + 1.067110I$	$-1.53101 - 1.39020I$	$-5.91926 + 3.88104I$
$u = -0.445418 - 0.865420I$ $a = -0.339938 + 0.644967I$ $b = 0.121992 - 1.067110I$	$-1.53101 + 1.39020I$	$-5.91926 - 3.88104I$
$u = -0.021735 + 1.036710I$ $a = 1.165230 + 0.128138I$ $b = -0.0067591 - 0.0148508I$	$-4.65557 - 2.80220I$	$-13.46250 + 3.05850I$
$u = -0.021735 - 1.036710I$ $a = 1.165230 - 0.128138I$ $b = -0.0067591 + 0.0148508I$	$-4.65557 + 2.80220I$	$-13.46250 - 3.05850I$
$u = 0.510043 + 0.798911I$ $a = -0.241579 + 1.067010I$ $b = -0.181458 - 1.313360I$	$-0.86573 + 6.45035I$	$-3.51752 - 9.65683I$
$u = 0.510043 - 0.798911I$ $a = -0.241579 - 1.067010I$ $b = -0.181458 + 1.313360I$	$-0.86573 - 6.45035I$	$-3.51752 + 9.65683I$
$u = -0.715186 + 0.790541I$ $a = -0.816990 + 0.099941I$ $b = 0.096344 - 0.304633I$	$9.65441 - 2.68529I$	$5.74999 + 0.I$
$u = -0.715186 - 0.790541I$ $a = -0.816990 - 0.099941I$ $b = 0.096344 + 0.304633I$	$9.65441 + 2.68529I$	$5.74999 + 0.I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.636482 + 0.681496I$ $a = -1.048850 + 0.124326I$ $b = -0.239480 - 0.007765I$	$4.80153 + 1.37625I$	$-0.64369 - 3.25078I$
$u = 0.636482 - 0.681496I$ $a = -1.048850 - 0.124326I$ $b = -0.239480 + 0.007765I$	$4.80153 - 1.37625I$	$-0.64369 + 3.25078I$
$u = 0.897043 + 0.224964I$ $a = -0.162901 + 0.141407I$ $b = -1.21809 - 1.38009I$	$1.29409 - 11.08640I$	$-1.19961 + 7.21378I$
$u = 0.897043 - 0.224964I$ $a = -0.162901 - 0.141407I$ $b = -1.21809 + 1.38009I$	$1.29409 + 11.08640I$	$-1.19961 - 7.21378I$
$u = 0.631106 + 0.872776I$ $a = -0.402460 + 0.142378I$ $b = -0.248913 + 0.600652I$	$4.24624 + 3.53311I$	0
$u = 0.631106 - 0.872776I$ $a = -0.402460 - 0.142378I$ $b = -0.248913 - 0.600652I$	$4.24624 - 3.53311I$	0
$u = 0.846306 + 0.300514I$ $a = -0.501209 + 0.065356I$ $b = -0.87761 - 1.19110I$	$6.84859 - 5.40917I$	$4.32977 + 4.44506I$
$u = 0.846306 - 0.300514I$ $a = -0.501209 - 0.065356I$ $b = -0.87761 + 1.19110I$	$6.84859 + 5.40917I$	$4.32977 - 4.44506I$
$u = -0.871978 + 0.210846I$ $a = -0.151648 - 0.024372I$ $b = -1.25701 + 1.25917I$	$0.32985 + 5.28991I$	$-2.86725 - 2.43047I$
$u = -0.871978 - 0.210846I$ $a = -0.151648 + 0.024372I$ $b = -1.25701 - 1.25917I$	$0.32985 - 5.28991I$	$-2.86725 + 2.43047I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.687105 + 0.897262I$ $a = -0.355479 + 0.167421I$ $b = -0.048600 - 0.750276I$	$5.48639 - 8.73923I$	0
$u = -0.687105 - 0.897262I$ $a = -0.355479 - 0.167421I$ $b = -0.048600 + 0.750276I$	$5.48639 + 8.73923I$	0
$u = -0.373591 + 1.075490I$ $a = -0.795520 + 0.588147I$ $b = 0.914345 + 0.454271I$	$-1.62900 - 0.89969I$	0
$u = -0.373591 - 1.075490I$ $a = -0.795520 - 0.588147I$ $b = 0.914345 - 0.454271I$	$-1.62900 + 0.89969I$	0
$u = 0.731325 + 0.421281I$ $a = -0.938294 - 0.092021I$ $b = -0.543242 - 0.716970I$	$5.06057 + 0.57857I$	$2.53258 - 2.78290I$
$u = 0.731325 - 0.421281I$ $a = -0.938294 + 0.092021I$ $b = -0.543242 + 0.716970I$	$5.06057 - 0.57857I$	$2.53258 + 2.78290I$
$u = 0.434112 + 1.098840I$ $a = 1.43799 + 1.59048I$ $b = -1.29963 + 0.70752I$	$-3.91899 + 0.31574I$	0
$u = 0.434112 - 1.098840I$ $a = 1.43799 - 1.59048I$ $b = -1.29963 - 0.70752I$	$-3.91899 - 0.31574I$	0
$u = -0.176032 + 0.776472I$ $a = 0.607805 - 0.218610I$ $b = -0.208597 + 0.304278I$	$-0.537446 - 1.039780I$	$-7.39933 + 6.43993I$
$u = -0.176032 - 0.776472I$ $a = 0.607805 + 0.218610I$ $b = -0.208597 - 0.304278I$	$-0.537446 + 1.039780I$	$-7.39933 - 6.43993I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.449003 + 1.119080I$ $a = 1.63202 - 1.42381I$ $b = -1.36040 - 0.78973I$	$-4.40703 - 6.33923I$	0
$u = -0.449003 - 1.119080I$ $a = 1.63202 + 1.42381I$ $b = -1.36040 + 0.78973I$	$-4.40703 + 6.33923I$	0
$u = -0.744106 + 0.270463I$ $a = -0.563605 + 0.288717I$ $b = -0.979045 + 0.832531I$	$2.95946 + 3.06631I$	$-2.59881 - 2.85106I$
$u = -0.744106 - 0.270463I$ $a = -0.563605 - 0.288717I$ $b = -0.979045 - 0.832531I$	$2.95946 - 3.06631I$	$-2.59881 + 2.85106I$
$u = 0.552939 + 1.084820I$ $a = 1.189260 + 0.464726I$ $b = -1.00752 + 1.13246I$	$3.08597 + 4.29718I$	0
$u = 0.552939 - 1.084820I$ $a = 1.189260 - 0.464726I$ $b = -1.00752 - 1.13246I$	$3.08597 - 4.29718I$	0
$u = 0.446332 + 1.136180I$ $a = -1.55976 - 0.67921I$ $b = 1.45534 - 0.61315I$	$-4.21610 + 3.94313I$	0
$u = 0.446332 - 1.136180I$ $a = -1.55976 + 0.67921I$ $b = 1.45534 + 0.61315I$	$-4.21610 - 3.94313I$	0
$u = -0.503355 + 1.117530I$ $a = -1.83906 + 0.22387I$ $b = 1.52918 + 1.02332I$	$-0.69715 - 6.51856I$	0
$u = -0.503355 - 1.117530I$ $a = -1.83906 - 0.22387I$ $b = 1.52918 - 1.02332I$	$-0.69715 + 6.51856I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.351656 + 1.195310I$ $a = -1.06860 + 1.58590I$ $b = 1.336950 - 0.118755I$	$-7.69997 + 3.36567I$	0
$u = -0.351656 - 1.195310I$ $a = -1.06860 - 1.58590I$ $b = 1.336950 + 0.118755I$	$-7.69997 - 3.36567I$	0
$u = 0.433087 + 0.616507I$ $a = 0.476384 + 1.128510I$ $b = -0.703167 - 0.846414I$	$2.94099 + 1.46804I$	$3.65440 - 4.55346I$
$u = 0.433087 - 0.616507I$ $a = 0.476384 - 1.128510I$ $b = -0.703167 + 0.846414I$	$2.94099 - 1.46804I$	$3.65440 + 4.55346I$
$u = 0.373707 + 1.194340I$ $a = -1.25946 - 1.48885I$ $b = 1.44389 + 0.01555I$	$-8.31434 + 2.51326I$	0
$u = 0.373707 - 1.194340I$ $a = -1.25946 + 1.48885I$ $b = 1.44389 - 0.01555I$	$-8.31434 - 2.51326I$	0
$u = -0.539852 + 1.141380I$ $a = 1.74162 - 0.49765I$ $b = -1.28546 - 1.23224I$	$0.41354 - 7.91454I$	0
$u = -0.539852 - 1.141380I$ $a = 1.74162 + 0.49765I$ $b = -1.28546 + 1.23224I$	$0.41354 + 7.91454I$	0
$u = 0.507249 + 1.175680I$ $a = -2.24365 - 0.60143I$ $b = 1.93649 - 0.85036I$	$-7.37474 + 6.05052I$	0
$u = 0.507249 - 1.175680I$ $a = -2.24365 + 0.60143I$ $b = 1.93649 + 0.85036I$	$-7.37474 - 6.05052I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.522861 + 1.172680I$ $a = -2.33810 + 0.47146I$ $b = 1.97499 + 0.97360I$	$-6.49800 - 11.91050I$	0
$u = -0.522861 - 1.172680I$ $a = -2.33810 - 0.47146I$ $b = 1.97499 - 0.97360I$	$-6.49800 + 11.91050I$	0
$u = 0.580331 + 1.159360I$ $a = 1.83849 + 0.06678I$ $b = -1.25582 + 1.48375I$	$4.28334 + 10.67080I$	0
$u = 0.580331 - 1.159360I$ $a = 1.83849 - 0.06678I$ $b = -1.25582 - 1.48375I$	$4.28334 - 10.67080I$	0
$u = -0.558133 + 1.198470I$ $a = 2.28120 - 0.20717I$ $b = -1.53555 - 1.48069I$	$-2.62731 - 10.51430I$	0
$u = -0.558133 - 1.198470I$ $a = 2.28120 + 0.20717I$ $b = -1.53555 + 1.48069I$	$-2.62731 + 10.51430I$	0
$u = 0.570313 + 1.204160I$ $a = 2.31459 + 0.06840I$ $b = -1.53389 + 1.56815I$	$-1.6552 + 16.4308I$	0
$u = 0.570313 - 1.204160I$ $a = 2.31459 - 0.06840I$ $b = -1.53389 - 1.56815I$	$-1.6552 - 16.4308I$	0
$u = 0.480253 + 0.227205I$ $a = 0.67734 + 1.74876I$ $b = -1.329360 - 0.229592I$	$-1.14902 - 3.02718I$	$-2.05661 + 1.63893I$
$u = 0.480253 - 0.227205I$ $a = 0.67734 - 1.74876I$ $b = -1.329360 + 0.229592I$	$-1.14902 + 3.02718I$	$-2.05661 - 1.63893I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.516663 + 0.054132I$		
$a = 0.10904 - 1.70032I$	$-1.56361 - 2.57718I$	$-3.22294 + 3.55315I$
$b = -1.347130 - 0.074477I$		
$u = -0.516663 - 0.054132I$		
$a = 0.10904 + 1.70032I$	$-1.56361 + 2.57718I$	$-3.22294 - 3.55315I$
$b = -1.347130 + 0.074477I$		
$u = 0.086910 + 0.474832I$		
$a = -3.26761 - 0.08964I$	$-1.51735 + 2.93358I$	$-0.76792 - 3.27761I$
$b = -0.892529 - 0.014603I$		
$u = 0.086910 - 0.474832I$		
$a = -3.26761 + 0.08964I$	$-1.51735 - 2.93358I$	$-0.76792 + 3.27761I$
$b = -0.892529 + 0.014603I$		

$$\text{II. } I_2^u = \langle -u^4 - 2u^2 + b, u^4 + u^2 + a - 1, u^{27} + 9u^{25} + \dots - u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^4 - u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{12} + 3u^{10} + 3u^8 - 2u^4 - u^2 + 1 \\ u^{14} + 4u^{12} + 7u^{10} + 6u^8 + 2u^6 + u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{10} + 3u^8 + 2u^6 - u^4 - u^2 + 1 \\ -u^{10} - 4u^8 - 5u^6 - 2u^4 + u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{21} + 6u^{19} + 15u^{17} + 18u^{15} + 6u^{13} - 10u^{11} - 11u^9 + 5u^5 + 2u^3 - u \\ u^{23} + 7u^{21} + 22u^{19} + 39u^{17} + 40u^{15} + 20u^{13} - 3u^9 + u^7 + u^5 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -4u^{21} - 28u^{19} - 84u^{17} - 132u^{15} - 100u^{13} + 4u^{12} - 4u^{11} + 16u^{10} + 44u^9 + 24u^8 + 12u^7 + 12u^6 - 16u^5 - 4u^4 - 12u^3 - 4u^2 - 4u - 2$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{27} + 18u^{26} + \dots + u - 1$
$c_2, c_4, c_7$ $c_8, c_9$	$u^{27} + 9u^{25} + \dots - u + 1$
$c_3$	$(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$
$c_5, c_{11}$	$(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^3$
$c_6$	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^3$
$c_{10}, c_{12}$	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{27} - 18y^{26} + \dots + 9y - 1$
$c_2, c_4, c_7$ $c_8, c_9$	$y^{27} + 18y^{26} + \dots + y - 1$
$c_3$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3$
$c_5, c_{11}$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^3$
$c_6$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^3$
$c_{10}, c_{12}$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.415679 + 1.005350I$ $a = 1.83437 + 0.56491I$ $b = -1.67231 + 0.27089I$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$u = 0.415679 - 1.005350I$ $a = 1.83437 - 0.56491I$ $b = -1.67231 - 0.27089I$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$u = -0.302378 + 1.128850I$ $a = 1.24974 - 0.93235I$ $b = -1.43261 + 0.24968I$	$-1.19845$	$-8.65235 + 0.I$
$u = -0.302378 - 1.128850I$ $a = 1.24974 + 0.93235I$ $b = -1.43261 - 0.24968I$	$-1.19845$	$-8.65235 + 0.I$
$u = 0.426564 + 0.710315I$ $a = 1.58575 - 0.21502I$ $b = -0.908339 + 0.821007I$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$u = 0.426564 - 0.710315I$ $a = 1.58575 + 0.21502I$ $b = -0.908339 - 0.821007I$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$u = -0.777660 + 0.179870I$ $a = 0.178219 + 0.600021I$ $b = 1.39418 - 0.87978I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.777660 - 0.179870I$ $a = 0.178219 - 0.600021I$ $b = 1.39418 + 0.87978I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = 0.476346 + 1.108800I$ $a = 2.11333 + 1.06168I$ $b = -2.11585 - 0.00534I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = 0.476346 - 1.108800I$ $a = 2.11333 - 1.06168I$ $b = -2.11585 + 0.00534I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.452506 + 1.125320I$ $a = 1.97182 - 1.14384I$ $b = -2.03340 + 0.12541I$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$u = -0.452506 - 1.125320I$ $a = 1.97182 + 1.14384I$ $b = -2.03340 - 0.12541I$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$u = 0.767882 + 0.142454I$ $a = 0.154353 - 0.467897I$ $b = 1.41500 + 0.68667I$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$u = 0.767882 - 0.142454I$ $a = 0.154353 + 0.467897I$ $b = 1.41500 - 0.68667I$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$u = 0.037522 + 1.261230I$ $a = 0.072421 + 0.206198I$ $b = -0.661704 - 0.111549I$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$u = 0.037522 - 1.261230I$ $a = 0.072421 - 0.206198I$ $b = -0.661704 + 0.111549I$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$u = 0.214742 + 1.244380I$ $a = 0.530910 + 1.071400I$ $b = -1.033270 - 0.536957I$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$u = 0.214742 - 1.244380I$ $a = 0.530910 - 1.071400I$ $b = -1.033270 + 0.536957I$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$u = -0.464087 + 0.550911I$ $a = 1.341830 + 0.421215I$ $b = -0.429958 - 0.932556I$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$u = -0.464087 - 0.550911I$ $a = 1.341830 - 0.421215I$ $b = -0.429958 + 0.932556I$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.315376 + 1.267770I$ $a = 0.87382 - 1.61174I$ $b = -1.38160 + 0.81209I$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$u = -0.315376 - 1.267770I$ $a = 0.87382 + 1.61174I$ $b = -1.38160 - 0.81209I$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$u = 0.301314 + 1.288670I$ $a = 0.70845 + 1.66170I$ $b = -1.27833 - 0.88511I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = 0.301314 - 1.288670I$ $a = 0.70845 - 1.66170I$ $b = -1.27833 + 0.88511I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.630422 + 0.239022I$ $a = 0.634720 + 0.506481I$ $b = 0.705580 - 0.807851I$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$u = -0.630422 - 0.239022I$ $a = 0.634720 - 0.506481I$ $b = 0.705580 + 0.807851I$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$u = 0.604756$ $a = 0.500513$ $b = 0.865217$	$-1.19845$	$-8.65230$

$$\text{III. } I_3^u = \langle b + 1, a^3 - a^2u - 3a^2 + 2au + a + 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ a - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a^2 + a + 1 \\ a - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a + 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -au \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -au \\ -a^2u + 3au - u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4a^2 + 4au + 8a - 4u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^6$
$c_2, c_4, c_7$ $c_8, c_9$	$(u^2 + 1)^3$
$c_3$	$u^6$
$c_5, c_{11}$	$u^6 + u^4 + 2u^2 + 1$
$c_6$	$u^6 - 3u^4 + 2u^2 + 1$
$c_{10}$	$(u^3 + u^2 + 2u + 1)^2$
$c_{12}$	$(u^3 - u^2 + 2u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)^6$
$c_2, c_4, c_7$ $c_8, c_9$	$(y + 1)^6$
$c_3$	$y^6$
$c_5, c_{11}$	$(y^3 + y^2 + 2y + 1)^2$
$c_6$	$(y^3 - 3y^2 + 2y + 1)^2$
$c_{10}, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = 1.000000 + 0.569840I$ $b = -1.00000$	1.11345	$-6 - 0.980489 + 0.10I$
$u = 1.000000I$ $a = -0.307141 + 0.215080I$ $b = -1.00000$	$-3.02413 + 2.82812I$	$-7.50976 - 2.97945I$
$u = 1.000000I$ $a = 2.30714 + 0.21508I$ $b = -1.00000$	$-3.02413 - 2.82812I$	$-7.50976 + 2.97945I$
$u = -1.000000I$ $a = 1.000000 - 0.569840I$ $b = -1.00000$	1.11345	$-6 - 0.980489 + 0.10I$
$u = -1.000000I$ $a = -0.307141 - 0.215080I$ $b = -1.00000$	$-3.02413 - 2.82812I$	$-7.50976 + 2.97945I$
$u = -1.000000I$ $a = 2.30714 - 0.21508I$ $b = -1.00000$	$-3.02413 + 2.82812I$	$-7.50976 - 2.97945I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^6)(u^{27} + 18u^{26} + \dots + u - 1)(u^{64} + 31u^{63} + \dots + 8u + 1)$
$c_2, c_7$	$((u^2 + 1)^3)(u^{27} + 9u^{25} + \dots - u + 1)(u^{64} + u^{63} + \dots + 2u + 1)$
$c_3$	$u^6(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{64} + 2u^{63} + \dots + 1984u + 128)$
$c_4, c_8, c_9$	$((u^2 + 1)^3)(u^{27} + 9u^{25} + \dots - u + 1)(u^{64} + u^{63} + \dots + 16u + 1)$
$c_5, c_{11}$	$(u^6 + u^4 + 2u^2 + 1)(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^3$ $\cdot (u^{64} + 2u^{63} + \dots + u + 2)$
$c_6$	$(u^6 - 3u^4 + 2u^2 + 1)$ $\cdot (u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^3$ $\cdot (u^{64} - 10u^{63} + \dots - 14873u + 1862)$
$c_{10}$	$(u^3 + u^2 + 2u + 1)^2$ $\cdot (u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^3$ $\cdot (u^{64} - 20u^{63} + \dots - 19u + 4)$
$c_{12}$	$(u^3 - u^2 + 2u - 1)^2$ $\cdot (u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^3$ $\cdot (u^{64} - 20u^{63} + \dots - 19u + 4)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y-1)^6)(y^{27} - 18y^{26} + \dots + 9y - 1)(y^{64} + 11y^{63} + \dots - 40y + 1)$
$c_2, c_7$	$((y+1)^6)(y^{27} + 18y^{26} + \dots + y - 1)(y^{64} + 31y^{63} + \dots + 8y + 1)$
$c_3$	$y^6(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3$ $\cdot (y^{64} - 30y^{63} + \dots + 1945600y + 16384)$
$c_4, c_8, c_9$	$((y+1)^6)(y^{27} + 18y^{26} + \dots + y - 1)(y^{64} + 59y^{63} + \dots + 104y + 1)$
$c_5, c_{11}$	$(y^3 + y^2 + 2y + 1)^2$ $\cdot (y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^3$ $\cdot (y^{64} + 20y^{63} + \dots + 19y + 4)$
$c_6$	$(y^3 - 3y^2 + 2y + 1)^2$ $\cdot (y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^3$ $\cdot (y^{64} - 12y^{63} + \dots - 37020813y + 3467044)$
$c_{10}, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^2$ $\cdot (y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^3$ $\cdot (y^{64} + 48y^{63} + \dots + 879y + 16)$