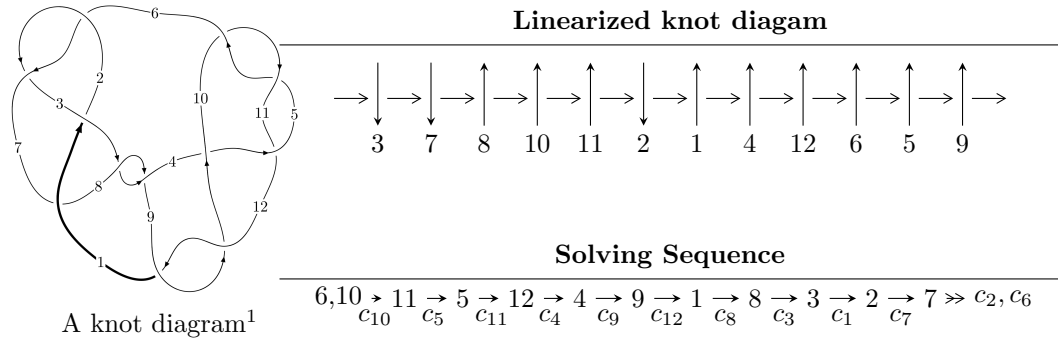


12a<sub>0534</sub> (K12a<sub>0534</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{81} + u^{80} + \dots - u - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 81 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle u^{81} + u^{80} + \dots - u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^6 - 3u^4 - 2u^2 + 1 \\ u^8 + 4u^6 + 4u^4 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1 \\ -u^{12} - 6u^{10} - 12u^8 - 8u^6 - u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{14} - 7u^{12} - 18u^{10} - 19u^8 - 6u^6 - 2u^4 - 4u^2 + 1 \\ u^{14} + 6u^{12} + 13u^{10} + 12u^8 + 6u^6 + 4u^4 + u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{25} + 12u^{23} + \dots + 4u^3 - 3u \\ -u^{25} - 11u^{23} + \dots - 3u^5 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{62} + 29u^{60} + \dots - 4u^2 + 1 \\ -u^{62} - 28u^{60} + \dots - 8u^4 - u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^{36} + 17u^{34} + \dots - 7u^2 + 1 \\ -u^{38} - 18u^{36} + \dots + 10u^4 + u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^{79} + 4u^{78} + \dots + 16u + 2$

(iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing            |
|-----------------------|---|
| $c_1$                 | $u^{81} + 37u^{80} + \dots + 5u + 1$      |
| $c_2, c_6$            | $u^{81} - u^{80} + \dots + u - 1$         |
| $c_3, c_8$            | $u^{81} + u^{80} + \dots - 453u - 61$     |
| $c_4$                 | $u^{81} - u^{80} + \dots - 1961u - 1237$  |
| $c_5, c_{10}, c_{11}$ | $u^{81} + u^{80} + \dots - u - 1$         |
| $c_7$                 | $u^{81} - 3u^{80} + \dots + 19u - 1$      |
| $c_9, c_{12}$         | $u^{81} + 13u^{80} + \dots - 5071u - 283$ |

(v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing                |
|-----------------------|---|
| $c_1$                 | $y^{81} + 15y^{80} + \dots - 7y - 1$              |
| $c_2, c_6$            | $y^{81} - 37y^{80} + \dots + 5y - 1$              |
| $c_3, c_8$            | $y^{81} - 53y^{80} + \dots + 186177y - 3721$      |
| $c_4$                 | $y^{81} + 23y^{80} + \dots - 35110083y - 1530169$ |
| $c_5, c_{10}, c_{11}$ | $y^{81} + 75y^{80} + \dots + 5y - 1$              |
| $c_7$                 | $y^{81} + 7y^{80} + \dots + 145y - 1$             |
| $c_9, c_{12}$         | $y^{81} + 59y^{80} + \dots - 6263y - 80089$       |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape              |
|-----------------------------|---------------------------------------|-------------------------|
| $u = 0.197771 + 1.183570I$  | $0.84481 - 3.23672I$                  | 0                       |
| $u = 0.197771 - 1.183570I$  | $0.84481 + 3.23672I$                  | 0                       |
| $u = 0.046171 + 1.211660I$  | $-2.27651 + 1.93915I$                 | 0                       |
| $u = 0.046171 - 1.211660I$  | $-2.27651 - 1.93915I$                 | 0                       |
| $u = -0.204035 + 1.199890I$ | $2.50774 - 1.86243I$                  | 0                       |
| $u = -0.204035 - 1.199890I$ | $2.50774 + 1.86243I$                  | 0                       |
| $u = -0.688192 + 0.370410I$ | $-0.29265 - 12.11820I$                | $5.45285 + 10.14700I$   |
| $u = -0.688192 - 0.370410I$ | $-0.29265 + 12.11820I$                | $5.45285 - 10.14700I$   |
| $u = 0.682734 + 0.364569I$  | $1.77767 + 6.96994I$                  | $8.59265 - 6.07951I$    |
| $u = 0.682734 - 0.364569I$  | $1.77767 - 6.96994I$                  | $8.59265 + 6.07951I$    |
| $u = -0.667182 + 0.376841I$ | $-3.10444 - 4.74353I$                 | $1.89111 + 5.31075I$    |
| $u = -0.667182 - 0.376841I$ | $-3.10444 + 4.74353I$                 | $1.89111 - 5.31075I$    |
| $u = 0.627167 + 0.427079I$  | $-5.80126 + 5.75467I$                 | $-0.15516 - 7.51536I$   |
| $u = 0.627167 - 0.427079I$  | $-5.80126 - 5.75467I$                 | $-0.15516 + 7.51536I$   |
| $u = 0.669087 + 0.343377I$  | $2.54734 + 4.35898I$                  | $9.79953 - 6.09005I$    |
| $u = 0.669087 - 0.343377I$  | $2.54734 - 4.35898I$                  | $9.79953 + 6.09005I$    |
| $u = -0.220135 + 1.228700I$ | $2.26970 - 4.55930I$                  | 0                       |
| $u = -0.220135 - 1.228700I$ | $2.26970 + 4.55930I$                  | 0                       |
| $u = 0.600027 + 0.450919I$  | $-5.90992 - 1.73415I$                 | $-0.700518 + 0.546897I$ |
| $u = 0.600027 - 0.450919I$  | $-5.90992 + 1.73415I$                 | $-0.700518 - 0.546897I$ |
| $u = -0.518361 + 0.541766I$ | $-0.99512 + 8.05238I$                 | $3.71543 - 4.26648I$    |
| $u = -0.518361 - 0.541766I$ | $-0.99512 - 8.05238I$                 | $3.71543 + 4.26648I$    |
| $u = 0.186058 + 1.245240I$  | $-2.71415 + 2.87763I$                 | 0                       |
| $u = 0.186058 - 1.245240I$  | $-2.71415 - 2.87763I$                 | 0                       |
| $u = 0.227678 + 1.238350I$  | $0.40246 + 9.70206I$                  | 0                       |
| $u = 0.227678 - 1.238350I$  | $0.40246 - 9.70206I$                  | 0                       |
| $u = -0.661462 + 0.328497I$ | $1.155840 + 0.658240I$                | $7.68128 + 0.74467I$    |
| $u = -0.661462 - 0.328497I$ | $1.155840 - 0.658240I$                | $7.68128 - 0.74467I$    |
| $u = 0.504244 + 0.533281I$  | $1.06272 - 2.96937I$                  | $6.86213 + 0.09191I$    |
| $u = 0.504244 - 0.533281I$  | $1.06272 + 2.96937I$                  | $6.86213 - 0.09191I$    |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.599806 + 0.419570I$ | $-2.86954 - 1.93751I$                 | $3.68977 + 3.76519I$   |
| $u = -0.599806 - 0.419570I$ | $-2.86954 + 1.93751I$                 | $3.68977 - 3.76519I$   |
| $u = -0.528049 + 0.500416I$ | $-3.65675 + 0.77452I$                 | $0.180179 + 1.063801I$ |
| $u = -0.528049 - 0.500416I$ | $-3.65675 - 0.77452I$                 | $0.180179 - 1.063801I$ |
| $u = 0.445960 + 0.514360I$  | $1.74475 - 0.56616I$                  | $7.81141 - 0.32467I$   |
| $u = 0.445960 - 0.514360I$  | $1.74475 + 0.56616I$                  | $7.81141 + 0.32467I$   |
| $u = 0.090833 + 1.321820I$  | $-3.48103 + 1.92013I$                 | 0                      |
| $u = 0.090833 - 1.321820I$  | $-3.48103 - 1.92013I$                 | 0                      |
| $u = 0.664571 + 0.032433I$  | $4.28824 + 6.44063I$                  | $11.37631 - 5.73427I$  |
| $u = 0.664571 - 0.032433I$  | $4.28824 - 6.44063I$                  | $11.37631 + 5.73427I$  |
| $u = -0.660958 + 0.017589I$ | $6.06487 - 1.33192I$                  | $14.4027 + 0.6799I$    |
| $u = -0.660958 - 0.017589I$ | $6.06487 + 1.33192I$                  | $14.4027 - 0.6799I$    |
| $u = -0.394768 + 0.518007I$ | $0.25427 - 4.31628I$                  | $4.96258 + 5.88678I$   |
| $u = -0.394768 - 0.518007I$ | $0.25427 + 4.31628I$                  | $4.96258 - 5.88678I$   |
| $u = -0.042555 + 1.365360I$ | $-6.77977 + 0.65328I$                 | 0                      |
| $u = -0.042555 - 1.365360I$ | $-6.77977 - 0.65328I$                 | 0                      |
| $u = -0.110213 + 1.375120I$ | $-5.52185 - 6.10195I$                 | 0                      |
| $u = -0.110213 - 1.375120I$ | $-5.52185 + 6.10195I$                 | 0                      |
| $u = 0.601777$              | 1.08479                               | 8.90280                |
| $u = -0.541617 + 0.228507I$ | $-0.25287 - 3.77283I$                 | $7.91061 + 8.40043I$   |
| $u = -0.541617 - 0.228507I$ | $-0.25287 + 3.77283I$                 | $7.91061 - 8.40043I$   |
| $u = -0.19013 + 1.41345I$   | $-5.52475 - 6.36348I$                 | 0                      |
| $u = -0.19013 - 1.41345I$   | $-5.52475 + 6.36348I$                 | 0                      |
| $u = 0.17372 + 1.43625I$    | $-4.34343 + 1.67894I$                 | 0                      |
| $u = 0.17372 - 1.43625I$    | $-4.34343 - 1.67894I$                 | 0                      |
| $u = -0.25166 + 1.43227I$   | $-4.49351 - 2.67497I$                 | 0                      |
| $u = -0.25166 - 1.43227I$   | $-4.49351 + 2.67497I$                 | 0                      |
| $u = 0.25453 + 1.43844I$    | $-3.17261 + 7.73200I$                 | 0                      |
| $u = 0.25453 - 1.43844I$    | $-3.17261 - 7.73200I$                 | 0                      |
| $u = 0.25853 + 1.44805I$    | $-4.04746 + 10.40670I$                | 0                      |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.25853 - 1.44805I$    | $-4.04746 - 10.40670I$                | 0                      |
| $u = 0.17326 + 1.46090I$    | $-5.28963 - 0.54466I$                 | 0                      |
| $u = 0.17326 - 1.46090I$    | $-5.28963 + 0.54466I$                 | 0                      |
| $u = -0.25138 + 1.45103I$   | $-8.98223 - 8.10218I$                 | 0                      |
| $u = -0.25138 - 1.45103I$   | $-8.98223 + 8.10218I$                 | 0                      |
| $u = -0.22226 + 1.45599I$   | $-8.89843 - 4.95649I$                 | 0                      |
| $u = -0.22226 - 1.45599I$   | $-8.89843 + 4.95649I$                 | 0                      |
| $u = -0.18698 + 1.46218I$   | $-9.93180 - 1.82433I$                 | 0                      |
| $u = -0.18698 - 1.46218I$   | $-9.93180 + 1.82433I$                 | 0                      |
| $u = -0.26014 + 1.45096I$   | $-6.1479 - 15.5799I$                  | 0                      |
| $u = -0.26014 - 1.45096I$   | $-6.1479 + 15.5799I$                  | 0                      |
| $u = -0.17307 + 1.46742I$   | $-7.42202 + 5.58777I$                 | 0                      |
| $u = -0.17307 - 1.46742I$   | $-7.42202 - 5.58777I$                 | 0                      |
| $u = 0.22921 + 1.46252I$    | $-11.8872 + 8.8870I$                  | 0                      |
| $u = 0.22921 - 1.46252I$    | $-11.8872 - 8.8870I$                  | 0                      |
| $u = 0.21649 + 1.46473I$    | $-12.07490 + 1.25015I$                | 0                      |
| $u = 0.21649 - 1.46473I$    | $-12.07490 - 1.25015I$                | 0                      |
| $u = 0.469947 + 0.071920I$  | $0.851920 + 0.071772I$                | $12.35395 - 1.18798I$  |
| $u = 0.469947 - 0.071920I$  | $0.851920 - 0.071772I$                | $12.35395 + 1.18798I$  |
| $u = -0.145910 + 0.409235I$ | $-1.47601 + 1.33170I$                 | $0.709363 - 0.772030I$ |
| $u = -0.145910 - 0.409235I$ | $-1.47601 - 1.33170I$                 | $0.709363 + 0.772030I$ |

## II. u-Polynomials

| Crossings             | u-Polynomials at each crossing            |
|-----------------------|---|
| $c_1$                 | $u^{81} + 37u^{80} + \dots + 5u + 1$      |
| $c_2, c_6$            | $u^{81} - u^{80} + \dots + u - 1$         |
| $c_3, c_8$            | $u^{81} + u^{80} + \dots - 453u - 61$     |
| $c_4$                 | $u^{81} - u^{80} + \dots - 1961u - 1237$  |
| $c_5, c_{10}, c_{11}$ | $u^{81} + u^{80} + \dots - u - 1$         |
| $c_7$                 | $u^{81} - 3u^{80} + \dots + 19u - 1$      |
| $c_9, c_{12}$         | $u^{81} + 13u^{80} + \dots - 5071u - 283$ |



### III. Riley Polynomials

| Crossings             | Riley Polynomials at each crossing                |
|-----------------------|---|
| $c_1$                 | $y^{81} + 15y^{80} + \dots - 7y - 1$              |
| $c_2, c_6$            | $y^{81} - 37y^{80} + \dots + 5y - 1$              |
| $c_3, c_8$            | $y^{81} - 53y^{80} + \dots + 186177y - 3721$      |
| $c_4$                 | $y^{81} + 23y^{80} + \dots - 35110083y - 1530169$ |
| $c_5, c_{10}, c_{11}$ | $y^{81} + 75y^{80} + \dots + 5y - 1$              |
| $c_7$                 | $y^{81} + 7y^{80} + \dots + 145y - 1$             |
| $c_9, c_{12}$         | $y^{81} + 59y^{80} + \dots - 6263y - 80089$       |