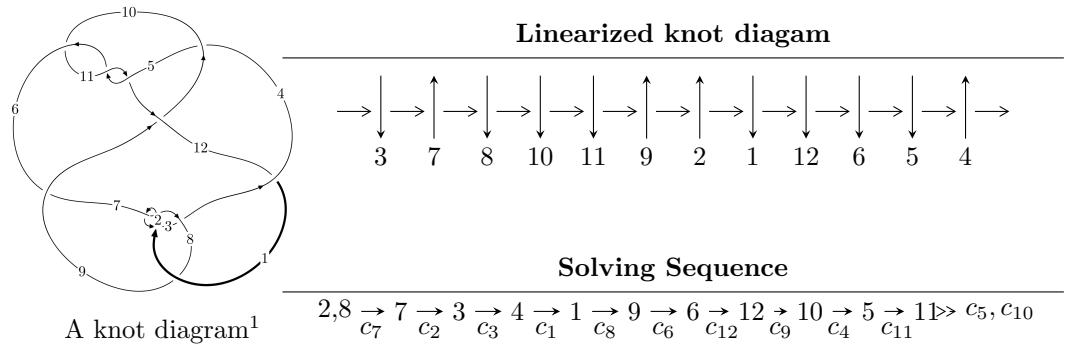


$12a_{0537}$  ( $K12a_{0537}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$I_1^u = \langle u^{89} - u^{88} + \cdots + u - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 89 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{89} - u^{88} + \cdots + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned}
a_2 &= \binom{0}{u} \\
a_8 &= \binom{1}{0} \\
a_7 &= \binom{1}{u^2} \\
a_3 &= \binom{u}{u^3 + u} \\
a_4 &= \binom{-u^3}{u^3 + u} \\
a_1 &= \binom{u^3}{u^5 + u^3 + u} \\
a_9 &= \binom{u^8 + u^6 + u^4 + 1}{u^{10} + 2u^8 + 3u^6 + 2u^4 + u^2} \\
a_6 &= \binom{u^{16} + 3u^{14} + 5u^{12} + 4u^{10} + 3u^8 + 2u^6 + 2u^4 + 1}{u^{18} + 4u^{16} + 9u^{14} + 12u^{12} + 11u^{10} + 6u^8 + 2u^6 + u^2} \\
a_{12} &= \binom{-u^{11} - 2u^9 - 2u^7 + u^3}{u^{11} + 3u^9 + 4u^7 + 3u^5 + u^3 + u} \\
a_{10} &= \binom{-u^{32} - 7u^{30} + \cdots + 2u^4 + 1}{u^{32} + 8u^{30} + \cdots + 4u^4 + 2u^2} \\
a_5 &= \binom{u^{61} + 14u^{59} + \cdots - 2u^3 - u}{-u^{61} - 15u^{59} + \cdots - u^3 + u} \\
a_{11} &= \binom{-u^{66} - 15u^{64} + \cdots - u^2 + 1}{-u^{68} - 16u^{66} + \cdots + 3u^4 + 2u^2}
\end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^{87} - 4u^{86} + \cdots - 4u^2 - 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{89} + 43u^{88} + \cdots + u - 1$
$c_2, c_7$	$u^{89} + u^{88} + \cdots + u + 1$
$c_3$	$u^{89} - u^{88} + \cdots + 1497u + 457$
$c_4$	$u^{89} - u^{88} + \cdots - 5u + 1$
$c_5, c_{10}, c_{11}$	$u^{89} + u^{88} + \cdots + 3u + 1$
$c_6, c_{12}$	$u^{89} + 7u^{88} + \cdots + 161u + 5$
$c_8$	$u^{89} + 5u^{88} + \cdots + u + 1$
$c_9$	$u^{89} - 21u^{88} + \cdots - 4023u + 187$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{89} + 7y^{88} + \cdots + 13y - 1$
$c_2, c_7$	$y^{89} + 43y^{88} + \cdots + y - 1$
$c_3$	$y^{89} - 29y^{88} + \cdots + 6081637y - 208849$
$c_4$	$y^{89} - 5y^{88} + \cdots + 17y - 1$
$c_5, c_{10}, c_{11}$	$y^{89} + 79y^{88} + \cdots + y - 1$
$c_6, c_{12}$	$y^{89} + 67y^{88} + \cdots + 201y - 25$
$c_8$	$y^{89} - y^{88} + \cdots + 61y - 1$
$c_9$	$y^{89} + 11y^{88} + \cdots - 1504923y - 34969$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.549845 + 0.852652I$	$3.32155 + 4.57387I$	0
$u = -0.549845 - 0.852652I$	$3.32155 - 4.57387I$	0
$u = 0.526296 + 0.826367I$	$-1.86086 - 1.10863I$	0
$u = 0.526296 - 0.826367I$	$-1.86086 + 1.10863I$	0
$u = -0.445113 + 0.947902I$	$-0.40489 - 1.97636I$	0
$u = -0.445113 - 0.947902I$	$-0.40489 + 1.97636I$	0
$u = -0.130520 + 0.933837I$	$3.46999 + 3.77804I$	$-4.00000 - 3.55964I$
$u = -0.130520 - 0.933837I$	$3.46999 - 3.77804I$	$-4.00000 + 3.55964I$
$u = 0.237242 + 0.899093I$	$-1.63382 - 0.87283I$	$-8.59634 + 3.63079I$
$u = 0.237242 - 0.899093I$	$-1.63382 + 0.87283I$	$-8.59634 - 3.63079I$
$u = -0.621956 + 0.688948I$	$3.81774 - 9.21070I$	$0. + 8.07606I$
$u = -0.621956 - 0.688948I$	$3.81774 + 9.21070I$	$0. - 8.07606I$
$u = 0.605630 + 0.694228I$	$-1.43820 + 5.63420I$	$-4.00000 - 7.71170I$
$u = 0.605630 - 0.694228I$	$-1.43820 - 5.63420I$	$-4.00000 + 7.71170I$
$u = 0.523965 + 0.945138I$	$5.28882 + 3.53448I$	0
$u = 0.523965 - 0.945138I$	$5.28882 - 3.53448I$	0
$u = -0.544235 + 0.732626I$	$0.19552 - 2.15749I$	$-2.95032 + 4.14794I$
$u = -0.544235 - 0.732626I$	$0.19552 + 2.15749I$	$-2.95032 - 4.14794I$
$u = -0.556700 + 0.687523I$	$0.25637 - 2.05649I$	$-1.44246 + 3.13624I$
$u = -0.556700 - 0.687523I$	$0.25637 + 2.05649I$	$-1.44246 - 3.13624I$
$u = 0.601306 + 0.620005I$	$6.23656 + 0.95324I$	$3.59693 - 2.99187I$
$u = 0.601306 - 0.620005I$	$6.23656 - 0.95324I$	$3.59693 + 2.99187I$
$u = -0.389004 + 1.075220I$	$-0.038564 - 0.742399I$	0
$u = -0.389004 - 1.075220I$	$-0.038564 + 0.742399I$	0
$u = -0.270428 + 1.114400I$	$0.573665 - 0.094345I$	0
$u = -0.270428 - 1.114400I$	$0.573665 + 0.094345I$	0
$u = 0.443236 + 1.076980I$	$-3.58294 + 3.54004I$	0
$u = 0.443236 - 1.076980I$	$-3.58294 - 3.54004I$	0
$u = 0.773116 + 0.297168I$	$1.90632 - 11.11310I$	$-1.08984 + 6.87770I$
$u = 0.773116 - 0.297168I$	$1.90632 + 11.11310I$	$-1.08984 - 6.87770I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.555744 + 1.035790I$	$6.42783 + 1.42029I$	0
$u = 0.555744 - 1.035790I$	$6.42783 - 1.42029I$	0
$u = -0.537606 + 1.047480I$	$0.71771 - 3.82158I$	0
$u = -0.537606 - 1.047480I$	$0.71771 + 3.82158I$	0
$u = -0.767527 + 0.290372I$	$-3.36844 + 7.41224I$	$-5.77885 - 6.28864I$
$u = -0.767527 - 0.290372I$	$-3.36844 - 7.41224I$	$-5.77885 + 6.28864I$
$u = 0.654390 + 0.489201I$	$8.03046 + 3.30236I$	$5.19136 - 3.35930I$
$u = 0.654390 - 0.489201I$	$8.03046 - 3.30236I$	$5.19136 + 3.35930I$
$u = 0.280299 + 1.149490I$	$-5.92026 - 0.49034I$	0
$u = 0.280299 - 1.149490I$	$-5.92026 + 0.49034I$	0
$u = 0.260330 + 1.156600I$	$-2.58902 - 8.08324I$	0
$u = 0.260330 - 1.156600I$	$-2.58902 + 8.08324I$	0
$u = -0.267783 + 1.155220I$	$-7.80687 + 4.35790I$	0
$u = -0.267783 - 1.155220I$	$-7.80687 - 4.35790I$	0
$u = 0.293939 + 1.151340I$	$-6.07434 - 0.28887I$	0
$u = 0.293939 - 1.151340I$	$-6.07434 + 0.28887I$	0
$u = -0.683893 + 0.428051I$	$7.74822 + 5.29418I$	$4.36161 - 4.33354I$
$u = -0.683893 - 0.428051I$	$7.74822 - 5.29418I$	$4.36161 + 4.33354I$
$u = -0.308826 + 1.154160I$	$-8.28930 - 3.48798I$	0
$u = -0.308826 - 1.154160I$	$-8.28930 + 3.48798I$	0
$u = -0.471075 + 1.098060I$	$0.51569 - 6.51976I$	0
$u = -0.471075 - 1.098060I$	$0.51569 + 6.51976I$	0
$u = 0.752387 + 0.281402I$	$-1.59860 - 3.55841I$	$-3.12371 + 1.57420I$
$u = 0.752387 - 0.281402I$	$-1.59860 + 3.55841I$	$-3.12371 - 1.57420I$
$u = 0.318069 + 1.155530I$	$-3.26936 + 7.19305I$	0
$u = 0.318069 - 1.155530I$	$-3.26936 - 7.19305I$	0
$u = -0.734105 + 0.315100I$	$4.84491 + 2.69309I$	$1.74893 - 2.46850I$
$u = -0.734105 - 0.315100I$	$4.84491 - 2.69309I$	$1.74893 + 2.46850I$
$u = 0.548293 + 1.068850I$	$0.30757 + 7.15974I$	0
$u = 0.548293 - 1.068850I$	$0.30757 - 7.15974I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.561612 + 1.069280I$	$5.87439 - 10.10820I$	0
$u = -0.561612 - 1.069280I$	$5.87439 + 10.10820I$	0
$u = 0.746796 + 0.262051I$	$-1.84029 - 3.44425I$	$-4.01435 + 3.41599I$
$u = 0.746796 - 0.262051I$	$-1.84029 + 3.44425I$	$-4.01435 - 3.41599I$
$u = -0.621550 + 0.465042I$	$2.42382 - 0.75571I$	$1.71757 + 3.84156I$
$u = -0.621550 - 0.465042I$	$2.42382 + 0.75571I$	$1.71757 - 3.84156I$
$u = 0.653966 + 0.417174I$	$2.20293 - 2.46586I$	$0.44156 + 5.21162I$
$u = 0.653966 - 0.417174I$	$2.20293 + 2.46586I$	$0.44156 - 5.21162I$
$u = -0.737893 + 0.238500I$	$-4.15809 - 0.23287I$	$-7.53192 + 1.38224I$
$u = -0.737893 - 0.238500I$	$-4.15809 + 0.23287I$	$-7.53192 - 1.38224I$
$u = 0.733536 + 0.221566I$	$0.79810 + 3.87164I$	$-2.73189 - 2.63327I$
$u = 0.733536 - 0.221566I$	$0.79810 - 3.87164I$	$-2.73189 + 2.63327I$
$u = -0.553875 + 1.124130I$	$2.48561 - 7.58332I$	0
$u = -0.553875 - 1.124130I$	$2.48561 + 7.58332I$	0
$u = 0.526277 + 1.142710I$	$-1.85636 + 0.86225I$	0
$u = 0.526277 - 1.142710I$	$-1.85636 - 0.86225I$	0
$u = -0.532862 + 1.141630I$	$-6.76881 - 4.54935I$	0
$u = -0.532862 - 1.141630I$	$-6.76881 + 4.54935I$	0
$u = 0.541979 + 1.140190I$	$-4.39315 + 8.29738I$	0
$u = 0.541979 - 1.140190I$	$-4.39315 - 8.29738I$	0
$u = 0.549916 + 1.137700I$	$-4.09560 + 8.46534I$	0
$u = 0.549916 - 1.137700I$	$-4.09560 - 8.46534I$	0
$u = -0.556243 + 1.140170I$	$-5.85930 - 12.38420I$	0
$u = -0.556243 - 1.140170I$	$-5.85930 + 12.38420I$	0
$u = 0.559891 + 1.140150I$	$-0.5695 + 16.1155I$	0
$u = 0.559891 - 1.140150I$	$-0.5695 - 16.1155I$	0
$u = -0.570709 + 0.131663I$	$3.08005 + 2.48479I$	$-2.33160 - 3.10830I$
$u = -0.570709 - 0.131663I$	$3.08005 - 2.48479I$	$-2.33160 + 3.10830I$
$u = 0.453510$	-1.01886	-9.58030

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^{89} + 43u^{88} + \cdots + u - 1$
$c_2, c_7$	$u^{89} + u^{88} + \cdots + u + 1$
$c_3$	$u^{89} - u^{88} + \cdots + 1497u + 457$
$c_4$	$u^{89} - u^{88} + \cdots - 5u + 1$
$c_5, c_{10}, c_{11}$	$u^{89} + u^{88} + \cdots + 3u + 1$
$c_6, c_{12}$	$u^{89} + 7u^{88} + \cdots + 161u + 5$
$c_8$	$u^{89} + 5u^{88} + \cdots + u + 1$
$c_9$	$u^{89} - 21u^{88} + \cdots - 4023u + 187$

### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{89} + 7y^{88} + \cdots + 13y - 1$
$c_2, c_7$	$y^{89} + 43y^{88} + \cdots + y - 1$
$c_3$	$y^{89} - 29y^{88} + \cdots + 6081637y - 208849$
$c_4$	$y^{89} - 5y^{88} + \cdots + 17y - 1$
$c_5, c_{10}, c_{11}$	$y^{89} + 79y^{88} + \cdots + y - 1$
$c_6, c_{12}$	$y^{89} + 67y^{88} + \cdots + 201y - 25$
$c_8$	$y^{89} - y^{88} + \cdots + 61y - 1$
$c_9$	$y^{89} + 11y^{88} + \cdots - 1504923y - 34969$