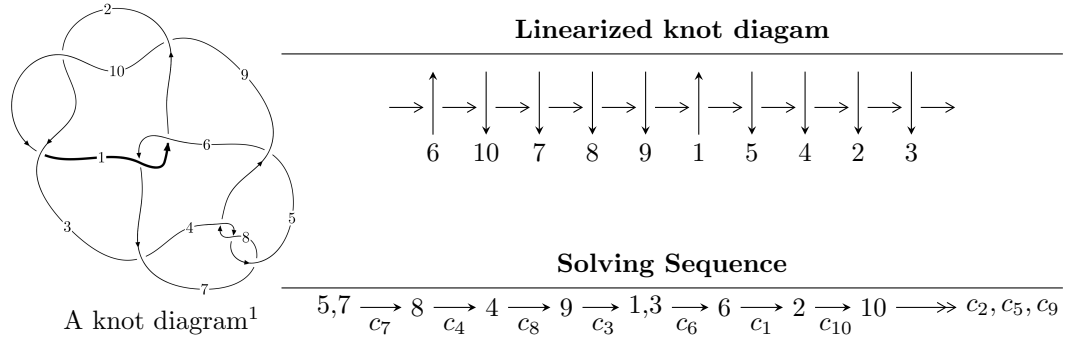


10<sub>50</sub> (K10a<sub>82</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{28} - 2u^{27} + \dots + b + 1, 2u^{28} - 2u^{27} + \dots + a + 2, u^{29} - 2u^{28} + \dots + u - 1 \rangle$$

$$I_2^u = \langle b, u^2 + a + 1, u^3 + u^2 + 2u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 32 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{28} - 2u^{27} + \dots + b + 1, 2u^{28} - 2u^{27} + \dots + a + 2, u^{29} - 2u^{28} + \dots + u - 1 \rangle$$

I.

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2u^{28} + 2u^{27} + \dots - 6u - 2 \\ -u^{28} + 2u^{27} + \dots + u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^5 - 2u^3 - u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{16} - 7u^{14} + \dots - 6u - 1 \\ u^{28} - 2u^{27} + \dots - u^2 + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{28} + u^{27} + \dots - 5u - 1 \\ u^{17} + 7u^{15} + \dots + 6u^2 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = u^{28} - 2u^{27} + 17u^{26} - 28u^{25} + 121u^{24} - 169u^{23} + 476u^{22} - 572u^{21} + 1124u^{20} - 1170u^{19} + 1569u^{18} - 1418u^{17} + 1069u^{16} - 834u^{15} - 98u^{14} + 112u^{13} - 636u^{12} + 544u^{11} - 270u^{10} + 426u^9 - 12u^8 + 183u^7 - 90u^6 - 34u^5 - 38u^4 - 76u^3 + 29u^2 + 2u - 3$$

(iv) u-Polynomials at the component

| Crossings          | u-Polynomials at each crossing       |
|--------------------|--------------------------------------|
| $c_1, c_6$         | $u^{29} + u^{28} + \dots - 4u - 8$   |
| $c_2, c_9, c_{10}$ | $u^{29} - 4u^{28} + \dots + 2u - 1$  |
| $c_3, c_5$         | $u^{29} + 2u^{28} + \dots - 15u - 9$ |
| $c_4, c_7, c_8$    | $u^{29} - 2u^{28} + \dots + u - 1$   |

(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing       |
|--------------------|--|
| $c_1, c_6$         | $y^{29} + 21y^{28} + \cdots + 144y - 64$ |
| $c_2, c_9, c_{10}$ | $y^{29} - 30y^{28} + \cdots + 18y - 1$   |
| $c_3, c_5$         | $y^{29} - 24y^{28} + \cdots + 621y - 81$ |
| $c_4, c_7, c_8$    | $y^{29} + 24y^{28} + \cdots + 13y - 1$   |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = 0.872970 + 0.113870I$<br>$a = 0.23209 + 2.29662I$<br>$b = -0.56484 + 1.49174I$      | $-12.27840 - 6.66801I$                | $-13.30046 + 3.89200I$ |
| $u = 0.872970 - 0.113870I$<br>$a = 0.23209 - 2.29662I$<br>$b = -0.56484 - 1.49174I$      | $-12.27840 + 6.66801I$                | $-13.30046 - 3.89200I$ |
| $u = -0.824312$<br>$a = -1.01744$<br>$b = -1.30242$                                      | $-7.43008$                            | $-12.5870$             |
| $u = 0.814174 + 0.046599I$<br>$a = -0.17300 - 2.55555I$<br>$b = 0.215027 - 1.248980I$    | $-5.26114 - 2.70743I$                 | $-11.83350 + 3.32702I$ |
| $u = 0.814174 - 0.046599I$<br>$a = -0.17300 + 2.55555I$<br>$b = 0.215027 + 1.248980I$    | $-5.26114 + 2.70743I$                 | $-11.83350 - 3.32702I$ |
| $u = 0.050561 + 1.224810I$<br>$a = 1.179120 - 0.735696I$<br>$b = -0.603790 - 0.612719I$  | $1.43725 - 1.10103I$                  | $-6.03106 - 0.28755I$  |
| $u = 0.050561 - 1.224810I$<br>$a = 1.179120 + 0.735696I$<br>$b = -0.603790 + 0.612719I$  | $1.43725 + 1.10103I$                  | $-6.03106 + 0.28755I$  |
| $u = 0.438893 + 1.153290I$<br>$a = 0.614951 + 0.762748I$<br>$b = 0.45548 + 1.52023I$     | $-9.09072 + 1.97634I$                 | $-10.56391 - 0.15391I$ |
| $u = 0.438893 - 1.153290I$<br>$a = 0.614951 - 0.762748I$<br>$b = 0.45548 - 1.52023I$     | $-9.09072 - 1.97634I$                 | $-10.56391 + 0.15391I$ |
| $u = -0.566873 + 0.506506I$<br>$a = -0.914731 + 0.813821I$<br>$b = 0.112616 + 1.303260I$ | $-6.34917 + 2.02688I$                 | $-11.64196 - 3.46616I$ |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = -0.566873 - 0.506506I$<br>$a = -0.914731 - 0.813821I$<br>$b = 0.112616 - 1.303260I$ | $-6.34917 - 2.02688I$                 | $-11.64196 + 3.46616I$ |
| $u = 0.357598 + 1.229040I$<br>$a = -0.75023 - 1.33832I$<br>$b = -0.063501 - 1.233240I$   | $-1.62082 - 1.51334I$                 | $-8.49380 + 0.41799I$  |
| $u = 0.357598 - 1.229040I$<br>$a = -0.75023 + 1.33832I$<br>$b = -0.063501 + 1.233240I$   | $-1.62082 + 1.51334I$                 | $-8.49380 - 0.41799I$  |
| $u = -0.255230 + 1.288030I$<br>$a = 0.111769 - 0.476267I$<br>$b = -0.607413 + 0.112242I$ | $2.53302 + 3.25312I$                  | $-0.46847 - 3.58405I$  |
| $u = -0.255230 - 1.288030I$<br>$a = 0.111769 + 0.476267I$<br>$b = -0.607413 - 0.112242I$ | $2.53302 - 3.25312I$                  | $-0.46847 + 3.58405I$  |
| $u = -0.075468 + 1.316000I$<br>$a = -0.969152 + 0.088875I$<br>$b = 0.538894 + 0.689414I$ | $4.46963 + 2.10537I$                  | $-0.57633 - 3.98592I$  |
| $u = -0.075468 - 1.316000I$<br>$a = -0.969152 - 0.088875I$<br>$b = 0.538894 - 0.689414I$ | $4.46963 - 2.10537I$                  | $-0.57633 + 3.98592I$  |
| $u = -0.369778 + 1.269420I$<br>$a = -0.182052 + 0.874747I$<br>$b = 1.298970 - 0.143296I$ | $-3.48935 + 4.29283I$                 | $-8.53955 - 3.19264I$  |
| $u = -0.369778 - 1.269420I$<br>$a = -0.182052 - 0.874747I$<br>$b = 1.298970 + 0.143296I$ | $-3.48935 - 4.29283I$                 | $-8.53955 + 3.19264I$  |
| $u = 0.361886 + 1.302780I$<br>$a = 1.27373 + 1.39712I$<br>$b = -0.338315 + 1.255880I$    | $-1.04610 - 6.94187I$                 | $-7.09973 + 6.05967I$  |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 0.361886 - 1.302780I$<br>$a = 1.27373 - 1.39712I$<br>$b = -0.338315 - 1.255880I$    | $-1.04610 + 6.94187I$                 | $-7.09973 - 6.05967I$ |
| $u = -0.645651$<br>$a = 0.563691$<br>$b = 0.525371$                                      | $-1.50367$                            | $-5.88400$            |
| $u = 0.389029 + 1.350370I$<br>$a = -1.50604 - 1.16997I$<br>$b = 0.63881 - 1.44580I$      | $-7.67865 - 11.19890I$                | $-9.19156 + 6.17598I$ |
| $u = 0.389029 - 1.350370I$<br>$a = -1.50604 + 1.16997I$<br>$b = 0.63881 + 1.44580I$      | $-7.67865 + 11.19890I$                | $-9.19156 - 6.17598I$ |
| $u = -0.14677 + 1.42338I$<br>$a = 0.845011 + 0.480671I$<br>$b = -0.257766 - 1.113060I$   | $-0.14603 + 4.37313I$                 | $-7.64888 - 4.01970I$ |
| $u = -0.14677 - 1.42338I$<br>$a = 0.845011 - 0.480671I$<br>$b = -0.257766 + 1.113060I$   | $-0.14603 - 4.37313I$                 | $-7.64888 + 4.01970I$ |
| $u = -0.274649 + 0.285133I$<br>$a = 0.844421 - 1.049180I$<br>$b = -0.175226 - 0.644435I$ | $-0.389560 + 0.938777I$               | $-6.80996 - 7.32576I$ |
| $u = -0.274649 - 0.285133I$<br>$a = 0.844421 + 1.049180I$<br>$b = -0.175226 + 0.644435I$ | $-0.389560 - 0.938777I$               | $-6.80996 + 7.32576I$ |
| $u = 0.277276$<br>$a = -2.75803$<br>$b = 0.479164$                                       | $-2.07267$                            | $-2.13090$            |

$$\text{II. } I_2^u = \langle b, u^2 + a + 1, u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^2 + u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 - 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 - 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^2 - 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u^2 + u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5u^2 - 4u - 16$



(iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing |
|---------------|--------------------------------|
| $c_1, c_6$    | $u^3$                          |
| $c_2$         | $(u + 1)^3$                    |
| $c_3, c_5$    | $u^3 + u^2 - 1$                |
| $c_4$         | $u^3 - u^2 + 2u - 1$           |
| $c_7, c_8$    | $u^3 + u^2 + 2u + 1$           |
| $c_9, c_{10}$ | $(u - 1)^3$                    |

(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing |
|--------------------|------------------------------------|
| $c_1, c_6$         | $y^3$                              |
| $c_2, c_9, c_{10}$ | $(y - 1)^3$                        |
| $c_3, c_5$         | $y^3 - y^2 + 2y - 1$               |
| $c_4, c_7, c_8$    | $y^3 + 3y^2 + 2y - 1$              |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.215080 + 1.307140I$<br>$a = 0.662359 + 0.562280I$<br>$b = 0$ | $1.37919 + 2.82812I$                  | $-6.82789 - 2.41717I$ |
| $u = -0.215080 - 1.307140I$<br>$a = 0.662359 - 0.562280I$<br>$b = 0$ | $1.37919 - 2.82812I$                  | $-6.82789 + 2.41717I$ |
| $u = -0.569840$<br>$a = -1.32472$<br>$b = 0$                         | $-2.75839$                            | $-15.3440$            |

### III. u-Polynomials

| Crossings     | u-Polynomials at each crossing                           |
|---------------|--|
| $c_1, c_6$    | $u^3(u^{29} + u^{28} + \dots - 4u - 8)$                  |
| $c_2$         | $((u + 1)^3)(u^{29} - 4u^{28} + \dots + 2u - 1)$         |
| $c_3, c_5$    | $(u^3 + u^2 - 1)(u^{29} + 2u^{28} + \dots - 15u - 9)$    |
| $c_4$         | $(u^3 - u^2 + 2u - 1)(u^{29} - 2u^{28} + \dots + u - 1)$ |
| $c_7, c_8$    | $(u^3 + u^2 + 2u + 1)(u^{29} - 2u^{28} + \dots + u - 1)$ |
| $c_9, c_{10}$ | $((u - 1)^3)(u^{29} - 4u^{28} + \dots + 2u - 1)$         |

#### IV. Riley Polynomials

| Crossings          | Riley Polynomials at each crossing                            |
|--------------------|---|
| $c_1, c_6$         | $y^3(y^{29} + 21y^{28} + \dots + 144y - 64)$                  |
| $c_2, c_9, c_{10}$ | $((y - 1)^3)(y^{29} - 30y^{28} + \dots + 18y - 1)$            |
| $c_3, c_5$         | $(y^3 - y^2 + 2y - 1)(y^{29} - 24y^{28} + \dots + 621y - 81)$ |
| $c_4, c_7, c_8$    | $(y^3 + 3y^2 + 2y - 1)(y^{29} + 24y^{28} + \dots + 13y - 1)$  |