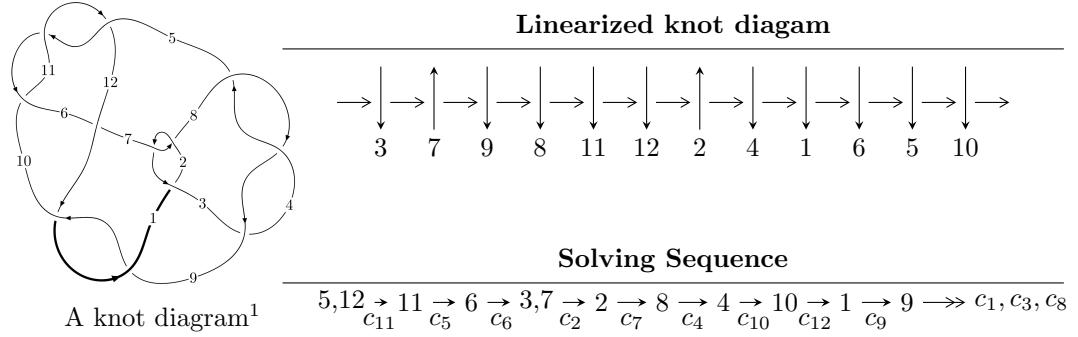


## $12a_{0564}$ ( $K12a_{0564}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -u^{53} + 4u^{52} + \dots + 4b + 4, 2u^{55} - 4u^{54} + \dots + 4a - 12, u^{56} - 2u^{55} + \dots - 5u + 2 \rangle \\
 I_2^u &= \langle a^2u^2 + 2u^2a + 2a^2 - 2u^2 + b + 4a - 4, 2a^2u^2 + a^3 + 2u^2a + 4a^2 + au - 2u^2 + 2a - u - 4, u^3 + 2u - 1 \rangle \\
 I_3^u &= \langle -u^8 + u^7 - 4u^6 + 3u^5 - 4u^4 + 2u^3 + b - u - 1, -u^9 - 5u^7 - 8u^5 - 3u^3 + a + u, \\
 &\quad u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1 \rangle \\
 I_4^u &= \langle 3a^2u^2 - 2u^3a + 4a^2u - 2u^2a + 2u^3 + 2a^2 - 2au + 2u^2 + b + 2u, \\
 &\quad -2u^3a^2 - 2a^2u^2 + 8u^3a + a^3 - 4a^2u + 3u^2a - 2u^3 - 4a^2 + 13au - u^2 + 8a - 3u - 2, \\
 &\quad u^4 + u^3 + 2u^2 + 2u + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 87 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^{53} + 4u^{52} + \dots + 4b + 4, \ 2u^{55} - 4u^{54} + \dots + 4a - 12, \ u^{56} - 2u^{55} + \dots - 5u + 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -\frac{1}{2}u^{55} + u^{54} + \dots - \frac{7}{4}u + 3 \\ \frac{1}{4}u^{53} - u^{52} + \dots + \frac{3}{2}u - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{1}{4}u^{51} + 6u^{49} + \dots + \frac{5}{4}u + 1 \\ -\frac{1}{4}u^{53} - \frac{25}{4}u^{51} + \dots + \frac{1}{2}u^2 + \frac{1}{2}u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{1}{4}u^{55} - \frac{13}{2}u^{53} + \dots - \frac{1}{4}u - 1 \\ \frac{3}{4}u^{55} - u^{54} + \dots + \frac{5}{2}u - 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{1}{4}u^{44} + \frac{21}{4}u^{42} + \dots + \frac{1}{2}u + \frac{1}{2} \\ -\frac{1}{4}u^{44} - 5u^{42} + \dots - \frac{3}{4}u^2 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^6 - 3u^4 - 2u^2 + 1 \\ u^8 + 4u^6 + 4u^4 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1 \\ -u^{12} - 6u^{10} - 12u^8 - 8u^6 - u^4 - 2u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $2u^{55} - 4u^{54} + \dots + 20u - 10$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{56} + 19u^{55} + \cdots - 20u + 1$
$c_2, c_7$	$u^{56} + u^{55} + \cdots - 10u^2 + 1$
$c_3, c_4, c_8$	$u^{56} + u^{55} + \cdots + 2u + 1$
$c_5, c_{10}, c_{11}$	$u^{56} + 2u^{55} + \cdots + 5u + 2$
$c_6$	$u^{56} - 2u^{55} + \cdots - 231u + 202$
$c_9, c_{12}$	$u^{56} - 8u^{55} + \cdots - 1317u + 136$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{56} + 47y^{55} + \cdots + 1224y + 1$
$c_2, c_7$	$y^{56} + 19y^{55} + \cdots - 20y + 1$
$c_3, c_4, c_8$	$y^{56} + 63y^{55} + \cdots - 84y + 1$
$c_5, c_{10}, c_{11}$	$y^{56} + 52y^{55} + \cdots + 19y + 4$
$c_6$	$y^{56} + 20y^{55} + \cdots + 498907y + 40804$
$c_9, c_{12}$	$y^{56} + 48y^{55} + \cdots - 423177y + 18496$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.167031 + 1.023460I$		
$a = 0.581239 + 0.389226I$	$4.78319 + 2.48153I$	$-3.50379 - 2.32484I$
$b = 0.786716 - 0.931788I$		
$u = 0.167031 - 1.023460I$		
$a = 0.581239 - 0.389226I$	$4.78319 - 2.48153I$	$-3.50379 + 2.32484I$
$b = 0.786716 + 0.931788I$		
$u = 0.692071 + 0.437803I$		
$a = -0.66383 - 2.04682I$	$10.54030 - 5.20317I$	$-1.76462 + 3.90235I$
$b = -0.37969 + 1.48563I$		
$u = 0.692071 - 0.437803I$		
$a = -0.66383 + 2.04682I$	$10.54030 + 5.20317I$	$-1.76462 - 3.90235I$
$b = -0.37969 - 1.48563I$		
$u = -0.708508 + 0.410403I$		
$a = 1.96906 - 2.08951I$	$8.5419 + 11.5420I$	$-4.16165 - 8.13234I$
$b = -1.10648 + 2.12776I$		
$u = -0.708508 - 0.410403I$		
$a = 1.96906 + 2.08951I$	$8.5419 - 11.5420I$	$-4.16165 + 8.13234I$
$b = -1.10648 - 2.12776I$		
$u = 0.622613 + 0.525563I$		
$a = 1.77821 + 0.87570I$	$10.86790 + 0.81891I$	$-1.02610 + 2.14303I$
$b = -0.85453 - 1.37150I$		
$u = 0.622613 - 0.525563I$		
$a = 1.77821 - 0.87570I$	$10.86790 - 0.81891I$	$-1.02610 - 2.14303I$
$b = -0.85453 + 1.37150I$		
$u = -0.592033 + 0.557273I$		
$a = -1.57209 + 2.23463I$	$9.08740 - 7.17759I$	$-2.84487 + 2.35339I$
$b = -0.22451 - 1.53219I$		
$u = -0.592033 - 0.557273I$		
$a = -1.57209 - 2.23463I$	$9.08740 + 7.17759I$	$-2.84487 - 2.35339I$
$b = -0.22451 + 1.53219I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.103142 + 1.185330I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.186061 - 0.410343I$	$-0.051945 - 0.385761I$	0
$b = 1.46690 + 0.65983I$		
$u = -0.103142 - 1.185330I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.186061 + 0.410343I$	$-0.051945 + 0.385761I$	0
$b = 1.46690 - 0.65983I$		
$u = 0.669252 + 0.412330I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 2.47043 + 1.87049I$	$2.26755 - 7.24573I$	$-6.66677 + 8.30952I$
$b = -1.39269 - 1.97696I$		
$u = 0.669252 - 0.412330I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 2.47043 - 1.87049I$	$2.26755 + 7.24573I$	$-6.66677 - 8.30952I$
$b = -1.39269 + 1.97696I$		
$u = -0.206699 + 0.752355I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.574163 - 0.045388I$	$4.95627 + 2.53829I$	$-2.18457 - 3.78654I$
$b = 0.468649 - 0.514420I$		
$u = -0.206699 - 0.752355I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.574163 + 0.045388I$	$4.95627 - 2.53829I$	$-2.18457 + 3.78654I$
$b = 0.468649 + 0.514420I$		
$u = 0.582613 + 0.498044I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.36009 - 2.66583I$	$2.62946 + 3.09884I$	$-5.44089 - 2.20028I$
$b = -0.26540 + 1.65618I$		
$u = 0.582613 - 0.498044I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.36009 + 2.66583I$	$2.62946 - 3.09884I$	$-5.44089 + 2.20028I$
$b = -0.26540 - 1.65618I$		
$u = -0.676046 + 0.203719I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.329443 + 0.139721I$	$3.00074 + 0.91231I$	$-5.60324 - 1.33604I$
$b = 0.294607 - 0.292968I$		
$u = -0.676046 - 0.203719I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.329443 - 0.139721I$	$3.00074 - 0.91231I$	$-5.60324 + 1.33604I$
$b = 0.294607 + 0.292968I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.692318 + 0.121292I$		
$a = -0.85392 - 1.33610I$	$2.08625 - 5.88981I$	$-8.03014 + 6.36741I$
$b = 0.25519 + 1.45796I$		
$u = 0.692318 - 0.121292I$		
$a = -0.85392 + 1.33610I$	$2.08625 + 5.88981I$	$-8.03014 - 6.36741I$
$b = 0.25519 - 1.45796I$		
$u = -0.201418 + 1.293670I$		
$a = -0.870058 - 0.579976I$	$1.14651 + 5.97963I$	0
$b = -0.43169 - 1.56082I$		
$u = -0.201418 - 1.293670I$		
$a = -0.870058 + 0.579976I$	$1.14651 - 5.97963I$	0
$b = -0.43169 + 1.56082I$		
$u = 0.261428 + 1.299180I$		
$a = -1.039600 + 0.218945I$	$6.50957 - 9.34599I$	0
$b = -0.49696 + 1.44809I$		
$u = 0.261428 - 1.299180I$		
$a = -1.039600 - 0.218945I$	$6.50957 + 9.34599I$	0
$b = -0.49696 - 1.44809I$		
$u = 0.580660 + 0.311133I$		
$a = 0.0703685 - 0.0523659I$	$-1.38214 - 1.50697I$	$-13.53047 + 3.87884I$
$b = 0.409701 + 0.523982I$		
$u = 0.580660 - 0.311133I$		
$a = 0.0703685 + 0.0523659I$	$-1.38214 + 1.50697I$	$-13.53047 - 3.87884I$
$b = 0.409701 - 0.523982I$		
$u = -0.008074 + 1.347070I$		
$a = 0.668271 + 0.576392I$	$4.43635 - 1.45929I$	0
$b = 0.353028 + 0.821443I$		
$u = -0.008074 - 1.347070I$		
$a = 0.668271 - 0.576392I$	$4.43635 + 1.45929I$	0
$b = 0.353028 - 0.821443I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.521433 + 0.341179I$		
$a = 1.33055 + 0.94373I$	$2.02037 + 1.59760I$	$-0.90500 - 4.85866I$
$b = -0.774976 - 0.280233I$		
$u = -0.521433 - 0.341179I$		
$a = 1.33055 - 0.94373I$	$2.02037 - 1.59760I$	$-0.90500 + 4.85866I$
$b = -0.774976 + 0.280233I$		
$u = -0.246474 + 1.358800I$		
$a = 0.252006 + 0.237582I$	$7.93137 + 4.24929I$	0
$b = -0.157937 - 0.612956I$		
$u = -0.246474 - 1.358800I$		
$a = 0.252006 - 0.237582I$	$7.93137 - 4.24929I$	0
$b = -0.157937 + 0.612956I$		
$u = -0.604464 + 0.090171I$		
$a = -1.22485 + 0.96150I$	$-3.13696 + 3.05067I$	$-15.3053 - 6.1769I$
$b = 0.55744 - 1.31425I$		
$u = -0.604464 - 0.090171I$		
$a = -1.22485 - 0.96150I$	$-3.13696 - 3.05067I$	$-15.3053 + 6.1769I$
$b = 0.55744 + 1.31425I$		
$u = -0.20414 + 1.41040I$		
$a = 0.154106 + 0.721195I$	$7.58921 + 4.29042I$	0
$b = -1.068550 - 0.531298I$		
$u = -0.20414 - 1.41040I$		
$a = 0.154106 - 0.721195I$	$7.58921 - 4.29042I$	0
$b = -1.068550 + 0.531298I$		
$u = 0.22437 + 1.42514I$		
$a = 0.0464407 - 0.0037704I$	$4.20552 - 4.47801I$	0
$b = -0.198621 + 1.070760I$		
$u = 0.22437 - 1.42514I$		
$a = 0.0464407 + 0.0037704I$	$4.20552 + 4.47801I$	0
$b = -0.198621 - 1.070760I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.02481 + 1.45160I$ $a = 0.437034 - 0.432649I$ $b = -0.071252 - 1.121650I$	$11.67150 + 3.02727I$	0
$u = -0.02481 - 1.45160I$ $a = 0.437034 + 0.432649I$ $b = -0.071252 + 1.121650I$	$11.67150 - 3.02727I$	0
$u = 0.24729 + 1.46542I$ $a = 1.75227 - 0.41488I$ $b = -1.92961 - 2.80986I$	$8.32154 - 10.59610I$	0
$u = 0.24729 - 1.46542I$ $a = 1.75227 + 0.41488I$ $b = -1.92961 + 2.80986I$	$8.32154 + 10.59610I$	0
$u = 0.20280 + 1.47543I$ $a = -1.64369 - 0.44402I$ $b = 0.68333 + 2.27056I$	$8.98647 + 0.24581I$	0
$u = 0.20280 - 1.47543I$ $a = -1.64369 + 0.44402I$ $b = 0.68333 - 2.27056I$	$8.98647 - 0.24581I$	0
$u = -0.26313 + 1.47028I$ $a = 1.68249 + 0.12616I$ $b = -1.40694 + 2.97582I$	$14.6067 + 15.0877I$	0
$u = -0.26313 - 1.47028I$ $a = 1.68249 - 0.12616I$ $b = -1.40694 - 2.97582I$	$14.6067 - 15.0877I$	0
$u = 0.25179 + 1.47848I$ $a = -1.236920 - 0.501404I$ $b = -0.07447 + 1.78181I$	$16.7327 - 8.6480I$	0
$u = 0.25179 - 1.47848I$ $a = -1.236920 + 0.501404I$ $b = -0.07447 - 1.78181I$	$16.7327 + 8.6480I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.18754 + 1.49529I$		
$a = -1.54445 + 0.24504I$	$15.7506 - 4.3922I$	0
$b = 0.90159 - 1.78028I$		
$u = -0.18754 - 1.49529I$		
$a = -1.54445 - 0.24504I$	$15.7506 + 4.3922I$	0
$b = 0.90159 + 1.78028I$		
$u = 0.20634 + 1.49448I$		
$a = 1.075950 - 0.501942I$	$17.4257 - 2.1759I$	0
$b = -1.36447 - 1.63496I$		
$u = 0.20634 - 1.49448I$		
$a = 1.075950 + 0.501942I$	$17.4257 + 2.1759I$	0
$b = -1.36447 + 1.63496I$		
$u = 0.147340 + 0.378273I$		
$a = 0.901441 + 0.594340I$	$-0.581405 - 1.167200I$	$-7.43245 + 5.35431I$
$b = 0.521618 + 0.321445I$		
$u = 0.147340 - 0.378273I$		
$a = 0.901441 - 0.594340I$	$-0.581405 + 1.167200I$	$-7.43245 - 5.35431I$
$b = 0.521618 - 0.321445I$		

III.

$$I_2^u = \langle a^2u^2 + 2u^2a + 2a^2 - 2u^2 + b + 4a - 4, 2a^2u^2 + 2u^2a + \dots + 2a - 4, u^3 + 2u - 1 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -a^2u^2 - 2u^2a - 2a^2 + 2u^2 - 4a + 4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a^2u^2 + 2u^2a + 2a^2 + au - 2u^2 + 4a - 4 \\ -2a^2u^2 - 3u^2a - 3a^2 - 2au + 4u^2 - 5a + 6 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 2a^2u^2 + a^2u + 3u^2a + 4a^2 + 2au - 4u^2 + 7a - 2u - 8 \\ -a^2u^2 - a^2u - a^2 - au + 2u^2 - 2a + 2u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a^2u^2 + 2u^2a + 2a^2 + au - 2u^2 + 4a - 4 \\ -2a^2u^2 - 3u^2a - 3a^2 - 2au + 4u^2 - 5a + 6 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ -u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^2 - 4u - 10$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^9 + 6u^8 + 15u^7 + 24u^6 + 31u^5 + 30u^4 + 21u^3 + 12u^2 + 4u - 1$
$c_2, c_3, c_4$ $c_7, c_8$	$u^9 + 3u^7 + 3u^5 + 3u^3 + 2u + 1$
$c_5, c_9, c_{10}$ $c_{11}, c_{12}$	$(u^3 + 2u + 1)^3$
$c_6$	$(u^3 + 3u^2 + 5u + 2)^3$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^9 - 6y^8 - y^7 + 36y^6 + 15y^5 - 42y^4 + 17y^3 + 84y^2 + 40y - 1$
$c_2, c_3, c_4$ $c_7, c_8$	$y^9 + 6y^8 + 15y^7 + 24y^6 + 31y^5 + 30y^4 + 21y^3 + 12y^2 + 4y - 1$
$c_5, c_9, c_{10}$ $c_{11}, c_{12}$	$(y^3 + 4y^2 + 4y - 1)^3$
$c_6$	$(y^3 + y^2 + 13y - 4)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.22670 + 1.46771I$		
$a = -1.41033 + 0.65322I$	$9.44074 + 5.13794I$	$-0.68207 - 3.20902I$
$b = 0.02182 - 2.22338I$		
$u = -0.22670 + 1.46771I$		
$a = 1.44687 + 0.73836I$	$9.44074 + 5.13794I$	$-0.68207 - 3.20902I$
$b = -2.15352 + 1.99644I$		
$u = -0.22670 + 1.46771I$		
$a = 0.169027 - 0.060668I$	$9.44074 + 5.13794I$	$-0.68207 - 3.20902I$
$b = -0.073872 - 1.103970I$		
$u = -0.22670 - 1.46771I$		
$a = -1.41033 - 0.65322I$	$9.44074 - 5.13794I$	$-0.68207 + 3.20902I$
$b = 0.02182 + 2.22338I$		
$u = -0.22670 - 1.46771I$		
$a = 1.44687 - 0.73836I$	$9.44074 - 5.13794I$	$-0.68207 + 3.20902I$
$b = -2.15352 - 1.99644I$		
$u = -0.22670 - 1.46771I$		
$a = 0.169027 + 0.060668I$	$9.44074 - 5.13794I$	$-0.68207 + 3.20902I$
$b = -0.073872 + 1.103970I$		
$u = 0.453398$		
$a = 0.733086$	-0.787199	-12.6360
$b = -0.00791217$		
$u = 0.453398$		
$a = -2.57211 + 0.14119I$	-0.787199	-12.6360
$b = 1.20953 + 0.97910I$		
$u = 0.453398$		
$a = -2.57211 - 0.14119I$	-0.787199	-12.6360
$b = 1.20953 - 0.97910I$		

$$\text{III. } I_3^u = \langle -u^8 + u^7 - 4u^6 + 3u^5 - 4u^4 + 2u^3 + b - u - 1, -u^9 - 5u^7 - 8u^5 - 3u^3 + a + u, u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^9 + 5u^7 + 8u^5 + 3u^3 - u \\ u^8 - u^7 + 4u^6 - 3u^5 + 4u^4 - 2u^3 + u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^9 + 5u^7 - u^6 + 8u^5 - 3u^4 + 3u^3 - 2u^2 - u + 1 \\ 2u^8 - u^7 + 8u^6 - 3u^5 + 8u^4 - 2u^3 + u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^8 - 4u^6 - 5u^4 - 2u^2 - 1 \\ u^9 + 4u^7 + 5u^5 + u^4 + u^3 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^9 + 5u^7 + 8u^5 + 3u^3 - u \\ u^8 - u^7 + 4u^6 - 3u^5 + 4u^4 - 2u^3 + 2u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^6 - 3u^4 - 2u^2 + 1 \\ u^8 + 4u^6 + 4u^4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u^8 + 3u^6 + u^4 - 2u^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4u^6 + 12u^4 + 8u^2 - 8$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^{10}$
$c_2, c_3, c_4$ $c_7, c_8$	$(u^2 + 1)^5$
$c_5, c_{10}, c_{11}$	$u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1$
$c_6$	$u^{10} + u^8 + 8u^6 + 3u^4 + 3u^2 + 1$
$c_9$	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$
$c_{12}$	$(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)^{10}$
$c_2, c_3, c_4$ $c_7, c_8$	$(y + 1)^{10}$
$c_5, c_{10}, c_{11}$	$(y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2$
$c_6$	$(y^5 + y^4 + 8y^3 + 3y^2 + 3y + 1)^2$
$c_9, c_{12}$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.217740I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.821196I$	2.40108	-6.51890
$b = 1.58802 + 0.76683I$		
$u = -1.217740I$		
$a = -0.821196I$	2.40108	-6.51890
$b = 1.58802 - 0.76683I$		
$u = 0.549911 + 0.309916I$		
$a = -1.38013 + 0.77780I$	0.32910 - 1.53058I	-7.48489 + 4.43065I
$b = 1.261070 + 0.218641I$		
$u = 0.549911 - 0.309916I$		
$a = -1.38013 - 0.77780I$	0.32910 + 1.53058I	-7.48489 - 4.43065I
$b = 1.261070 - 0.218641I$		
$u = -0.549911 + 0.309916I$		
$a = 1.38013 + 0.77780I$	0.32910 + 1.53058I	-7.48489 - 4.43065I
$b = -0.383681 - 0.896862I$		
$u = -0.549911 - 0.309916I$		
$a = 1.38013 - 0.77780I$	0.32910 - 1.53058I	-7.48489 + 4.43065I
$b = -0.383681 + 0.896862I$		
$u = -0.21917 + 1.41878I$		
$a = 0.106340 + 0.688402I$	5.87256 + 4.40083I	-3.25569 - 3.49859I
$b = -1.43286 - 1.54951I$		
$u = -0.21917 - 1.41878I$		
$a = 0.106340 - 0.688402I$	5.87256 - 4.40083I	-3.25569 + 3.49859I
$b = -1.43286 + 1.54951I$		
$u = 0.21917 + 1.41878I$		
$a = -0.106340 + 0.688402I$	5.87256 - 4.40083I	-3.25569 + 3.49859I
$b = 0.967447 + 0.638115I$		
$u = 0.21917 - 1.41878I$		
$a = -0.106340 - 0.688402I$	5.87256 + 4.40083I	-3.25569 - 3.49859I
$b = 0.967447 - 0.638115I$		

$$\text{IV. } I_4^u = \langle -2u^3a + 2u^3 + \dots + 2a^2 + b, -2u^3a^2 + 8u^3a + \dots + 8a - 2, u^4 + u^3 + 2u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -3a^2u^2 + 2u^3a - 4a^2u + 2u^2a - 2u^3 - 2a^2 + 2au - 2u^2 - 2u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3a^2 - a^2u^2 - a^2u - u^2a + 2u^3 - au + 2u^2 - a + 4u + 4 \\ -5a^2u^2 + 3u^3a - 6a^2u + 4u^2a - 4u^3 - 3a^2 + 3au - 4u^2 + a - 4u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3a^2 + 2a^2u^2 - 2u^3a + 2a^2u - u^2a + 2u^3 + a^2 - 2au - a + 2u \\ -2u^3a^2 - 2a^2u^2 + u^3a - a^2u - 2u^2a - 2au + 2u^2 - a + 2u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3a^2 - a^2u^2 - a^2u - u^2a + 2u^3 - au + 2u^2 - a + 4u + 4 \\ -5a^2u^2 + 3u^3a - 6a^2u + 4u^2a - 4u^3 - 3a^2 + 3au - 4u^2 + a - 4u - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^3 + 2u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 2u^3 + u^2 + 3u + 3 \\ -u^3 - u^2 - u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 + 2u \\ -u^3 - u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^3 - 4u - 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{12} + 8u^{11} + \cdots + 2u^2 + 1$
$c_2, c_3, c_4$ $c_7, c_8$	$u^{12} + 4u^{10} - u^9 + 6u^8 - 3u^7 + 6u^6 - 3u^5 + 5u^4 - 3u^3 + 2u^2 - 2u + 1$
$c_5, c_9, c_{10}$ $c_{11}, c_{12}$	$(u^4 - u^3 + 2u^2 - 2u + 1)^3$
$c_6$	$(u^2 - u + 1)^6$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{12} - 8y^{11} + \cdots + 4y + 1$
$c_2, c_3, c_4$ $c_7, c_8$	$y^{12} + 8y^{11} + \cdots + 2y^2 + 1$
$c_5, c_9, c_{10}$ $c_{11}, c_{12}$	$(y^4 + 3y^3 + 2y^2 + 1)^3$
$c_6$	$(y^2 + y + 1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.621744 + 0.440597I$		
$a = 0.231503 - 0.048586I$	$3.28987 + 2.02988I$	$-4.00000 - 3.46410I$
$b = 0.496332 - 0.463157I$		
$u = -0.621744 + 0.440597I$		
$a = -0.64313 + 2.57341I$	$3.28987 + 2.02988I$	$-4.00000 - 3.46410I$
$b = -0.45889 - 1.59209I$		
$u = -0.621744 + 0.440597I$		
$a = 2.55302 - 1.00733I$	$3.28987 + 2.02988I$	$-4.00000 - 3.46410I$
$b = -1.42232 + 1.41895I$		
$u = -0.621744 - 0.440597I$		
$a = 0.231503 + 0.048586I$	$3.28987 - 2.02988I$	$-4.00000 + 3.46410I$
$b = 0.496332 + 0.463157I$		
$u = -0.621744 - 0.440597I$		
$a = -0.64313 - 2.57341I$	$3.28987 - 2.02988I$	$-4.00000 + 3.46410I$
$b = -0.45889 + 1.59209I$		
$u = -0.621744 - 0.440597I$		
$a = 2.55302 + 1.00733I$	$3.28987 - 2.02988I$	$-4.00000 + 3.46410I$
$b = -1.42232 - 1.41895I$		
$u = 0.121744 + 1.306620I$		
$a = -0.305126 + 1.095260I$	$3.28987 - 2.02988I$	$-4.00000 + 3.46410I$
$b = -0.07449 + 1.73534I$		
$u = 0.121744 + 1.306620I$		
$a = -0.365118 + 0.741654I$	$3.28987 - 2.02988I$	$-4.00000 + 3.46410I$
$b = 2.37156 - 0.58328I$		
$u = 0.121744 + 1.306620I$		
$a = 0.528852 - 0.319426I$	$3.28987 - 2.02988I$	$-4.00000 + 3.46410I$
$b = 0.0878104 - 0.0563109I$		
$u = 0.121744 - 1.306620I$		
$a = -0.305126 - 1.095260I$	$3.28987 + 2.02988I$	$-4.00000 - 3.46410I$
$b = -0.07449 - 1.73534I$		

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.121744 - 1.306620I$		
$a = -0.365118 - 0.741654I$	$3.28987 + 2.02988I$	$-4.00000 - 3.46410I$
$b = 2.37156 + 0.58328I$		
$u = 0.121744 - 1.306620I$		
$a = 0.528852 + 0.319426I$	$3.28987 + 2.02988I$	$-4.00000 - 3.46410I$
$b = 0.0878104 + 0.0563109I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^{10}$ $\cdot (u^9 + 6u^8 + 15u^7 + 24u^6 + 31u^5 + 30u^4 + 21u^3 + 12u^2 + 4u - 1)$ $\cdot (u^{12} + 8u^{11} + \dots + 2u^2 + 1)(u^{56} + 19u^{55} + \dots - 20u + 1)$
$c_2, c_7$	$(u^2 + 1)^5(u^9 + 3u^7 + 3u^5 + 3u^3 + 2u + 1)$ $\cdot (u^{12} + 4u^{10} - u^9 + 6u^8 - 3u^7 + 6u^6 - 3u^5 + 5u^4 - 3u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{56} + u^{55} + \dots - 10u^2 + 1)$
$c_3, c_4, c_8$	$(u^2 + 1)^5(u^9 + 3u^7 + 3u^5 + 3u^3 + 2u + 1)$ $\cdot (u^{12} + 4u^{10} - u^9 + 6u^8 - 3u^7 + 6u^6 - 3u^5 + 5u^4 - 3u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{56} + u^{55} + \dots + 2u + 1)$
$c_5, c_{10}, c_{11}$	$((u^3 + 2u + 1)^3)(u^4 - u^3 + 2u^2 - 2u + 1)^3(u^{10} + 5u^8 + \dots - u^2 + 1)$ $\cdot (u^{56} + 2u^{55} + \dots + 5u + 2)$
$c_6$	$(u^2 - u + 1)^6(u^3 + 3u^2 + 5u + 2)^3(u^{10} + u^8 + 8u^6 + 3u^4 + 3u^2 + 1)$ $\cdot (u^{56} - 2u^{55} + \dots - 231u + 202)$
$c_9$	$(u^3 + 2u + 1)^3(u^4 - u^3 + 2u^2 - 2u + 1)^3(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$ $\cdot (u^{56} - 8u^{55} + \dots - 1317u + 136)$
$c_{12}$	$(u^3 + 2u + 1)^3(u^4 - u^3 + 2u^2 - 2u + 1)^3(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$ $\cdot (u^{56} - 8u^{55} + \dots - 1317u + 136)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)^{10}$ $\cdot (y^9 - 6y^8 - y^7 + 36y^6 + 15y^5 - 42y^4 + 17y^3 + 84y^2 + 40y - 1)$ $\cdot (y^{12} - 8y^{11} + \dots + 4y + 1)(y^{56} + 47y^{55} + \dots + 1224y + 1)$
$c_2, c_7$	$(y + 1)^{10}$ $\cdot (y^9 + 6y^8 + 15y^7 + 24y^6 + 31y^5 + 30y^4 + 21y^3 + 12y^2 + 4y - 1)$ $\cdot (y^{12} + 8y^{11} + \dots + 2y^2 + 1)(y^{56} + 19y^{55} + \dots - 20y + 1)$
$c_3, c_4, c_8$	$(y + 1)^{10}$ $\cdot (y^9 + 6y^8 + 15y^7 + 24y^6 + 31y^5 + 30y^4 + 21y^3 + 12y^2 + 4y - 1)$ $\cdot (y^{12} + 8y^{11} + \dots + 2y^2 + 1)(y^{56} + 63y^{55} + \dots - 84y + 1)$
$c_5, c_{10}, c_{11}$	$(y^3 + 4y^2 + 4y - 1)^3(y^4 + 3y^3 + 2y^2 + 1)^3$ $\cdot ((y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2)(y^{56} + 52y^{55} + \dots + 19y + 4)$
$c_6$	$(y^2 + y + 1)^6(y^3 + y^2 + 13y - 4)^3(y^5 + y^4 + 8y^3 + 3y^2 + 3y + 1)^2$ $\cdot (y^{56} + 20y^{55} + \dots + 498907y + 40804)$
$c_9, c_{12}$	$(y^3 + 4y^2 + 4y - 1)^3(y^4 + 3y^3 + 2y^2 + 1)^3$ $\cdot ((y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2)(y^{56} + 48y^{55} + \dots - 423177y + 18496)$