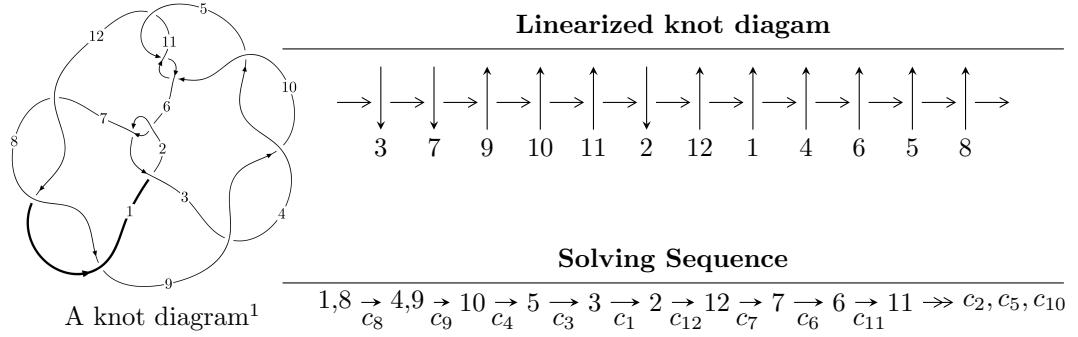


## $12a_{0577}$ ( $K12a_{0577}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -2.56312 \times 10^{33}u^{48} + 2.83092 \times 10^{33}u^{47} + \dots + 7.56342 \times 10^{33}b + 4.45246 \times 10^{32}, \\
 &\quad - 1.28759 \times 10^{35}u^{48} + 2.69158 \times 10^{35}u^{47} + \dots + 1.21015 \times 10^{35}a + 9.76615 \times 10^{34}, u^{49} - 2u^{48} + \dots - u + \\
 I_2^u &= \langle -u^5 + u^3 + b - u, u^3 + a, u^{18} - 6u^{16} + \dots - u - 1 \rangle \\
 I_3^u &= \langle b + 1, a^4 - 4a^3 + 3a^2 + 2a + 1, u + 1 \rangle \\
 I_4^u &= \langle b - 1, a^4 + 4a^3 + 5a^2 + 2a - 1, u - 1 \rangle \\
 I_5^u &= \langle b + 1, a - 1, u + 1 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 76 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

**I.**

$$I_1^u = \langle -2.56 \times 10^{33}u^{48} + 2.83 \times 10^{33}u^{47} + \dots + 7.56 \times 10^{33}b + 4.45 \times 10^{32}, -1.29 \times 10^{35}u^{48} + 2.69 \times 10^{35}u^{47} + \dots + 1.21 \times 10^{35}a + 9.77 \times 10^{34}, u^{49} - 2u^{48} + \dots - u + 1 \rangle$$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1.06400u^{48} - 2.22417u^{47} + \dots - 66.3671u - 0.807022 \\ 0.338884u^{48} - 0.374291u^{47} + \dots - 9.12038u - 0.0588683 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0728905u^{48} + 0.0869859u^{47} + \dots - 20.9570u - 12.0327 \\ -0.0255946u^{48} - 0.118358u^{47} + \dots + 0.625886u - 1.30939 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.437918u^{48} + 0.654552u^{47} + \dots + 53.0608u + 0.351204 \\ 0.194691u^{48} - 0.265650u^{47} + \dots + 6.68311u + 0.189616 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.998861u^{48} - 2.15004u^{47} + \dots - 56.0865u - 0.844336 \\ 0.314692u^{48} - 0.206403u^{47} + \dots - 9.12938u - 0.115001 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.24728u^{48} - 2.43234u^{47} + \dots - 64.0218u - 0.840988 \\ 0.0651347u^{48} - 0.0741368u^{47} + \dots - 9.28056u + 0.0373145 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0588683u^{48} + 0.221147u^{47} + \dots - 22.4060u - 9.17925 \\ -0.0961828u^{48} - 0.0813832u^{47} + \dots + 0.256973u - 1.06400 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.471607u^{48} + 1.41230u^{47} + \dots - 23.3549u - 5.40971 \\ -0.141421u^{48} + 0.0729172u^{47} + \dots + 2.01016u - 1.08423 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-0.776631u^{48} + 0.563664u^{47} + \dots + 20.3985u + 3.27444$

**(iv) u-Polynomials at the component**

| Crossings             | u-Polynomials at each crossing         |
|-----------------------|--|
| $c_1$                 | $u^{49} + 16u^{48} + \cdots + 51u + 1$ |
| $c_2, c_6$            | $u^{49} - 2u^{48} + \cdots + 3u - 1$   |
| $c_3, c_4, c_9$       | $u^{49} + 2u^{48} + \cdots - 24u + 16$ |
| $c_5, c_{10}, c_{11}$ | $u^{49} - 2u^{48} + \cdots - 2u + 2$   |
| $c_7, c_8, c_{12}$    | $u^{49} + 2u^{48} + \cdots - u - 1$    |

**(v) Riley Polynomials at the component**

| Crossings             | Riley Polynomials at each crossing         |
|-----------------------|--|
| $c_1$                 | $y^{49} + 44y^{48} + \cdots + 1819y - 1$   |
| $c_2, c_6$            | $y^{49} - 16y^{48} + \cdots + 51y - 1$     |
| $c_3, c_4, c_9$       | $y^{49} - 50y^{48} + \cdots - 8256y - 256$ |
| $c_5, c_{10}, c_{11}$ | $y^{49} + 38y^{48} + \cdots + 8y - 4$      |
| $c_7, c_8, c_{12}$    | $y^{49} - 56y^{48} + \cdots + 99y - 1$     |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.506103 + 0.862902I$ |                                       |                       |
| $a = 0.500355 + 1.042960I$  | $3.13730 - 0.87606I$                  | $7.33623 + 1.94038I$  |
| $b = 0.781459 + 0.968591I$  |                                       |                       |
| $u = -0.506103 - 0.862902I$ |                                       |                       |
| $a = 0.500355 - 1.042960I$  | $3.13730 + 0.87606I$                  | $7.33623 - 1.94038I$  |
| $b = 0.781459 - 0.968591I$  |                                       |                       |
| $u = -0.441469 + 0.898603I$ |                                       |                       |
| $a = 0.587546 + 0.830187I$  | $2.66998 - 10.11010I$                 | $6.39603 + 7.85117I$  |
| $b = 1.30109 + 0.70065I$    |                                       |                       |
| $u = -0.441469 - 0.898603I$ |                                       |                       |
| $a = 0.587546 - 0.830187I$  | $2.66998 + 10.11010I$                 | $6.39603 - 7.85117I$  |
| $b = 1.30109 - 0.70065I$    |                                       |                       |
| $u = 0.473125 + 0.885514I$  |                                       |                       |
| $a = -0.561307 + 0.937339I$ | $6.86021 + 5.51403I$                  | $10.47160 - 5.14621I$ |
| $b = -1.076850 + 0.869299I$ |                                       |                       |
| $u = 0.473125 - 0.885514I$  |                                       |                       |
| $a = -0.561307 - 0.937339I$ | $6.86021 - 5.51403I$                  | $10.47160 + 5.14621I$ |
| $b = -1.076850 - 0.869299I$ |                                       |                       |
| $u = 1.06485$               |                                       |                       |
| $a = 1.21417$               | 5.55834                               | 16.5270               |
| $b = -0.142650$             |                                       |                       |
| $u = -1.080520 + 0.079944I$ |                                       |                       |
| $a = -1.207880 + 0.284396I$ | $1.65369 - 3.96617I$                  | $11.77753 + 3.57951I$ |
| $b = 0.160341 - 0.198571I$  |                                       |                       |
| $u = -1.080520 - 0.079944I$ |                                       |                       |
| $a = -1.207880 - 0.284396I$ | $1.65369 + 3.96617I$                  | $11.77753 - 3.57951I$ |
| $b = 0.160341 + 0.198571I$  |                                       |                       |
| $u = 0.272859 + 0.717075I$  |                                       |                       |
| $a = 0.097380 + 0.638899I$  | $-4.96406 + 6.00920I$                 | $0.78370 - 7.92298I$  |
| $b = -0.442768 - 0.568471I$ |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = 0.272859 - 0.717075I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $0.78370 + 7.92298I$ |
| $a = 0.097380 - 0.638899I$  | $-4.96406 - 6.00920I$                 |                      |
| $b = -0.442768 + 0.568471I$ |                                       |                      |
| $u = 0.635672 + 0.423399I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $7.38226 - 4.62534I$ |
| $a = 0.152656 + 0.981747I$  | $-1.98468 + 1.46890I$                 |                      |
| $b = 0.481748 - 0.043197I$  |                                       |                      |
| $u = 0.635672 - 0.423399I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $7.38226 + 4.62534I$ |
| $a = 0.152656 - 0.981747I$  | $-1.98468 - 1.46890I$                 |                      |
| $b = 0.481748 + 0.043197I$  |                                       |                      |
| $u = -0.377239 + 0.635400I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $7.57049 + 8.69582I$ |
| $a = -0.042557 + 0.925611I$ | $-0.22370 - 3.57957I$                 |                      |
| $b = 0.106013 - 0.171567I$  |                                       |                      |
| $u = -0.377239 - 0.635400I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $7.57049 - 8.69582I$ |
| $a = -0.042557 - 0.925611I$ | $-0.22370 + 3.57957I$                 |                      |
| $b = 0.106013 + 0.171567I$  |                                       |                      |
| $u = -0.629729$             |                                       |                      |
| $a = 0.0259489$             | $0.715837$                            | $14.7920$            |
| $b = -0.419260$             |                                       |                      |
| $u = 1.367690 + 0.118584I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $0$                  |
| $a = -0.083488 - 0.457258I$ | $-1.71441 + 2.34609I$                 |                      |
| $b = 0.151194 - 0.356963I$  |                                       |                      |
| $u = 1.367690 - 0.118584I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $0$                  |
| $a = -0.083488 + 0.457258I$ | $-1.71441 - 2.34609I$                 |                      |
| $b = 0.151194 + 0.356963I$  |                                       |                      |
| $u = -1.370000 + 0.090098I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $0$                  |
| $a = -1.174840 + 0.183507I$ | $2.02971 - 4.19323I$                  |                      |
| $b = 1.076130 + 0.107236I$  |                                       |                      |
| $u = -1.370000 - 0.090098I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $0$                  |
| $a = -1.174840 - 0.183507I$ | $2.02971 + 4.19323I$                  |                      |
| $b = 1.076130 - 0.107236I$  |                                       |                      |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.45161 + 0.04249I$    |                                       |            |
| $a = 0.952579 - 0.218245I$  | $6.85291 + 0.94088I$                  | 0          |
| $b = -1.17797 + 0.84568I$   |                                       |            |
| $u = 1.45161 - 0.04249I$    |                                       |            |
| $a = 0.952579 + 0.218245I$  | $6.85291 - 0.94088I$                  | 0          |
| $b = -1.17797 - 0.84568I$   |                                       |            |
| $u = -1.43096 + 0.24886I$   |                                       |            |
| $a = 1.232470 + 0.036520I$  | $0.52977 - 9.47056I$                  | 0          |
| $b = -1.54657 - 0.17959I$   |                                       |            |
| $u = -1.43096 - 0.24886I$   |                                       |            |
| $a = 1.232470 - 0.036520I$  | $0.52977 + 9.47056I$                  | 0          |
| $b = -1.54657 + 0.17959I$   |                                       |            |
| $u = -1.46839 + 0.13155I$   |                                       |            |
| $a = 0.244748 + 0.347671I$  | $4.54898 - 2.99003I$                  | 0          |
| $b = -0.535951 - 1.225870I$ |                                       |            |
| $u = -1.46839 - 0.13155I$   |                                       |            |
| $a = 0.244748 - 0.347671I$  | $4.54898 + 2.99003I$                  | 0          |
| $b = -0.535951 + 1.225870I$ |                                       |            |
| $u = -1.48327 + 0.04934I$   |                                       |            |
| $a = -0.376466 + 0.449946I$ | $4.87290 - 2.72445I$                  | 0          |
| $b = 0.38527 - 1.44906I$    |                                       |            |
| $u = -1.48327 - 0.04934I$   |                                       |            |
| $a = -0.376466 - 0.449946I$ | $4.87290 + 2.72445I$                  | 0          |
| $b = 0.38527 + 1.44906I$    |                                       |            |
| $u = 1.47136 + 0.20824I$    |                                       |            |
| $a = -0.878047 + 0.378522I$ | $5.80687 + 6.61465I$                  | 0          |
| $b = 1.42808 - 0.90342I$    |                                       |            |
| $u = 1.47136 - 0.20824I$    |                                       |            |
| $a = -0.878047 - 0.378522I$ | $5.80687 - 6.61465I$                  | 0          |
| $b = 1.42808 + 0.90342I$    |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.315421 + 0.397601I$  |                                       |                       |
| $a = 0.039889 + 1.284920I$  | $-1.36715 + 1.10974I$                 | $0.89311 - 1.51851I$  |
| $b = 0.405532 - 0.300525I$  |                                       |                       |
| $u = 0.315421 - 0.397601I$  |                                       |                       |
| $a = 0.039889 - 1.284920I$  | $-1.36715 - 1.10974I$                 | $0.89311 + 1.51851I$  |
| $b = 0.405532 + 0.300525I$  |                                       |                       |
| $u = -0.094951 + 0.466215I$ |                                       |                       |
| $a = -0.95838 + 1.34005I$   | $-6.38447 - 0.32683I$                 | $-3.51715 + 0.79678I$ |
| $b = -0.572924 - 0.727360I$ |                                       |                       |
| $u = -0.094951 - 0.466215I$ |                                       |                       |
| $a = -0.95838 - 1.34005I$   | $-6.38447 + 0.32683I$                 | $-3.51715 - 0.79678I$ |
| $b = -0.572924 + 0.727360I$ |                                       |                       |
| $u = 1.52723 + 0.33642I$    |                                       |                       |
| $a = -1.97469 + 0.88742I$   | $9.0434 + 14.6216I$                   | 0                     |
| $b = 3.60061 - 0.27568I$    |                                       |                       |
| $u = 1.52723 - 0.33642I$    |                                       |                       |
| $a = -1.97469 - 0.88742I$   | $9.0434 - 14.6216I$                   | 0                     |
| $b = 3.60061 + 0.27568I$    |                                       |                       |
| $u = -1.53962 + 0.32307I$   |                                       |                       |
| $a = 1.85586 + 0.99438I$    | $13.4023 - 9.9407I$                   | 0                     |
| $b = -3.59315 - 0.63275I$   |                                       |                       |
| $u = -1.53962 - 0.32307I$   |                                       |                       |
| $a = 1.85586 - 0.99438I$    | $13.4023 + 9.9407I$                   | 0                     |
| $b = -3.59315 + 0.63275I$   |                                       |                       |
| $u = 1.54894 + 0.30323I$    |                                       |                       |
| $a = -1.67927 + 1.07256I$   | $9.85027 + 5.15212I$                  | 0                     |
| $b = 3.42720 - 1.03218I$    |                                       |                       |
| $u = 1.54894 - 0.30323I$    |                                       |                       |
| $a = -1.67927 - 1.07256I$   | $9.85027 - 5.15212I$                  | 0                     |
| $b = 3.42720 + 1.03218I$    |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = 1.57332 + 0.22114I$    |                                       |                      |
| $a = 2.12554 - 0.50767I$    | $11.13740 + 8.11094I$                 | 0                    |
| $b = -3.82426 - 0.00661I$   |                                       |                      |
| $u = 1.57332 - 0.22114I$    |                                       |                      |
| $a = 2.12554 + 0.50767I$    | $11.13740 - 8.11094I$                 | 0                    |
| $b = -3.82426 + 0.00661I$   |                                       |                      |
| $u = -1.58534 + 0.20019I$   |                                       |                      |
| $a = -2.05798 - 0.63877I$   | $15.3567 - 3.3643I$                   | 0                    |
| $b = 3.85771 + 0.41371I$    |                                       |                      |
| $u = -1.58534 - 0.20019I$   |                                       |                      |
| $a = -2.05798 + 0.63877I$   | $15.3567 + 3.3643I$                   | 0                    |
| $b = 3.85771 - 0.41371I$    |                                       |                      |
| $u = 1.59138 + 0.17411I$    |                                       |                      |
| $a = 1.93614 - 0.75434I$    | $11.62880 - 1.45194I$                 | 0                    |
| $b = -3.71746 + 0.86616I$   |                                       |                      |
| $u = 1.59138 - 0.17411I$    |                                       |                      |
| $a = 1.93614 + 0.75434I$    | $11.62880 + 1.45194I$                 | 0                    |
| $b = -3.71746 - 0.86616I$   |                                       |                      |
| $u = -0.121685 + 0.105182I$ |                                       |                      |
| $a = 6.95371 + 3.79591I$    | $-1.63772 - 4.11971I$                 | $0.12488 + 3.37346I$ |
| $b = 1.189100 - 0.168206I$  |                                       |                      |
| $u = -0.121685 - 0.105182I$ |                                       |                      |
| $a = 6.95371 - 3.79591I$    | $-1.63772 + 4.11971I$                 | $0.12488 - 3.37346I$ |
| $b = 1.189100 + 0.168206I$  |                                       |                      |
| $u = 0.106744$              |                                       |                      |
| $a = -11.6080$              | 2.32826                               | 4.47140              |
| $b = -1.16523$              |                                       |                      |

$$\text{II. } I_2^u = \langle -u^5 + u^3 + b - u, \ u^3 + a, \ u^{18} - 6u^{16} + \cdots - u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^6 + u^4 + 1 \\ u^8 - 2u^6 + 2u^4 - 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^9 - 2u^7 + u^5 - 2u^3 + u \\ -u^{11} + 3u^9 - 4u^7 + 5u^5 - 3u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{16} - 5u^{14} + 11u^{12} - 16u^{10} + 17u^8 - 14u^6 + 8u^4 - 2u^2 + 1 \\ -u^{16} + 4u^{14} - 6u^{12} + 6u^{10} - 4u^8 + 2u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^9 + 12u^7 - 12u^5 + 12u^3 - 8u + 10$

**(iv) u-Polynomials at the component**

| Crossings                        | u-Polynomials at each crossing               |
|----------------------------------|--|
| $c_1$                            | $u^{18} + 12u^{17} + \cdots + 5u + 1$        |
| $c_2, c_6, c_7$<br>$c_8, c_{12}$ | $u^{18} - 6u^{16} + \cdots + u - 1$          |
| $c_3, c_4, c_9$                  | $(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)^3$ |
| $c_5, c_{10}, c_{11}$            | $(u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1)^3$ |

**(v) Riley Polynomials at the component**

| Crossings                        | Riley Polynomials at each crossing               |
|----------------------------------|--|
| $c_1$                            | $y^{18} - 12y^{17} + \cdots + 7y + 1$            |
| $c_2, c_6, c_7$<br>$c_8, c_{12}$ | $y^{18} - 12y^{17} + \cdots - 5y + 1$            |
| $c_3, c_4, c_9$                  | $(y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1)^3$ |
| $c_5, c_{10}, c_{11}$            | $(y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1)^3$   |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.672231 + 0.755934I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = -0.848635 - 0.592839I$ | $3.69558 - 4.59213I$                  | $8.58114 + 3.20482I$ |
| $b = -1.019800 - 0.770263I$ |                                       |                      |
| $u = -0.672231 - 0.755934I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = -0.848635 + 0.592839I$ | $3.69558 + 4.59213I$                  | $8.58114 - 3.20482I$ |
| $b = -1.019800 + 0.770263I$ |                                       |                      |
| $u = 0.945797 + 0.372369I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = -0.452617 - 0.947657I$ | $-2.96024 - 1.97241I$                 | $4.57572 + 3.68478I$ |
| $b = 0.167799 + 0.459832I$  |                                       |                      |
| $u = 0.945797 - 0.372369I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = -0.452617 + 0.947657I$ | $-2.96024 + 1.97241I$                 | $4.57572 - 3.68478I$ |
| $b = 0.167799 - 0.459832I$  |                                       |                      |
| $u = 0.719335 + 0.743187I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = 0.819709 - 0.743187I$  | $7.66009$                             | $12.26950 + 0.I$     |
| $b = 0.773023 - 0.902358I$  |                                       |                      |
| $u = 0.719335 - 0.743187I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = 0.819709 + 0.743187I$  | $7.66009$                             | $12.26950 + 0.I$     |
| $b = 0.773023 + 0.902358I$  |                                       |                      |
| $u = -0.763761 + 0.724480I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = -0.757105 - 0.887576I$ | $3.69558 + 4.59213I$                  | $8.58114 - 3.20482I$ |
| $b = -0.494362 - 0.949066I$ |                                       |                      |
| $u = -0.763761 - 0.724480I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = -0.757105 + 0.887576I$ | $3.69558 - 4.59213I$                  | $8.58114 + 3.20482I$ |
| $b = -0.494362 + 0.949066I$ |                                       |                      |
| $u = 1.18645$               | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = -1.67012$              | $0.738851$                            | $13.4170$            |
| $b = 1.86730$               |                                       |                      |
| $u = -1.219960 + 0.167385I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = 1.71314 - 0.74267I$    | $-2.96024 - 1.97241I$                 | $4.57572 + 3.68478I$ |
| $b = -1.70520 + 1.20889I$   |                                       |                      |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -1.219960 - 0.167385I$ |                                       |                      |
| $a = 1.71314 + 0.74267I$    | $-2.96024 + 1.97241I$                 | $4.57572 - 3.68478I$ |
| $b = -1.70520 - 1.20889I$   |                                       |                      |
| $u = -0.593225 + 0.236109I$ |                                       |                      |
| $a = 0.109553 - 0.236109I$  | 0.738851                              | $13.41678 + 0.I$     |
| $b = -0.449977 + 0.100617I$ |                                       |                      |
| $u = -0.593225 - 0.236109I$ |                                       |                      |
| $a = 0.109553 + 0.236109I$  | 0.738851                              | $13.41678 + 0.I$     |
| $b = -0.449977 - 0.100617I$ |                                       |                      |
| $u = 0.274166 + 0.539754I$  |                                       |                      |
| $a = 0.219014 + 0.035534I$  | $-2.96024 + 1.97241I$                 | $4.57572 - 3.68478I$ |
| $b = 0.551041 + 0.518149I$  |                                       |                      |
| $u = 0.274166 - 0.539754I$  |                                       |                      |
| $a = 0.219014 - 0.035534I$  | $-2.96024 - 1.97241I$                 | $4.57572 + 3.68478I$ |
| $b = 0.551041 - 0.518149I$  |                                       |                      |
| $u = 1.43599 + 0.03145I$    |                                       |                      |
| $a = -2.95686 - 0.19455I$   | $3.69558 + 4.59213I$                  | $8.58114 - 3.20482I$ |
| $b = 4.55589 + 0.50499I$    |                                       |                      |
| $u = 1.43599 - 0.03145I$    |                                       |                      |
| $a = -2.95686 + 0.19455I$   | $3.69558 - 4.59213I$                  | $8.58114 + 3.20482I$ |
| $b = 4.55589 - 0.50499I$    |                                       |                      |
| $u = -1.43867$              |                                       |                      |
| $a = 2.97771$               | 7.66009                               | 12.2690              |
| $b = -4.62413$              |                                       |                      |

$$\text{III. } I_3^u = \langle b + 1, a^4 - 4a^3 + 3a^2 + 2a + 1, u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -a^2 + a + 1 \\ a - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a^3 + 2a^2 + a - 1 \\ a^2 - 3a + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ a - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ a - 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ a - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^3 - 4a^2 + 3a + 1 \\ -a^3 + 5a^2 - 5a - 3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4a^2 + 8a + 8$

**(iv) u-Polynomials at the component**

| Crossings             | u-Polynomials at each crossing |
|-----------------------|--------------------------------|
| $c_1, c_2, c_{12}$    | $(u - 1)^4$                    |
| $c_3, c_4, c_9$       | $u^4 - 3u^2 + 3$               |
| $c_5, c_{10}, c_{11}$ | $u^4 + 3u^2 + 3$               |
| $c_6, c_7, c_8$       | $(u + 1)^4$                    |

**(v) Riley Polynomials at the component**

| Crossings                             | Riley Polynomials at each crossing |
|---------------------------------------|------------------------------------|
| $c_1, c_2, c_6$<br>$c_7, c_8, c_{12}$ | $(y - 1)^4$                        |
| $c_3, c_4, c_9$                       | $(y^2 - 3y + 3)^2$                 |
| $c_5, c_{10}, c_{11}$                 | $(y^2 + 3y + 3)^2$                 |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -1.00000$              |                                       |                      |
| $a = -0.271230 + 0.340625I$ | $- 4.05977I$                          | $6.00000 + 3.46410I$ |
| $b = -1.00000$              |                                       |                      |
| $u = -1.00000$              |                                       |                      |
| $a = -0.271230 - 0.340625I$ | $4.05977I$                            | $6.00000 - 3.46410I$ |
| $b = -1.00000$              |                                       |                      |
| $u = -1.00000$              |                                       |                      |
| $a = 2.27123 + 0.34063I$    | $4.05977I$                            | $6.00000 - 3.46410I$ |
| $b = -1.00000$              |                                       |                      |
| $u = -1.00000$              |                                       |                      |
| $a = 2.27123 - 0.34063I$    | $- 4.05977I$                          | $6.00000 + 3.46410I$ |
| $b = -1.00000$              |                                       |                      |

$$\text{IV. } I_4^u = \langle b - 1, a^4 + 4a^3 + 5a^2 + 2a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -a^2 - a + 1 \\ -a - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a^3 - 2a^2 + a + 1 \\ -a^2 - 3a - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ a + 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ a + 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -a - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -a^3 - 4a^2 - 3a + 1 \\ a^3 + 3a^2 + a - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4a^2 + 8a + 8$

**(iv) u-Polynomials at the component**

| Crossings                | u-Polynomials at each crossing |
|--------------------------|--------------------------------|
| $c_1, c_6, c_7$<br>$c_8$ | $(u - 1)^4$                    |
| $c_2, c_{12}$            | $(u + 1)^4$                    |
| $c_3, c_4, c_9$          | $u^4 - u^2 - 1$                |
| $c_5, c_{10}, c_{11}$    | $u^4 + u^2 - 1$                |

**(v) Riley Polynomials at the component**

| Crossings                             | Riley Polynomials at each crossing |
|---------------------------------------|------------------------------------|
| $c_1, c_2, c_6$<br>$c_7, c_8, c_{12}$ | $(y - 1)^4$                        |
| $c_3, c_4, c_9$                       | $(y^2 - y - 1)^2$                  |
| $c_5, c_{10}, c_{11}$                 | $(y^2 + y - 1)^2$                  |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_4^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape      |
|-----------------------------|---------------------------------------|-----------------|
| $u = 1.00000$               |                                       |                 |
| $a = -1.000000 + 0.786151I$ | -3.94784                              | $1.52786 + 0.I$ |
| $b = 1.00000$               |                                       |                 |
| $u = 1.00000$               |                                       |                 |
| $a = -1.000000 - 0.786151I$ | -3.94784                              | $1.52786 + 0.I$ |
| $b = 1.00000$               |                                       |                 |
| $u = 1.00000$               |                                       |                 |
| $a = 0.272020$              | 3.94784                               | 10.4720         |
| $b = 1.00000$               |                                       |                 |
| $u = 1.00000$               |                                       |                 |
| $a = -2.27202$              | 3.94784                               | 10.4720         |
| $b = 1.00000$               |                                       |                 |

$$\mathbf{V} \cdot I_5^u = \langle b+1, a-1, u+1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

**(iv) u-Polynomials at the component**

| Crossings                                | u-Polynomials at each crossing |
|--|--------------------------------|
| $c_1, c_2, c_{12}$                       | $u - 1$                        |
| $c_3, c_4, c_5$<br>$c_9, c_{10}, c_{11}$ | $u$                            |
| $c_6, c_7, c_8$                          | $u + 1$                        |

**(v) Riley Polynomials at the component**

| Crossings                                | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_6$<br>$c_7, c_8, c_{12}$    | $y - 1$                            |
| $c_3, c_4, c_5$<br>$c_9, c_{10}, c_{11}$ | $y$                                |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_3^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = -1.00000$       |                                       |            |
| $a = 1.00000$        | 0                                     | 0          |
| $b = -1.00000$       |                                       |            |

## VI. u-Polynomials

| Crossings             | u-Polynomials at each crossing  |
|-----------------------|---|
| $c_1$                 | $((u - 1)^9)(u^{18} + 12u^{17} + \dots + 5u + 1)(u^{49} + 16u^{48} + \dots + 51u + 1)$  |
| $c_2$                 | $((u - 1)^5)(u + 1)^4(u^{18} - 6u^{16} + \dots + u - 1)(u^{49} - 2u^{48} + \dots + 3u - 1)$                                   |
| $c_3, c_4, c_9$       | $u(u^4 - 3u^2 + 3)(u^4 - u^2 - 1)(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)^3$<br>$\cdot (u^{49} + 2u^{48} + \dots - 24u + 16)$ |
| $c_5, c_{10}, c_{11}$ | $u(u^4 + u^2 - 1)(u^4 + 3u^2 + 3)(u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1)^3$<br>$\cdot (u^{49} - 2u^{48} + \dots - 2u + 2)$   |
| $c_6$                 | $((u - 1)^4)(u + 1)^5(u^{18} - 6u^{16} + \dots + u - 1)(u^{49} - 2u^{48} + \dots + 3u - 1)$                                   |
| $c_7, c_8$            | $((u - 1)^4)(u + 1)^5(u^{18} - 6u^{16} + \dots + u - 1)(u^{49} + 2u^{48} + \dots - u - 1)$                                    |
| $c_{12}$              | $((u - 1)^5)(u + 1)^4(u^{18} - 6u^{16} + \dots + u - 1)(u^{49} + 2u^{48} + \dots - u - 1)$                                    |

## VII. Riley Polynomials

| Crossings             | Riley Polynomials at each crossing  |
|-----------------------|---|
| $c_1$                 | $((y - 1)^9)(y^{18} - 12y^{17} + \dots + 7y + 1)(y^{49} + 44y^{48} + \dots + 1819y - 1)$  |
| $c_2, c_6$            | $((y - 1)^9)(y^{18} - 12y^{17} + \dots - 5y + 1)(y^{49} - 16y^{48} + \dots + 51y - 1)$  |
| $c_3, c_4, c_9$       | $y(y^2 - 3y + 3)^2(y^2 - y - 1)^2$<br>$\cdot (y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1)^3$<br>$\cdot (y^{49} - 50y^{48} + \dots - 8256y - 256)$ |
| $c_5, c_{10}, c_{11}$ | $y(y^2 + y - 1)^2(y^2 + 3y + 3)^2(y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1)^3$<br>$\cdot (y^{49} + 38y^{48} + \dots + 8y - 4)$                    |
| $c_7, c_8, c_{12}$    | $((y - 1)^9)(y^{18} - 12y^{17} + \dots - 5y + 1)(y^{49} - 56y^{48} + \dots + 99y - 1)$  |