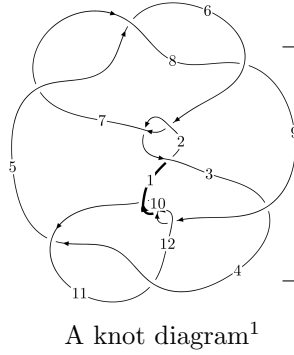
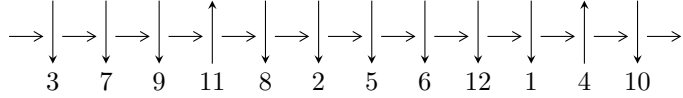


12a<sub>0590</sub> (K12a<sub>0590</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$5,8 \xrightarrow{c_5} 6 \xrightarrow{c_8} 9,11 \xrightarrow{c_4} 4 \xrightarrow{c_{11}} 12 \xrightarrow{c_9} 10 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \rightsquigarrow c_6, c_{10}, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1.68464 \times 10^{28} u^{87} + 9.72953 \times 10^{28} u^{86} + \dots + 7.00197 \times 10^{26} b + 1.37834 \times 10^{28}, \\ - 1.24196 \times 10^{28} u^{87} - 9.51690 \times 10^{28} u^{86} + \dots + 1.40039 \times 10^{27} a - 3.17252 \times 10^{28}, u^{88} + 7u^{87} + \dots - 5u \rangle$$

$$I_2^u = \langle b, u^7 + 2u^6 - 2u^5 - 4u^4 + 2u^3 + u^2 + a - u + 3, u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1 \rangle$$

$$I_3^u = \langle a^4 - a^3 + a^2 + b - 2a + 1, a^5 - a^4 + a^3 - 2a^2 + a - 1, u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 101 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.68 \times 10^{28} u^{87} + 9.73 \times 10^{28} u^{86} + \dots + 7.00 \times 10^{26} b + 1.38 \times 10^{28}, -1.24 \times 10^{28} u^{87} - 9.52 \times 10^{28} u^{86} + \dots + 1.40 \times 10^{27} a - 3.17 \times 10^{28}, u^{88} + 7u^{87} + \dots - 5u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 8.86862u^{87} + 67.9587u^{86} + \dots - 105.878u + 22.6545 \\ -24.0595u^{87} - 138.954u^{86} + \dots + 110.889u - 19.6850 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 25.3526u^{87} + 133.819u^{86} + \dots - 76.7949u + 11.9623 \\ 89.2486u^{87} + 498.120u^{86} + \dots - 348.549u + 61.5438 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -17.3831u^{87} - 77.2993u^{86} + \dots - 14.1162u + 6.54485 \\ -73.5892u^{87} - 406.913u^{86} + \dots + 271.995u - 48.9600 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 24.9048u^{87} + 121.952u^{86} + \dots - 30.6185u - 0.170725 \\ 107.854u^{87} + 601.429u^{86} + \dots - 418.226u + 74.6075 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 110.590u^{87} + 613.566u^{86} + \dots - 427.222u + 73.2837 \\ 162.309u^{87} + 914.917u^{86} + \dots - 667.930u + 117.137 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 177.819u^{87} + 1015.19u^{86} + \dots - 782.351u + 133.966 \\ 229.538u^{87} + 1316.54u^{86} + \dots - 1023.06u + 177.819 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 17.8946u^{87} + 106.795u^{86} + \dots - 102.627u + 15.4769 \\ 61.3214u^{87} + 344.013u^{86} + \dots - 248.957u + 43.8200 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{3994510142988588901229060665}{700197468586696191749097992} u^{87} - \frac{42648575021416709506457400371}{700197468586696191749097992} u^{86} + \dots + \frac{107123801345113766348171177997}{700197468586696191749097992} u - \frac{4216109697287061694606989229}{175049367146674047937274498}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{88} + 36u^{87} + \dots + 16896u + 1024$
$c_2, c_6$	$u^{88} - 2u^{87} + \dots + 64u - 32$
$c_3$	$u^{88} - 3u^{87} + \dots + 49703u - 30649$
$c_4, c_{11}$	$u^{88} - 2u^{87} + \dots - 1664u - 256$
$c_5, c_7, c_8$	$u^{88} - 7u^{87} + \dots + 5u + 1$
$c_9, c_{10}, c_{12}$	$u^{88} - 10u^{87} + \dots - 13u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{88} + 24y^{87} + \dots - 10092544y + 1048576$
$c_2, c_6$	$y^{88} - 36y^{87} + \dots - 16896y + 1024$
$c_3$	$y^{88} - 37y^{87} + \dots - 880685877y + 939361201$
$c_4, c_{11}$	$y^{88} + 54y^{87} + \dots - 49152y + 65536$
$c_5, c_7, c_8$	$y^{88} - 77y^{87} + \dots - 7y + 1$
$c_9, c_{10}, c_{12}$	$y^{88} - 86y^{87} + \dots - 85y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.888121 + 0.465628I$	$-5.34037 + 0.66509I$	0
$a = -0.674944 - 0.581430I$		
$b = 1.115510 - 0.134578I$		
$u = 0.888121 - 0.465628I$	$-5.34037 - 0.66509I$	0
$a = -0.674944 + 0.581430I$		
$b = 1.115510 + 0.134578I$		
$u = 0.766339 + 0.598583I$	$-10.41430 - 4.71583I$	0
$a = -1.036980 - 0.856681I$		
$b = 0.42193 - 1.40540I$		
$u = 0.766339 - 0.598583I$	$-10.41430 + 4.71583I$	0
$a = -1.036980 + 0.856681I$		
$b = 0.42193 + 1.40540I$		
$u = 0.952850 + 0.465179I$	$-2.96134 + 2.94865I$	0
$a = -0.065021 - 0.913422I$		
$b = -0.351118 - 1.102560I$		
$u = 0.952850 - 0.465179I$	$-2.96134 - 2.94865I$	0
$a = -0.065021 + 0.913422I$		
$b = -0.351118 + 1.102560I$		
$u = 0.800920 + 0.458340I$	$-3.55064 - 1.70767I$	0
$a = 0.73265 + 1.28159I$		
$b = -0.112227 + 1.047930I$		
$u = 0.800920 - 0.458340I$	$-3.55064 + 1.70767I$	0
$a = 0.73265 - 1.28159I$		
$b = -0.112227 - 1.047930I$		
$u = 0.238802 + 0.874394I$	$-6.87264 - 11.71080I$	0
$a = -1.51165 - 0.29886I$		
$b = 0.64367 - 1.34705I$		
$u = 0.238802 - 0.874394I$	$-6.87264 + 11.71080I$	0
$a = -1.51165 + 0.29886I$		
$b = 0.64367 + 1.34705I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.106230 + 0.101887I$ $a = -0.38448 + 2.75149I$ $b = 0.253569 + 0.477806I$	$-3.31594 - 0.58556I$	0
$u = 1.106230 - 0.101887I$ $a = -0.38448 - 2.75149I$ $b = 0.253569 - 0.477806I$	$-3.31594 + 0.58556I$	0
$u = 1.074860 + 0.294544I$ $a = 0.609880 + 0.504609I$ $b = -0.493783 + 0.368228I$	$-0.723913 - 0.558805I$	0
$u = 1.074860 - 0.294544I$ $a = 0.609880 - 0.504609I$ $b = -0.493783 - 0.368228I$	$-0.723913 + 0.558805I$	0
$u = 0.998684 + 0.532410I$ $a = 0.123794 + 0.448994I$ $b = 0.58280 + 1.35034I$	$-9.19064 + 6.74935I$	0
$u = 0.998684 - 0.532410I$ $a = 0.123794 - 0.448994I$ $b = 0.58280 - 1.35034I$	$-9.19064 - 6.74935I$	0
$u = 0.394607 + 0.770272I$ $a = 0.455783 + 0.010772I$ $b = 0.31689 + 1.42777I$	$-9.29942 - 0.08924I$	0
$u = 0.394607 - 0.770272I$ $a = 0.455783 - 0.010772I$ $b = 0.31689 - 1.42777I$	$-9.29942 + 0.08924I$	0
$u = 0.236702 + 0.827946I$ $a = 1.33516 + 0.60966I$ $b = -0.428462 + 1.161060I$	$-0.75062 - 7.56823I$	0
$u = 0.236702 - 0.827946I$ $a = 1.33516 - 0.60966I$ $b = -0.428462 - 1.161060I$	$-0.75062 + 7.56823I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.257930 + 0.804225I$ $a = -0.992899 - 0.708956I$ $b = 1.176510 + 0.257378I$	$-3.37075 - 5.18603I$	0
$u = 0.257930 - 0.804225I$ $a = -0.992899 + 0.708956I$ $b = 1.176510 - 0.257378I$	$-3.37075 + 5.18603I$	0
$u = 0.044598 + 0.812501I$ $a = 0.012409 - 0.949891I$ $b = -0.068037 + 0.976812I$	$-0.94317 - 2.91824I$	$-8.00000 + 0.I$
$u = 0.044598 - 0.812501I$ $a = 0.012409 + 0.949891I$ $b = -0.068037 - 0.976812I$	$-0.94317 + 2.91824I$	$-8.00000 + 0.I$
$u = 0.265848 + 0.760527I$ $a = -0.709338 - 0.763779I$ $b = 0.074648 - 1.085590I$	$-1.85509 - 2.57254I$	0
$u = 0.265848 - 0.760527I$ $a = -0.709338 + 0.763779I$ $b = 0.074648 + 1.085590I$	$-1.85509 + 2.57254I$	0
$u = 0.164802 + 0.765395I$ $a = 0.640282 + 0.424932I$ $b = -0.640037 - 0.265485I$	$1.98407 - 3.37950I$	$-3.18324 + 4.49505I$
$u = 0.164802 - 0.765395I$ $a = 0.640282 - 0.424932I$ $b = -0.640037 + 0.265485I$	$1.98407 + 3.37950I$	$-3.18324 - 4.49505I$
$u = -1.210690 + 0.142812I$ $a = 0.167563 + 0.494552I$ $b = -0.564547 + 1.141500I$	$-8.03151 - 3.54347I$	0
$u = -1.210690 - 0.142812I$ $a = 0.167563 - 0.494552I$ $b = -0.564547 - 1.141500I$	$-8.03151 + 3.54347I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.239120 + 0.245897I$ $a = 0.512434 - 0.571361I$ $b = 0.566252 + 0.257444I$	$-1.10788 - 1.71772I$	0
$u = 1.239120 - 0.245897I$ $a = 0.512434 + 0.571361I$ $b = 0.566252 - 0.257444I$	$-1.10788 + 1.71772I$	0
$u = 1.215600 + 0.383630I$ $a = -0.934428 - 0.097206I$ $b = 0.033207 - 1.038470I$	$-4.54745 - 1.38520I$	0
$u = 1.215600 - 0.383630I$ $a = -0.934428 + 0.097206I$ $b = 0.033207 + 1.038470I$	$-4.54745 + 1.38520I$	0
$u = -1.276630 + 0.183299I$ $a = -0.215638 - 0.758974I$ $b = 0.582952 - 0.942243I$	$-2.95506 + 0.13185I$	0
$u = -1.276630 - 0.183299I$ $a = -0.215638 + 0.758974I$ $b = 0.582952 + 0.942243I$	$-2.95506 - 0.13185I$	0
$u = 0.051522 + 0.675391I$ $a = -0.742113 + 0.645879I$ $b = 0.611315 - 0.427751I$	$2.51572 - 1.61584I$	$-1.91976 + 3.16837I$
$u = 0.051522 - 0.675391I$ $a = -0.742113 - 0.645879I$ $b = 0.611315 + 0.427751I$	$2.51572 + 1.61584I$	$-1.91976 - 3.16837I$
$u = 1.314380 + 0.174281I$ $a = 1.09840 + 2.65275I$ $b = 0.010805 + 1.079500I$	$-4.65633 - 0.63571I$	0
$u = 1.314380 - 0.174281I$ $a = 1.09840 - 2.65275I$ $b = 0.010805 - 1.079500I$	$-4.65633 + 0.63571I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.320720 + 0.187553I$ $a = 0.655900 - 0.911111I$ $b = -0.908877 - 0.545626I$	$-6.01527 + 1.89183I$	0
$u = -1.320720 - 0.187553I$ $a = 0.655900 + 0.911111I$ $b = -0.908877 + 0.545626I$	$-6.01527 - 1.89183I$	0
$u = -1.307460 + 0.264842I$ $a = -0.436161 + 0.563621I$ $b = 0.704898 + 0.536481I$	$-1.74045 + 5.01419I$	0
$u = -1.307460 - 0.264842I$ $a = -0.436161 - 0.563621I$ $b = 0.704898 - 0.536481I$	$-1.74045 - 5.01419I$	0
$u = -1.292640 + 0.344864I$ $a = 0.615494 - 0.130607I$ $b = -0.165716 - 0.926745I$	$-5.11018 + 7.07530I$	0
$u = -1.292640 - 0.344864I$ $a = 0.615494 + 0.130607I$ $b = -0.165716 + 0.926745I$	$-5.11018 - 7.07530I$	0
$u = -0.174131 + 0.636836I$ $a = 2.02360 - 0.48082I$ $b = -0.580461 - 1.285720I$	$-5.14037 + 6.25877I$	$-9.44624 - 3.66252I$
$u = -0.174131 - 0.636836I$ $a = 2.02360 + 0.48082I$ $b = -0.580461 + 1.285720I$	$-5.14037 - 6.25877I$	$-9.44624 + 3.66252I$
$u = 1.330870 + 0.207803I$ $a = -0.933904 + 0.972883I$ $b = -1.166170 - 0.198096I$	$-6.30741 - 3.16964I$	0
$u = 1.330870 - 0.207803I$ $a = -0.933904 - 0.972883I$ $b = -1.166170 + 0.198096I$	$-6.30741 + 3.16964I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.332230 + 0.235913I$ $a = -1.36376 - 2.55428I$ $b = 0.386394 - 1.149300I$	$-3.80107 - 5.54437I$	0
$u = 1.332230 - 0.235913I$ $a = -1.36376 + 2.55428I$ $b = 0.386394 + 1.149300I$	$-3.80107 + 5.54437I$	0
$u = -1.339550 + 0.224805I$ $a = 0.091229 + 1.306420I$ $b = -0.487922 + 0.888767I$	$-5.42509 + 4.45293I$	0
$u = -1.339550 - 0.224805I$ $a = 0.091229 - 1.306420I$ $b = -0.487922 - 0.888767I$	$-5.42509 - 4.45293I$	0
$u = 1.380100 + 0.123580I$ $a = -1.09435 - 2.36932I$ $b = -0.37266 - 1.42969I$	$-11.86110 + 2.15849I$	0
$u = 1.380100 - 0.123580I$ $a = -1.09435 + 2.36932I$ $b = -0.37266 + 1.42969I$	$-11.86110 - 2.15849I$	0
$u = 1.365220 + 0.261535I$ $a = 1.33626 + 2.41346I$ $b = -0.61664 + 1.35909I$	$-10.02730 - 9.55714I$	0
$u = 1.365220 - 0.261535I$ $a = 1.33626 - 2.41346I$ $b = -0.61664 - 1.35909I$	$-10.02730 + 9.55714I$	0
$u = -1.363890 + 0.319129I$ $a = -0.234330 - 0.481461I$ $b = -0.705464 + 0.206220I$	$-2.84821 + 7.30244I$	0
$u = -1.363890 - 0.319129I$ $a = -0.234330 + 0.481461I$ $b = -0.705464 - 0.206220I$	$-2.84821 - 7.30244I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.40144$ $a = -0.385644$ $b = -0.577672$	-7.10454	0
$u = -0.087677 + 0.585925I$ $a = -1.96671 + 0.65542I$ $b = 0.433173 + 1.031780I$	$0.69910 + 2.52777I$	$-5.84354 - 3.35799I$
$u = -0.087677 - 0.585925I$ $a = -1.96671 - 0.65542I$ $b = 0.433173 - 1.031780I$	$0.69910 - 2.52777I$	$-5.84354 + 3.35799I$
$u = 0.563116$ $a = 0.509143$ $b = -0.313068$	-0.958674	-9.85690
$u = -1.40715 + 0.30877I$ $a = -0.99962 + 1.99298I$ $b = 0.120608 + 1.188840I$	$-7.16857 + 6.45126I$	0
$u = -1.40715 - 0.30877I$ $a = -0.99962 - 1.99298I$ $b = 0.120608 - 1.188840I$	$-7.16857 - 6.45126I$	0
$u = 0.124503 + 0.544345I$ $a = 1.27598 - 0.81112I$ $b = -0.260698 - 0.771913I$	$-0.80366 - 1.58561I$	$-10.67225 + 2.90476I$
$u = 0.124503 - 0.544345I$ $a = 1.27598 + 0.81112I$ $b = -0.260698 + 0.771913I$	$-0.80366 + 1.58561I$	$-10.67225 - 2.90476I$
$u = -1.40680 + 0.34051I$ $a = 1.26967 - 1.96871I$ $b = -0.455387 - 1.216770I$	$-5.97118 + 11.78330I$	0
$u = -1.40680 - 0.34051I$ $a = 1.26967 + 1.96871I$ $b = -0.455387 + 1.216770I$	$-5.97118 - 11.78330I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.41173 + 0.32636I$ $a = 0.451797 + 0.801134I$ $b = 1.251800 - 0.295347I$	$-8.68021 + 9.27069I$	0
$u = -1.41173 - 0.32636I$ $a = 0.451797 - 0.801134I$ $b = 1.251800 + 0.295347I$	$-8.68021 - 9.27069I$	0
$u = -1.41652 + 0.36230I$ $a = -1.32614 + 1.85531I$ $b = 0.68460 + 1.36460I$	$-12.1310 + 16.1617I$	0
$u = -1.41652 - 0.36230I$ $a = -1.32614 - 1.85531I$ $b = 0.68460 - 1.36460I$	$-12.1310 - 16.1617I$	0
$u = -1.45238 + 0.27357I$ $a = 0.98226 - 1.57277I$ $b = 0.26475 - 1.52039I$	$-15.2401 + 3.8156I$	0
$u = -1.45238 - 0.27357I$ $a = 0.98226 + 1.57277I$ $b = 0.26475 + 1.52039I$	$-15.2401 - 3.8156I$	0
$u = -1.47888 + 0.02352I$ $a = 0.11238 - 2.43472I$ $b = -0.196285 - 1.246890I$	$-11.09960 + 2.70583I$	0
$u = -1.47888 - 0.02352I$ $a = 0.11238 + 2.43472I$ $b = -0.196285 + 1.246890I$	$-11.09960 - 2.70583I$	0
$u = -1.48451$ $a = 0.899695$ $b = 1.29707$	$-13.2474$	0
$u = -0.051131 + 0.501827I$ $a = 1.30705 - 1.31645I$ $b = -0.963746 + 0.258016I$	$-1.87492 + 0.52113I$	$-7.46007 + 0.33584I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.051131 - 0.501827I$ $a = 1.30705 + 1.31645I$ $b = -0.963746 - 0.258016I$	$-1.87492 - 0.52113I$	$-7.46007 - 0.33584I$
$u = -1.51084 + 0.06009I$ $a = -0.09053 + 2.25061I$ $b = 0.52441 + 1.48832I$	$-18.1852 + 6.5334I$	0
$u = -1.51084 - 0.06009I$ $a = -0.09053 - 2.25061I$ $b = 0.52441 - 1.48832I$	$-18.1852 - 6.5334I$	0
$u = -0.346736 + 0.293540I$ $a = -1.47471 + 0.88660I$ $b = -0.407022 + 1.274040I$	$-6.45539 - 3.75624I$	$-8.92208 + 2.37124I$
$u = -0.346736 - 0.293540I$ $a = -1.47471 - 0.88660I$ $b = -0.407022 - 1.274040I$	$-6.45539 + 3.75624I$	$-8.92208 - 2.37124I$
$u = -0.109910 + 0.191162I$ $a = 2.62502 - 1.00223I$ $b = 0.221171 - 0.788369I$	$-0.464107 - 1.212900I$	$-5.34512 + 5.07325I$
$u = -0.109910 - 0.191162I$ $a = 2.62502 + 1.00223I$ $b = 0.221171 + 0.788369I$	$-0.464107 + 1.212900I$	$-5.34512 - 5.07325I$
$u = 0.164075$ $a = 6.48224$ $b = -0.479550$	$-2.12876$	$-0.110400$

$$\text{II. } I_2^u = \langle b, u^7 + 2u^6 - 2u^5 - 4u^4 + 2u^3 + u^2 + a - u + 3, u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^7 - 2u^6 + 2u^5 + 4u^4 - 2u^3 - u^2 + u - 3 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^7 - 2u^6 + 2u^5 + 4u^4 - 2u^3 - u^2 + u - 3 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^7 - 2u^6 + 2u^5 + 4u^4 - 2u^3 - u^2 - 3 \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^4 + u^2 + 1 \\ -u^6 + 2u^4 - u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^7 - u^6 - 2u^5 + 3u^4 - 2u^2 + 2u - 1 \\ u^7 - 2u^5 + 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u^3 - u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -3u^7 - 10u^6 + 7u^5 + 25u^4 - 9u^3 - 12u^2 + 8u - 25$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$
$c_2$	$u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$
$c_4, c_{11}$	$u^8$
$c_5$	$u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$
$c_6$	$u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$
$c_7, c_8$	$u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$
$c_9, c_{10}$	$(u - 1)^8$
$c_{12}$	$(u + 1)^8$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$
$c_2, c_6$	$y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$
$c_4, c_{11}$	$y^8$
$c_5, c_7, c_8$	$y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$
$c_9, c_{10}, c_{12}$	$(y - 1)^8$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.180120 + 0.268597I$ $a = 0.281371 - 1.128550I$ $b = 0$	$-2.68559 - 1.13123I$	$-9.56807 + 0.79885I$
$u = 1.180120 - 0.268597I$ $a = 0.281371 + 1.128550I$ $b = 0$	$-2.68559 + 1.13123I$	$-9.56807 - 0.79885I$
$u = 0.108090 + 0.747508I$ $a = -0.208670 + 0.825203I$ $b = 0$	$0.51448 - 2.57849I$	$-6.42531 + 3.25625I$
$u = 0.108090 - 0.747508I$ $a = -0.208670 - 0.825203I$ $b = 0$	$0.51448 + 2.57849I$	$-6.42531 - 3.25625I$
$u = -1.37100$ $a = -0.829189$ $b = 0$	$-8.14766$	$-20.0060$
$u = -1.334530 + 0.318930I$ $a = -0.284386 - 0.605794I$ $b = 0$	$-4.02461 + 6.44354I$	$-11.71592 - 3.92092I$
$u = -1.334530 - 0.318930I$ $a = -0.284386 + 0.605794I$ $b = 0$	$-4.02461 - 6.44354I$	$-11.71592 + 3.92092I$
$u = 0.463640$ $a = -2.74744$ $b = 0$	$-2.48997$	$-23.5750$

$$\text{III. } I_3^u = \langle a^4 - a^3 + a^2 + b - 2a + 1, a^5 - a^4 + a^3 - 2a^2 + a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -a^4 + a^3 - a^2 + 2a - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ a^4 - a - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ -a^3 + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^4 - a - 1 \\ a^3 - a^2 - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a^4 - a - 1 \\ a^4 - a - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a^4 - a - 1 \\ a^4 - a - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a^4 - a - 1 \\ a^4 - a - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5a^4 + 5a^3 + 7a - 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_6$	$u^5$
$c_3$	$u^5 + 3u^4 + 4u^3 + u^2 - u - 1$
$c_4$	$u^5 + u^4 + 2u^3 + u^2 + u + 1$
$c_5$	$(u - 1)^5$
$c_7, c_8$	$(u + 1)^5$
$c_9, c_{10}$	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
$c_{11}$	$u^5 - u^4 + 2u^3 - u^2 + u - 1$
$c_{12}$	$u^5 - u^4 - 2u^3 + u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$	$y^5$
$c_3$	$y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$
$c_4, c_{11}$	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$
$c_5, c_7, c_8$	$(y - 1)^5$
$c_9, c_{10}, c_{12}$	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = -0.428550 + 1.039280I$ $b = 0.339110 + 0.822375I$	$-1.97403 + 1.53058I$	$-10.50099 - 3.45976I$
$u = 1.00000$ $a = -0.428550 - 1.039280I$ $b = 0.339110 - 0.822375I$	$-1.97403 - 1.53058I$	$-10.50099 + 3.45976I$
$u = 1.00000$ $a = 0.276511 + 0.728237I$ $b = -0.455697 + 1.200150I$	$-7.51750 - 4.40083I$	$-14.3774 + 5.8297I$
$u = 1.00000$ $a = 0.276511 - 0.728237I$ $b = -0.455697 - 1.200150I$	$-7.51750 + 4.40083I$	$-14.3774 - 5.8297I$
$u = 1.00000$ $a = 1.30408$ $b = -0.766826$	$-4.04602$	$-8.24330$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^5(u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1) \cdot (u^{88} + 36u^{87} + \dots + 16896u + 1024)$
$c_2$	$u^5(u^8 - u^7 + \dots + 2u - 1)(u^{88} - 2u^{87} + \dots + 64u - 32)$
$c_3$	$(u^5 + 3u^4 + 4u^3 + u^2 - u - 1) \cdot (u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1) \cdot (u^{88} - 3u^{87} + \dots + 49703u - 30649)$
$c_4$	$u^8(u^5 + u^4 + \dots + u + 1)(u^{88} - 2u^{87} + \dots - 1664u - 256)$
$c_5$	$((u - 1)^5)(u^8 + u^7 + \dots + 2u - 1)(u^{88} - 7u^{87} + \dots + 5u + 1)$
$c_6$	$u^5(u^8 + u^7 + \dots - 2u - 1)(u^{88} - 2u^{87} + \dots + 64u - 32)$
$c_7, c_8$	$((u + 1)^5)(u^8 - u^7 + \dots - 2u - 1)(u^{88} - 7u^{87} + \dots + 5u + 1)$
$c_9, c_{10}$	$((u - 1)^8)(u^5 + u^4 + \dots + u - 1)(u^{88} - 10u^{87} + \dots - 13u + 1)$
$c_{11}$	$u^8(u^5 - u^4 + \dots + u - 1)(u^{88} - 2u^{87} + \dots - 1664u - 256)$
$c_{12}$	$((u + 1)^8)(u^5 - u^4 + \dots + u + 1)(u^{88} - 10u^{87} + \dots - 13u + 1)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^5(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1)$ $\cdot (y^{88} + 24y^{87} + \dots - 10092544y + 1048576)$
$c_2, c_6$	$y^5(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)$ $\cdot (y^{88} - 36y^{87} + \dots - 16896y + 1024)$
$c_3$	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)$ $\cdot (y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1)$ $\cdot (y^{88} - 37y^{87} + \dots - 880685877y + 939361201)$
$c_4, c_{11}$	$y^8(y^5 + 3y^4 + \dots - y - 1)(y^{88} + 54y^{87} + \dots - 49152y + 65536)$
$c_5, c_7, c_8$	$(y - 1)^5(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1)$ $\cdot (y^{88} - 77y^{87} + \dots - 7y + 1)$
$c_9, c_{10}, c_{12}$	$((y - 1)^8)(y^5 - 5y^4 + \dots - y - 1)(y^{88} - 86y^{87} + \dots - 85y + 1)$