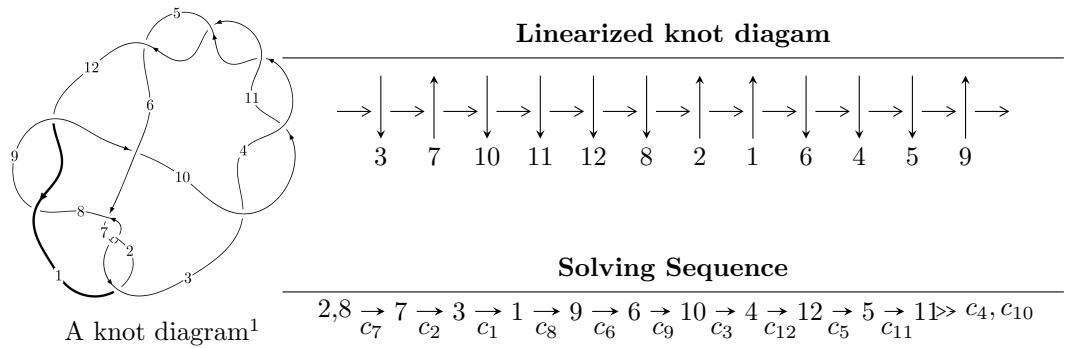


## $12a_{0651}$ ( $K12a_{0651}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$I_1^u = \langle u^{48} - u^{47} + \cdots - 2u^2 - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 48 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{48} - u^{47} + \cdots - 2u^2 - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned}
a_2 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\
a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\
a_1 &= \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix} \\
a_9 &= \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ -u^{10} - 2u^8 - 3u^6 - 2u^4 - u^2 \end{pmatrix} \\
a_6 &= \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix} \\
a_{10} &= \begin{pmatrix} u^{14} + 3u^{12} + 6u^{10} + 7u^8 + 6u^6 + 4u^4 + 2u^2 + 1 \\ u^{14} + 2u^{12} + 3u^{10} + 2u^8 - u^2 \end{pmatrix} \\
a_4 &= \begin{pmatrix} -u^{31} - 6u^{29} + \cdots - 18u^5 - 6u^3 \\ -u^{31} - 5u^{29} + \cdots + 2u^3 + u \end{pmatrix} \\
a_{12} &= \begin{pmatrix} u^{13} + 2u^{11} + 3u^9 + 2u^7 - u \\ u^{15} + 3u^{13} + 6u^{11} + 7u^9 + 6u^7 + 4u^5 + 2u^3 + u \end{pmatrix} \\
a_5 &= \begin{pmatrix} -u^{30} - 5u^{28} + \cdots + 2u^2 + 1 \\ -u^{32} - 6u^{30} + \cdots - 18u^6 - 6u^4 \end{pmatrix} \\
a_{11} &= \begin{pmatrix} -u^{47} - 8u^{45} + \cdots + 18u^5 + 6u^3 \\ -u^{47} + u^{46} + \cdots - 2u^2 - 1 \end{pmatrix}
\end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $4u^{46} - 4u^{45} + \cdots + 12u - 6$

**(iv) u-Polynomials at the component**

| Crossings                           | u-Polynomials at each crossing            |
|-------------------------------------|---|
| $c_1, c_6$                          | $u^{48} + 17u^{47} + \cdots + 4u + 1$     |
| $c_2, c_7$                          | $u^{48} + u^{47} + \cdots - 2u^2 - 1$     |
| $c_3, c_4, c_5$<br>$c_{10}, c_{11}$ | $u^{48} - u^{47} + \cdots - 2u - 1$       |
| $c_8, c_{12}$                       | $u^{48} - 5u^{47} + \cdots + 100u - 39$   |
| $c_9$                               | $u^{48} - 5u^{47} + \cdots + 912u + 1305$ |

**(v) Riley Polynomials at the component**

| Crossings                           | Riley Polynomials at each crossing                 |
|-------------------------------------|--|
| $c_1, c_6$                          | $y^{48} + 29y^{47} + \cdots - 16y + 1$             |
| $c_2, c_7$                          | $y^{48} + 17y^{47} + \cdots + 4y + 1$              |
| $c_3, c_4, c_5$<br>$c_{10}, c_{11}$ | $y^{48} - 63y^{47} + \cdots + 4y + 1$              |
| $c_8, c_{12}$                       | $y^{48} + 37y^{47} + \cdots + 24632y + 1521$       |
| $c_9$                               | $y^{48} - 23y^{47} + \cdots - 23246424y + 1703025$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.802127 + 0.589214I$  | $-13.2341 - 6.6512I$                  | $-8.69292 + 2.70499I$  |
| $u = 0.802127 - 0.589214I$  | $-13.2341 + 6.6512I$                  | $-8.69292 - 2.70499I$  |
| $u = -0.780450 + 0.595412I$ | $-3.45383 + 5.14659I$                 | $-7.86923 - 4.15340I$  |
| $u = -0.780450 - 0.595412I$ | $-3.45383 - 5.14659I$                 | $-7.86923 + 4.15340I$  |
| $u = -0.306787 + 0.928044I$ | $-13.29560 - 2.74578I$                | $-13.24399 + 4.02587I$ |
| $u = -0.306787 - 0.928044I$ | $-13.29560 + 2.74578I$                | $-13.24399 - 4.02587I$ |
| $u = 0.744340 + 0.609755I$  | $0.47988 - 2.41400I$                  | $-2.77620 + 3.95017I$  |
| $u = 0.744340 - 0.609755I$  | $0.47988 + 2.41400I$                  | $-2.77620 - 3.95017I$  |
| $u = -0.709694 + 0.805377I$ | $1.43993 - 0.10326I$                  | $-4.11691 - 1.57301I$  |
| $u = -0.709694 - 0.805377I$ | $1.43993 + 0.10326I$                  | $-4.11691 + 1.57301I$  |
| $u = -0.019095 + 1.077630I$ | $-5.06998 - 1.60211I$                 | $-10.45738 + 4.05120I$ |
| $u = -0.019095 - 1.077630I$ | $-5.06998 + 1.60211I$                 | $-10.45738 - 4.05120I$ |
| $u = 0.750182 + 0.779791I$  | $-7.19201 - 0.77835I$                 | $-5.36224 + 0.06889I$  |
| $u = 0.750182 - 0.779791I$  | $-7.19201 + 0.77835I$                 | $-5.36224 - 0.06889I$  |
| $u = -0.669363 + 0.604587I$ | $0.001527 - 0.587302I$                | $-4.68221 + 4.09309I$  |
| $u = -0.669363 - 0.604587I$ | $0.001527 + 0.587302I$                | $-4.68221 - 4.09309I$  |
| $u = 0.040819 + 1.103530I$  | $-9.34090 + 4.19623I$                 | $-14.8023 - 4.2142I$   |
| $u = 0.040819 - 1.103530I$  | $-9.34090 - 4.19623I$                 | $-14.8023 + 4.2142I$   |
| $u = 0.701243 + 0.856750I$  | $3.68589 + 2.68723I$                  | $1.90848 - 3.59326I$   |
| $u = 0.701243 - 0.856750I$  | $3.68589 - 2.68723I$                  | $1.90848 + 3.59326I$   |
| $u = 0.303851 + 0.826787I$  | $-3.75546 + 2.27659I$                 | $-12.89646 - 5.30128I$ |
| $u = 0.303851 - 0.826787I$  | $-3.75546 - 2.27659I$                 | $-12.89646 + 5.30128I$ |
| $u = -0.050388 + 1.121400I$ | $-19.3092 - 5.5995I$                  | $-15.3152 + 3.0524I$   |
| $u = -0.050388 - 1.121400I$ | $-19.3092 + 5.5995I$                  | $-15.3152 - 3.0524I$   |
| $u = -0.701027 + 0.900492I$ | $1.15320 - 5.29793I$                  | $-5.03627 + 7.68449I$  |
| $u = -0.701027 - 0.900492I$ | $1.15320 + 5.29793I$                  | $-5.03627 - 7.68449I$  |
| $u = -0.715058 + 0.438137I$ | $-14.1380 - 3.7995I$                  | $-9.38326 + 2.79474I$  |
| $u = -0.715058 - 0.438137I$ | $-14.1380 + 3.7995I$                  | $-9.38326 - 2.79474I$  |
| $u = 0.719743 + 0.928582I$  | $-7.64175 + 6.35454I$                 | $-6.48748 - 5.77861I$  |
| $u = 0.719743 - 0.928582I$  | $-7.64175 - 6.35454I$                 | $-6.48748 + 5.77861I$  |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.672923 + 0.473750I$  | $-4.26296 + 2.63953I$                 | $-9.04168 - 4.04694I$  |
| $u = 0.672923 - 0.473750I$  | $-4.26296 - 2.63953I$                 | $-9.04168 + 4.04694I$  |
| $u = 0.620090 + 1.027290I$  | $-5.75948 + 2.34942I$                 | $-11.55550 - 1.52820I$ |
| $u = 0.620090 - 1.027290I$  | $-5.75948 - 2.34942I$                 | $-11.55550 + 1.52820I$ |
| $u = -0.648633 + 1.012460I$ | $-1.18407 - 4.57916I$                 | $-6.64611 + 1.38024I$  |
| $u = -0.648633 - 1.012460I$ | $-1.18407 + 4.57916I$                 | $-6.64611 - 1.38024I$  |
| $u = -0.608868 + 1.044010I$ | $-15.8277 - 1.2103I$                  | $-12.22073 + 2.35699I$ |
| $u = -0.608868 - 1.044010I$ | $-15.8277 + 1.2103I$                  | $-12.22073 - 2.35699I$ |
| $u = 0.668938 + 1.023950I$  | $-0.74329 + 7.81387I$                 | $-4.00000 - 8.53366I$  |
| $u = 0.668938 - 1.023950I$  | $-0.74329 - 7.81387I$                 | $-4.00000 + 8.53366I$  |
| $u = -0.676813 + 1.038570I$ | $-4.76998 - 10.66020I$                | $-9.85701 + 8.71110I$  |
| $u = -0.676813 - 1.038570I$ | $-4.76998 + 10.66020I$                | $-9.85701 - 8.71110I$  |
| $u = 0.681817 + 1.047990I$  | $-14.6043 + 12.2368I$                 | $-10.70547 - 7.24531I$ |
| $u = 0.681817 - 1.047990I$  | $-14.6043 - 12.2368I$                 | $-10.70547 + 7.24531I$ |
| $u = -0.545430$             | $-10.6248$                            | $-6.00350$             |
| $u = -0.257194 + 0.480005I$ | $-0.181190 - 0.868139I$               | $-4.26608 + 7.69273I$  |
| $u = -0.257194 - 0.480005I$ | $-0.181190 + 0.868139I$               | $-4.26608 - 7.69273I$  |
| $u = 0.420030$              | $-1.58694$                            | $-4.88980$             |

## II. u-Polynomials

| Crossings                           | u-Polynomials at each crossing            |
|-------------------------------------|---|
| $c_1, c_6$                          | $u^{48} + 17u^{47} + \cdots + 4u + 1$     |
| $c_2, c_7$                          | $u^{48} + u^{47} + \cdots - 2u^2 - 1$     |
| $c_3, c_4, c_5$<br>$c_{10}, c_{11}$ | $u^{48} - u^{47} + \cdots - 2u - 1$       |
| $c_8, c_{12}$                       | $u^{48} - 5u^{47} + \cdots + 100u - 39$   |
| $c_9$                               | $u^{48} - 5u^{47} + \cdots + 912u + 1305$ |

### III. Riley Polynomials

| Crossings                           | Riley Polynomials at each crossing                 |
|-------------------------------------|--|
| $c_1, c_6$                          | $y^{48} + 29y^{47} + \cdots - 16y + 1$             |
| $c_2, c_7$                          | $y^{48} + 17y^{47} + \cdots + 4y + 1$              |
| $c_3, c_4, c_5$<br>$c_{10}, c_{11}$ | $y^{48} - 63y^{47} + \cdots + 4y + 1$              |
| $c_8, c_{12}$                       | $y^{48} + 37y^{47} + \cdots + 24632y + 1521$       |
| $c_9$                               | $y^{48} - 23y^{47} + \cdots - 23246424y + 1703025$ |