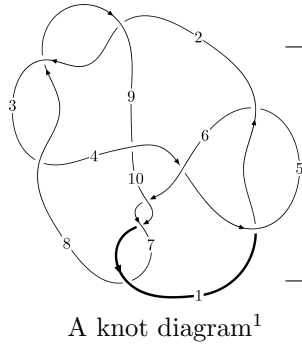
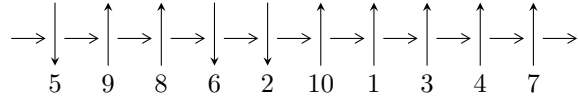


10₆₅ (*K10a₄₂*)



Linearized knot diagram



Solving Sequence

$$2,9 \xrightarrow{c_2} 3,6 \xrightarrow{c_5} 5 \xrightarrow{c_1} 1 \xrightarrow{c_8} 8 \xrightarrow{c_3} 4 \xrightarrow{c_9} 10 \xrightarrow{c_7} 7 \longrightarrow c_4, c_6, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -2u^{24} + 2u^{23} + \dots + 4b + 2, 2u^{24} - u^{23} + \dots + 4a - 6, u^{25} - 2u^{24} + \dots - 4u + 2 \rangle$$

$$I_2^u = \langle -a^2u^2 + u^2a + 2au + b + 2a + 2u, -2a^2u^2 + a^3 + 2u^2a - 2a^2 + 3au + 5a + u + 1, u^3 + u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle b + 1, 2a + u + 2, u^2 + 2 \rangle$$

$$I_1^v = \langle a, b - 1, v - 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 37 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -2u^{24} + 2u^{23} + \dots + 4b + 2, 2u^{24} - u^{23} + \dots + 4a - 6, u^{25} - 2u^{24} + \dots - 4u + 2 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}u^{24} + \frac{1}{4}u^{23} + \dots - 2u + \frac{3}{2} \\ \frac{1}{2}u^{24} - \frac{1}{2}u^{23} + \dots + \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{4}u^{23} - \frac{5}{2}u^{21} + \dots - \frac{1}{2}u + 1 \\ \frac{1}{2}u^{24} - \frac{1}{2}u^{23} + \dots + \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{2}u^{24} + u^{23} + \dots - 3u + \frac{3}{2} \\ \frac{1}{4}u^{22} - \frac{1}{4}u^{21} + \dots - \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{4}u^{18} + 2u^{16} + \dots - \frac{3}{2}u + \frac{1}{2} \\ \frac{1}{2}u^{11} + \frac{5}{2}u^9 + \dots - u^2 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -2u^{24} + 4u^{23} - 26u^{22} + 40u^{21} - 138u^{20} + 164u^{19} - 384u^{18} + \\ &346u^{17} - 584u^{16} + 380u^{15} - 430u^{14} + 186u^{13} - 50u^{12} + 32u^{11} + 80u^{10} + 56u^9 - 74u^8 + \\ &110u^7 - 178u^6 + 100u^5 - 82u^4 + 18u^3 + 24u^2 - 14u + 8 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$u^{25} + 2u^{24} + \dots - u - 3$
c_2, c_3, c_8	$u^{25} + 2u^{24} + \dots - 4u - 2$
c_4	$u^{25} + 10u^{24} + \dots + 97u + 9$
c_6, c_7, c_{10}	$u^{25} - 2u^{24} + \dots - 5u - 3$
c_9	$u^{25} - 2u^{24} + \dots + 56u - 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5	$y^{25} - 10y^{24} + \dots + 97y - 9$
c_2, c_3, c_8	$y^{25} + 22y^{24} + \dots + 8y - 4$
c_4	$y^{25} + 14y^{24} + \dots + 1561y - 81$
c_6, c_7, c_{10}	$y^{25} - 26y^{24} + \dots - 47y - 9$
c_9	$y^{25} - 2y^{24} + \dots - 2624y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.498082 + 0.831864I$ $a = -0.210637 + 0.234020I$ $b = 0.969881 - 0.673526I$	$4.11705 + 3.30443I$	$6.15585 - 1.80924I$
$u = -0.498082 - 0.831864I$ $a = -0.210637 - 0.234020I$ $b = 0.969881 + 0.673526I$	$4.11705 - 3.30443I$	$6.15585 + 1.80924I$
$u = 0.404191 + 1.026880I$ $a = 0.433491 + 0.988124I$ $b = 0.686093 - 0.799024I$	$4.98459 + 2.21818I$	$7.23817 - 3.39990I$
$u = 0.404191 - 1.026880I$ $a = 0.433491 - 0.988124I$ $b = 0.686093 + 0.799024I$	$4.98459 - 2.21818I$	$7.23817 + 3.39990I$
$u = -0.814894 + 0.282583I$ $a = 0.16059 + 1.77022I$ $b = -1.096790 - 0.679709I$	$5.88761 - 7.92352I$	$7.71863 + 6.25521I$
$u = -0.814894 - 0.282583I$ $a = 0.16059 - 1.77022I$ $b = -1.096790 + 0.679709I$	$5.88761 + 7.92352I$	$7.71863 - 6.25521I$
$u = 0.045104 + 1.169880I$ $a = -0.509198 - 0.822038I$ $b = 0.611097 + 0.519026I$	$-2.09053 - 1.42730I$	$3.69318 + 4.01748I$
$u = 0.045104 - 1.169880I$ $a = -0.509198 + 0.822038I$ $b = 0.611097 - 0.519026I$	$-2.09053 + 1.42730I$	$3.69318 - 4.01748I$
$u = 0.809668 + 0.163514I$ $a = 0.706041 + 1.184160I$ $b = -0.516228 - 0.881834I$	$7.64625 + 2.15851I$	$10.42476 - 1.29245I$
$u = 0.809668 - 0.163514I$ $a = 0.706041 - 1.184160I$ $b = -0.516228 + 0.881834I$	$7.64625 - 2.15851I$	$10.42476 + 1.29245I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.678633 + 0.221561I$ $a = 0.45061 - 2.11636I$ $b = -0.976768 + 0.540770I$	$0.03499 + 4.24383I$	$4.60496 - 6.78537I$
$u = 0.678633 - 0.221561I$ $a = 0.45061 + 2.11636I$ $b = -0.976768 - 0.540770I$	$0.03499 - 4.24383I$	$4.60496 + 6.78537I$
$u = 0.339400 + 1.358960I$ $a = -0.547153 - 0.230670I$ $b = 0.378354 + 0.934639I$	$2.85055 + 6.29490I$	$6.20266 - 3.49250I$
$u = 0.339400 - 1.358960I$ $a = -0.547153 + 0.230670I$ $b = 0.378354 - 0.934639I$	$2.85055 - 6.29490I$	$6.20266 + 3.49250I$
$u = 0.276880 + 1.384380I$ $a = 0.88077 + 1.63584I$ $b = 1.090160 - 0.576724I$	$-5.06500 + 7.73599I$	$-0.26723 - 6.67404I$
$u = 0.276880 - 1.384380I$ $a = 0.88077 - 1.63584I$ $b = 1.090160 + 0.576724I$	$-5.06500 - 7.73599I$	$-0.26723 + 6.67404I$
$u = 0.11000 + 1.41509I$ $a = -0.998644 - 0.147362I$ $b = -1.121400 - 0.226598I$	$-7.43417 + 0.37131I$	$-4.72924 + 0.01538I$
$u = 0.11000 - 1.41509I$ $a = -0.998644 + 0.147362I$ $b = -1.121400 + 0.226598I$	$-7.43417 - 0.37131I$	$-4.72924 - 0.01538I$
$u = 0.245363 + 0.498558I$ $a = 0.003216 - 0.172185I$ $b = 0.901860 + 0.293308I$	$-1.52585 - 1.04428I$	$-1.27127 + 1.42914I$
$u = 0.245363 - 0.498558I$ $a = 0.003216 + 0.172185I$ $b = 0.901860 - 0.293308I$	$-1.52585 + 1.04428I$	$-1.27127 - 1.42914I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.33191 + 1.42709I$ $a = 1.00745 - 1.40966I$ $b = 1.172920 + 0.648513I$	$0.44144 - 12.07650I$	$3.42339 + 7.22441I$
$u = -0.33191 - 1.42709I$ $a = 1.00745 + 1.40966I$ $b = 1.172920 - 0.648513I$	$0.44144 + 12.07650I$	$3.42339 - 7.22441I$
$u = -0.06236 + 1.52702I$ $a = -0.863474 + 0.102113I$ $b = -0.881284 + 0.447818I$	$-3.72172 + 1.83282I$	$3.75932 - 4.01286I$
$u = -0.06236 - 1.52702I$ $a = -0.863474 - 0.102113I$ $b = -0.881284 - 0.447818I$	$-3.72172 - 1.83282I$	$3.75932 + 4.01286I$
$u = -0.403977$ $a = 1.97386$ $b = -0.435793$	0.909052	12.0940

$$\langle -a^2u^2 + u^2a + 2au + b + 2a + 2u, -2a^2u^2 + 2u^2a + \dots + 5a + 1, u^3 + u^2 + 2u + 1 \rangle$$

II. $I_2^u =$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ a^2u^2 - u^2a - 2au - 2a - 2u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a^2u^2 - u^2a - 2au - a - 2u \\ a^2u^2 - u^2a - 2au - 2a - 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a^2u^2 - a^2u - u^2a - a^2 - 4au - 2u^2 - a - 4u - 2 \\ -a^2u - u^2a - a^2 - 2au - 2u^2 - 2u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a^2u^2 - u^2a - 2au - a - 2u \\ a^2u^2 - u^2a - 2au - 2a - 2u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $4u^2 + 4u + 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{10}	$u^9 - 3u^7 - u^6 + 3u^5 + 2u^4 - u^3 - u^2 + 1$
c_2, c_3, c_8	$(u^3 - u^2 + 2u - 1)^3$
c_4	$u^9 + 6u^8 + 15u^7 + 21u^6 + 19u^5 + 12u^4 + 7u^3 + 5u^2 + 2u + 1$
c_9	$(u^3 + u^2 - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{10}	$y^9 - 6y^8 + 15y^7 - 21y^6 + 19y^5 - 12y^4 + 7y^3 - 5y^2 + 2y - 1$
c_2, c_3, c_8	$(y^3 + 3y^2 + 2y - 1)^3$
c_4	$y^9 - 6y^8 + 11y^7 - y^6 + 11y^5 - 40y^4 - 37y^3 - 21y^2 - 6y - 1$
c_9	$(y^3 - y^2 + 2y - 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215080 + 1.307140I$ $a = -1.110710 + 0.304480I$ $b = -1.324820 + 0.175904I$	$-3.02413 - 2.82812I$	$2.49024 + 2.97945I$
$u = -0.215080 + 1.307140I$ $a = -0.633796 + 0.350292I$ $b = 0.376870 - 0.700062I$	$-3.02413 - 2.82812I$	$2.49024 + 2.97945I$
$u = -0.215080 + 1.307140I$ $a = 0.41979 - 1.77933I$ $b = 0.947946 + 0.524157I$	$-3.02413 - 2.82812I$	$2.49024 + 2.97945I$
$u = -0.215080 - 1.307140I$ $a = -1.110710 - 0.304480I$ $b = -1.324820 - 0.175904I$	$-3.02413 + 2.82812I$	$2.49024 - 2.97945I$
$u = -0.215080 - 1.307140I$ $a = -0.633796 - 0.350292I$ $b = 0.376870 + 0.700062I$	$-3.02413 + 2.82812I$	$2.49024 - 2.97945I$
$u = -0.215080 - 1.307140I$ $a = 0.41979 + 1.77933I$ $b = 0.947946 - 0.524157I$	$-3.02413 + 2.82812I$	$2.49024 - 2.97945I$
$u = -0.569840$ $a = -0.101925$ $b = 1.26384$	1.11345	9.01950
$u = -0.569840$ $a = 1.37568 + 1.52573I$ $b = -0.631920 - 0.444935I$	1.11345	9.01950
$u = -0.569840$ $a = 1.37568 - 1.52573I$ $b = -0.631920 + 0.444935I$	1.11345	9.01950

$$\text{III. } I_3^u = \langle b + 1, 2a + u + 2, u^2 + 2 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}u - 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{2}u - 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{2}u - 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{3}{2}u - 1 \\ -u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_{10}	$(u + 1)^2$
c_2, c_3, c_8 c_9	$u^2 + 2$
c_4, c_5, c_6 c_7	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4, c_5 c_6, c_7, c_{10}	$(y - 1)^2$
c_2, c_3, c_8 c_9	$(y + 2)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.414210I$ $a = -1.000000 - 0.707107I$ $b = -1.000000$	-4.93480	0
$u = -1.414210I$ $a = -1.000000 + 0.707107I$ $b = -1.000000$	-4.93480	0

$$\text{IV. } I_1^v = \langle a, b - 1, v - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
c_1, c_4, c_{10}	$u - 1$
c_2, c_3, c_8 c_9	u
c_5, c_6, c_7	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4, c_5 c_6, c_7, c_{10}	$y - 1$
c_2, c_3, c_8 c_9	y

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$	0	0
$b = 1.00000$		

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u-1)(u+1)^2(u^9 - 3u^7 - u^6 + 3u^5 + 2u^4 - u^3 - u^2 + 1)$ $\cdot (u^{25} + 2u^{24} + \dots - u - 3)$
c_2, c_3, c_8	$u(u^2 + 2)(u^3 - u^2 + 2u - 1)^3(u^{25} + 2u^{24} + \dots - 4u - 2)$
c_4	$((u-1)^3)(u^9 + 6u^8 + \dots + 2u + 1)$ $\cdot (u^{25} + 10u^{24} + \dots + 97u + 9)$
c_5	$(u-1)^2(u+1)(u^9 - 3u^7 - u^6 + 3u^5 + 2u^4 - u^3 - u^2 + 1)$ $\cdot (u^{25} + 2u^{24} + \dots - u - 3)$
c_6, c_7	$(u-1)^2(u+1)(u^9 - 3u^7 - u^6 + 3u^5 + 2u^4 - u^3 - u^2 + 1)$ $\cdot (u^{25} - 2u^{24} + \dots - 5u - 3)$
c_9	$u(u^2 + 2)(u^3 + u^2 - 1)^3(u^{25} - 2u^{24} + \dots + 56u - 16)$
c_{10}	$(u-1)(u+1)^2(u^9 - 3u^7 - u^6 + 3u^5 + 2u^4 - u^3 - u^2 + 1)$ $\cdot (u^{25} - 2u^{24} + \dots - 5u - 3)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_5	$((y-1)^3)(y^9 - 6y^8 + \dots + 2y - 1)$ $\cdot (y^{25} - 10y^{24} + \dots + 97y - 9)$
c_2, c_3, c_8	$y(y+2)^2(y^3 + 3y^2 + 2y - 1)^3(y^{25} + 22y^{24} + \dots + 8y - 4)$
c_4	$((y-1)^3)(y^9 - 6y^8 + \dots - 6y - 1)$ $\cdot (y^{25} + 14y^{24} + \dots + 1561y - 81)$
c_6, c_7, c_{10}	$((y-1)^3)(y^9 - 6y^8 + \dots + 2y - 1)$ $\cdot (y^{25} - 26y^{24} + \dots - 47y - 9)$
c_9	$y(y+2)^2(y^3 - y^2 + 2y - 1)^3(y^{25} - 2y^{24} + \dots - 2624y - 256)$