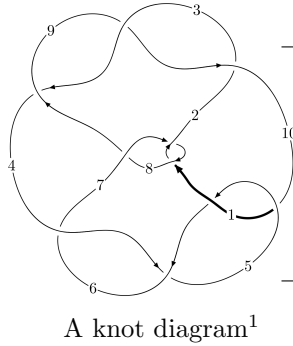
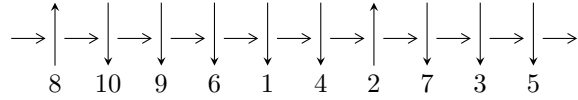


10<sub>67</sub> (K10a<sub>37</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$4,9 \xrightarrow{c_3} 3 \xrightarrow{c_9} 10 \xrightarrow{c_2} 2,7 \xrightarrow{c_6} 6 \xrightarrow{c_4} 5 \xrightarrow{c_8} 8 \xrightarrow{c_1} 1 \longrightarrow c_5, c_7, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 54165895u^{25} - 37175946u^{24} + \dots + 40233748b - 246895131, \\ 25054784u^{25} - 23549273u^{24} + \dots + 10058437a - 172885695, u^{26} - u^{25} + \dots - 10u + 1 \rangle$$

$$I_2^u = \langle -u^3 + b - u, a + u, u^9 + 3u^7 + u^6 + 3u^5 + 2u^4 + 3u^3 + u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle b^2 - b + 1, a + u, u^2 + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 39 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } J_1^u = \langle 5.42 \times 10^7 u^{25} - 3.72 \times 10^7 u^{24} + \dots + 4.02 \times 10^7 b - 2.47 \times 10^8, 2.51 \times 10^7 u^{25} - 2.35 \times 10^7 u^{24} + \dots + 1.01 \times 10^7 a - 1.73 \times 10^8, u^{26} - u^{25} + \dots - 10u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2.49092u^{25} + 2.34125u^{24} + \dots - 66.6876u + 17.1881 \\ -1.34628u^{25} + 0.923999u^{24} + \dots - 34.6377u + 6.13652 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -3.83720u^{25} + 3.26524u^{24} + \dots - 101.325u + 23.3246 \\ -1.34628u^{25} + 0.923999u^{24} + \dots - 34.6377u + 6.13652 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -4.25185u^{25} + 3.16846u^{24} + \dots - 103.985u + 15.7177 \\ 1.25534u^{25} - 1.00540u^{24} + \dots + 37.9947u - 7.88999 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -4.11984u^{25} + 3.49052u^{24} + \dots - 105.381u + 24.5259 \\ -1.33333u^{25} + 0.849641u^{24} + \dots - 31.4642u + 5.50719 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -6.70848u^{25} + 5.09250u^{24} + \dots - 173.700u + 30.5647 \\ 1.11302u^{25} - 1.09292u^{24} + \dots + 24.4986u - 5.45317 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{46161492}{10058437}u^{25} - \frac{42859051}{10058437}u^{24} + \dots + \frac{1130296717}{10058437}u - \frac{328648814}{10058437}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^{26} - u^{25} + \dots - 8u + 1$
$c_2, c_3, c_9$	$u^{26} - u^{25} + \dots - 10u + 1$
$c_4, c_6$	$u^{26} + 8u^{25} + \dots - 19u + 4$
$c_5, c_{10}$	$u^{26} + 2u^{25} + \dots + 3u + 2$
$c_8$	$u^{26} + 9u^{25} + \dots - 10u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y^{26} + 9y^{25} + \dots - 10y + 1$
$c_2, c_3, c_9$	$y^{26} + 29y^{25} + \dots - 42y + 1$
$c_4, c_6$	$y^{26} + 20y^{25} + \dots - 289y + 16$
$c_5, c_{10}$	$y^{26} - 8y^{25} + \dots + 19y + 4$
$c_8$	$y^{26} + 21y^{25} + \dots + 102y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.142027 + 0.957282I$ $a = -0.0519905 + 0.0539815I$ $b = -0.331584 + 0.800882I$	$1.78211 + 2.09880I$	$0.37548 - 4.34730I$
$u = -0.142027 - 0.957282I$ $a = -0.0519905 - 0.0539815I$ $b = -0.331584 - 0.800882I$	$1.78211 - 2.09880I$	$0.37548 + 4.34730I$
$u = 0.867268 + 0.410491I$ $a = 1.15659 + 0.97828I$ $b = -0.39998 - 1.44546I$	$1.87436 - 8.06990I$	$-5.21390 + 7.61920I$
$u = 0.867268 - 0.410491I$ $a = 1.15659 - 0.97828I$ $b = -0.39998 + 1.44546I$	$1.87436 + 8.06990I$	$-5.21390 - 7.61920I$
$u = -0.805271 + 0.489072I$ $a = -1.057530 + 0.864294I$ $b = 0.050804 - 1.204580I$	$2.52884 + 2.28245I$	$-3.60243 - 2.76883I$
$u = -0.805271 - 0.489072I$ $a = -1.057530 - 0.864294I$ $b = 0.050804 + 1.204580I$	$2.52884 - 2.28245I$	$-3.60243 + 2.76883I$
$u = 0.005357 + 1.342280I$ $a = 0.598391 - 0.082953I$ $b = -1.020530 + 0.849992I$	$2.37838 + 1.33649I$	$-3.37936 - 0.64092I$
$u = 0.005357 - 1.342280I$ $a = 0.598391 + 0.082953I$ $b = -1.020530 - 0.849992I$	$2.37838 - 1.33649I$	$-3.37936 + 0.64092I$
$u = 0.620125 + 0.190982I$ $a = 1.70404 + 0.76762I$ $b = -0.941748 - 0.311004I$	$-3.68014 - 3.21386I$	$-12.77386 + 5.40899I$
$u = 0.620125 - 0.190982I$ $a = 1.70404 - 0.76762I$ $b = -0.941748 + 0.311004I$	$-3.68014 + 3.21386I$	$-12.77386 - 5.40899I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.203679 + 1.390330I$ $a = 0.917399 - 0.307104I$ $b = -1.237320 - 0.529870I$	$1.38330 - 6.14693I$	$-5.92538 + 6.07633I$
$u = 0.203679 - 1.390330I$ $a = 0.917399 + 0.307104I$ $b = -1.237320 + 0.529870I$	$1.38330 + 6.14693I$	$-5.92538 - 6.07633I$
$u = -0.09127 + 1.45225I$ $a = -0.858293 - 0.088928I$ $b = 0.632773 + 0.158193I$	$5.55732 + 2.75521I$	$0.17738 - 3.03141I$
$u = -0.09127 - 1.45225I$ $a = -0.858293 + 0.088928I$ $b = 0.632773 - 0.158193I$	$5.55732 - 2.75521I$	$0.17738 + 3.03141I$
$u = -0.345805 + 0.407161I$ $a = -1.277870 - 0.234930I$ $b = 0.165885 + 0.110267I$	$-0.439201 + 1.278560I$	$-4.70955 - 5.15889I$
$u = -0.345805 - 0.407161I$ $a = -1.277870 + 0.234930I$ $b = 0.165885 - 0.110267I$	$-0.439201 - 1.278560I$	$-4.70955 + 5.15889I$
$u = 0.32724 + 1.50601I$ $a = 1.191910 - 0.296128I$ $b = -0.49080 - 1.60111I$	$8.0695 - 12.4216I$	$-2.63275 + 7.54670I$
$u = 0.32724 - 1.50601I$ $a = 1.191910 + 0.296128I$ $b = -0.49080 + 1.60111I$	$8.0695 + 12.4216I$	$-2.63275 - 7.54670I$
$u = -0.28252 + 1.52523I$ $a = -1.160510 - 0.229643I$ $b = 0.300935 - 1.274240I$	$9.09667 + 6.25190I$	$-1.00234 - 2.90360I$
$u = -0.28252 - 1.52523I$ $a = -1.160510 + 0.229643I$ $b = 0.300935 + 1.274240I$	$9.09667 - 6.25190I$	$-1.00234 + 2.90360I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.21524 + 1.54201I$ $a = 0.711239 + 0.409154I$ $b = -0.33688 + 1.58737I$	$10.14430 + 6.11174I$	$0. - 3.37506I$
$u = -0.21524 - 1.54201I$ $a = 0.711239 - 0.409154I$ $b = -0.33688 - 1.58737I$	$10.14430 - 6.11174I$	$0. + 3.37506I$
$u = 0.15473 + 1.55892I$ $a = -0.778021 + 0.341219I$ $b = 0.146371 + 1.395820I$	$10.76070 + 0.12219I$	$0.65472 - 1.66625I$
$u = 0.15473 - 1.55892I$ $a = -0.778021 - 0.341219I$ $b = 0.146371 - 1.395820I$	$10.76070 - 0.12219I$	$0.65472 + 1.66625I$
$u = 0.203738 + 0.030867I$ $a = 4.90464 - 1.72660I$ $b = -0.537925 - 0.970190I$	$-1.75304 - 2.04961I$	$-11.77790 + 2.96215I$
$u = 0.203738 - 0.030867I$ $a = 4.90464 + 1.72660I$ $b = -0.537925 + 0.970190I$	$-1.75304 + 2.04961I$	$-11.77790 - 2.96215I$

$$\text{II. } I_2^u = \langle -u^3 + b - u, a + u, u^9 + 3u^7 + u^6 + 3u^5 + 2u^4 + 3u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^6 + u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 \\ -u^5 - u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^4 + u^2 + 1 \\ -u^6 - 2u^4 - u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^6 - 8u^4 - 4u^3 - 4u^2 - 4u - 10$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_7, c_9$	$u^9 + 3u^7 + u^6 + 3u^5 + 2u^4 + 3u^3 + u^2 + 2u + 1$
$c_4, c_6$	$(u^3 + u^2 + 2u + 1)^3$
$c_5, c_{10}$	$(u^3 - u^2 + 1)^3$
$c_8$	$u^9 + 6u^8 + 15u^7 + 23u^6 + 27u^5 + 24u^4 + 15u^3 + 7u^2 + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_7, c_9$	$y^9 + 6y^8 + 15y^7 + 23y^6 + 27y^5 + 24y^4 + 15y^3 + 7y^2 + 2y - 1$
$c_4, c_6$	$(y^3 + 3y^2 + 2y - 1)^3$
$c_5, c_{10}$	$(y^3 - y^2 + 2y - 1)^3$
$c_8$	$y^9 - 6y^8 + 3y^7 + 23y^6 - 5y^5 - 16y^4 + 43y^3 + 59y^2 + 18y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.656619 + 0.765660I$ $a = -0.656619 - 0.765660I$ $b = -0.215080 + 1.307140I$	$3.02413 + 2.82812I$	$-2.49024 - 2.97945I$
$u = 0.656619 - 0.765660I$ $a = -0.656619 + 0.765660I$ $b = -0.215080 - 1.307140I$	$3.02413 - 2.82812I$	$-2.49024 + 2.97945I$
$u = -0.701160 + 0.628458I$ $a = 0.701160 - 0.628458I$ $b = -0.215080 + 1.307140I$	$3.02413 + 2.82812I$	$-2.49024 - 2.97945I$
$u = -0.701160 - 0.628458I$ $a = 0.701160 + 0.628458I$ $b = -0.215080 - 1.307140I$	$3.02413 - 2.82812I$	$-2.49024 + 2.97945I$
$u = 0.233800 + 1.078880I$ $a = -0.233800 - 1.078880I$ $b = -0.569840$	$-1.11345$	$-9.01951 + 0.I$
$u = 0.233800 - 1.078880I$ $a = -0.233800 + 1.078880I$ $b = -0.569840$	$-1.11345$	$-9.01951 + 0.I$
$u = 0.044542 + 1.394120I$ $a = -0.044542 - 1.394120I$ $b = -0.215080 - 1.307140I$	$3.02413 - 2.82812I$	$-2.49024 + 2.97945I$
$u = 0.044542 - 1.394120I$ $a = -0.044542 + 1.394120I$ $b = -0.215080 + 1.307140I$	$3.02413 + 2.82812I$	$-2.49024 - 2.97945I$
$u = -0.467600$ $a = 0.467600$ $b = -0.569840$	$-1.11345$	$-9.01950$

$$\text{III. } I_3^u = \langle b^2 - b + 1, a + u, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ b \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b - u \\ b \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -bu + b \\ b - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ b + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ bu \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4b - 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_7, c_9$	$(u^2 + 1)^2$
$c_4$	$(u^2 - u + 1)^2$
$c_5, c_{10}$	$u^4 - u^2 + 1$
$c_6$	$(u^2 + u + 1)^2$
$c_8$	$(u + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_7, c_9$	$(y + 1)^4$
$c_4, c_6$	$(y^2 + y + 1)^2$
$c_5, c_{10}$	$(y^2 - y + 1)^2$
$c_8$	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$		$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$1.000000I$		
$a =$	$-1.000000I$	$-2.02988I$	$-6.00000 + 3.46410I$
$b =$	$0.500000 + 0.866025I$		
$u =$	$1.000000I$		
$a =$	$-1.000000I$	$2.02988I$	$-6.00000 - 3.46410I$
$b =$	$0.500000 - 0.866025I$		
$u =$	$-1.000000I$		
$a =$	$1.000000I$	$-2.02988I$	$-6.00000 + 3.46410I$
$b =$	$0.500000 + 0.866025I$		
$u =$	$-1.000000I$		
$a =$	$1.000000I$	$2.02988I$	$-6.00000 - 3.46410I$
$b =$	$0.500000 - 0.866025I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$(u^2 + 1)^2(u^9 + 3u^7 + u^6 + 3u^5 + 2u^4 + 3u^3 + u^2 + 2u + 1)$ $\cdot (u^{26} - u^{25} + \dots - 8u + 1)$
$c_2, c_3, c_9$	$(u^2 + 1)^2(u^9 + 3u^7 + u^6 + 3u^5 + 2u^4 + 3u^3 + u^2 + 2u + 1)$ $\cdot (u^{26} - u^{25} + \dots - 10u + 1)$
$c_4$	$((u^2 - u + 1)^2)(u^3 + u^2 + 2u + 1)^3(u^{26} + 8u^{25} + \dots - 19u + 4)$
$c_5, c_{10}$	$((u^3 - u^2 + 1)^3)(u^4 - u^2 + 1)(u^{26} + 2u^{25} + \dots + 3u + 2)$
$c_6$	$((u^2 + u + 1)^2)(u^3 + u^2 + 2u + 1)^3(u^{26} + 8u^{25} + \dots - 19u + 4)$
$c_8$	$((u + 1)^4)(u^9 + 6u^8 + \dots + 2u - 1)$ $\cdot (u^{26} + 9u^{25} + \dots - 10u + 1)$



### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$((y+1)^4)(y^9 + 6y^8 + \dots + 2y - 1)$ $\cdot (y^{26} + 9y^{25} + \dots - 10y + 1)$
$c_2, c_3, c_9$	$((y+1)^4)(y^9 + 6y^8 + \dots + 2y - 1)$ $\cdot (y^{26} + 29y^{25} + \dots - 42y + 1)$
$c_4, c_6$	$((y^2 + y + 1)^2)(y^3 + 3y^2 + 2y - 1)^3(y^{26} + 20y^{25} + \dots - 289y + 16)$
$c_5, c_{10}$	$((y^2 - y + 1)^2)(y^3 - y^2 + 2y - 1)^3(y^{26} - 8y^{25} + \dots + 19y + 4)$
$c_8$	$((y-1)^4)(y^9 - 6y^8 + \dots + 18y - 1)$ $\cdot (y^{26} + 21y^{25} + \dots + 102y + 1)$