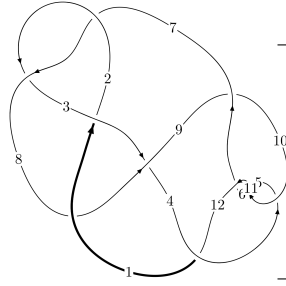
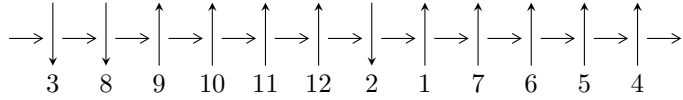


12a₀₇₂₁ (K12a₀₇₂₁)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$6, 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 5 \xrightarrow{c_{11}} 12 \xrightarrow{c_6} 7 \xrightarrow{c_4} 4 \xrightarrow{c_{12}} 1 \xrightarrow{c_9} 9 \xrightarrow{c_3} 3 \xrightarrow{c_8} 8 \xrightarrow{c_2} 2 \gg c_1, c_7$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{85} + u^{84} + \dots + u + 1 \rangle$$

* 1 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 85 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle u^{85} + u^{84} + \dots + u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{10} - 5u^8 - 8u^6 - 3u^4 + 3u^2 + 1 \\ u^{10} + 4u^8 + 5u^6 - 3u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{12} - 5u^{10} - 9u^8 - 6u^6 + u^2 + 1 \\ u^{14} + 6u^{12} + 13u^{10} + 10u^8 - 2u^6 - 4u^4 + u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{29} + 12u^{27} + \dots - 6u^3 - 3u \\ -u^{31} - 13u^{29} + \dots + 24u^7 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{34} - 15u^{32} + \dots - 3u^2 + 1 \\ u^{34} + 14u^{32} + \dots + 8u^4 + u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{70} + 29u^{68} + \dots + 9u^4 + 1 \\ -u^{72} - 30u^{70} + \dots - 6u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $4u^{84} + 4u^{83} + \dots - 8u + 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{85} + 41u^{84} + \dots + 3u + 1$
c_2, c_7	$u^{85} + u^{84} + \dots - u - 1$
c_3	$u^{85} - u^{84} + \dots - 3u - 1$
c_4, c_6	$u^{85} + u^{84} + \dots - 3u - 2$
c_5, c_{10}, c_{11}	$u^{85} - u^{84} + \dots + u - 1$
c_8	$u^{85} + 3u^{84} + \dots - 703u - 192$
c_9, c_{12}	$u^{85} + 7u^{84} + \dots + 433u + 37$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{85} + 7y^{84} + \dots - 21y - 1$
c_2, c_7	$y^{85} - 41y^{84} + \dots + 3y - 1$
c_3	$y^{85} - y^{84} + \dots + 67y - 1$
c_4, c_6	$y^{85} - 45y^{84} + \dots + 9y - 4$
c_5, c_{10}, c_{11}	$y^{85} + 71y^{84} + \dots + 3y - 1$
c_8	$y^{85} + 27y^{84} + \dots + 92545y - 36864$
c_9, c_{12}	$y^{85} + 59y^{84} + \dots - 33697y - 1369$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.248900 + 1.008010I$	$-5.94190 + 0.14890I$	0
$u = -0.248900 - 1.008010I$	$-5.94190 - 0.14890I$	0
$u = -0.297171 + 1.034020I$	$-4.01353 + 7.94113I$	0
$u = -0.297171 - 1.034020I$	$-4.01353 - 7.94113I$	0
$u = 0.280740 + 1.047720I$	$-1.61529 - 3.02389I$	0
$u = 0.280740 - 1.047720I$	$-1.61529 + 3.02389I$	0
$u = 0.270441 + 1.112840I$	$-0.089929 - 1.275270I$	0
$u = 0.270441 - 1.112840I$	$-0.089929 + 1.275270I$	0
$u = -0.278034 + 1.156140I$	$-0.94658 - 3.20959I$	0
$u = -0.278034 - 1.156140I$	$-0.94658 + 3.20959I$	0
$u = 0.209551 + 0.776333I$	$-6.17352 + 0.11601I$	$-1.51814 - 0.75097I$
$u = 0.209551 - 0.776333I$	$-6.17352 - 0.11601I$	$-1.51814 + 0.75097I$
$u = -0.781173 + 0.165218I$	$-1.36801 - 11.97790I$	$5.82993 + 9.11891I$
$u = -0.781173 - 0.165218I$	$-1.36801 + 11.97790I$	$5.82993 - 9.11891I$
$u = 0.775804 + 0.160398I$	$1.06779 + 6.99922I$	$9.02457 - 5.56636I$
$u = 0.775804 - 0.160398I$	$1.06779 - 6.99922I$	$9.02457 + 5.56636I$
$u = -0.766023 + 0.170399I$	$-3.38713 - 4.04703I$	$2.85028 + 3.33634I$
$u = -0.766023 - 0.170399I$	$-3.38713 + 4.04703I$	$2.85028 - 3.33634I$
$u = -0.778318 + 0.031728I$	$4.10355 - 5.77938I$	$10.92900 + 6.00912I$
$u = -0.778318 - 0.031728I$	$4.10355 + 5.77938I$	$10.92900 - 6.00912I$
$u = 0.764543 + 0.137328I$	$2.81551 + 5.13000I$	$10.71873 - 6.57822I$
$u = 0.764543 - 0.137328I$	$2.81551 - 5.13000I$	$10.71873 + 6.57822I$
$u = 0.772607 + 0.016397I$	$5.85261 + 1.00201I$	$14.4008 - 0.7177I$
$u = 0.772607 - 0.016397I$	$5.85261 - 1.00201I$	$14.4008 + 0.7177I$
$u = 0.264885 + 0.713873I$	$-4.48668 + 7.92179I$	$1.27242 - 7.67068I$
$u = 0.264885 - 0.713873I$	$-4.48668 - 7.92179I$	$1.27242 + 7.67068I$
$u = -0.750929 + 0.115587I$	$2.17145 - 0.56664I$	$9.65396 + 0.21560I$
$u = -0.750929 - 0.115587I$	$2.17145 + 0.56664I$	$9.65396 - 0.21560I$
$u = 0.719433 + 0.187623I$	$-4.06922 + 3.45026I$	$2.04119 - 4.45417I$
$u = 0.719433 - 0.187623I$	$-4.06922 - 3.45026I$	$2.04119 + 4.45417I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.228274 + 0.698343I$	$-2.02866 - 3.11378I$	$4.29634 + 4.05625I$
$u = -0.228274 - 0.698343I$	$-2.02866 + 3.11378I$	$4.29634 - 4.05625I$
$u = -0.326512 + 1.230870I$	$0.41498 + 1.78773I$	0
$u = -0.326512 - 1.230870I$	$0.41498 - 1.78773I$	0
$u = -0.184745 + 1.263020I$	$-3.07305 - 2.43438I$	0
$u = -0.184745 - 1.263020I$	$-3.07305 + 2.43438I$	0
$u = 0.688445 + 0.200059I$	$-2.66519 - 4.42958I$	$4.16803 + 2.23694I$
$u = 0.688445 - 0.200059I$	$-2.66519 + 4.42958I$	$4.16803 - 2.23694I$
$u = -0.691627 + 0.177718I$	$-0.102256 - 0.240928I$	$7.49528 + 1.37110I$
$u = -0.691627 - 0.177718I$	$-0.102256 + 0.240928I$	$7.49528 - 1.37110I$
$u = 0.324883 + 1.246210I$	$2.05753 + 2.96009I$	0
$u = 0.324883 - 1.246210I$	$2.05753 - 2.96009I$	0
$u = 0.116828 + 1.284750I$	$-6.28256 - 0.70523I$	0
$u = 0.116828 - 1.284750I$	$-6.28256 + 0.70523I$	0
$u = -0.699942$	1.55328	6.87670
$u = 0.329649 + 1.271860I$	$1.85314 + 4.97870I$	0
$u = 0.329649 - 1.271860I$	$1.85314 - 4.97870I$	0
$u = -0.290553 + 1.282560I$	$-2.46212 - 3.58115I$	0
$u = -0.290553 - 1.282560I$	$-2.46212 + 3.58115I$	0
$u = 0.182008 + 1.306080I$	$-5.59206 + 6.55252I$	0
$u = 0.182008 - 1.306080I$	$-5.59206 - 6.55252I$	0
$u = -0.334981 + 1.281900I$	$0.01669 - 9.79487I$	0
$u = -0.334981 - 1.281900I$	$0.01669 + 9.79487I$	0
$u = -0.317650 + 1.339370I$	$-2.41072 - 4.43457I$	0
$u = -0.317650 - 1.339370I$	$-2.41072 + 4.43457I$	0
$u = -0.013172 + 1.384380I$	$-6.34751 - 2.22482I$	0
$u = -0.013172 - 1.384380I$	$-6.34751 + 2.22482I$	0
$u = 0.324897 + 1.349170I$	$-1.86872 + 9.07355I$	0
$u = 0.324897 - 1.349170I$	$-1.86872 - 9.07355I$	0
$u = -0.293142 + 1.358620I$	$-4.94324 - 3.84382I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.293142 - 1.358620I$	$-4.94324 + 3.84382I$	0
$u = 0.288385 + 1.364890I$	$-7.59509 - 0.86185I$	0
$u = 0.288385 - 1.364890I$	$-7.59509 + 0.86185I$	0
$u = 0.301046 + 1.365670I$	$-8.97185 + 7.16378I$	0
$u = 0.301046 - 1.365670I$	$-8.97185 - 7.16378I$	0
$u = 0.328741 + 1.361380I$	$-3.73450 + 10.99570I$	0
$u = 0.328741 - 1.361380I$	$-3.73450 - 10.99570I$	0
$u = -0.323051 + 1.364830I$	$-8.23465 - 7.99145I$	0
$u = -0.323051 - 1.364830I$	$-8.23465 + 7.99145I$	0
$u = -0.330797 + 1.364300I$	$-6.1963 - 15.9996I$	0
$u = -0.330797 - 1.364300I$	$-6.1963 + 15.9996I$	0
$u = -0.023413 + 1.410440I$	$-8.46842 - 3.63559I$	0
$u = -0.023413 - 1.410440I$	$-8.46842 + 3.63559I$	0
$u = 0.02698 + 1.41604I$	$-11.02750 + 8.52728I$	0
$u = 0.02698 - 1.41604I$	$-11.02750 - 8.52728I$	0
$u = 0.01432 + 1.41634I$	$-12.76900 + 0.46813I$	0
$u = 0.01432 - 1.41634I$	$-12.76900 - 0.46813I$	0
$u = -0.159545 + 0.546638I$	$-0.43421 - 1.85967I$	$4.91547 + 5.62191I$
$u = -0.159545 - 0.546638I$	$-0.43421 + 1.85967I$	$4.91547 - 5.62191I$
$u = 0.408138 + 0.257025I$	$-0.93232 + 4.40586I$	$5.40236 - 8.36399I$
$u = 0.408138 - 0.257025I$	$-0.93232 - 4.40586I$	$5.40236 + 8.36399I$
$u = 0.266823 + 0.380763I$	$-1.43413 - 1.94308I$	$2.89552 - 0.96140I$
$u = 0.266823 - 0.380763I$	$-1.43413 + 1.94308I$	$2.89552 + 0.96140I$
$u = -0.391169 + 0.128683I$	$0.923187 - 0.319535I$	$11.07004 + 2.67367I$
$u = -0.391169 - 0.128683I$	$0.923187 + 0.319535I$	$11.07004 - 2.67367I$

II. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$u^{85} + 41u^{84} + \dots + 3u + 1$
c_2, c_7	$u^{85} + u^{84} + \dots - u - 1$
c_3	$u^{85} - u^{84} + \dots - 3u - 1$
c_4, c_6	$u^{85} + u^{84} + \dots - 3u - 2$
c_5, c_{10}, c_{11}	$u^{85} - u^{84} + \dots + u - 1$
c_8	$u^{85} + 3u^{84} + \dots - 703u - 192$
c_9, c_{12}	$u^{85} + 7u^{84} + \dots + 433u + 37$

III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$y^{85} + 7y^{84} + \dots - 21y - 1$
c_2, c_7	$y^{85} - 41y^{84} + \dots + 3y - 1$
c_3	$y^{85} - y^{84} + \dots + 67y - 1$
c_4, c_6	$y^{85} - 45y^{84} + \dots + 9y - 4$
c_5, c_{10}, c_{11}	$y^{85} + 71y^{84} + \dots + 3y - 1$
c_8	$y^{85} + 27y^{84} + \dots + 92545y - 36864$
c_9, c_{12}	$y^{85} + 59y^{84} + \dots - 33697y - 1369$