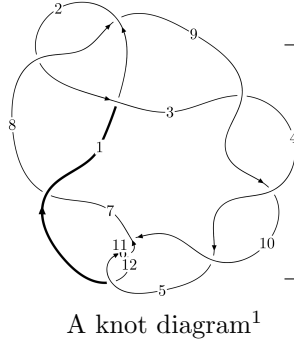
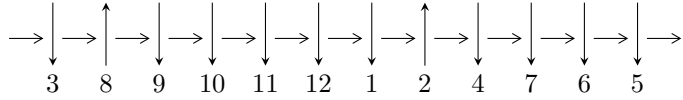


12a<sub>0724</sub> (K12a<sub>0724</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$2,9 \xrightarrow{c_8} 8 \xrightarrow{c_2} 3 \xrightarrow{c_3} 4 \xrightarrow{c_9} 10 \xrightarrow{c_4} 5 \xrightarrow{c_1} 1 \xrightarrow{c_7} 7 \xrightarrow{c_{10}} 11 \xrightarrow{c_{12}} 12 \xrightarrow{c_6} 6 \gg c_5, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{53} - u^{52} + \dots - u - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 53 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{53} - u^{52} + \dots - u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^9 + 2u^7 + u^5 - 2u^3 - u \\ -u^9 - 3u^7 - 3u^5 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^6 - u^4 + 1 \\ -u^8 - 2u^6 - 2u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{20} - 5u^{18} - 11u^{16} - 10u^{14} + 2u^{12} + 13u^{10} + 9u^8 - 2u^6 - 5u^4 - u^2 + 1 \\ -u^{22} - 6u^{20} - 17u^{18} - 26u^{16} - 20u^{14} + 13u^{10} + 10u^8 + 3u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{23} + 6u^{21} + \dots + 6u^5 + 2u^3 \\ -u^{23} - 7u^{21} + \dots - 3u^5 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{51} + 14u^{49} + \dots - u^3 - 2u \\ u^{52} - u^{51} + \dots + 2u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^{52} - 4u^{51} + \dots - 8u - 14$

(iv) u-Polynomials at the component

| Crossings                | u-Polynomials at each crossing       |
|--------------------------|--------------------------------------|
| $c_1$                    | $u^{53} + 31u^{52} + \dots + 3u - 1$ |
| $c_2, c_8$               | $u^{53} - u^{52} + \dots - u - 1$    |
| $c_3, c_4, c_7$<br>$c_9$ | $u^{53} + u^{52} + \dots + 17u - 5$  |
| $c_5, c_6, c_{11}$       | $u^{53} - u^{52} + \dots - 3u - 1$   |
| $c_{10}, c_{12}$         | $u^{53} + 3u^{52} + \dots - 15u - 3$ |

(v) Riley Polynomials at the component

| Crossings                | Riley Polynomials at each crossing      |
|--------------------------|---|
| $c_1$                    | $y^{53} - 17y^{52} + \dots + 35y - 1$   |
| $c_2, c_8$               | $y^{53} + 31y^{52} + \dots + 3y - 1$    |
| $c_3, c_4, c_7$<br>$c_9$ | $y^{53} - 65y^{52} + \dots + 899y - 25$ |
| $c_5, c_6, c_{11}$       | $y^{53} - 45y^{52} + \dots + 3y - 1$    |
| $c_{10}, c_{12}$         | $y^{53} + 23y^{52} + \dots + 39y - 9$   |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.128755 + 1.019230I$ | $-4.90434 - 2.79376I$                 | $-17.4626 + 3.5787I$   |
| $u = -0.128755 - 1.019230I$ | $-4.90434 + 2.79376I$                 | $-17.4626 - 3.5787I$   |
| $u = -0.911842$             | $-15.0851$                            | $-15.7790$             |
| $u = 0.452670 + 0.785816I$  | $-0.74858 + 5.61733I$                 | $-7.84958 - 7.79371I$  |
| $u = 0.452670 - 0.785816I$  | $-0.74858 - 5.61733I$                 | $-7.84958 + 7.79371I$  |
| $u = 0.904077 + 0.035348I$  | $-10.76820 - 8.15829I$                | $-12.92275 + 4.70754I$ |
| $u = 0.904077 - 0.035348I$  | $-10.76820 + 8.15829I$                | $-12.92275 - 4.70754I$ |
| $u = -0.894263 + 0.030410I$ | $-5.73332 + 4.23818I$                 | $-8.49578 - 3.55105I$  |
| $u = -0.894263 - 0.030410I$ | $-5.73332 - 4.23818I$                 | $-8.49578 + 3.55105I$  |
| $u = -0.435840 + 1.018520I$ | $-3.18288 - 2.63277I$                 | $-11.73208 + 4.34581I$ |
| $u = -0.435840 - 1.018520I$ | $-3.18288 + 2.63277I$                 | $-11.73208 - 4.34581I$ |
| $u = 0.270662 + 1.080700I$  | $-1.60759 + 0.28866I$                 | $-11.63603 + 0.60703I$ |
| $u = 0.270662 - 1.080700I$  | $-1.60759 - 0.28866I$                 | $-11.63603 - 0.60703I$ |
| $u = 0.885161 + 0.012504I$  | $-7.93829 - 0.20732I$                 | $-11.52979 - 0.97702I$ |
| $u = 0.885161 - 0.012504I$  | $-7.93829 + 0.20732I$                 | $-11.52979 + 0.97702I$ |
| $u = -0.366265 + 1.058630I$ | $-3.39452 - 3.18652I$                 | $-15.1026 + 5.9997I$   |
| $u = -0.366265 - 1.058630I$ | $-3.39452 + 3.18652I$                 | $-15.1026 - 5.9997I$   |
| $u = -0.438529 + 0.736447I$ | $3.30946 - 1.89439I$                  | $-2.29810 + 4.47995I$  |
| $u = -0.438529 - 0.736447I$ | $3.30946 + 1.89439I$                  | $-2.29810 - 4.47995I$  |
| $u = 0.459270 + 1.056820I$  | $-0.23945 + 6.31415I$                 | $-8.00000 - 7.97292I$  |
| $u = 0.459270 - 1.056820I$  | $-0.23945 - 6.31415I$                 | $-8.00000 + 7.97292I$  |
| $u = -0.271764 + 1.127110I$ | $-6.33973 + 3.10223I$                 | $-16.8942 - 2.0365I$   |
| $u = -0.271764 - 1.127110I$ | $-6.33973 - 3.10223I$                 | $-16.8942 + 2.0365I$   |
| $u = -0.471846 + 1.075850I$ | $-4.85947 - 10.15110I$                | $-13.4245 + 9.4204I$   |
| $u = -0.471846 - 1.075850I$ | $-4.85947 + 10.15110I$                | $-13.4245 - 9.4204I$   |
| $u = 0.147653 + 0.799603I$  | $-0.621747 + 0.938340I$               | $-10.16569 - 6.80292I$ |
| $u = 0.147653 - 0.799603I$  | $-0.621747 - 0.938340I$               | $-10.16569 + 6.80292I$ |
| $u = 0.443085 + 0.672743I$  | $-0.43986 - 1.77287I$                 | $-6.55805 - 0.17659I$  |
| $u = 0.443085 - 0.672743I$  | $-0.43986 + 1.77287I$                 | $-6.55805 + 0.17659I$  |
| $u = 0.386940 + 1.130380I$  | $-9.24218 + 3.74726I$                 | $-18.6066 + 0.I$       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.386940 - 1.130380I$  | $-9.24218 - 3.74726I$                 | $-18.6066 + 0.I$       |
| $u = -0.626369 + 0.230684I$ | $-2.49578 + 5.92364I$                 | $-10.03468 - 5.69400I$ |
| $u = -0.626369 - 0.230684I$ | $-2.49578 - 5.92364I$                 | $-10.03468 + 5.69400I$ |
| $u = 0.461426 + 1.259080I$  | $-11.80210 + 4.57211I$                | 0                      |
| $u = 0.461426 - 1.259080I$  | $-11.80210 - 4.57211I$                | 0                      |
| $u = 0.474991 + 1.254660I$  | $-11.70120 + 5.05761I$                | 0                      |
| $u = 0.474991 - 1.254660I$  | $-11.70120 - 5.05761I$                | 0                      |
| $u = -0.452029 + 1.266230I$ | $-9.69650 - 0.52013I$                 | 0                      |
| $u = -0.452029 - 1.266230I$ | $-9.69650 + 0.52013I$                 | 0                      |
| $u = -0.485137 + 1.256070I$ | $-9.45189 - 9.16998I$                 | 0                      |
| $u = -0.485137 - 1.256070I$ | $-9.45189 + 9.16998I$                 | 0                      |
| $u = 0.450332 + 1.273070I$  | $-14.7839 - 3.3745I$                  | 0                      |
| $u = 0.450332 - 1.273070I$  | $-14.7839 + 3.3745I$                  | 0                      |
| $u = 0.489645 + 1.259800I$  | $-14.4913 + 13.1415I$                 | 0                      |
| $u = 0.489645 - 1.259800I$  | $-14.4913 - 13.1415I$                 | 0                      |
| $u = 0.647347$              | $-6.05533$                            | $-14.6560$             |
| $u = -0.472487 + 1.271320I$ | $-18.9745 - 4.9215I$                  | 0                      |
| $u = -0.472487 - 1.271320I$ | $-18.9745 + 4.9215I$                  | 0                      |
| $u = 0.573524 + 0.250742I$  | $1.98282 - 2.24507I$                  | $-4.39655 + 3.93832I$  |
| $u = 0.573524 - 0.250742I$  | $1.98282 + 2.24507I$                  | $-4.39655 - 3.93832I$  |
| $u = -0.505614 + 0.326260I$ | $-1.29579 - 1.22009I$                 | $-7.56412 + 0.50390I$  |
| $u = -0.505614 - 0.326260I$ | $-1.29579 + 1.22009I$                 | $-7.56412 - 0.50390I$  |
| $u = -0.436579$             | $-0.780224$                           | $-12.8270$             |

## II. u-Polynomials

| Crossings                | u-Polynomials at each crossing       |
|--------------------------|--------------------------------------|
| $c_1$                    | $u^{53} + 31u^{52} + \dots + 3u - 1$ |
| $c_2, c_8$               | $u^{53} - u^{52} + \dots - u - 1$    |
| $c_3, c_4, c_7$<br>$c_9$ | $u^{53} + u^{52} + \dots + 17u - 5$  |
| $c_5, c_6, c_{11}$       | $u^{53} - u^{52} + \dots - 3u - 1$   |
| $c_{10}, c_{12}$         | $u^{53} + 3u^{52} + \dots - 15u - 3$ |

### III. Riley Polynomials

| Crossings                | Riley Polynomials at each crossing      |
|--------------------------|---|
| $c_1$                    | $y^{53} - 17y^{52} + \dots + 35y - 1$   |
| $c_2, c_8$               | $y^{53} + 31y^{52} + \dots + 3y - 1$    |
| $c_3, c_4, c_7$<br>$c_9$ | $y^{53} - 65y^{52} + \dots + 899y - 25$ |
| $c_5, c_6, c_{11}$       | $y^{53} - 45y^{52} + \dots + 3y - 1$    |
| $c_{10}, c_{12}$         | $y^{53} + 23y^{52} + \dots + 39y - 9$   |