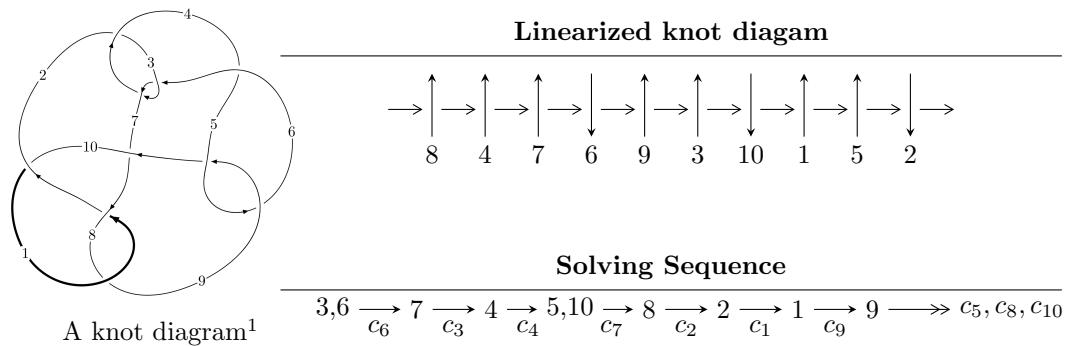


## 10<sub>73</sub> ( $K10a_3$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -u^{42} - u^{41} + \dots + u^2 + b, -11u^{42} - 26u^{41} + \dots + 2a + 15, u^{43} + 3u^{42} + \dots - 3u - 1 \rangle$$

$$I_2^u = \langle b, a^2 - a + 1, u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^{42} - u^{41} + \dots + u^2 + b, -11u^{42} - 26u^{41} + \dots + 2a + 15, u^{43} + 3u^{42} + \dots - 3u - 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{11}{2}u^{42} + 13u^{41} + \dots - 13u - \frac{15}{2} \\ u^{42} + u^{41} + \dots - u^3 - u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{2}u^{42} - u^{41} + \dots + u + \frac{1}{2} \\ u^{11} - 3u^9 - 2u^8 + 4u^7 + 4u^6 - u^5 - 4u^4 - u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 5u^{42} + 11u^{41} + \dots - 11u - 6 \\ \frac{3}{2}u^{42} + 3u^{41} + \dots - 2u - \frac{3}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{11}{2}u^{42} + 11u^{41} + \dots - 11u - \frac{13}{2} \\ u^{41} + 2u^{40} + \dots - u - 1 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-6u^{42} - 15u^{41} + \dots + 19u + 13$

**(iv) u-Polynomials at the component**

| Crossings  | u-Polynomials at each crossing           |
|------------|--|
| $c_1, c_8$ | $u^{43} + 2u^{42} + \cdots + 4u^2 - 1$   |
| $c_2$      | $u^{43} - 23u^{42} + \cdots + 3u - 1$    |
| $c_3, c_6$ | $u^{43} + 3u^{42} + \cdots - 3u - 1$     |
| $c_4$      | $u^{43} + 15u^{42} + \cdots - 136u - 16$ |
| $c_5, c_9$ | $u^{43} - u^{42} + \cdots + 8u - 4$      |
| $c_7$      | $u^{43} - 2u^{42} + \cdots + 54u - 9$    |
| $c_{10}$   | $u^{43} + 20u^{42} + \cdots + 8u - 1$    |

**(v) Riley Polynomials at the component**

| Crossings  | Riley Polynomials at each crossing         |
|------------|--|
| $c_1, c_8$ | $y^{43} + 20y^{42} + \cdots + 8y - 1$      |
| $c_2$      | $y^{43} - 3y^{42} + \cdots + 23y - 1$      |
| $c_3, c_6$ | $y^{43} - 23y^{42} + \cdots + 3y - 1$      |
| $c_4$      | $y^{43} + 23y^{42} + \cdots + 4128y - 256$ |
| $c_5, c_9$ | $y^{43} + 15y^{42} + \cdots - 136y - 16$   |
| $c_7$      | $y^{43} - 4y^{42} + \cdots + 2520y - 81$   |
| $c_{10}$   | $y^{43} + 8y^{42} + \cdots + 140y - 1$     |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.702205 + 0.692426I$ |                                       |                       |
| $a = -0.216763 + 1.063530I$ | $-5.79250 + 1.33127I$                 | $-3.13829 - 0.68119I$ |
| $b = -0.000164 - 0.427737I$ |                                       |                       |
| $u = -0.702205 - 0.692426I$ |                                       |                       |
| $a = -0.216763 - 1.063530I$ | $-5.79250 - 1.33127I$                 | $-3.13829 + 0.68119I$ |
| $b = -0.000164 + 0.427737I$ |                                       |                       |
| $u = -0.781262 + 0.586254I$ |                                       |                       |
| $a = 0.083513 - 0.751531I$  | $-2.37041 - 2.31340I$                 | $1.61332 + 3.65794I$  |
| $b = -0.318284 + 0.078334I$ |                                       |                       |
| $u = -0.781262 - 0.586254I$ |                                       |                       |
| $a = 0.083513 + 0.751531I$  | $-2.37041 + 2.31340I$                 | $1.61332 - 3.65794I$  |
| $b = -0.318284 - 0.078334I$ |                                       |                       |
| $u = 0.983429 + 0.401988I$  |                                       |                       |
| $a = -0.18299 + 1.51178I$   | $0.117899 + 0.694763I$                | $2.77512 - 0.93635I$  |
| $b = 0.95580 - 1.21635I$    |                                       |                       |
| $u = 0.983429 - 0.401988I$  |                                       |                       |
| $a = -0.18299 - 1.51178I$   | $0.117899 - 0.694763I$                | $2.77512 + 0.93635I$  |
| $b = 0.95580 + 1.21635I$    |                                       |                       |
| $u = -0.856054 + 0.662832I$ |                                       |                       |
| $a = -0.459912 + 0.582589I$ | $-5.34910 - 6.48185I$                 | $-1.72488 + 7.04551I$ |
| $b = 0.671689 - 0.315858I$  |                                       |                       |
| $u = -0.856054 - 0.662832I$ |                                       |                       |
| $a = -0.459912 - 0.582589I$ | $-5.34910 + 6.48185I$                 | $-1.72488 - 7.04551I$ |
| $b = 0.671689 + 0.315858I$  |                                       |                       |
| $u = -0.225042 + 0.862192I$ |                                       |                       |
| $a = -0.295884 - 0.330542I$ | $-1.69061 + 8.49752I$                 | $0.86281 - 6.51033I$  |
| $b = 1.27608 - 1.18759I$    |                                       |                       |
| $u = -0.225042 - 0.862192I$ |                                       |                       |
| $a = -0.295884 + 0.330542I$ | $-1.69061 - 8.49752I$                 | $0.86281 + 6.51033I$  |
| $b = 1.27608 + 1.18759I$    |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.344780 + 0.758252I$ |                                       |                        |
| $a = -0.130381 - 0.811333I$ | $-4.05606 + 1.05891I$                 | $-2.88403 - 0.52575I$  |
| $b = 0.921218 - 0.514197I$  |                                       |                        |
| $u = -0.344780 - 0.758252I$ |                                       |                        |
| $a = -0.130381 + 0.811333I$ | $-4.05606 - 1.05891I$                 | $-2.88403 + 0.52575I$  |
| $b = 0.921218 + 0.514197I$  |                                       |                        |
| $u = -0.199953 + 0.800457I$ |                                       |                        |
| $a = 0.051467 + 0.372242I$  | $0.47003 + 3.49797I$                  | $3.95877 - 2.64358I$   |
| $b = -0.93072 + 1.17107I$   |                                       |                        |
| $u = -0.199953 - 0.800457I$ |                                       |                        |
| $a = 0.051467 - 0.372242I$  | $0.47003 - 3.49797I$                  | $3.95877 + 2.64358I$   |
| $b = -0.93072 - 1.17107I$   |                                       |                        |
| $u = 1.178400 + 0.107020I$  |                                       |                        |
| $a = 0.396216 - 0.024715I$  | $0.86535 + 1.34877I$                  | $0.663414 + 0.523198I$ |
| $b = -0.090847 - 0.484893I$ |                                       |                        |
| $u = 1.178400 - 0.107020I$  |                                       |                        |
| $a = 0.396216 + 0.024715I$  | $0.86535 - 1.34877I$                  | $0.663414 - 0.523198I$ |
| $b = -0.090847 + 0.484893I$ |                                       |                        |
| $u = -1.113040 + 0.411275I$ |                                       |                        |
| $a = -1.45881 + 1.05016I$   | $3.14686 - 0.23394I$                  | $6.25545 + 1.76917I$   |
| $b = -0.432177 - 1.242820I$ |                                       |                        |
| $u = -1.113040 - 0.411275I$ |                                       |                        |
| $a = -1.45881 - 1.05016I$   | $3.14686 + 0.23394I$                  | $6.25545 - 1.76917I$   |
| $b = -0.432177 + 1.242820I$ |                                       |                        |
| $u = 1.140070 + 0.437496I$  |                                       |                        |
| $a = -0.80318 - 1.92969I$   | $4.51030 + 2.45703I$                  | $9.07720 - 1.39524I$   |
| $b = -0.35123 + 1.92571I$   |                                       |                        |
| $u = 1.140070 - 0.437496I$  |                                       |                        |
| $a = -0.80318 + 1.92969I$   | $4.51030 - 2.45703I$                  | $9.07720 + 1.39524I$   |
| $b = -0.35123 - 1.92571I$   |                                       |                        |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = 1.126240 + 0.485857I$  |                                       |                      |
| $a = 0.62977 + 2.31079I$    | $2.59778 + 7.42216I$                  | $5.67783 - 6.16302I$ |
| $b = 0.62085 - 2.17017I$    |                                       |                      |
| $u = 1.126240 - 0.485857I$  |                                       |                      |
| $a = 0.62977 - 2.31079I$    | $2.59778 - 7.42216I$                  | $5.67783 + 6.16302I$ |
| $b = 0.62085 + 2.17017I$    |                                       |                      |
| $u = -1.139980 + 0.455119I$ |                                       |                      |
| $a = 1.12604 - 1.46501I$    | $4.38701 - 5.48645I$                  | $8.10083 + 6.46210I$ |
| $b = 0.68367 + 1.40137I$    |                                       |                      |
| $u = -1.139980 - 0.455119I$ |                                       |                      |
| $a = 1.12604 + 1.46501I$    | $4.38701 + 5.48645I$                  | $8.10083 - 6.46210I$ |
| $b = 0.68367 - 1.40137I$    |                                       |                      |
| $u = 0.769344$              |                                       |                      |
| $a = -0.716816$             | 1.12210                               | 9.24310              |
| $b = 0.736269$              |                                       |                      |
| $u = -1.116400 + 0.556388I$ |                                       |                      |
| $a = -0.04192 + 1.41433I$   | $-1.77735 - 6.01104I$                 | $0. + 4.92263I$      |
| $b = -1.30408 - 1.10564I$   |                                       |                      |
| $u = -1.116400 - 0.556388I$ |                                       |                      |
| $a = -0.04192 - 1.41433I$   | $-1.77735 + 6.01104I$                 | $0. - 4.92263I$      |
| $b = -1.30408 + 1.10564I$   |                                       |                      |
| $u = 1.207770 + 0.337329I$  |                                       |                      |
| $a = -1.27016 - 1.08338I$   | $4.74199 + 0.21154I$                  | $9.28481 + 0.I$      |
| $b = 0.27337 + 1.44443I$    |                                       |                      |
| $u = 1.207770 - 0.337329I$  |                                       |                      |
| $a = -1.27016 + 1.08338I$   | $4.74199 - 0.21154I$                  | $9.28481 + 0.I$      |
| $b = 0.27337 - 1.44443I$    |                                       |                      |
| $u = 0.596984 + 0.406248I$  |                                       |                      |
| $a = 1.37593 - 0.78349I$    | $-1.01538 + 2.84865I$                 | $1.39768 - 5.43636I$ |
| $b = -1.384640 - 0.071781I$ |                                       |                      |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.596984 - 0.406248I$  | $-1.01538 - 2.84865I$                 | $1.39768 + 5.43636I$  |
| $a = 1.37593 + 0.78349I$    |                                       |                       |
| $b = -1.384640 + 0.071781I$ |                                       |                       |
| $u = 1.253070 + 0.301863I$  | $3.01994 - 4.67918I$                  | $0. + 5.37573I$       |
| $a = 1.51757 + 0.68122I$    |                                       |                       |
| $b = -0.561583 - 1.231910I$ |                                       |                       |
| $u = 1.253070 - 0.301863I$  | $3.01994 + 4.67918I$                  | $0. - 5.37573I$       |
| $a = 1.51757 - 0.68122I$    |                                       |                       |
| $b = -0.561583 + 1.231910I$ |                                       |                       |
| $u = -1.177230 + 0.535254I$ | $3.34693 - 8.44363I$                  | 0                     |
| $a = 0.33951 - 2.06230I$    |                                       |                       |
| $b = 1.28426 + 1.59104I$    |                                       |                       |
| $u = -1.177230 - 0.535254I$ | $3.34693 + 8.44363I$                  | 0                     |
| $a = 0.33951 + 2.06230I$    |                                       |                       |
| $b = 1.28426 - 1.59104I$    |                                       |                       |
| $u = -0.674002 + 0.118500I$ | $0.77235 - 2.35753I$                  | $-0.15632 + 5.03988I$ |
| $a = -0.26643 - 1.82830I$   |                                       |                       |
| $b = -0.006255 - 0.381927I$ |                                       |                       |
| $u = -0.674002 - 0.118500I$ | $0.77235 + 2.35753I$                  | $-0.15632 - 5.03988I$ |
| $a = -0.26643 + 1.82830I$   |                                       |                       |
| $b = -0.006255 + 0.381927I$ |                                       |                       |
| $u = -1.191540 + 0.559537I$ | $1.20075 - 13.70690I$                 | 0                     |
| $a = -0.06666 + 2.26638I$   |                                       |                       |
| $b = -1.51037 - 1.66131I$   |                                       |                       |
| $u = -1.191540 - 0.559537I$ | $1.20075 + 13.70690I$                 | 0                     |
| $a = -0.06666 - 2.26638I$   |                                       |                       |
| $b = -1.51037 + 1.66131I$   |                                       |                       |
| $u = -0.025551 + 0.621606I$ | $1.39154 + 1.44262I$                  | $5.16219 - 3.23191I$  |
| $a = -0.721932 + 0.454368I$ |                                       |                       |
| $b = 0.017381 + 1.186670I$  |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.025551 - 0.621606I$ |                                       |                      |
| $a = -0.721932 - 0.454368I$ | $1.39154 - 1.44262I$                  | $5.16219 + 3.23191I$ |
| $b = 0.017381 - 1.186670I$  |                                       |                      |
| $u = 0.176403 + 0.591173I$  |                                       |                      |
| $a = 1.253380 - 0.348319I$  | $-0.03125 - 3.16118I$                 | $2.63487 + 2.30647I$ |
| $b = -0.682100 - 1.225820I$ |                                       |                      |
| $u = 0.176403 - 0.591173I$  |                                       |                      |
| $a = 1.253380 + 0.348319I$  | $-0.03125 + 3.16118I$                 | $2.63487 - 2.30647I$ |
| $b = -0.682100 + 1.225820I$ |                                       |                      |

$$\text{II. } I_2^u = \langle b, a^2 - a + 1, u - 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ a \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** =  $4a + 7$

**(iv) u-Polynomials at the component**

| Crossings          | u-Polynomials at each crossing |
|--------------------|--------------------------------|
| $c_1, c_7, c_{10}$ | $u^2 - u + 1$                  |
| $c_2, c_3$         | $(u + 1)^2$                    |
| $c_4, c_5, c_9$    | $u^2$                          |
| $c_6$              | $(u - 1)^2$                    |
| $c_8$              | $u^2 + u + 1$                  |

**(v) Riley Polynomials at the component**

| Crossings                   | Riley Polynomials at each crossing |
|-----------------------------|------------------------------------|
| $c_1, c_7, c_8$<br>$c_{10}$ | $y^2 + y + 1$                      |
| $c_2, c_3, c_6$             | $(y - 1)^2$                        |
| $c_4, c_5, c_9$             | $y^2$                              |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_2^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|----------------------------|---------------------------------------|----------------------|
| $u = 1.00000$              |                                       |                      |
| $a = 0.500000 + 0.866025I$ | $1.64493 - 2.02988I$                  | $9.00000 + 3.46410I$ |
| $b = 0$                    |                                       |                      |
| $u = 1.00000$              |                                       |                      |
| $a = 0.500000 - 0.866025I$ | $1.64493 + 2.02988I$                  | $9.00000 - 3.46410I$ |
| $b = 0$                    |                                       |                      |

### III. u-Polynomials

| Crossings  | u-Polynomials at each crossing                        |
|------------|---|
| $c_1$      | $(u^2 - u + 1)(u^{43} + 2u^{42} + \cdots + 4u^2 - 1)$ |
| $c_2$      | $((u + 1)^2)(u^{43} - 23u^{42} + \cdots + 3u - 1)$    |
| $c_3$      | $((u + 1)^2)(u^{43} + 3u^{42} + \cdots - 3u - 1)$     |
| $c_4$      | $u^2(u^{43} + 15u^{42} + \cdots - 136u - 16)$         |
| $c_5, c_9$ | $u^2(u^{43} - u^{42} + \cdots + 8u - 4)$              |
| $c_6$      | $((u - 1)^2)(u^{43} + 3u^{42} + \cdots - 3u - 1)$     |
| $c_7$      | $(u^2 - u + 1)(u^{43} - 2u^{42} + \cdots + 54u - 9)$  |
| $c_8$      | $(u^2 + u + 1)(u^{43} + 2u^{42} + \cdots + 4u^2 - 1)$ |
| $c_{10}$   | $(u^2 - u + 1)(u^{43} + 20u^{42} + \cdots + 8u - 1)$  |

#### IV. Riley Polynomials

| Crossings  | Riley Polynomials at each crossing                      |
|------------|---|
| $c_1, c_8$ | $(y^2 + y + 1)(y^{43} + 20y^{42} + \cdots + 8y - 1)$    |
| $c_2$      | $((y - 1)^2)(y^{43} - 3y^{42} + \cdots + 23y - 1)$      |
| $c_3, c_6$ | $((y - 1)^2)(y^{43} - 23y^{42} + \cdots + 3y - 1)$      |
| $c_4$      | $y^2(y^{43} + 23y^{42} + \cdots + 4128y - 256)$         |
| $c_5, c_9$ | $y^2(y^{43} + 15y^{42} + \cdots - 136y - 16)$           |
| $c_7$      | $(y^2 + y + 1)(y^{43} - 4y^{42} + \cdots + 2520y - 81)$ |
| $c_{10}$   | $(y^2 + y + 1)(y^{43} + 8y^{42} + \cdots + 140y - 1)$   |