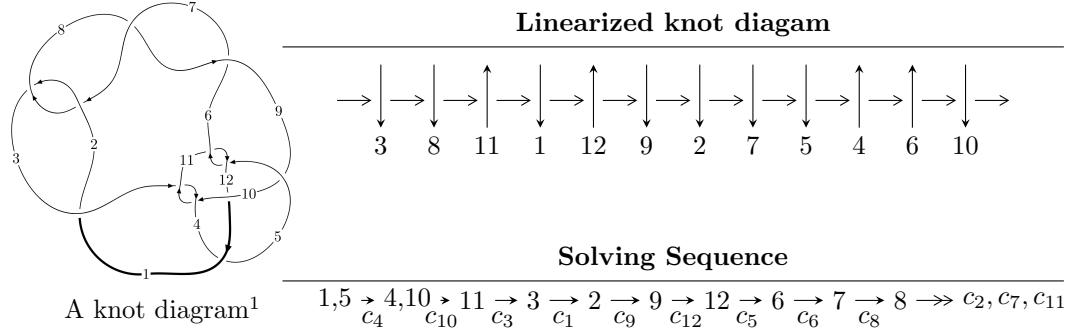


## $12a_{0799}$ ( $K12a_{0799}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle b - u, -4.30859 \times 10^{43}u^{34} - 5.23230 \times 10^{43}u^{33} + \dots + 2.27410 \times 10^{43}a + 1.99881 \times 10^{44}, \\
 &\quad u^{35} + u^{34} + \dots - 2u - 1 \rangle \\
 I_2^u &= \langle 1.34503 \times 10^{309}u^{71} + 4.07190 \times 10^{309}u^{70} + \dots + 3.30547 \times 10^{309}b + 2.52151 \times 10^{310}, \\
 &\quad - 2.10209 \times 10^{240}u^{71} - 6.36722 \times 10^{240}u^{70} + \dots + 3.89663 \times 10^{240}a - 1.36055 \times 10^{242}, \\
 &\quad u^{72} + 3u^{71} + \dots + 48u + 1 \rangle \\
 I_3^u &= \langle b + u, -886u^{19} - 1725u^{18} + \dots + 2249a + 1906, u^{20} + u^{19} + \dots - 2u + 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 127 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b - u, -4.31 \times 10^{43}u^{34} - 5.23 \times 10^{43}u^{33} + \dots + 2.27 \times 10^{43}a + 2.00 \times 10^{44}, u^{35} + u^{34} + \dots - 2u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1.89464u^{34} + 2.30083u^{33} + \dots - 29.6286u - 8.78949 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1.95202u^{34} + 2.28719u^{33} + \dots - 25.9216u - 8.38330 \\ 0.0586830u^{34} + 0.0132193u^{33} + \dots + 1.08465u + 0.0710140 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1.63631u^{34} + 1.06267u^{33} + \dots - 17.1111u + 4.79896 \\ -0.136168u^{34} - 0.222641u^{33} + \dots + 0.865605u + 0.173572 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.267879u^{34} + 1.37848u^{33} + \dots - 3.97515u - 10.7436 \\ -0.167035u^{34} - 0.151989u^{33} + \dots + 3.05890u + 0.326704 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1.89464u^{34} + 2.30083u^{33} + \dots - 28.6286u - 8.78949 \\ u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 2.30439u^{34} + 3.64678u^{33} + \dots - 19.4192u - 18.0743 \\ 0.0573800u^{34} - 0.0136340u^{33} + \dots + 3.70702u + 0.406189 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -4.47995u^{34} - 3.38545u^{33} + \dots + 40.8417u + 3.13769 \\ 0.112272u^{34} + 0.228464u^{33} + \dots - 1.35463u + 0.400070 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.207182u^{34} + 0.352338u^{33} + \dots - 1.38655u + 0.769048 \\ 0.136168u^{34} + 0.222641u^{33} + \dots - 0.865605u - 0.173572 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1.04114u^{34} + 1.50676u^{33} + \dots - 16.4681u - 6.55811 \\ -0.167035u^{34} - 0.151989u^{33} + \dots + 3.05890u + 0.326704 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-8.40302u^{34} - 4.98573u^{33} + \dots + 50.7095u - 6.32050$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_8$	$u^{35} + 9u^{34} + \cdots + 16u + 64$
$c_2, c_7$	$u^{35} + 7u^{34} + \cdots + 20u + 8$
$c_3, c_5, c_{10}$ $c_{11}$	$u^{35} + 10u^{33} + \cdots + 3u + 1$
$c_4, c_9$	$u^{35} - u^{34} + \cdots - 2u + 1$
$c_{12}$	$u^{35} - 27u^{34} + \cdots + 73728u - 4096$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_8$	$y^{35} + 35y^{34} + \cdots + 34048y - 4096$
$c_2, c_7$	$y^{35} - 9y^{34} + \cdots + 16y - 64$
$c_3, c_5, c_{10}$ $c_{11}$	$y^{35} + 20y^{34} + \cdots + y - 1$
$c_4, c_9$	$y^{35} + 15y^{34} + \cdots - 34y - 1$
$c_{12}$	$y^{35} - 11y^{34} + \cdots + 125829120y - 16777216$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.591089 + 0.775481I$		
$a = -0.687556 + 0.152845I$	$1.33872 - 3.31510I$	$0.58501 + 5.76749I$
$b = 0.591089 + 0.775481I$		
$u = 0.591089 - 0.775481I$		
$a = -0.687556 - 0.152845I$	$1.33872 + 3.31510I$	$0.58501 - 5.76749I$
$b = 0.591089 - 0.775481I$		
$u = -0.597092 + 0.966307I$		
$a = 1.29984 + 0.98350I$	$-3.80954 - 0.35655I$	$-7.72758 - 2.31082I$
$b = -0.597092 + 0.966307I$		
$u = -0.597092 - 0.966307I$		
$a = 1.29984 - 0.98350I$	$-3.80954 + 0.35655I$	$-7.72758 + 2.31082I$
$b = -0.597092 - 0.966307I$		
$u = -0.274359 + 0.767854I$		
$a = 0.872835 + 0.188368I$	$2.17204 - 0.64743I$	$3.30372 + 2.66194I$
$b = -0.274359 + 0.767854I$		
$u = -0.274359 - 0.767854I$		
$a = 0.872835 - 0.188368I$	$2.17204 + 0.64743I$	$3.30372 - 2.66194I$
$b = -0.274359 - 0.767854I$		
$u = -0.413251 + 1.183840I$		
$a = 0.674185 + 0.327128I$	$9.66329 - 0.96587I$	$3.05582 + 0.39367I$
$b = -0.413251 + 1.183840I$		
$u = -0.413251 - 1.183840I$		
$a = 0.674185 - 0.327128I$	$9.66329 + 0.96587I$	$3.05582 - 0.39367I$
$b = -0.413251 - 1.183840I$		
$u = 0.419219 + 0.615155I$		
$a = 1.22242 + 1.49117I$	$5.07676 - 3.71447I$	$-0.77708 + 4.68220I$
$b = 0.419219 + 0.615155I$		
$u = 0.419219 - 0.615155I$		
$a = 1.22242 - 1.49117I$	$5.07676 + 3.71447I$	$-0.77708 - 4.68220I$
$b = 0.419219 - 0.615155I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.466745 + 0.574137I$		
$a = -1.13727 + 1.70318I$	$4.38894 + 9.97061I$	$-2.42520 - 9.73459I$
$b = -0.466745 + 0.574137I$		
$u = -0.466745 - 0.574137I$		
$a = -1.13727 - 1.70318I$	$4.38894 - 9.97061I$	$-2.42520 + 9.73459I$
$b = -0.466745 - 0.574137I$		
$u = 0.474572 + 1.194770I$		
$a = -0.658032 + 0.313634I$	$9.55181 - 5.46707I$	$2.92000 + 4.74682I$
$b = 0.474572 + 1.194770I$		
$u = 0.474572 - 1.194770I$		
$a = -0.658032 - 0.313634I$	$9.55181 + 5.46707I$	$2.92000 - 4.74682I$
$b = 0.474572 - 1.194770I$		
$u = 0.723524 + 1.111440I$		
$a = -1.045310 + 0.708906I$	$-2.05608 - 5.08661I$	$-4.00000 + 6.93227I$
$b = 0.723524 + 1.111440I$		
$u = 0.723524 - 1.111440I$		
$a = -1.045310 - 0.708906I$	$-2.05608 + 5.08661I$	$-4.00000 - 6.93227I$
$b = 0.723524 - 1.111440I$		
$u = -0.950167 + 0.965088I$		
$a = 1.212470 + 0.335142I$	$-8.23917 + 6.19708I$	$-11.53177 - 4.77423I$
$b = -0.950167 + 0.965088I$		
$u = -0.950167 - 0.965088I$		
$a = 1.212470 - 0.335142I$	$-8.23917 - 6.19708I$	$-11.53177 + 4.77423I$
$b = -0.950167 - 0.965088I$		
$u = 0.597400$		
$a = -0.567434$	$-1.22075$	$-7.22590$
$b = 0.597400$		
$u = 0.097938 + 0.514145I$		
$a = 1.96245 + 0.19680I$	$0.44134 - 1.63347I$	$1.73800 + 4.33093I$
$b = 0.097938 + 0.514145I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.097938 - 0.514145I$		
$a = 1.96245 - 0.19680I$	$0.44134 + 1.63347I$	$1.73800 - 4.33093I$
$b = 0.097938 - 0.514145I$		
$u = -0.271525 + 0.415826I$		
$a = -2.75306 + 1.67750I$	$-2.74916 + 4.77966I$	$-3.72482 - 10.00221I$
$b = -0.271525 + 0.415826I$		
$u = -0.271525 - 0.415826I$		
$a = -2.75306 - 1.67750I$	$-2.74916 - 4.77966I$	$-3.72482 + 10.00221I$
$b = -0.271525 - 0.415826I$		
$u = 1.03004 + 1.11959I$		
$a = -0.999328 + 0.306692I$	$-3.63302 - 8.69335I$	0
$b = 1.03004 + 1.11959I$		
$u = 1.03004 - 1.11959I$		
$a = -0.999328 - 0.306692I$	$-3.63302 + 8.69335I$	0
$b = 1.03004 - 1.11959I$		
$u = 0.06773 + 1.55270I$		
$a = -0.068133 + 0.960500I$	$8.19666 - 3.43452I$	0
$b = 0.06773 + 1.55270I$		
$u = 0.06773 - 1.55270I$		
$a = -0.068133 - 0.960500I$	$8.19666 + 3.43452I$	0
$b = 0.06773 - 1.55270I$		
$u = -1.13426 + 1.07638I$		
$a = 1.002730 + 0.193039I$	$-6.3568 + 12.9060I$	0
$b = -1.13426 + 1.07638I$		
$u = -1.13426 - 1.07638I$		
$a = 1.002730 - 0.193039I$	$-6.3568 - 12.9060I$	0
$b = -1.13426 - 1.07638I$		
$u = -0.067600 + 0.311475I$		
$a = -3.61790 - 2.90700I$	$-2.02184 - 1.48778I$	$-5.29371 + 6.36546I$
$b = -0.067600 + 0.311475I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.067600 - 0.311475I$		
$a = -3.61790 + 2.90700I$	$-2.02184 + 1.48778I$	$-5.29371 - 6.36546I$
$b = -0.067600 - 0.311475I$		
$u = 1.20419 + 1.21154I$		
$a = -0.874512 + 0.183122I$	$2.43884 - 11.28800I$	0
$b = 1.20419 + 1.21154I$		
$u = 1.20419 - 1.21154I$		
$a = -0.874512 - 0.183122I$	$2.43884 + 11.28800I$	0
$b = 1.20419 - 1.21154I$		
$u = -1.23200 + 1.19581I$		
$a = 0.877886 + 0.159904I$	$1.8345 + 17.7184I$	0
$b = -1.23200 + 1.19581I$		
$u = -1.23200 - 1.19581I$		
$a = 0.877886 - 0.159904I$	$1.8345 - 17.7184I$	0
$b = -1.23200 - 1.19581I$		

$$\text{III. } I_2^u = \langle 1.35 \times 10^{309} u^{71} + 4.07 \times 10^{309} u^{70} + \dots + 3.31 \times 10^{309} b + 2.52 \times 10^{310}, -2.10 \times 10^{240} u^{71} - 6.37 \times 10^{240} u^{70} + \dots + 3.90 \times 10^{240} a - 1.36 \times 10^{242}, u^{72} + 3u^{71} + \dots + 48u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.539465u^{71} + 1.63403u^{70} + \dots + 603.712u + 34.9160 \\ -0.406910u^{71} - 1.23187u^{70} + \dots - 242.608u - 7.62829 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.135898u^{71} + 0.410976u^{70} + \dots + 359.814u + 27.2721 \\ -0.433293u^{71} - 1.29628u^{70} + \dots - 243.604u - 7.64065 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -5.47361u^{71} - 15.9771u^{70} + \dots - 3245.98u - 92.7647 \\ 0.0926148u^{71} + 0.257322u^{70} + \dots + 41.1552u - 2.78210 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.130468u^{71} - 0.583660u^{70} + \dots - 769.572u - 70.4281 \\ 1.03009u^{71} + 3.02070u^{70} + \dots + 634.312u + 21.1555 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.132555u^{71} + 0.402165u^{70} + \dots + 361.104u + 27.2877 \\ -0.406910u^{71} - 1.23187u^{70} + \dots - 242.608u - 7.62829 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.232683u^{71} - 0.798062u^{70} + \dots - 461.851u - 26.5601 \\ 0.400276u^{71} + 1.09127u^{70} + \dots + 167.198u + 5.35353 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 4.24388u^{71} + 12.1560u^{70} + \dots + 1995.98u + 55.1998 \\ -0.237755u^{71} - 0.677729u^{70} + \dots - 47.8013u + 1.19648 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 7.24447u^{71} + 21.3193u^{70} + \dots + 4321.80u + 124.943 \\ -0.396176u^{71} - 1.16932u^{70} + \dots - 127.116u + 1.79571 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.727709u^{71} + 1.96306u^{70} + \dots - 275.156u - 53.7910 \\ 0.803345u^{71} + 2.34508u^{70} + \dots + 560.708u + 19.6459 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-0.619107u^{71} - 1.70406u^{70} + \dots + 144.641u - 5.48872$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_8$	$(u^{12} + 3u^{11} + \cdots + 2u + 1)^6$
$c_2, c_7$	$(u^{12} - u^{11} - u^{10} + 2u^9 + 3u^8 - 4u^7 - 2u^6 + 4u^5 + 2u^4 - 3u^3 - u^2 + 1)^6$
$c_3, c_5, c_{10}$ $c_{11}$	$u^{72} - u^{71} + \cdots + 13014u + 2943$
$c_4, c_9$	$u^{72} - 3u^{71} + \cdots - 48u + 1$
$c_{12}$	$(u^3 + u^2 - 1)^{24}$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_8$	$(y^{12} + 13y^{11} + \cdots + 6y + 1)^6$
$c_2, c_7$	$(y^{12} - 3y^{11} + \cdots - 2y + 1)^6$
$c_3, c_5, c_{10}$ $c_{11}$	$y^{72} + 51y^{71} + \cdots + 376303320y + 8661249$
$c_4, c_9$	$y^{72} - 17y^{71} + \cdots - 552y + 1$
$c_{12}$	$(y^3 - y^2 + 2y - 1)^{24}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.568176 + 0.839836I$ $a = -1.093330 - 0.305104I$ $b = 1.23118 - 1.38930I$	$6.00451 + 4.31046I$	0
$u = -0.568176 - 0.839836I$ $a = -1.093330 + 0.305104I$ $b = 1.23118 + 1.38930I$	$6.00451 - 4.31046I$	0
$u = 0.891554 + 0.489577I$ $a = 1.108640 + 0.226678I$ $b = -1.30602 - 0.59539I$	$-3.34798 - 2.47502I$	0
$u = 0.891554 - 0.489577I$ $a = 1.108640 - 0.226678I$ $b = -1.30602 + 0.59539I$	$-3.34798 + 2.47502I$	0
$u = 0.701909 + 0.683885I$ $a = 1.171710 - 0.080430I$ $b = -1.28434 - 1.06706I$	$-1.98742 - 7.07733I$	0
$u = 0.701909 - 0.683885I$ $a = 1.171710 + 0.080430I$ $b = -1.28434 + 1.06706I$	$-1.98742 + 7.07733I$	0
$u = 0.977106 + 0.046716I$ $a = 0.859586 - 0.803411I$ $b = -0.875721 + 0.368859I$	$-3.34798 + 3.18123I$	0
$u = 0.977106 - 0.046716I$ $a = 0.859586 + 0.803411I$ $b = -0.875721 - 0.368859I$	$-3.34798 - 3.18123I$	0
$u = 0.604256 + 0.853075I$ $a = 1.066580 - 0.273076I$ $b = -1.29161 - 1.38021I$	$5.64748 - 10.62950I$	0
$u = 0.604256 - 0.853075I$ $a = 1.066580 + 0.273076I$ $b = -1.29161 + 1.38021I$	$5.64748 + 10.62950I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.509449 + 0.806111I$		
$a = 1.151870 - 0.360525I$	$-0.17094 - 2.11219I$	0
$b = -0.302346 - 0.194987I$		
$u = 0.509449 - 0.806111I$		
$a = 1.151870 + 0.360525I$	$-0.17094 + 2.11219I$	0
$b = -0.302346 + 0.194987I$		
$u = -0.875721 + 0.368859I$		
$a = -1.155270 + 0.363964I$	$-3.34798 + 3.18123I$	0
$b = 0.977106 + 0.046716I$		
$u = -0.875721 - 0.368859I$		
$a = -1.155270 - 0.363964I$	$-3.34798 - 3.18123I$	0
$b = 0.977106 - 0.046716I$		
$u = -0.904826 + 0.206753I$		
$a = 0.792882 + 0.181173I$	$-6.12500 + 4.24921I$	$-13.1960 - 6.9831I$
$b = -1.32231 - 1.27743I$		
$u = -0.904826 - 0.206753I$		
$a = 0.792882 - 0.181173I$	$-6.12500 - 4.24921I$	$-13.1960 + 6.9831I$
$b = -1.32231 + 1.27743I$		
$u = 1.013100 + 0.432835I$		
$a = -0.630105 + 0.269206I$	$-4.30852 - 0.71593I$	0
$b = 1.22185 - 0.91863I$		
$u = 1.013100 - 0.432835I$		
$a = -0.630105 - 0.269206I$	$-4.30852 + 0.71593I$	0
$b = 1.22185 + 0.91863I$		
$u = -1.102800 + 0.079429I$		
$a = 0.680979 + 0.049047I$	$1.50990 + 7.80134I$	0
$b = -1.75324 - 1.20623I$		
$u = -1.102800 - 0.079429I$		
$a = 0.680979 - 0.049047I$	$1.50990 - 7.80134I$	0
$b = -1.75324 + 1.20623I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.062360 + 0.384623I$		
$a = -0.954650 + 0.355513I$	$2.12951 + 5.84119I$	0
$b = 1.52012 - 0.07163I$		
$u = -1.062360 - 0.384623I$		
$a = -0.954650 - 0.355513I$	$2.12951 - 5.84119I$	0
$b = 1.52012 + 0.07163I$		
$u = 1.131690 + 0.108519I$		
$a = -0.660959 + 0.063380I$	$1.86693 - 1.48234I$	0
$b = 1.74780 - 1.12060I$		
$u = 1.131690 - 0.108519I$		
$a = -0.660959 - 0.063380I$	$1.86693 + 1.48234I$	0
$b = 1.74780 + 1.12060I$		
$u = 1.064500 + 0.420736I$		
$a = 0.952102 + 0.323418I$	$2.12951 + 0.18495I$	0
$b = -1.55590 - 0.16376I$		
$u = 1.064500 - 0.420736I$		
$a = 0.952102 - 0.323418I$	$2.12951 - 0.18495I$	0
$b = -1.55590 + 0.16376I$		
$u = -0.566692 + 0.558756I$		
$a = -1.44223 - 0.10763I$	$-0.17094 + 3.54405I$	$-0.53377 - 3.62818I$
$b = 1.00879 - 1.02877I$		
$u = -0.566692 - 0.558756I$		
$a = -1.44223 + 0.10763I$	$-0.17094 - 3.54405I$	$-0.53377 + 3.62818I$
$b = 1.00879 + 1.02877I$		
$u = 0.171015 + 1.222870I$		
$a = -0.499006 - 0.787307I$	$5.64748 - 4.97322I$	0
$b = -0.313284 - 0.368426I$		
$u = 0.171015 - 1.222870I$		
$a = -0.499006 + 0.787307I$	$5.64748 + 4.97322I$	0
$b = -0.313284 + 0.368426I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.073230 + 1.236080I$		
$a = 0.558583 - 0.742946I$	$6.00451 - 1.34579I$	0
$b = 0.246654 - 0.392628I$		
$u = -0.073230 - 1.236080I$		
$a = 0.558583 + 0.742946I$	$6.00451 + 1.34579I$	0
$b = 0.246654 + 0.392628I$		
$u = 0.266780 + 0.539724I$		
$a = -0.46331 - 1.85473I$	$-1.98742 - 1.42109I$	$-6.66674 + 4.00366I$
$b = -0.331284 + 0.154458I$		
$u = 0.266780 - 0.539724I$		
$a = -0.46331 + 1.85473I$	$-1.98742 + 1.42109I$	$-6.66674 - 4.00366I$
$b = -0.331284 - 0.154458I$		
$u = -0.453297 + 0.338937I$		
$a = 1.068140 + 0.798660I$	$-7.48556 - 0.35310I$	$-17.6864 + 0.6298I$
$b = -0.62453 - 1.40533I$		
$u = -0.453297 - 0.338937I$		
$a = 1.068140 - 0.798660I$	$-7.48556 + 0.35310I$	$-17.6864 - 0.6298I$
$b = -0.62453 + 1.40533I$		
$u = -1.30602 + 0.59539I$		
$a = -0.771502 + 0.218617I$	$-3.34798 + 2.47502I$	0
$b = 0.891554 - 0.489577I$		
$u = -1.30602 - 0.59539I$		
$a = -0.771502 - 0.218617I$	$-3.34798 - 2.47502I$	0
$b = 0.891554 + 0.489577I$		
$u = 1.00879 + 1.02877I$		
$a = 0.795484 - 0.072863I$	$-0.17094 - 3.54405I$	0
$b = -0.566692 - 0.558756I$		
$u = 1.00879 - 1.02877I$		
$a = 0.795484 + 0.072863I$	$-0.17094 + 3.54405I$	0
$b = -0.566692 + 0.558756I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.313284 + 0.368426I$		
$a = -0.00197 - 2.37991I$	$5.64748 + 4.97322I$	$-2.12413 - 2.66036I$
$b = 0.171015 - 1.222870I$		
$u = -0.313284 - 0.368426I$		
$a = -0.00197 + 2.37991I$	$5.64748 - 4.97322I$	$-2.12413 + 2.66036I$
$b = 0.171015 + 1.222870I$		
$u = 1.52012 + 0.07163I$		
$a = 0.598977 + 0.461776I$	$2.12951 - 5.84119I$	0
$b = -1.062360 - 0.384623I$		
$u = 1.52012 - 0.07163I$		
$a = 0.598977 - 0.461776I$	$2.12951 + 5.84119I$	0
$b = -1.062360 + 0.384623I$		
$u = 1.22185 + 0.91863I$		
$a = -0.394705 + 0.296753I$	$-4.30852 + 0.71593I$	0
$b = 1.013100 - 0.432835I$		
$u = 1.22185 - 0.91863I$		
$a = -0.394705 - 0.296753I$	$-4.30852 - 0.71593I$	0
$b = 1.013100 + 0.432835I$		
$u = 0.246654 + 0.392628I$		
$a = -0.35363 - 2.45694I$	$6.00451 + 1.34579I$	$-1.33766 - 2.30403I$
$b = -0.073230 - 1.236080I$		
$u = 0.246654 - 0.392628I$		
$a = -0.35363 + 2.45694I$	$6.00451 - 1.34579I$	$-1.33766 + 2.30403I$
$b = -0.073230 + 1.236080I$		
$u = -0.62453 + 1.40533I$		
$a = 0.199342 + 0.448567I$	$-7.48556 + 0.35310I$	0
$b = -0.453297 - 0.338937I$		
$u = -0.62453 - 1.40533I$		
$a = 0.199342 - 0.448567I$	$-7.48556 - 0.35310I$	0
$b = -0.453297 + 0.338937I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.55590 + 0.16376I$		
$a = -0.607599 + 0.414781I$	$2.12951 - 0.18495I$	0
$b = 1.064500 - 0.420736I$		
$u = -1.55590 - 0.16376I$		
$a = -0.607599 - 0.414781I$	$2.12951 + 0.18495I$	0
$b = 1.064500 + 0.420736I$		
$u = -0.331284 + 0.154458I$		
$a = -3.03677 + 0.83254I$	$-1.98742 - 1.42109I$	$-6.66674 + 4.00366I$
$b = 0.266780 + 0.539724I$		
$u = -0.331284 - 0.154458I$		
$a = -3.03677 - 0.83254I$	$-1.98742 + 1.42109I$	$-6.66674 - 4.00366I$
$b = 0.266780 - 0.539724I$		
$u = -0.302346 + 0.194987I$		
$a = -3.17175 + 0.41810I$	$-0.17094 + 2.11219I$	$-0.53377 - 2.33071I$
$b = 0.509449 - 0.806111I$		
$u = -0.302346 - 0.194987I$		
$a = -3.17175 - 0.41810I$	$-0.17094 - 2.11219I$	$-0.53377 + 2.33071I$
$b = 0.509449 + 0.806111I$		
$u = -1.28434 + 1.06706I$		
$a = -0.689254 + 0.007309I$	$-1.98742 + 7.07733I$	0
$b = 0.701909 - 0.683885I$		
$u = -1.28434 - 1.06706I$		
$a = -0.689254 - 0.007309I$	$-1.98742 - 7.07733I$	0
$b = 0.701909 + 0.683885I$		
$u = -1.32231 + 1.27743I$		
$a = 0.295292 + 0.285269I$	$-6.12500 - 4.24921I$	0
$b = -0.904826 - 0.206753I$		
$u = -1.32231 - 1.27743I$		
$a = 0.295292 - 0.285269I$	$-6.12500 + 4.24921I$	0
$b = -0.904826 + 0.206753I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.23118 + 1.38930I$	$6.00451 - 4.31046I$	0
$a = 0.613796 - 0.087629I$		
$b = -0.568176 - 0.839836I$		
$u = 1.23118 - 1.38930I$	$6.00451 + 4.31046I$	0
$a = 0.613796 + 0.087629I$		
$b = -0.568176 + 0.839836I$		
$u = -1.29161 + 1.38021I$	$5.64748 + 10.62950I$	0
$a = -0.604880 - 0.069680I$		
$b = 0.604256 - 0.853075I$		
$u = -1.29161 - 1.38021I$	$5.64748 - 10.62950I$	0
$a = -0.604880 + 0.069680I$		
$b = 0.604256 + 0.853075I$		
$u = -0.0431717 + 0.0210889I$	$-2.00808 - 3.01307I$	$-11.65126 + 2.63251I$
$a = 14.1169 + 6.8959I$		
$b = -0.07263 - 1.98324I$		
$u = -0.0431717 - 0.0210889I$	$-2.00808 + 3.01307I$	$-11.65126 - 2.63251I$
$a = 14.1169 - 6.8959I$		
$b = -0.07263 + 1.98324I$		
$u = -0.07263 + 1.98324I$	$-2.00808 + 3.01307I$	0
$a = 0.013921 + 0.380119I$		
$b = -0.0431717 - 0.0210889I$		
$u = -0.07263 - 1.98324I$	$-2.00808 - 3.01307I$	0
$a = 0.013921 - 0.380119I$		
$b = -0.0431717 + 0.0210889I$		
$u = 1.74780 + 1.12060I$	$1.86693 + 1.48234I$	0
$a = -0.306081 + 0.196243I$		
$b = 1.131690 - 0.108519I$		
$u = 1.74780 - 1.12060I$	$1.86693 - 1.48234I$	0
$a = -0.306081 - 0.196243I$		
$b = 1.131690 + 0.108519I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.75324 + 1.20623I$		
$a = 0.292233 + 0.201057I$	$1.50990 - 7.80134I$	0
$b = -1.102800 - 0.079429I$		
$u = -1.75324 - 1.20623I$		
$a = 0.292233 - 0.201057I$	$1.50990 + 7.80134I$	0
$b = -1.102800 + 0.079429I$		

### III.

$$I_3^u = \langle b + u, -886u^{19} - 1725u^{18} + \dots + 2249a + 1906, u^{20} + u^{19} + \dots - 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.393953u^{19} + 0.767008u^{18} + \dots + 2.40907u - 0.847488 \\ -u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1.15918u^{19} + 2.42730u^{18} + \dots + 1.76123u - 1.22054 \\ -0.650067u^{19} - 1.04669u^{18} + \dots - 2.02490u + 0.895064 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1.10494u^{19} + 1.45487u^{18} + \dots + 2.84260u - 0.234771 \\ -0.498444u^{19} - 0.910627u^{18} + \dots - 0.752334u + 0.115162 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.292574u^{19} + 0.197866u^{18} + \dots - 1.56114u + 2.34949 \\ 0.00489106u^{19} - 0.576256u^{18} + \dots + 2.49266u - 0.638061 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.393953u^{19} + 0.767008u^{18} + \dots + 1.40907u - 0.847488 \\ -u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1.39395u^{19} + 3.76701u^{18} + \dots - 0.590929u + 1.15251 \\ -0.765229u^{19} - 1.66029u^{18} + \dots + 0.647843u + 0.373055 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.847488u^{19} - 1.24144u^{18} + \dots - 1.72877u + 0.285905 \\ 0.895064u^{19} + 1.54513u^{18} + \dots + 1.15740u + 0.234771 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.396621u^{19} - 0.634504u^{18} + \dots - 0.405069u - 0.349933 \\ 0.498444u^{19} + 0.910627u^{18} + \dots + 0.752334u - 0.115162 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.211650u^{19} + 0.154735u^{18} + \dots + 2.68253u - 1.33793 \\ -0.00489106u^{19} + 0.576256u^{18} + \dots - 2.49266u + 0.638061 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $\frac{16424}{2249}u^{19} + \frac{35896}{2249}u^{18} + \dots + \frac{2352}{2249}u - \frac{32819}{2249}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{20} - 6u^{19} + \cdots - 11u + 1$
$c_2$	$u^{20} - 3u^{18} + \cdots - u + 1$
$c_3, c_{11}$	$u^{20} + 10u^{18} + \cdots - u + 1$
$c_4, c_9$	$u^{20} + u^{19} + \cdots - 2u + 1$
$c_5, c_{10}$	$u^{20} + 10u^{18} + \cdots + u + 1$
$c_7$	$u^{20} - 3u^{18} + \cdots + u + 1$
$c_8$	$u^{20} + 6u^{19} + \cdots + 11u + 1$
$c_{12}$	$u^{20} + 8u^{19} + \cdots - 6u^2 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_8$	$y^{20} + 22y^{19} + \cdots + 5y + 1$
$c_2, c_7$	$y^{20} - 6y^{19} + \cdots - 11y + 1$
$c_3, c_5, c_{10}$ $c_{11}$	$y^{20} + 20y^{19} + \cdots + 19y + 1$
$c_4, c_9$	$y^{20} - y^{19} + \cdots + 2y + 1$
$c_{12}$	$y^{20} - 10y^{19} + \cdots - 12y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.803742 + 0.640038I$		
$a = -1.312270 - 0.216838I$	$-0.80556 + 3.51175I$	$-5.16057 - 6.47153I$
$b = 0.803742 - 0.640038I$		
$u = -0.803742 - 0.640038I$		
$a = -1.312270 + 0.216838I$	$-0.80556 - 3.51175I$	$-5.16057 + 6.47153I$
$b = 0.803742 + 0.640038I$		
$u = 0.109977 + 0.933392I$		
$a = -0.202191 + 0.691646I$	$-6.93544 - 0.76917I$	$-4.93268 + 9.83438I$
$b = -0.109977 - 0.933392I$		
$u = 0.109977 - 0.933392I$		
$a = -0.202191 - 0.691646I$	$-6.93544 + 0.76917I$	$-4.93268 - 9.83438I$
$b = -0.109977 + 0.933392I$		
$u = 0.025092 + 1.157510I$		
$a = -0.023307 + 0.429548I$	$-1.20551 - 3.04014I$	$0.81171 + 2.97210I$
$b = -0.025092 - 1.157510I$		
$u = 0.025092 - 1.157510I$		
$a = -0.023307 - 0.429548I$	$-1.20551 + 3.04014I$	$0.81171 - 2.97210I$
$b = -0.025092 + 1.157510I$		
$u = 0.838930 + 0.068318I$		
$a = 0.82153 + 1.21370I$	$-3.71829 - 4.43650I$	$-12.2519 + 8.7425I$
$b = -0.838930 - 0.068318I$		
$u = 0.838930 - 0.068318I$		
$a = 0.82153 - 1.21370I$	$-3.71829 + 4.43650I$	$-12.2519 - 8.7425I$
$b = -0.838930 + 0.068318I$		
$u = -1.130550 + 0.326356I$		
$a = -0.801063 + 0.358429I$	$-2.11436 + 2.39551I$	$-2.32396 - 1.51464I$
$b = 1.130550 - 0.326356I$		
$u = -1.130550 - 0.326356I$		
$a = -0.801063 - 0.358429I$	$-2.11436 - 2.39551I$	$-2.32396 + 1.51464I$
$b = 1.130550 + 0.326356I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.186100 + 0.148412I$		
$a = 0.238472 - 0.592250I$	$3.07275 + 8.15795I$	$-2.68462 - 7.66785I$
$b = -1.186100 - 0.148412I$		
$u = 1.186100 - 0.148412I$		
$a = 0.238472 + 0.592250I$	$3.07275 - 8.15795I$	$-2.68462 + 7.66785I$
$b = -1.186100 + 0.148412I$		
$u = -1.231270 + 0.086350I$		
$a = -0.309856 - 0.538687I$	$3.39949 - 1.94064I$	$-1.75418 + 2.97120I$
$b = 1.231270 - 0.086350I$		
$u = -1.231270 - 0.086350I$		
$a = -0.309856 + 0.538687I$	$3.39949 + 1.94064I$	$-1.75418 - 2.97120I$
$b = 1.231270 + 0.086350I$		
$u = 0.506464 + 0.461594I$		
$a = 2.66341 - 0.41964I$	$-2.11393 + 0.95837I$	$-7.35023 + 6.82243I$
$b = -0.506464 - 0.461594I$		
$u = 0.506464 - 0.461594I$		
$a = 2.66341 + 0.41964I$	$-2.11393 - 0.95837I$	$-7.35023 - 6.82243I$
$b = -0.506464 + 0.461594I$		
$u = 0.077140 + 0.632787I$		
$a = -0.49697 + 1.73221I$	$-4.80805 + 2.38684I$	$-9.41924 - 2.88689I$
$b = -0.077140 - 0.632787I$		
$u = 0.077140 - 0.632787I$		
$a = -0.49697 - 1.73221I$	$-4.80805 - 2.38684I$	$-9.41924 + 2.88689I$
$b = -0.077140 + 0.632787I$		
$u = -0.078140 + 1.399020I$		
$a = -0.077754 - 0.975047I$	$8.64916 + 3.38003I$	$6.56566 - 1.45355I$
$b = 0.078140 - 1.399020I$		
$u = -0.078140 - 1.399020I$		
$a = -0.077754 + 0.975047I$	$8.64916 - 3.38003I$	$6.56566 + 1.45355I$
$b = 0.078140 + 1.399020I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$((u^{12} + 3u^{11} + \dots + 2u + 1)^6)(u^{20} - 6u^{19} + \dots - 11u + 1)$ $\cdot (u^{35} + 9u^{34} + \dots + 16u + 64)$
$c_2$	$(u^{12} - u^{11} - u^{10} + 2u^9 + 3u^8 - 4u^7 - 2u^6 + 4u^5 + 2u^4 - 3u^3 - u^2 + 1)^6$ $\cdot (u^{20} - 3u^{18} + \dots - u + 1)(u^{35} + 7u^{34} + \dots + 20u + 8)$
$c_3, c_{11}$	$(u^{20} + 10u^{18} + \dots - u + 1)(u^{35} + 10u^{33} + \dots + 3u + 1)$ $\cdot (u^{72} - u^{71} + \dots + 13014u + 2943)$
$c_4, c_9$	$(u^{20} + u^{19} + \dots - 2u + 1)(u^{35} - u^{34} + \dots - 2u + 1)$ $\cdot (u^{72} - 3u^{71} + \dots - 48u + 1)$
$c_5, c_{10}$	$(u^{20} + 10u^{18} + \dots + u + 1)(u^{35} + 10u^{33} + \dots + 3u + 1)$ $\cdot (u^{72} - u^{71} + \dots + 13014u + 2943)$
$c_7$	$(u^{12} - u^{11} - u^{10} + 2u^9 + 3u^8 - 4u^7 - 2u^6 + 4u^5 + 2u^4 - 3u^3 - u^2 + 1)^6$ $\cdot (u^{20} - 3u^{18} + \dots + u + 1)(u^{35} + 7u^{34} + \dots + 20u + 8)$
$c_8$	$((u^{12} + 3u^{11} + \dots + 2u + 1)^6)(u^{20} + 6u^{19} + \dots + 11u + 1)$ $\cdot (u^{35} + 9u^{34} + \dots + 16u + 64)$
$c_{12}$	$((u^3 + u^2 - 1)^{24})(u^{20} + 8u^{19} + \dots - 6u^2 + 1)$ $\cdot (u^{35} - 27u^{34} + \dots + 73728u - 4096)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_8$	$((y^{12} + 13y^{11} + \dots + 6y + 1)^6)(y^{20} + 22y^{19} + \dots + 5y + 1)$ $\cdot (y^{35} + 35y^{34} + \dots + 34048y - 4096)$
$c_2, c_7$	$((y^{12} - 3y^{11} + \dots - 2y + 1)^6)(y^{20} - 6y^{19} + \dots - 11y + 1)$ $\cdot (y^{35} - 9y^{34} + \dots + 16y - 64)$
$c_3, c_5, c_{10}$ $c_{11}$	$(y^{20} + 20y^{19} + \dots + 19y + 1)(y^{35} + 20y^{34} + \dots + y - 1)$ $\cdot (y^{72} + 51y^{71} + \dots + 376303320y + 8661249)$
$c_4, c_9$	$(y^{20} - y^{19} + \dots + 2y + 1)(y^{35} + 15y^{34} + \dots - 34y - 1)$ $\cdot (y^{72} - 17y^{71} + \dots - 552y + 1)$
$c_{12}$	$((y^3 - y^2 + 2y - 1)^{24})(y^{20} - 10y^{19} + \dots - 12y + 1)$ $\cdot (y^{35} - 11y^{34} + \dots + 125829120y - 16777216)$