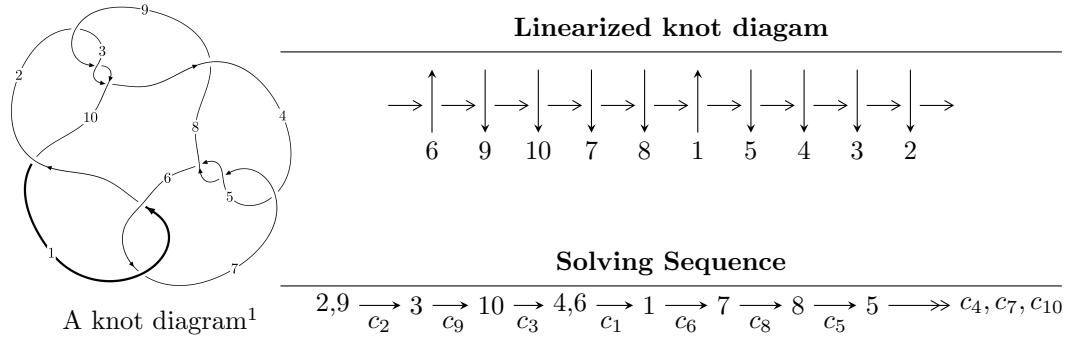


10<sub>76</sub> ( $K10a_{73}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -u^9 + 4u^7 + u^6 - 5u^5 - 3u^4 + 2u^2 + b + 3u + 1, -u^6 + 3u^4 - 2u^2 + a - 1, u^{11} - u^{10} - 5u^9 + 4u^8 + 9u^7 - 4u^6 - 5u^5 - 3u^4 - 3u^3 + 5u^2 + 3u + 1 \rangle$$

$$I_2^u = \langle u^{11} - 3u^9 - u^8 + 2u^7 + 2u^6 + 3u^5 - 3u^3 - 2u^2 + b - u, 2u^{17} - 12u^{15} + \dots + a + 3, u^{18} - u^{17} + \dots + 2u - 1 \rangle$$

$$I_3^u = \langle b, a + 1, u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 30 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^9 + 4u^7 + \dots + b + 1, -u^6 + 3u^4 - 2u^2 + a - 1, u^{11} - u^{10} + \dots + 3u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ u^9 - 4u^7 - u^6 + 5u^5 + 3u^4 - 2u^2 - 3u - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^3 - 2u \\ -u^{10} + u^9 + 4u^8 - 3u^7 - 5u^6 + 2u^5 + u^3 + 3u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^5 - 2u^3 + u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^4 + u^2 + 1 \\ u^9 - u^8 - 4u^7 + 2u^6 + 5u^5 + u^4 - 3u^2 - 3u - 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes**

$$= -2u^{10} + 6u^9 + 8u^8 - 26u^7 - 14u^6 + 34u^5 + 16u^4 + 4u^3 - 10u^2 - 30u - 14$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{11} + 3u^{10} + 6u^9 + 7u^8 + 7u^7 + 3u^6 - 2u^5 - 8u^4 - 7u^3 - 5u^2 - 2u - 2$
$c_2, c_3, c_4$ $c_5, c_7, c_9$	$u^{11} - u^{10} - 5u^9 + 4u^8 + 9u^7 - 4u^6 - 5u^5 - 3u^4 - 3u^3 + 5u^2 + 3u + 1$
$c_8, c_{10}$	$u^{11} + 3u^{10} + \dots - 16u - 4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{11} + 3y^{10} + \cdots - 16y - 4$
$c_2, c_3, c_4$ $c_5, c_7, c_9$	$y^{11} - 11y^{10} + \cdots - y - 1$
$c_8, c_{10}$	$y^{11} + 7y^{10} + \cdots + 24y - 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.062122 + 0.811051I$		
$a = -1.82009 - 0.72518I$	$4.60381 + 2.87937I$	$-1.58714 - 3.23335I$
$b = 0.762686 + 0.875309I$		
$u = -0.062122 - 0.811051I$		
$a = -1.82009 + 0.72518I$	$4.60381 - 2.87937I$	$-1.58714 + 3.23335I$
$b = 0.762686 - 0.875309I$		
$u = -1.32132$		
$a = 0.669088$	$-6.97991$	$-12.6670$
$b = -0.992754$		
$u = -1.296720 + 0.321683I$		
$a = -0.591796 + 0.578733I$	$-3.08453 + 5.20915I$	$-9.44226 - 3.72118I$
$b = 0.958422 - 0.661375I$		
$u = -1.296720 - 0.321683I$		
$a = -0.591796 - 0.578733I$	$-3.08453 - 5.20915I$	$-9.44226 + 3.72118I$
$b = 0.958422 + 0.661375I$		
$u = 1.360100 + 0.374662I$		
$a = -1.56319 - 0.53861I$	$-4.40916 - 11.51290I$	$-10.44081 + 7.44023I$
$b = 0.764438 - 1.080520I$		
$u = 1.360100 - 0.374662I$		
$a = -1.56319 + 0.53861I$	$-4.40916 + 11.51290I$	$-10.44081 - 7.44023I$
$b = 0.764438 + 1.080520I$		
$u = 1.42406 + 0.13076I$		
$a = 0.601423 + 0.717547I$	$-11.39950 - 4.33574I$	$-15.3124 + 3.6840I$
$b = -0.273627 + 1.210650I$		
$u = 1.42406 - 0.13076I$		
$a = 0.601423 - 0.717547I$	$-11.39950 + 4.33574I$	$-15.3124 - 3.6840I$
$b = -0.273627 - 1.210650I$		
$u = -0.264651 + 0.295634I$		
$a = 1.039110 - 0.325568I$	$-0.314917 + 0.927579I$	$-5.88395 - 7.40073I$
$b = -0.215541 - 0.601634I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.264651 - 0.295634I$		
$a = 1.039110 + 0.325568I$	$-0.314917 - 0.927579I$	$-5.88395 + 7.40073I$
$b = -0.215541 + 0.601634I$		

$$I_2^u = \langle u^{11} - 3u^9 + \dots + b - u, \ 2u^{17} - 12u^{15} + \dots + a + 3, \ u^{18} - u^{17} + \dots + 2u - 1 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2u^{17} + 12u^{15} + \dots - 2u - 3 \\ -u^{11} + 3u^9 + u^8 - 2u^7 - 2u^6 - 3u^5 + 3u^3 + 2u^2 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2u^{17} + 12u^{15} + \dots - 2u - 3 \\ u^{14} - 4u^{12} + \dots + 3u^2 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2u^{17} + 12u^{15} + \dots - 3u - 2 \\ u^{13} - 5u^{11} - 2u^{10} + 9u^9 + 8u^8 - 4u^7 - 10u^6 - 6u^5 + 5u^3 + 6u^2 + u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $4u^{17} - 24u^{15} - 4u^{14} + 56u^{13} + 20u^{12} - 48u^{11} - 36u^{10} - 24u^9 + 16u^8 + 64u^7 + 24u^6 - 12u^5 - 20u^4 - 24u^3 - 8u^2 - 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^2$
$c_2, c_3, c_4$ $c_5, c_7, c_9$	$u^{18} - u^{17} + \dots + 2u - 1$
$c_8, c_{10}$	$(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^2$
$c_2, c_3, c_4$ $c_5, c_7, c_9$	$y^{18} - 13y^{17} + \dots - 12y + 1$
$c_8, c_{10}$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.11181$		
$a = -0.294140$	-2.09142	-3.34770
$b = 0.512358$		
$u = -0.138557 + 0.857281I$		
$a = 1.70857 + 0.83690I$	$0.30826 + 7.08493I$	$-6.42320 - 5.91335I$
$b = -0.728966 - 0.986295I$		
$u = -0.138557 - 0.857281I$		
$a = 1.70857 - 0.83690I$	$0.30826 - 7.08493I$	$-6.42320 + 5.91335I$
$b = -0.728966 + 0.986295I$		
$u = -1.112360 + 0.436175I$		
$a = -0.238783 + 0.723669I$	-2.67293 - 2.45442I	-9.67208 + 2.91298I
$b = 0.628449 - 0.875112I$		
$u = -1.112360 - 0.436175I$		
$a = -0.238783 - 0.723669I$	-2.67293 + 2.45442I	-9.67208 - 2.91298I
$b = 0.628449 + 0.875112I$		
$u = -0.535620 + 0.576021I$		
$a = -0.792096 - 0.581161I$	-5.07330 + 2.09337I	-12.51499 - 4.16283I
$b = 0.140343 + 0.966856I$		
$u = -0.535620 - 0.576021I$		
$a = -0.792096 + 0.581161I$	-5.07330 - 2.09337I	-12.51499 + 4.16283I
$b = 0.140343 - 0.966856I$		
$u = 0.035822 + 0.749326I$		
$a = 1.96913 + 0.59401I$	1.08148 - 1.33617I	-4.71591 + 0.70175I
$b = -0.796005 - 0.733148I$		
$u = 0.035822 - 0.749326I$		
$a = 1.96913 - 0.59401I$	1.08148 + 1.33617I	-4.71591 - 0.70175I
$b = -0.796005 + 0.733148I$		
$u = -1.209730 + 0.357771I$		
$a = 0.429481 - 0.621272I$	1.08148 + 1.33617I	-4.71591 - 0.70175I
$b = -0.796005 + 0.733148I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.209730 - 0.357771I$		
$a = 0.429481 + 0.621272I$	$1.08148 - 1.33617I$	$-4.71591 + 0.70175I$
$b = -0.796005 - 0.733148I$		
$u = 1.253840 + 0.303492I$		
$a = -1.61989 - 0.98839I$	$-2.67293 - 2.45442I$	$-9.67208 + 2.91298I$
$b = 0.628449 - 0.875112I$		
$u = 1.253840 - 0.303492I$		
$a = -1.61989 + 0.98839I$	$-2.67293 + 2.45442I$	$-9.67208 - 2.91298I$
$b = 0.628449 + 0.875112I$		
$u = 1.308540 + 0.065670I$		
$a = -0.41325 - 1.38121I$	$-5.07330 - 2.09337I$	$-12.51499 + 4.16283I$
$b = 0.140343 - 0.966856I$		
$u = 1.308540 - 0.065670I$		
$a = -0.41325 + 1.38121I$	$-5.07330 + 2.09337I$	$-12.51499 - 4.16283I$
$b = 0.140343 + 0.966856I$		
$u = 1.311030 + 0.356898I$		
$a = 1.61494 + 0.70203I$	$0.30826 - 7.08493I$	$-6.42320 + 5.91335I$
$b = -0.728966 + 0.986295I$		
$u = 1.311030 - 0.356898I$		
$a = 1.61494 - 0.70203I$	$0.30826 + 7.08493I$	$-6.42320 - 5.91335I$
$b = -0.728966 - 0.986295I$		
$u = 0.285873$		
$a = -3.02207$	$-2.09142$	$-3.34770$
$b = 0.512358$		

$$\text{III. } I_3^u = \langle b, a+1, u+1 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** = -12

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_8$ $c_{10}$	$u$
$c_2, c_3, c_7$	$u + 1$
$c_4, c_5, c_9$	$u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_8$ $c_{10}$	$y$
$c_2, c_3, c_4$ $c_5, c_7, c_9$	$y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = -1.00000$	-3.28987	-12.0000
$b = 0$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^2 \\ \cdot (u^{11} + 3u^{10} + 6u^9 + 7u^8 + 7u^7 + 3u^6 - 2u^5 - 8u^4 - 7u^3 - 5u^2 - 2u - 2)$
$c_2, c_3, c_7$	$(u + 1) \\ \cdot (u^{11} - u^{10} - 5u^9 + 4u^8 + 9u^7 - 4u^6 - 5u^5 - 3u^4 - 3u^3 + 5u^2 + 3u + 1) \\ \cdot (u^{18} - u^{17} + \dots + 2u - 1)$
$c_4, c_5, c_9$	$(u - 1) \\ \cdot (u^{11} - u^{10} - 5u^9 + 4u^8 + 9u^7 - 4u^6 - 5u^5 - 3u^4 - 3u^3 + 5u^2 + 3u + 1) \\ \cdot (u^{18} - u^{17} + \dots + 2u - 1)$
$c_8, c_{10}$	$u(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)^2 \\ \cdot (u^{11} + 3u^{10} + \dots - 16u - 4)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^2 \cdot (y^{11} + 3y^{10} + \dots - 16y - 4)$
$c_2, c_3, c_4$ $c_5, c_7, c_9$	$(y - 1)(y^{11} - 11y^{10} + \dots - y - 1)(y^{18} - 13y^{17} + \dots - 12y + 1)$
$c_8, c_{10}$	$y(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^2 \cdot (y^{11} + 7y^{10} + \dots + 24y - 16)$