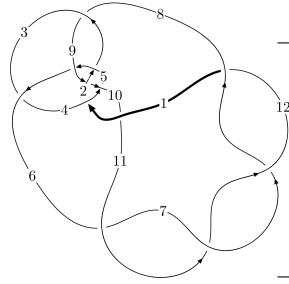
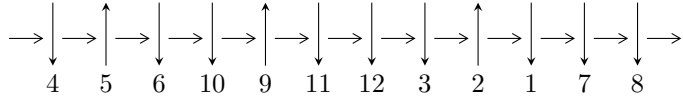


12a₀₈₀₉ (K12a₀₈₀₉)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$7,12 \xrightarrow{c_7} 3,8 \xrightarrow{c_8} 9 \xrightarrow{c_{12}} 1 \xrightarrow{c_{11}} 11 \xrightarrow{c_6} 6 \xrightarrow{c_3} 4 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \xrightarrow{c_{10}} 10 \rightsquigarrow c_1, c_4, c_9$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 148539u^{48} - 527493u^{47} + \dots + 8051b - 394683, 95347u^{48} - 282451u^{47} + \dots + 32204a + 36495, \\ u^{49} - 5u^{48} + \dots + 17u + 4 \rangle$$

$$I_2^u = \langle 2517u^{34}a + 42256u^{34} + \dots + 6152a + 31050, 6u^{34}a - 3u^{34} + \dots + 6a - 17, u^{35} + 2u^{34} + \dots + 4u - 1 \rangle$$

$$I_3^u = \langle u^{12} + u^{11} - 6u^{10} - 6u^9 + 12u^8 + 13u^7 - 9u^6 - 12u^5 + 2u^4 + 4u^3 + u^2 + b + u + 1, \\ -u^{14} + u^{13} + 8u^{12} - 7u^{11} - 23u^{10} + 17u^9 + 28u^8 - 16u^7 - 13u^6 + 5u^5 + u^4 - 3u^3 + 3u^2 + a + 2u + 1, \\ u^{15} - 2u^{14} - 7u^{13} + 15u^{12} + 17u^{11} - 40u^{10} - 18u^9 + 45u^8 + 14u^7 - 22u^6 - 13u^5 + 8u^4 + u^3 + u^2 + 1 \rangle$$

$$I_4^u = \langle au + b + u + 1, a^2 + 3au + 2a + u + 4, u^2 + u - 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 138 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 148539u^{48} - 527493u^{47} + \dots + 8051b - 394683, 95347u^{48} - 282451u^{47} + \dots + 32204a + 36495, u^{49} - 5u^{48} + \dots + 17u + 4 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2.96072u^{48} + 8.77068u^{47} + \dots - 24.7516u - 1.13324 \\ -18.4498u^{48} + 65.5189u^{47} + \dots + 241.353u + 49.0229 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -7.08294u^{48} + 17.6739u^{47} + \dots + 1.25894u + 5.64181 \\ -27.2013u^{48} + 89.0489u^{47} + \dots + 287.738u + 59.6427 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -4.22094u^{48} + 9.52301u^{47} + \dots - 21.4049u + 0.492516 \\ -11.5817u^{48} + 33.6645u^{47} + \dots + 72.2484u + 16.8837 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -8.39172u^{48} + 25.3461u^{47} + \dots + 57.0803u + 14.9414 \\ -12.9692u^{48} + 37.3577u^{47} + \dots + 90.6477u + 20.3169 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 4.12132u^{48} - 18.5185u^{47} + \dots - 157.649u - 27.2511 \\ 2.08806u^{48} - 10.1386u^{47} + \dots - 96.3135u - 16.4853 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^5 + 2u^3 + u \\ -u^7 + 3u^5 - 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{1218}{83}u^{48} - \frac{2750}{83}u^{47} + \dots + \frac{7009}{83}u - \frac{594}{83}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$u^{49} + 8u^{48} + \dots + 17u - 1$
c_2	$u^{49} + 26u^{48} + \dots + 11u + 2$
c_4, c_8	$u^{49} + 5u^{47} + \dots + 3u + 1$
c_5, c_9	$u^{49} - u^{48} + \dots + 27u^2 + 1$
c_6, c_7, c_{11} c_{12}	$u^{49} - 5u^{48} + \dots + 17u + 4$
c_{10}	$u^{49} - 9u^{48} + \dots - 1017u + 2272$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3	$y^{49} - 22y^{48} + \dots + 199y - 1$
c_2	$y^{49} + 20y^{47} + \dots + 89y - 4$
c_4, c_8	$y^{49} + 10y^{48} + \dots - 9y - 1$
c_5, c_9	$y^{49} + 25y^{48} + \dots - 54y - 1$
c_6, c_7, c_{11} c_{12}	$y^{49} - 55y^{48} + \dots + 137y - 16$
c_{10}	$y^{49} + 9y^{48} + \dots - 108326159y - 5161984$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.860395 + 0.482404I$ $a = 0.024941 + 0.522248I$ $b = -0.236258 + 0.004668I$	$-1.333090 - 0.442268I$	$-22.7302 - 2.7893I$
$u = -0.860395 - 0.482404I$ $a = 0.024941 - 0.522248I$ $b = -0.236258 - 0.004668I$	$-1.333090 + 0.442268I$	$-22.7302 + 2.7893I$
$u = 1.038190 + 0.218664I$ $a = 0.962395 + 0.159463I$ $b = 0.063672 - 0.241113I$	$-3.12377 - 8.13177I$	$0. + 9.34743I$
$u = 1.038190 - 0.218664I$ $a = 0.962395 - 0.159463I$ $b = 0.063672 + 0.241113I$	$-3.12377 + 8.13177I$	$0. - 9.34743I$
$u = -0.656302 + 0.593975I$ $a = 1.73077 + 1.26119I$ $b = 0.157164 + 0.032896I$	$1.0974 + 15.3120I$	$-6.69862 - 10.70010I$
$u = -0.656302 - 0.593975I$ $a = 1.73077 - 1.26119I$ $b = 0.157164 - 0.032896I$	$1.0974 - 15.3120I$	$-6.69862 + 10.70010I$
$u = -0.527749 + 0.624204I$ $a = -0.344437 - 0.796756I$ $b = -0.374375 + 0.028886I$	$-0.22239 + 2.13464I$	$-12.97767 - 4.41434I$
$u = -0.527749 - 0.624204I$ $a = -0.344437 + 0.796756I$ $b = -0.374375 - 0.028886I$	$-0.22239 - 2.13464I$	$-12.97767 + 4.41434I$
$u = -0.598351 + 0.535692I$ $a = -1.55845 - 1.25421I$ $b = 0.013056 + 0.352563I$	$-0.78788 + 6.56431I$	$-12.9454 - 9.8564I$
$u = -0.598351 - 0.535692I$ $a = -1.55845 + 1.25421I$ $b = 0.013056 - 0.352563I$	$-0.78788 - 6.56431I$	$-12.9454 + 9.8564I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.747144$ $a = 0.385007$ $b = -0.305862$	-1.10744	-7.81270
$u = -0.162177 + 0.729155I$ $a = 0.300367 - 0.459004I$ $b = 0.409646 - 0.408558I$	$0.80721 + 4.71794I$	$-9.1417 - 13.3340I$
$u = -0.162177 - 0.729155I$ $a = 0.300367 + 0.459004I$ $b = 0.409646 + 0.408558I$	$0.80721 - 4.71794I$	$-9.1417 + 13.3340I$
$u = 0.744466 + 0.003975I$ $a = -1.81736 + 0.85970I$ $b = -0.328629 + 0.159289I$	$-4.13096 + 1.69814I$	$-18.2040 - 4.3712I$
$u = 0.744466 - 0.003975I$ $a = -1.81736 - 0.85970I$ $b = -0.328629 - 0.159289I$	$-4.13096 - 1.69814I$	$-18.2040 + 4.3712I$
$u = -0.300631 + 0.671867I$ $a = 0.481511 + 0.645526I$ $b = 0.987848 + 0.795214I$	$2.15150 - 11.04750I$	$-4.44153 + 5.63378I$
$u = -0.300631 - 0.671867I$ $a = 0.481511 - 0.645526I$ $b = 0.987848 - 0.795214I$	$2.15150 + 11.04750I$	$-4.44153 - 5.63378I$
$u = 0.485135 + 0.542391I$ $a = 0.943805 - 0.987006I$ $b = 0.402923 - 0.436742I$	$2.90214 - 1.87444I$	$-0.73211 + 3.66192I$
$u = 0.485135 - 0.542391I$ $a = 0.943805 + 0.987006I$ $b = 0.402923 + 0.436742I$	$2.90214 + 1.87444I$	$-0.73211 - 3.66192I$
$u = 1.289650 + 0.140107I$ $a = 0.300793 - 0.515547I$ $b = -0.125058 + 0.334394I$	$-2.81136 + 8.04498I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.289650 - 0.140107I$ $a = 0.300793 + 0.515547I$ $b = -0.125058 - 0.334394I$	$-2.81136 - 8.04498I$	0
$u = 0.506307 + 0.409416I$ $a = -2.22196 + 1.72599I$ $b = -0.776269 + 0.644378I$	$-1.37259 - 1.45940I$	$-10.10356 + 4.62979I$
$u = 0.506307 - 0.409416I$ $a = -2.22196 - 1.72599I$ $b = -0.776269 - 0.644378I$	$-1.37259 + 1.45940I$	$-10.10356 - 4.62979I$
$u = -0.340049 + 0.552838I$ $a = 0.176095 - 0.121875I$ $b = -0.914800 - 0.629603I$	$-0.03939 - 2.80450I$	$-9.90854 + 3.00975I$
$u = -0.340049 - 0.552838I$ $a = 0.176095 + 0.121875I$ $b = -0.914800 + 0.629603I$	$-0.03939 + 2.80450I$	$-9.90854 - 3.00975I$
$u = -0.537786 + 0.350030I$ $a = -0.059222 - 1.272190I$ $b = 0.103070 + 0.635374I$	$-1.62694 + 1.54828I$	$-11.08710 - 6.22827I$
$u = -0.537786 - 0.350030I$ $a = -0.059222 + 1.272190I$ $b = 0.103070 - 0.635374I$	$-1.62694 - 1.54828I$	$-11.08710 + 6.22827I$
$u = 1.47621 + 0.08489I$ $a = -0.950241 + 0.354999I$ $b = -1.43618 - 0.18131I$	$-5.81539 + 0.81969I$	0
$u = 1.47621 - 0.08489I$ $a = -0.950241 - 0.354999I$ $b = -1.43618 + 0.18131I$	$-5.81539 - 0.81969I$	0
$u = -1.52067 + 0.14417I$ $a = -0.937215 - 0.026137I$ $b = -1.98715 - 0.67865I$	$-3.73933 + 4.27877I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.52067 - 0.14417I$ $a = -0.937215 + 0.026137I$ $b = -1.98715 + 0.67865I$	$-3.73933 - 4.27877I$	0
$u = -1.55060 + 0.10978I$ $a = 1.84193 - 0.18622I$ $b = 4.05332 + 0.45056I$	$-8.35293 + 3.28009I$	0
$u = -1.55060 - 0.10978I$ $a = 1.84193 + 0.18622I$ $b = 4.05332 - 0.45056I$	$-8.35293 - 3.28009I$	0
$u = 1.54635 + 0.18703I$ $a = 0.757838 - 0.546719I$ $b = 1.80903 - 1.20397I$	$-7.12280 - 5.06000I$	0
$u = 1.54635 - 0.18703I$ $a = 0.757838 + 0.546719I$ $b = 1.80903 + 1.20397I$	$-7.12280 + 5.06000I$	0
$u = 1.55747 + 0.09309I$ $a = 0.98887 - 1.45323I$ $b = 2.04164 - 2.22854I$	$-8.74919 - 3.11091I$	0
$u = 1.55747 - 0.09309I$ $a = 0.98887 + 1.45323I$ $b = 2.04164 + 2.22854I$	$-8.74919 + 3.11091I$	0
$u = 1.56503 + 0.15811I$ $a = 2.12720 - 0.54206I$ $b = 4.43010 - 0.79741I$	$-8.03789 - 9.09579I$	0
$u = 1.56503 - 0.15811I$ $a = 2.12720 + 0.54206I$ $b = 4.43010 + 0.79741I$	$-8.03789 + 9.09579I$	0
$u = -1.59257 + 0.00650I$ $a = 1.97070 + 0.65045I$ $b = 4.19761 + 1.43756I$	$-12.06900 - 1.62283I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.59257 - 0.00650I$ $a = 1.97070 - 0.65045I$ $b = 4.19761 - 1.43756I$	$-12.06900 + 1.62283I$	0
$u = 1.58602 + 0.18202I$ $a = -2.19854 + 0.10847I$ $b = -4.50456 + 0.32567I$	$-6.4148 - 18.1914I$	0
$u = 1.58602 - 0.18202I$ $a = -2.19854 - 0.10847I$ $b = -4.50456 - 0.32567I$	$-6.4148 + 18.1914I$	0
$u = -0.240166 + 0.320881I$ $a = 0.947458 + 0.195457I$ $b = -0.450401 + 0.404469I$	$-0.963675 + 0.866301I$	$-7.31478 - 5.07695I$
$u = -0.240166 - 0.320881I$ $a = 0.947458 - 0.195457I$ $b = -0.450401 - 0.404469I$	$-0.963675 - 0.866301I$	$-7.31478 + 5.07695I$
$u = 1.61021 + 0.11898I$ $a = -1.070280 + 0.513665I$ $b = -1.94637 + 0.86375I$	$-9.61044 - 1.58418I$	0
$u = 1.61021 - 0.11898I$ $a = -1.070280 - 0.513665I$ $b = -1.94637 - 0.86375I$	$-9.61044 + 1.58418I$	0
$u = -1.64403 + 0.02832I$ $a = -1.71447 + 0.78931I$ $b = -3.43609 + 1.41784I$	$-12.1970 + 8.7921I$	0
$u = -1.64403 - 0.02832I$ $a = -1.71447 - 0.78931I$ $b = -3.43609 - 1.41784I$	$-12.1970 - 8.7921I$	0

$$\text{II. } I_2^u = \langle 2517u^{34}a + 42256u^{34} + \dots + 6152a + 31050, 6u^{34}a - 3u^{34} + \dots + 6a - 17, u^{35} + 2u^{34} + \dots + 4u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} a \\ -0.143068au^{34} - 2.40186u^{34} + \dots - 0.349685a - 1.76491 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1.40186au^{34} - 0.835844u^{34} + \dots + 1.76491a - 8.26067 \\ 1.14671au^{34} + 2.94168u^{34} + \dots - 0.548059a - 2.67055 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.291480au^{34} + 3.12783u^{34} + \dots + 1.31831a - 0.266015 \\ -0.215483au^{34} + 1.75865u^{34} + \dots - 0.291480a - 5.12783 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.255158au^{34} + 3.22247u^{34} + \dots + 1.31297a + 1.40988 \\ 0.112090au^{34} + 1.82061u^{34} + \dots - 0.0367191a - 4.35503 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -1.03268au^{34} - 3.36554u^{34} + \dots + 3.09691a - 2.75956 \\ -3.43455au^{34} - 2.52970u^{34} + \dots + 1.33201a + 3.50111 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^5 + 2u^3 + u \\ -u^7 + 3u^5 - 2u^3 + u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= u^{34} + 2u^{33} - 17u^{32} - 29u^{31} + 126u^{30} + 160u^{29} - 539u^{28} - 330u^{27} + \\ &1491u^{26} - 522u^{25} - 2809u^{24} + 4690u^{23} + 3456u^{22} - 12414u^{21} - 1644u^{20} + 18572u^{19} - \\ &3263u^{18} - 17872u^{17} + 7947u^{16} + 11650u^{15} - 8304u^{14} - 4754u^{13} + 5714u^{12} + 816u^{11} - \\ &3062u^{10} + 144u^9 + 1032u^8 - 416u^7 - 370u^6 + 110u^5 + 8u^4 - 50u^3 - 9u^2 + 2u - 11 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$u^{70} - 5u^{69} + \dots + 118u - 11$
c_2	$(u^{35} - 17u^{34} + \dots - 2u + 4)^2$
c_4, c_8	$u^{70} - 2u^{69} + \dots - 3755u - 389$
c_5, c_9	$u^{70} - 4u^{69} + \dots - u + 1$
c_6, c_7, c_{11} c_{12}	$(u^{35} + 2u^{34} + \dots + 4u - 1)^2$
c_{10}	$(u^{35} - 8u^{34} + \dots - 34u - 17)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3	$y^{70} + 23y^{69} + \dots - 3012y + 121$
c_2	$(y^{35} - 5y^{34} + \dots + 268y - 16)^2$
c_4, c_8	$y^{70} + 4y^{69} + \dots - 6317691y + 151321$
c_5, c_9	$y^{70} - 16y^{69} + \dots + 9y + 1$
c_6, c_7, c_{11} c_{12}	$(y^{35} - 40y^{34} + \dots + 12y - 1)^2$
c_{10}	$(y^{35} + 8y^{34} + \dots + 884y - 289)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.666512 + 0.582064I$ $a = -1.239150 + 0.250233I$ $b = -0.059661 - 0.188761I$	$2.64852 - 7.06572I$	$-2.24468 + 9.47416I$
$u = 0.666512 + 0.582064I$ $a = 1.50375 - 1.16447I$ $b = 0.070870 - 0.248710I$	$2.64852 - 7.06572I$	$-2.24468 + 9.47416I$
$u = 0.666512 - 0.582064I$ $a = -1.239150 - 0.250233I$ $b = -0.059661 + 0.188761I$	$2.64852 + 7.06572I$	$-2.24468 - 9.47416I$
$u = 0.666512 - 0.582064I$ $a = 1.50375 + 1.16447I$ $b = 0.070870 + 0.248710I$	$2.64852 + 7.06572I$	$-2.24468 - 9.47416I$
$u = -1.16124$ $a = 0.043408 + 0.442130I$ $b = -0.393345 - 0.073439I$	-0.859981	-0.877410
$u = -1.16124$ $a = 0.043408 - 0.442130I$ $b = -0.393345 + 0.073439I$	-0.859981	-0.877410
$u = -0.782419 + 0.220868I$ $a = -0.54049 - 1.41055I$ $b = -0.306204 + 0.132537I$	$-2.98205 - 1.23863I$	$-15.1065 + 4.7419I$
$u = -0.782419 + 0.220868I$ $a = 1.64861 + 0.56272I$ $b = -0.050193 + 0.786535I$	$-2.98205 - 1.23863I$	$-15.1065 + 4.7419I$
$u = -0.782419 - 0.220868I$ $a = -0.54049 + 1.41055I$ $b = -0.306204 - 0.132537I$	$-2.98205 + 1.23863I$	$-15.1065 - 4.7419I$
$u = -0.782419 - 0.220868I$ $a = 1.64861 - 0.56272I$ $b = -0.050193 - 0.786535I$	$-2.98205 + 1.23863I$	$-15.1065 - 4.7419I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.20404$ $a = 0.010704 + 0.441967I$ $b = -0.418731 - 0.084162I$	-0.860321	-1.06770
$u = -1.20404$ $a = 0.010704 - 0.441967I$ $b = -0.418731 + 0.084162I$	-0.860321	-1.06770
$u = 0.638463 + 0.472891I$ $a = 0.00841 - 1.58949I$ $b = -0.732835 + 0.165675I$	$-1.26211 - 6.69833I$	$-12.2764 + 10.3456I$
$u = 0.638463 + 0.472891I$ $a = -2.23392 + 0.77030I$ $b = -0.191691 - 0.277776I$	$-1.26211 - 6.69833I$	$-12.2764 + 10.3456I$
$u = 0.638463 - 0.472891I$ $a = 0.00841 + 1.58949I$ $b = -0.732835 - 0.165675I$	$-1.26211 + 6.69833I$	$-12.2764 - 10.3456I$
$u = 0.638463 - 0.472891I$ $a = -2.23392 - 0.77030I$ $b = -0.191691 + 0.277776I$	$-1.26211 + 6.69833I$	$-12.2764 - 10.3456I$
$u = 0.476081 + 0.547627I$ $a = 0.849827 - 0.724384I$ $b = 0.297746 - 0.578232I$	$2.91093 - 1.88971I$	$-0.44498 + 3.89733I$
$u = 0.476081 + 0.547627I$ $a = 1.08918 - 1.23722I$ $b = 0.547443 - 0.288098I$	$2.91093 - 1.88971I$	$-0.44498 + 3.89733I$
$u = 0.476081 - 0.547627I$ $a = 0.849827 + 0.724384I$ $b = 0.297746 + 0.578232I$	$2.91093 + 1.88971I$	$-0.44498 - 3.89733I$
$u = 0.476081 - 0.547627I$ $a = 1.08918 + 1.23722I$ $b = 0.547443 + 0.288098I$	$2.91093 + 1.88971I$	$-0.44498 - 3.89733I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.525223 + 0.491556I$		
$a = -0.62016 + 1.42991I$	$2.43912 + 5.99758I$	$-1.93287 - 10.06250I$
$b = 0.689553 + 1.077310I$		
$u = -0.525223 + 0.491556I$		
$a = -2.07561 - 1.78920I$	$2.43912 + 5.99758I$	$-1.93287 - 10.06250I$
$b = 0.191089 - 0.259118I$		
$u = -0.525223 - 0.491556I$		
$a = -0.62016 - 1.42991I$	$2.43912 - 5.99758I$	$-1.93287 + 10.06250I$
$b = 0.689553 - 1.077310I$		
$u = -0.525223 - 0.491556I$		
$a = -2.07561 + 1.78920I$	$2.43912 - 5.99758I$	$-1.93287 + 10.06250I$
$b = 0.191089 + 0.259118I$		
$u = 0.277580 + 0.662679I$		
$a = 0.736054 - 0.530277I$	$3.79715 + 2.86775I$	$1.19785 - 3.30855I$
$b = 0.797040 - 0.685996I$		
$u = 0.277580 + 0.662679I$		
$a = 0.163136 + 0.349177I$	$3.79715 + 2.86775I$	$1.19785 - 3.30855I$
$b = -0.295111 + 0.682840I$		
$u = 0.277580 - 0.662679I$		
$a = 0.736054 + 0.530277I$	$3.79715 - 2.86775I$	$1.19785 + 3.30855I$
$b = 0.797040 + 0.685996I$		
$u = 0.277580 - 0.662679I$		
$a = 0.163136 - 0.349177I$	$3.79715 - 2.86775I$	$1.19785 + 3.30855I$
$b = -0.295111 - 0.682840I$		
$u = -0.441250 + 0.489469I$		
$a = -0.884679 - 0.035500I$	$2.68875 - 2.55506I$	$-0.147951 + 0.889172I$
$b = -0.971326 - 0.931519I$		
$u = -0.441250 + 0.489469I$		
$a = 2.35888 + 1.07821I$	$2.68875 - 2.55506I$	$-0.147951 + 0.889172I$
$b = 0.371733 - 0.548181I$		

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.441250 - 0.489469I$ $a = -0.884679 + 0.035500I$ $b = -0.971326 + 0.931519I$	$2.68875 + 2.55506I$	$-0.147951 - 0.889172I$
$u = -0.441250 - 0.489469I$ $a = 2.35888 - 1.07821I$ $b = 0.371733 + 0.548181I$	$2.68875 + 2.55506I$	$-0.147951 - 0.889172I$
$u = 0.195556 + 0.466781I$ $a = 0.358284 + 0.485136I$ $b = -0.729100 + 0.903609I$	$-0.07204 + 3.38846I$	$-7.99570 - 4.25357I$
$u = 0.195556 + 0.466781I$ $a = 0.96362 + 1.74995I$ $b = 0.805890 + 0.233688I$	$-0.07204 + 3.38846I$	$-7.99570 - 4.25357I$
$u = 0.195556 - 0.466781I$ $a = 0.358284 - 0.485136I$ $b = -0.729100 - 0.903609I$	$-0.07204 - 3.38846I$	$-7.99570 + 4.25357I$
$u = 0.195556 - 0.466781I$ $a = 0.96362 - 1.74995I$ $b = 0.805890 - 0.233688I$	$-0.07204 - 3.38846I$	$-7.99570 + 4.25357I$
$u = -1.51268 + 0.13583I$ $a = -0.621893 + 0.392051I$ $b = -1.172090 - 0.041405I$	$-3.63443 + 4.26143I$	0
$u = -1.51268 + 0.13583I$ $a = -1.215730 - 0.406169I$ $b = -2.85058 - 1.22060I$	$-3.63443 + 4.26143I$	0
$u = -1.51268 - 0.13583I$ $a = -0.621893 - 0.392051I$ $b = -1.172090 + 0.041405I$	$-3.63443 - 4.26143I$	0
$u = -1.51268 - 0.13583I$ $a = -1.215730 + 0.406169I$ $b = -2.85058 + 1.22060I$	$-3.63443 - 4.26143I$	0

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.51779 + 0.11529I$ $a = -0.190719 + 1.045250I$ $b = 0.047370 + 0.888797I$	$-3.82932 + 0.52023I$	0
$u = 1.51779 + 0.11529I$ $a = -2.07253 + 0.17597I$ $b = -4.69665 + 0.02384I$	$-3.82932 + 0.52023I$	0
$u = 1.51779 - 0.11529I$ $a = -0.190719 - 1.045250I$ $b = 0.047370 - 0.888797I$	$-3.82932 - 0.52023I$	0
$u = 1.51779 - 0.11529I$ $a = -2.07253 - 0.17597I$ $b = -4.69665 - 0.02384I$	$-3.82932 - 0.52023I$	0
$u = -1.53311 + 0.06521I$ $a = -0.718843 + 0.254928I$ $b = -1.17807 + 1.78768I$	$-6.32420 - 2.55827I$	$-11.80080 + 5.60834I$
$u = -1.53311 + 0.06521I$ $a = 1.89671 + 1.84534I$ $b = 3.23347 + 3.48987I$	$-6.32420 - 2.55827I$	$-11.80080 + 5.60834I$
$u = -1.53311 - 0.06521I$ $a = -0.718843 - 0.254928I$ $b = -1.17807 - 1.78768I$	$-6.32420 + 2.55827I$	$-11.80080 - 5.60834I$
$u = -1.53311 - 0.06521I$ $a = 1.89671 - 1.84534I$ $b = 3.23347 - 3.48987I$	$-6.32420 + 2.55827I$	$-11.80080 - 5.60834I$
$u = 1.54485 + 0.13337I$ $a = 0.385384 + 0.615349I$ $b = 0.65878 + 2.45832I$	$-4.50128 - 8.20533I$	0
$u = 1.54485 + 0.13337I$ $a = 2.79157 - 0.12318I$ $b = 5.31687 - 0.42575I$	$-4.50128 - 8.20533I$	0

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.54485 - 0.13337I$ $a = 0.385384 - 0.615349I$ $b = 0.65878 - 2.45832I$	$-4.50128 + 8.20533I$	0
$u = 1.54485 - 0.13337I$ $a = 2.79157 + 0.12318I$ $b = 5.31687 + 0.42575I$	$-4.50128 + 8.20533I$	0
$u = -1.58137 + 0.13915I$ $a = -1.53160 - 1.51990I$ $b = -2.59358 - 2.56426I$	$-8.76037 + 8.95548I$	0
$u = -1.58137 + 0.13915I$ $a = 2.26630 - 0.09882I$ $b = 4.81897 - 0.31491I$	$-8.76037 + 8.95548I$	0
$u = -1.58137 - 0.13915I$ $a = -1.53160 + 1.51990I$ $b = -2.59358 + 2.56426I$	$-8.76037 - 8.95548I$	0
$u = -1.58137 - 0.13915I$ $a = 2.26630 + 0.09882I$ $b = 4.81897 + 0.31491I$	$-8.76037 - 8.95548I$	0
$u = 0.384702 + 0.130377I$ $a = 1.34643 + 1.15599I$ $b = -0.479286 + 1.191100I$	$0.28705 + 3.45586I$	$-12.59187 - 3.72340I$
$u = 0.384702 + 0.130377I$ $a = -0.33211 + 4.09606I$ $b = 0.594555 + 0.086997I$	$0.28705 + 3.45586I$	$-12.59187 - 3.72340I$
$u = 0.384702 - 0.130377I$ $a = 1.34643 - 1.15599I$ $b = -0.479286 - 1.191100I$	$0.28705 - 3.45586I$	$-12.59187 + 3.72340I$
$u = 0.384702 - 0.130377I$ $a = -0.33211 - 4.09606I$ $b = 0.594555 - 0.086997I$	$0.28705 - 3.45586I$	$-12.59187 + 3.72340I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.58992 + 0.17781I$		
$a = 1.314390 - 0.220603I$	$-4.92419 + 9.89136I$	0
$b = 2.77301 - 0.55986I$		
$u = -1.58992 + 0.17781I$		
$a = -2.04710 - 0.00757I$	$-4.92419 + 9.89136I$	0
$b = -4.02959 - 0.25930I$		
$u = -1.58992 - 0.17781I$		
$a = 1.314390 + 0.220603I$	$-4.92419 - 9.89136I$	0
$b = 2.77301 + 0.55986I$		
$u = -1.58992 - 0.17781I$		
$a = -2.04710 + 0.00757I$	$-4.92419 - 9.89136I$	0
$b = -4.02959 + 0.25930I$		
$u = 1.61834 + 0.05147I$		
$a = 0.99213 - 1.13861I$	$-11.22110 + 0.25726I$	0
$b = 2.24075 - 2.24946I$		
$u = 1.61834 + 0.05147I$		
$a = -2.18543 - 0.68568I$	$-11.22110 + 0.25726I$	0
$b = -4.13160 - 0.81782I$		
$u = 1.61834 - 0.05147I$		
$a = 0.99213 + 1.13861I$	$-11.22110 - 0.25726I$	0
$b = 2.24075 + 2.24946I$		
$u = 1.61834 - 0.05147I$		
$a = -2.18543 + 0.68568I$	$-11.22110 - 0.25726I$	0
$b = -4.13160 + 0.81782I$		
$u = 1.65747$		
$a = 0.394240$	-10.1124	0
$b = 0.976487$		
$u = 1.65747$		
$a = -1.82785$	-10.1124	0
$b = -3.32748$		

III.

$$I_3^u = \langle u^{12} + u^{11} + \dots + b + 1, -u^{14} + u^{13} + \dots + a + 1, u^{15} - 2u^{14} + \dots + u^2 + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{14} - u^{13} + \dots - 2u - 1 \\ -u^{12} - u^{11} + \dots - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 3u^{14} - u^{13} + \dots - u - 1 \\ 5u^{14} - 3u^{13} + \dots - u - 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 5u^{14} - 4u^{13} + \dots - 2u - 3 \\ 6u^{14} - 3u^{13} + \dots - 3u - 5 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2u^{14} - 2u^{13} + \dots - u - 1 \\ 2u^{14} - u^{13} + \dots - 2u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 3u^{14} - u^{13} + \dots - u - 3 \\ 5u^{14} - 2u^{13} + \dots - 2u - 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^5 + 2u^3 + u \\ -u^7 + 3u^5 - 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-10u^{14} + 3u^{13} + 78u^{12} - 14u^{11} - 227u^{10} - u^9 + 307u^8 + 85u^7 - 202u^6 - 117u^5 + 54u^4 + 24u^3 + 18u^2 + 11u + 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$u^{15} - 4u^{14} + \dots + 5u - 1$
c_2	$u^{15} + 11u^{14} + \dots + 69u + 5$
c_4, c_8	$u^{15} - 2u^{13} + \dots - u + 1$
c_5, c_9	$u^{15} - u^{14} + \dots - 2u^2 + 1$
c_6, c_7	$u^{15} - 2u^{14} + \dots + u^2 + 1$
c_{10}	$u^{15} + 2u^{14} + \dots + 4u + 1$
c_{11}, c_{12}	$u^{15} + 2u^{14} + \dots - u^2 - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3	$y^{15} + 12y^{14} + \dots - 7y - 1$
c_2	$y^{15} + 5y^{14} + \dots + 1201y - 25$
c_4, c_8	$y^{15} - 4y^{14} + \dots + 5y - 1$
c_5, c_9	$y^{15} - 5y^{14} + \dots + 4y - 1$
c_6, c_7, c_{11} c_{12}	$y^{15} - 18y^{14} + \dots - 2y - 1$
c_{10}	$y^{15} - 2y^{14} + \dots - 10y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.968088 + 0.372476I$ $a = -0.059767 + 0.569906I$ $b = 0.162535 + 0.150354I$	$-1.117930 + 0.672381I$	$-5.5717 - 15.5217I$
$u = 0.968088 - 0.372476I$ $a = -0.059767 - 0.569906I$ $b = 0.162535 - 0.150354I$	$-1.117930 - 0.672381I$	$-5.5717 + 15.5217I$
$u = -0.617443 + 0.491186I$ $a = -1.52967 - 0.80405I$ $b = 0.275235 + 0.217089I$	$0.46809 + 6.63284I$	$-5.87049 - 10.29818I$
$u = -0.617443 - 0.491186I$ $a = -1.52967 + 0.80405I$ $b = 0.275235 - 0.217089I$	$0.46809 - 6.63284I$	$-5.87049 + 10.29818I$
$u = -0.334963 + 0.434830I$ $a = 0.218876 + 0.780240I$ $b = -0.646634 - 0.822557I$	$1.34167 - 3.29522I$	$-2.79998 + 3.51950I$
$u = -0.334963 - 0.434830I$ $a = 0.218876 - 0.780240I$ $b = -0.646634 + 0.822557I$	$1.34167 + 3.29522I$	$-2.79998 - 3.51950I$
$u = -1.48976 + 0.10689I$ $a = -0.711932 - 0.669447I$ $b = -1.26873 - 2.07242I$	$-4.60411 + 5.60570I$	$-9.56653 - 7.15919I$
$u = -1.48976 - 0.10689I$ $a = -0.711932 + 0.669447I$ $b = -1.26873 + 2.07242I$	$-4.60411 - 5.60570I$	$-9.56653 + 7.15919I$
$u = 1.51063 + 0.09194I$ $a = -1.41929 + 0.71032I$ $b = -2.56043 + 0.38952I$	$-4.92279 + 1.66323I$	$-7.24786 - 5.12167I$
$u = 1.51063 - 0.09194I$ $a = -1.41929 - 0.71032I$ $b = -2.56043 - 0.38952I$	$-4.92279 - 1.66323I$	$-7.24786 + 5.12167I$

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.209564 + 0.438491I$ $a = -1.14877 - 1.22839I$ $b = -0.198242 - 0.661573I$	$1.25166 - 3.87018I$	$-2.48614 + 6.40598I$
$u = 0.209564 - 0.438491I$ $a = -1.14877 + 1.22839I$ $b = -0.198242 + 0.661573I$	$1.25166 + 3.87018I$	$-2.48614 - 6.40598I$
$u = 1.57469 + 0.14763I$ $a = 2.00341 - 0.20449I$ $b = 3.95483 - 0.13857I$	$-6.92174 - 8.98940I$	$-8.76043 + 7.91883I$
$u = 1.57469 - 0.14763I$ $a = 2.00341 + 0.20449I$ $b = 3.95483 + 0.13857I$	$-6.92174 + 8.98940I$	$-8.76043 - 7.91883I$
$u = -1.64161$ $a = 1.29429$ $b = 2.56286$	-10.4681	-17.3940

$$\text{IV. } \Gamma_4^u = \langle au + b + u + 1, a^2 + 3au + 2a + u + 4, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -au - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2au + a + u + 5 \\ 2au - a - 3u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a + u \\ -au - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2a + 3u + 1 \\ -2au + a + 3u - 3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -au - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-u - 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$(u - 1)^4$
c_2	u^4
c_4, c_5, c_8 c_9	$u^4 + u^3 + u^2 + u + 1$
c_6, c_7, c_{10}	$(u^2 + u - 1)^2$
c_{11}, c_{12}	$(u^2 - u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3	$(y - 1)^4$
c_2	y^4
c_4, c_5, c_8 c_9	$y^4 + y^3 + y^2 + y + 1$
c_6, c_7, c_{10} c_{11}, c_{12}	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = -1.92705 + 0.95106I$ $b = -0.427051 - 0.587785I$	-2.63189	-14.6180
$u = 0.618034$ $a = -1.92705 - 0.95106I$ $b = -0.427051 + 0.587785I$	-2.63189	-14.6180
$u = -1.61803$ $a = 1.42705 + 0.58779I$ $b = 2.92705 + 0.95106I$	-10.5276	-12.3820
$u = -1.61803$ $a = 1.42705 - 0.58779I$ $b = 2.92705 - 0.95106I$	-10.5276	-12.3820

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_3	$((u-1)^4)(u^{15} - 4u^{14} + \dots + 5u - 1)(u^{49} + 8u^{48} + \dots + 17u - 1)$ $\cdot (u^{70} - 5u^{69} + \dots + 118u - 11)$
c_2	$u^4(u^{15} + 11u^{14} + \dots + 69u + 5)(u^{35} - 17u^{34} + \dots - 2u + 4)^2$ $\cdot (u^{49} + 26u^{48} + \dots + 11u + 2)$
c_4, c_8	$(u^4 + u^3 + u^2 + u + 1)(u^{15} - 2u^{13} + \dots - u + 1)(u^{49} + 5u^{47} + \dots + 3u + 1)$ $\cdot (u^{70} - 2u^{69} + \dots - 3755u - 389)$
c_5, c_9	$(u^4 + u^3 + u^2 + u + 1)(u^{15} - u^{14} + \dots - 2u^2 + 1)$ $\cdot (u^{49} - u^{48} + \dots + 27u^2 + 1)(u^{70} - 4u^{69} + \dots - u + 1)$
c_6, c_7	$((u^2 + u - 1)^2)(u^{15} - 2u^{14} + \dots + u^2 + 1)(u^{35} + 2u^{34} + \dots + 4u - 1)^2$ $\cdot (u^{49} - 5u^{48} + \dots + 17u + 4)$
c_{10}	$((u^2 + u - 1)^2)(u^{15} + 2u^{14} + \dots + 4u + 1)$ $\cdot ((u^{35} - 8u^{34} + \dots - 34u - 17)^2)(u^{49} - 9u^{48} + \dots - 1017u + 2272)$
c_{11}, c_{12}	$((u^2 - u - 1)^2)(u^{15} + 2u^{14} + \dots - u^2 - 1)(u^{35} + 2u^{34} + \dots + 4u - 1)^2$ $\cdot (u^{49} - 5u^{48} + \dots + 17u + 4)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_3	$((y-1)^4)(y^{15} + 12y^{14} + \dots - 7y - 1)(y^{49} - 22y^{48} + \dots + 199y - 1)$ $\cdot (y^{70} + 23y^{69} + \dots - 3012y + 121)$
c_2	$y^4(y^{15} + 5y^{14} + \dots + 1201y - 25)(y^{35} - 5y^{34} + \dots + 268y - 16)^2$ $\cdot (y^{49} + 20y^{47} + \dots + 89y - 4)$
c_4, c_8	$(y^4 + y^3 + y^2 + y + 1)(y^{15} - 4y^{14} + \dots + 5y - 1)$ $\cdot (y^{49} + 10y^{48} + \dots - 9y - 1)(y^{70} + 4y^{69} + \dots - 6317691y + 151321)$
c_5, c_9	$(y^4 + y^3 + y^2 + y + 1)(y^{15} - 5y^{14} + \dots + 4y - 1)$ $\cdot (y^{49} + 25y^{48} + \dots - 54y - 1)(y^{70} - 16y^{69} + \dots + 9y + 1)$
c_6, c_7, c_{11} c_{12}	$((y^2 - 3y + 1)^2)(y^{15} - 18y^{14} + \dots - 2y - 1)$ $\cdot ((y^{35} - 40y^{34} + \dots + 12y - 1)^2)(y^{49} - 55y^{48} + \dots + 137y - 16)$
c_{10}	$((y^2 - 3y + 1)^2)(y^{15} - 2y^{14} + \dots - 10y - 1)$ $\cdot (y^{35} + 8y^{34} + \dots + 884y - 289)^2$ $\cdot (y^{49} + 9y^{48} + \dots - 108326159y - 5161984)$