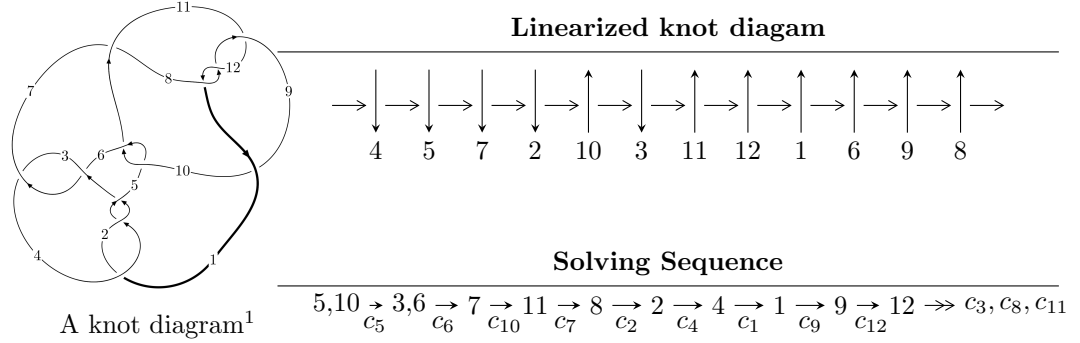


12a<sub>0816</sub> (K12a<sub>0816</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 3.88375 \times 10^{234} u^{85} - 1.46902 \times 10^{234} u^{84} + \dots + 2.70951 \times 10^{236} b + 2.78190 \times 10^{236}, \\ 1.64525 \times 10^{236} u^{85} + 2.08852 \times 10^{236} u^{84} + \dots + 5.41901 \times 10^{236} a + 7.89723 \times 10^{237}, \\ u^{86} + 2u^{85} + \dots + 352u + 64 \rangle$$

$$I_2^u = \langle b + 1, u^5 - 4u^3 + u^2 + a + 4u - 3, u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

$$I_1^v = \langle a, 8v^5 + 21v^4 + 63v^3 + 21v^2 + 503b - v - 817, v^6 + 3v^5 + v^4 - 18v^3 - 7v^2 + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 98 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew (<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose (<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 3.88 \times 10^{234} u^{85} - 1.47 \times 10^{234} u^{84} + \dots + 2.71 \times 10^{236} b + 2.78 \times 10^{236}, 1.65 \times 10^{236} u^{85} + 2.09 \times 10^{236} u^{84} + \dots + 5.42 \times 10^{236} a + 7.90 \times 10^{237}, u^{86} + 2u^{85} + \dots + 352u + 64 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.303607u^{85} - 0.385406u^{84} + \dots - 98.1776u - 14.5732 \\ -0.0143338u^{85} + 0.00542171u^{84} + \dots - 2.27870u - 1.02672 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.400196u^{85} - 0.562734u^{84} + \dots - 159.471u - 37.7347 \\ 0.0373459u^{85} + 0.124701u^{84} + \dots + 33.4026u + 11.9056 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.364855u^{85} - 0.475874u^{84} + \dots - 132.797u - 29.2352 \\ 0.103811u^{85} + 0.242890u^{84} + \dots + 68.0341u + 21.4406 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.317940u^{85} - 0.379984u^{84} + \dots - 100.456u - 15.5999 \\ -0.0143338u^{85} + 0.00542171u^{84} + \dots - 2.27870u - 1.02672 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.000379134u^{85} - 0.00662213u^{84} + \dots + 10.0057u + 7.46172 \\ 0.0314098u^{85} - 0.0261001u^{84} + \dots - 6.20145u - 6.59007 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.313635u^{85} - 0.494466u^{84} + \dots - 134.831u - 34.4302 \\ 0.0865603u^{85} + 0.0682676u^{84} + \dots + 24.6403u + 3.30443 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.428449u^{85} - 0.506093u^{84} + \dots - 128.967u - 23.4151 \\ -0.112532u^{85} - 0.102360u^{84} + \dots - 14.4207u - 1.77881 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.518000u^{85} - 0.878705u^{84} + \dots - 263.329u - 71.7071 \\ -0.388762u^{85} - 0.550043u^{84} + \dots - 149.561u - 34.9025 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-1.25246u^{85} - 1.96111u^{84} + \dots - 563.188u - 165.262$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_4$	$u^{86} - 10u^{85} + \dots + 18u + 1$
$c_3, c_6$	$u^{86} + 4u^{85} + \dots - 1152u^2 + 64$
$c_5, c_{10}$	$u^{86} + 2u^{85} + \dots + 352u + 64$
$c_7, c_9$	$u^{86} - 4u^{85} + \dots - 13134u + 977$
$c_8, c_{11}, c_{12}$	$u^{86} + 4u^{85} + \dots - 8u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$y^{86} - 82y^{85} + \dots - 478y + 1$
$c_3, c_6$	$y^{86} - 48y^{85} + \dots - 147456y + 4096$
$c_5, c_{10}$	$y^{86} - 42y^{85} + \dots - 107520y + 4096$
$c_7, c_9$	$y^{86} - 56y^{85} + \dots - 14579676y + 954529$
$c_8, c_{11}, c_{12}$	$y^{86} + 72y^{85} + \dots - 20y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.552054 + 0.828557I$		
$a = 0.192966 - 0.000278I$	$-13.69310 - 2.82580I$	0
$b = 1.55396 + 0.16056I$		
$u = 0.552054 - 0.828557I$		
$a = 0.192966 + 0.000278I$	$-13.69310 + 2.82580I$	0
$b = 1.55396 - 0.16056I$		
$u = 0.712992 + 0.675491I$		
$a = 0.581320 + 0.515681I$	$-6.37937 + 0.07950I$	0
$b = -0.631213 - 0.658080I$		
$u = 0.712992 - 0.675491I$		
$a = 0.581320 - 0.515681I$	$-6.37937 - 0.07950I$	0
$b = -0.631213 + 0.658080I$		
$u = 0.293714 + 0.923956I$		
$a = 0.598122 + 0.230114I$	$1.77443 - 1.89708I$	0
$b = -0.220725 - 0.596939I$		
$u = 0.293714 - 0.923956I$		
$a = 0.598122 - 0.230114I$	$1.77443 + 1.89708I$	0
$b = -0.220725 + 0.596939I$		
$u = -0.399332 + 0.964359I$		
$a = 0.562555 - 0.274132I$	$-2.56815 + 5.72788I$	0
$b = -0.274017 + 0.680285I$		
$u = -0.399332 - 0.964359I$		
$a = 0.562555 + 0.274132I$	$-2.56815 - 5.72788I$	0
$b = -0.274017 - 0.680285I$		
$u = -0.814919 + 0.658478I$		
$a = -0.82638 + 1.33174I$	$-8.14347 - 2.53737I$	0
$b = -1.383480 - 0.068743I$		
$u = -0.814919 - 0.658478I$		
$a = -0.82638 - 1.33174I$	$-8.14347 + 2.53737I$	0
$b = -1.383480 + 0.068743I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.983266 + 0.394126I$ $a = 0.04078 + 1.47966I$ $b = -0.260699 - 0.690733I$	$0.29357 - 3.54409I$	0
$u = -0.983266 - 0.394126I$ $a = 0.04078 - 1.47966I$ $b = -0.260699 + 0.690733I$	$0.29357 + 3.54409I$	0
$u = -0.225473 + 0.906689I$ $a = 0.191216 - 0.000872I$ $b = 1.48450 - 0.07065I$	$-8.06829 + 1.47587I$	$-6.04730 + 0.I$
$u = -0.225473 - 0.906689I$ $a = 0.191216 + 0.000872I$ $b = 1.48450 + 0.07065I$	$-8.06829 - 1.47587I$	$-6.04730 + 0.I$
$u = -1.049590 + 0.241828I$ $a = 0.357510 - 0.885888I$ $b = -1.048150 + 0.593109I$	$-0.89394 + 2.01684I$	0
$u = -1.049590 - 0.241828I$ $a = 0.357510 + 0.885888I$ $b = -1.048150 - 0.593109I$	$-0.89394 - 2.01684I$	0
$u = -0.130183 + 0.912720I$ $a = 0.615451 - 0.146529I$ $b = -0.106806 + 0.503836I$	$-1.74508 - 1.81197I$	0
$u = -0.130183 - 0.912720I$ $a = 0.615451 + 0.146529I$ $b = -0.106806 - 0.503836I$	$-1.74508 + 1.81197I$	0
$u = 0.909805 + 0.583851I$ $a = -0.30401 - 1.55635I$ $b = -0.426541 + 0.738548I$	$-5.77290 + 4.80475I$	0
$u = 0.909805 - 0.583851I$ $a = -0.30401 + 1.55635I$ $b = -0.426541 - 0.738548I$	$-5.77290 - 4.80475I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.048040 + 0.370428I$ $a = 0.390246 + 0.782737I$ $b = -0.981638 - 0.659900I$	$2.46498 + 1.91776I$	0
$u = 1.048040 - 0.370428I$ $a = 0.390246 - 0.782737I$ $b = -0.981638 + 0.659900I$	$2.46498 - 1.91776I$	0
$u = 0.771535 + 0.431699I$ $a = -0.47760 - 1.71983I$ $b = -1.262540 + 0.145425I$	$-2.36374 + 1.81286I$	$0. - 3.83527I$
$u = 0.771535 - 0.431699I$ $a = -0.47760 + 1.71983I$ $b = -1.262540 - 0.145425I$	$-2.36374 - 1.81286I$	$0. + 3.83527I$
$u = 0.852981 + 0.159244I$ $a = 0.58828 - 1.49094I$ $b = -0.159548 + 0.473962I$	$1.120900 + 0.300961I$	$6.91660 - 0.58498I$
$u = 0.852981 - 0.159244I$ $a = 0.58828 + 1.49094I$ $b = -0.159548 - 0.473962I$	$1.120900 - 0.300961I$	$6.91660 + 0.58498I$
$u = 1.059140 + 0.410939I$ $a = -0.287658 - 1.211040I$ $b = -1.376810 + 0.289151I$	$-1.68586 + 0.96431I$	0
$u = 1.059140 - 0.410939I$ $a = -0.287658 + 1.211040I$ $b = -1.376810 - 0.289151I$	$-1.68586 - 0.96431I$	0
$u = -1.060240 + 0.459416I$ $a = 0.391196 - 0.717519I$ $b = -0.943184 + 0.714225I$	$-1.95224 - 5.90463I$	0
$u = -1.060240 - 0.459416I$ $a = 0.391196 + 0.717519I$ $b = -0.943184 - 0.714225I$	$-1.95224 + 5.90463I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.438702 + 0.719830I$ $a = -1.86531 - 1.41789I$ $b = -1.244600 - 0.118813I$	$-5.13889 - 4.02609I$	$-2.76635 + 0.76522I$
$u = 0.438702 - 0.719830I$ $a = -1.86531 + 1.41789I$ $b = -1.244600 + 0.118813I$	$-5.13889 + 4.02609I$	$-2.76635 - 0.76522I$
$u = -1.081380 + 0.516007I$ $a = -0.405516 + 1.145080I$ $b = -1.43564 - 0.25261I$	$1.40001 - 4.97319I$	0
$u = -1.081380 - 0.516007I$ $a = -0.405516 - 1.145080I$ $b = -1.43564 + 0.25261I$	$1.40001 + 4.97319I$	0
$u = -1.136010 + 0.403070I$ $a = -1.18436 - 1.39457I$ $b = 1.41697 + 0.15814I$	$-9.55306 + 0.49039I$	0
$u = -1.136010 - 0.403070I$ $a = -1.18436 + 1.39457I$ $b = 1.41697 - 0.15814I$	$-9.55306 - 0.49039I$	0
$u = -0.562219 + 0.524976I$ $a = 0.716658 - 0.329576I$ $b = 0.182504 + 0.015855I$	$-3.19093 - 1.95911I$	$3.32674 + 3.69322I$
$u = -0.562219 - 0.524976I$ $a = 0.716658 + 0.329576I$ $b = 0.182504 - 0.015855I$	$-3.19093 + 1.95911I$	$3.32674 - 3.69322I$
$u = 1.092220 + 0.579762I$ $a = -0.466720 - 1.099830I$ $b = -1.46979 + 0.22913I$	$-3.18556 + 9.02341I$	0
$u = 1.092220 - 0.579762I$ $a = -0.466720 + 1.099830I$ $b = -1.46979 - 0.22913I$	$-3.18556 - 9.02341I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.187690 + 0.506855I$ $a = -0.111325 + 1.217970I$ $b = -0.237680 - 0.887129I$	$1.53780 - 3.15145I$	0
$u = -1.187690 - 0.506855I$ $a = -0.111325 - 1.217970I$ $b = -0.237680 + 0.887129I$	$1.53780 + 3.15145I$	0
$u = 1.291170 + 0.123828I$ $a = 0.278328 + 0.884185I$ $b = 0.269267 - 0.656632I$	$3.52569 - 2.53556I$	0
$u = 1.291170 - 0.123828I$ $a = 0.278328 - 0.884185I$ $b = 0.269267 + 0.656632I$	$3.52569 + 2.53556I$	0
$u = -0.657648 + 0.222079I$ $a = 0.190415 + 0.000646I$ $b = 1.68329 - 0.04881I$	$-11.53680 - 3.32788I$	$1.60100 + 7.68257I$
$u = -0.657648 - 0.222079I$ $a = 0.190415 - 0.000646I$ $b = 1.68329 + 0.04881I$	$-11.53680 + 3.32788I$	$1.60100 - 7.68257I$
$u = 1.127830 + 0.663427I$ $a = -0.35766 + 1.65601I$ $b = 1.47079 - 0.27396I$	$-11.8702 + 8.4794I$	0
$u = 1.127830 - 0.663427I$ $a = -0.35766 - 1.65601I$ $b = 1.47079 + 0.27396I$	$-11.8702 - 8.4794I$	0
$u = -1.294930 + 0.226061I$ $a = 0.289669 - 0.819710I$ $b = 0.347991 + 0.605697I$	$7.12157 - 1.76447I$	0
$u = -1.294930 - 0.226061I$ $a = 0.289669 + 0.819710I$ $b = 0.347991 - 0.605697I$	$7.12157 + 1.76447I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.231000 + 0.473921I$ $a = -0.82743 + 1.23132I$ $b = 1.381250 - 0.202296I$	$-3.88741 + 2.87017I$	0
$u = 1.231000 - 0.473921I$ $a = -0.82743 - 1.23132I$ $b = 1.381250 + 0.202296I$	$-3.88741 - 2.87017I$	0
$u = -0.432450 + 1.250560I$ $a = 0.193237 - 0.006450I$ $b = 1.367100 - 0.183599I$	$-6.49234 + 0.65249I$	0
$u = -0.432450 - 1.250560I$ $a = 0.193237 + 0.006450I$ $b = 1.367100 + 0.183599I$	$-6.49234 - 0.65249I$	0
$u = -0.353875 + 0.574365I$ $a = -2.39311 + 2.12630I$ $b = -1.150500 + 0.085662I$	$-0.680663 + 0.581964I$	$4.76633 + 3.68087I$
$u = -0.353875 - 0.574365I$ $a = -2.39311 - 2.12630I$ $b = -1.150500 - 0.085662I$	$-0.680663 - 0.581964I$	$4.76633 - 3.68087I$
$u = 1.189690 + 0.590585I$ $a = -0.192525 - 1.202200I$ $b = -0.293585 + 0.928049I$	$4.52893 + 7.39783I$	0
$u = 1.189690 - 0.590585I$ $a = -0.192525 + 1.202200I$ $b = -0.293585 - 0.928049I$	$4.52893 - 7.39783I$	0
$u = 1.294060 + 0.316520I$ $a = 0.291115 + 0.764351I$ $b = 0.414957 - 0.554533I$	$2.91745 + 6.05254I$	0
$u = 1.294060 - 0.316520I$ $a = 0.291115 - 0.764351I$ $b = 0.414957 + 0.554533I$	$2.91745 - 6.05254I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.537174 + 1.231980I$ $a = 0.196295 + 0.005454I$ $b = 1.389820 + 0.235157I$	$-3.37770 - 4.95391I$	0
$u = 0.537174 - 1.231980I$ $a = 0.196295 - 0.005454I$ $b = 1.389820 - 0.235157I$	$-3.37770 + 4.95391I$	0
$u = -1.181470 + 0.644258I$ $a = -0.244491 + 1.194170I$ $b = -0.333360 - 0.947743I$	$-0.12892 - 11.58520I$	0
$u = -1.181470 - 0.644258I$ $a = -0.244491 - 1.194170I$ $b = -0.333360 + 0.947743I$	$-0.12892 + 11.58520I$	0
$u = -0.602863 + 1.211500I$ $a = 0.197803 - 0.003918I$ $b = 1.41379 - 0.26593I$	$-7.97081 + 9.17889I$	0
$u = -0.602863 - 1.211500I$ $a = 0.197803 + 0.003918I$ $b = 1.41379 + 0.26593I$	$-7.97081 - 9.17889I$	0
$u = -1.232100 + 0.594842I$ $a = -0.51016 - 1.34439I$ $b = 1.40089 + 0.26628I$	$-4.99770 - 7.01531I$	0
$u = -1.232100 - 0.594842I$ $a = -0.51016 + 1.34439I$ $b = 1.40089 - 0.26628I$	$-4.99770 + 7.01531I$	0
$u = -0.560073 + 0.243224I$ $a = 1.11682 + 2.93594I$ $b = -0.400437 - 0.305942I$	$-3.84146 + 2.44487I$	$2.67833 + 5.70811I$
$u = -0.560073 - 0.243224I$ $a = 1.11682 - 2.93594I$ $b = -0.400437 + 0.305942I$	$-3.84146 - 2.44487I$	$2.67833 - 5.70811I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.447171 + 0.368366I$ $a = 0.977140 - 0.529183I$ $b = -0.649137 + 0.321962I$	$-1.244520 + 0.136004I$	$-5.67462 + 0.66860I$
$u = -0.447171 - 0.368366I$ $a = 0.977140 + 0.529183I$ $b = -0.649137 - 0.321962I$	$-1.244520 - 0.136004I$	$-5.67462 - 0.66860I$
$u = 0.559835$ $a = 0.190472$ $b = 1.67112$	$-7.43832$	$13.1970$
$u = -1.26876 + 0.73301I$ $a = -0.171599 - 1.310850I$ $b = 1.42110 + 0.35592I$	$-3.74537 - 7.60591I$	$0$
$u = -1.26876 - 0.73301I$ $a = -0.171599 + 1.310850I$ $b = 1.42110 - 0.35592I$	$-3.74537 + 7.60591I$	$0$
$u = -1.22662 + 0.81031I$ $a = -0.010802 - 1.395770I$ $b = 1.47568 + 0.37982I$	$-5.9049 - 16.3706I$	$0$
$u = -1.22662 - 0.81031I$ $a = -0.010802 + 1.395770I$ $b = 1.47568 - 0.37982I$	$-5.9049 + 16.3706I$	$0$
$u = 1.24904 + 0.78295I$ $a = -0.069120 + 1.354280I$ $b = 1.45236 - 0.37556I$	$-1.03547 + 12.08560I$	$0$
$u = 1.24904 - 0.78295I$ $a = -0.069120 - 1.354280I$ $b = 1.45236 + 0.37556I$	$-1.03547 - 12.08560I$	$0$
$u = 0.099100 + 0.510038I$ $a = -5.06181 - 1.25504I$ $b = -1.001060 - 0.128912I$	$-4.35085 + 2.48127I$	$-12.9227 - 14.9608I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.099100 - 0.510038I$ $a = -5.06181 + 1.25504I$ $b = -1.001060 + 0.128912I$	$-4.35085 - 2.48127I$	$-12.9227 + 14.9608I$
$u = 0.446361$ $a = 1.34862$ $b = -0.0485703$	0.791292	12.9620
$u = -0.390544$ $a = 2.53371$ $b = -0.859860$	-1.16619	-12.5130
$u = 1.68218 + 0.12717I$ $a = -0.651799 + 0.146716I$ $b = 1.190290 - 0.040584I$	$1.47173 + 4.79342I$	0
$u = 1.68218 - 0.12717I$ $a = -0.651799 - 0.146716I$ $b = 1.190290 + 0.040584I$	$1.47173 - 4.79342I$	0
$u = -1.70399$ $a = -0.648277$ $b = 1.18657$	5.42800	0

$$\text{II. } \Gamma_2^u = \langle b + 1, u^5 - 4u^3 + u^2 + a + 4u - 3, u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^5 + 4u^3 - u^2 - 4u + 3 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^5 + 4u^3 - u^2 - 4u + 2 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^5 + 4u^3 - u^2 - 4u + 3 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^5 + 2u^3 + u \\ u^5 - 3u^3 + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-7u^5 - 3u^4 + 27u^3 + 5u^2 - 24u + 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^6$
$c_3, c_6$	$u^6$
$c_4$	$(u + 1)^6$
$c_5, c_7, c_9$	$u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1$
$c_8$	$u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1$
$c_{10}$	$u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1$
$c_{11}, c_{12}$	$u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^6$
$c_3, c_6$	$y^6$
$c_5, c_7, c_9$ $c_{10}$	$y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1$
$c_8, c_{11}, c_{12}$	$y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.493180 + 0.575288I$ $a = -0.26610 - 1.72116I$ $b = -1.00000$	$-4.60518 + 1.97241I$	$-6.63014 - 2.86834I$
$u = 0.493180 - 0.575288I$ $a = -0.26610 + 1.72116I$ $b = -1.00000$	$-4.60518 - 1.97241I$	$-6.63014 + 2.86834I$
$u = -0.483672$ $a = 4.27462$ $b = -1.00000$	$-0.906083$	23.7440
$u = -1.52087 + 0.16310I$ $a = 0.417699 + 0.090629I$ $b = -1.00000$	$2.05064 - 4.59213I$	$5.72906 + 1.01197I$
$u = -1.52087 - 0.16310I$ $a = 0.417699 - 0.090629I$ $b = -1.00000$	$2.05064 + 4.59213I$	$5.72906 - 1.01197I$
$u = 1.53904$ $a = 0.422181$ $b = -1.00000$	6.01515	10.0580

### III.

$$I_1^v = \langle a, 8v^5 + 21v^4 + 63v^3 + 21v^2 + 503b - v - 817, v^6 + 3v^5 + v^4 - 18v^3 - 7v^2 + 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -0.0159046v^5 - 0.0417495v^4 + \dots + 0.00198807v + 1.62425 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -0.0159046v^5 - 0.0417495v^4 + \dots + 0.00198807v + 2.62425 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.127237v^5 - 0.333996v^4 + \dots + 0.0159046v + 0.994036 \\ -0.0159046v^5 - 0.0417495v^4 + \dots + 0.00198807v + 2.62425 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0159046v^5 - 0.0417495v^4 + \dots + 0.00198807v + 1.62425 \\ -0.0159046v^5 - 0.0417495v^4 + \dots + 0.00198807v + 1.62425 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0159046v^5 + 0.0417495v^4 + \dots - 0.00198807v - 1.62425 \\ 0.0159046v^5 + 0.0417495v^4 + \dots - 0.00198807v - 2.62425 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0.0159046v^5 + 0.0417495v^4 + \dots - 0.00198807v - 2.62425 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.00596421v^5 - 0.109344v^4 + \dots + 3.62425v + 0.0159046 \\ 0.0178926v^5 - 0.328032v^4 + \dots + 6.87276v + 0.0477137 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.524851v^5 - 1.37773v^4 + \dots + 1.06561v - 1.39960 \\ -1.00199v^5 - 2.63022v^4 + \dots + 0.125249v - 2.67197 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =**  $\frac{12}{503}v^5 + \frac{283}{503}v^4 + \frac{849}{503}v^3 - \frac{220}{503}v^2 - \frac{3774}{503}v - \frac{4495}{503}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$	$(u^2 + u - 1)^3$
$c_4, c_6$	$(u^2 - u - 1)^3$
$c_5, c_{10}$	$u^6$
$c_7, c_9$	$(u^3 - u^2 + 1)^2$
$c_8$	$(u^3 + u^2 + 2u + 1)^2$
$c_{11}, c_{12}$	$(u^3 - u^2 + 2u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_6$	$(y^2 - 3y + 1)^3$
$c_5, c_{10}$	$y^6$
$c_7, c_9$	$(y^3 - y^2 + 2y - 1)^2$
$c_8, c_{11}, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.335152 + 0.284512I$ $a = 0$ $b = 1.61803$	$-11.90680 - 2.82812I$	$-6.38118 - 1.93520I$
$v = -0.335152 - 0.284512I$ $a = 0$ $b = 1.61803$	$-11.90680 + 2.82812I$	$-6.38118 + 1.93520I$
$v = 0.288338$ $a = 0$ $b = 1.61803$	$-7.76919$	$-11.0920$
$v = 1.97630$ $a = 0$ $b = -0.618034$	$0.126494$	$-3.14230$
$v = -2.29716 + 1.95007I$ $a = 0$ $b = -0.618034$	$-4.01109 - 2.82812I$	$-7.00182 + 11.83005I$
$v = -2.29716 - 1.95007I$ $a = 0$ $b = -0.618034$	$-4.01109 + 2.82812I$	$-7.00182 - 11.83005I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$((u-1)^6)(u^2+u-1)^3(u^{86}-10u^{85}+\dots+18u+1)$
$c_3$	$u^6(u^2+u-1)^3(u^{86}+4u^{85}+\dots-1152u^2+64)$
$c_4$	$((u+1)^6)(u^2-u-1)^3(u^{86}-10u^{85}+\dots+18u+1)$
$c_5$	$u^6(u^6+u^5+\dots-u-1)(u^{86}+2u^{85}+\dots+352u+64)$
$c_6$	$u^6(u^2-u-1)^3(u^{86}+4u^{85}+\dots-1152u^2+64)$
$c_7, c_9$	$(u^3-u^2+1)^2(u^6+u^5-3u^4-2u^3+2u^2-u-1)$ $\cdot (u^{86}-4u^{85}+\dots-13134u+977)$
$c_8$	$(u^3+u^2+2u+1)^2(u^6-u^5+3u^4-2u^3+2u^2-u-1)$ $\cdot (u^{86}+4u^{85}+\dots-8u+1)$
$c_{10}$	$u^6(u^6-u^5+\dots+u-1)(u^{86}+2u^{85}+\dots+352u+64)$
$c_{11}, c_{12}$	$(u^3-u^2+2u-1)^2(u^6+u^5+3u^4+2u^3+2u^2+u-1)$ $\cdot (u^{86}+4u^{85}+\dots-8u+1)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$((y-1)^6)(y^2-3y+1)^3(y^{86}-82y^{85}+\dots-478y+1)$
$c_3, c_6$	$y^6(y^2-3y+1)^3(y^{86}-48y^{85}+\dots-147456y+4096)$
$c_5, c_{10}$	$y^6(y^6-7y^5+17y^4-16y^3+6y^2-5y+1) \cdot (y^{86}-42y^{85}+\dots-107520y+4096)$
$c_7, c_9$	$(y^3-y^2+2y-1)^2(y^6-7y^5+17y^4-16y^3+6y^2-5y+1) \cdot (y^{86}-56y^{85}+\dots-14579676y+954529)$
$c_8, c_{11}, c_{12}$	$(y^3+3y^2+2y-1)^2(y^6+5y^5+9y^4+4y^3-6y^2-5y+1) \cdot (y^{86}+72y^{85}+\dots-20y+1)$