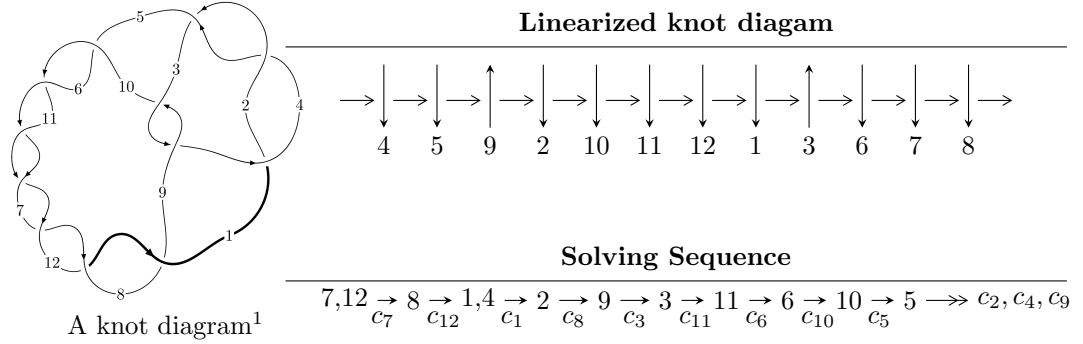


12a₀₈₃₈ (K12a₀₈₃₈)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{22} - 17u^{20} + \dots + b + 1, u^{22} + u^{21} + \dots + a + 2, u^{23} + 2u^{22} + \dots - 12u^2 + 1 \rangle$$

$$I_2^u = \langle -u^2 + b + 1, -u^2 + a + 2, u^3 - u^2 - 2u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 26 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{22} - 17u^{20} + \dots + b + 1, u^{22} + u^{21} + \dots + a + 2, u^{23} + 2u^{22} + \dots - 12u^2 + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{22} - u^{21} + \dots + 11u - 2 \\ -u^{22} + 17u^{20} + \dots + 2u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{21} - 16u^{19} + \dots - 11u + 2 \\ -u^{22} + 16u^{20} + \dots + 9u^2 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{22} - u^{21} + \dots + 10u - 1 \\ 3u^{22} - 48u^{20} + \dots + u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^4 - 3u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= 5u^{22} + 8u^{21} - 81u^{20} - 126u^{19} + 556u^{18} + 835u^{17} - 2107u^{16} - \\ &3020u^{15} + 4822u^{14} + 6443u^{13} - 6906u^{12} - 8110u^{11} + 6388u^{10} + 5547u^9 - 4175u^8 - \\ &1464u^7 + 2179u^6 - 280u^5 - 757u^4 + 196u^3 + 80u^2 - 23u - 5 \end{aligned}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------------------------------------------|----------------------------------------|
| c_1, c_2, c_4 | $u^{23} - 4u^{22} + \dots + 5u - 1$ |
| c_3, c_9 | $u^{23} - u^{22} + \dots - 28u - 8$ |
| c_5, c_6, c_7 c_8, c_{10}, c_{11} c_{12} | $u^{23} - 2u^{22} + \dots + 12u^2 - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|------------------------------------------------------|------------------------------------------|
| c_1, c_2, c_4 | $y^{23} - 26y^{22} + \cdots + 57y - 1$ |
| c_3, c_9 | $y^{23} + 21y^{22} + \cdots + 592y - 64$ |
| c_5, c_6, c_7 c_8, c_{10}, c_{11} c_{12} | $y^{23} - 36y^{22} + \cdots + 24y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------------------------------------------------------------------------------------------|---------------------------------------|----------------------|
| $u = -0.899656 + 0.367597I$ $a = -0.129750 - 0.316248I$ $b = 1.37701 + 0.64432I$ | $-10.62640 + 4.79693I$ | $-18.4963 - 4.5941I$ |
| $u = -0.899656 - 0.367597I$ $a = -0.129750 + 0.316248I$ $b = 1.37701 - 0.64432I$ | $-10.62640 - 4.79693I$ | $-18.4963 + 4.5941I$ |
| $u = 0.869158$ $a = -0.611937$ $b = 1.66429$ | -5.48753 | -17.2890 |
| $u = -0.821958 + 0.135064I$ $a = -0.253247 + 1.039930I$ $b = -0.445233 + 0.309895I$ | $-3.58507 + 2.11349I$ | $-17.2477 - 5.0037I$ |
| $u = -0.821958 - 0.135064I$ $a = -0.253247 - 1.039930I$ $b = -0.445233 - 0.309895I$ | $-3.58507 - 2.11349I$ | $-17.2477 + 5.0037I$ |
| $u = -1.29295$ $a = -0.815349$ $b = -0.215176$ | -6.99093 | -10.8460 |
| $u = 0.292199 + 0.547469I$ $a = -0.70419 + 1.55774I$ $b = -0.871306 + 0.010708I$ | $-6.92984 - 1.76193I$ | $-14.7690 + 3.3456I$ |
| $u = 0.292199 - 0.547469I$ $a = -0.70419 - 1.55774I$ $b = -0.871306 - 0.010708I$ | $-6.92984 + 1.76193I$ | $-14.7690 - 3.3456I$ |
| $u = 1.43893 + 0.05540I$ $a = -0.573918 + 0.627821I$ $b = -0.269240 + 1.142030I$ | $-11.26780 - 2.80601I$ | $-17.5990 + 3.0357I$ |
| $u = 1.43893 - 0.05540I$ $a = -0.573918 - 0.627821I$ $b = -0.269240 - 1.142030I$ | $-11.26780 + 2.80601I$ | $-17.5990 - 3.0357I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------------------------------------------------------------------------|---------------------------------------|-----------------------|
| $u = -1.45875$ $a = 2.49389$ $b = 1.79311$ | -13.4340 | -18.2600 |
| $u = 0.523970$ $a = 0.174078$ $b = -0.424666$ | -0.880680 | -10.8440 |
| $u = 1.46882 + 0.17141I$ $a = 1.75548 - 0.96316I$ $b = 1.371010 - 0.251551I$ | $-18.5944 - 6.8465I$ | $-19.2959 + 3.6692I$ |
| $u = 1.46882 - 0.17141I$ $a = 1.75548 + 0.96316I$ $b = 1.371010 + 0.251551I$ | $-18.5944 + 6.8465I$ | $-19.2959 - 3.6692I$ |
| $u = 0.198961 + 0.259775I$ $a = 1.162630 + 0.050871I$ $b = 0.098000 - 0.372398I$ | $-0.444837 - 0.821194I$ | $-9.62649 + 8.14856I$ |
| $u = 0.198961 - 0.259775I$ $a = 1.162630 - 0.050871I$ $b = 0.098000 + 0.372398I$ | $-0.444837 + 0.821194I$ | $-9.62649 - 8.14856I$ |
| $u = -0.236506$ $a = -3.87954$ $b = -0.871608$ | -1.99765 | 0.552820 |
| $u = 1.81292$ $a = 1.34454$ $b = 2.75785$ | -18.5335 | -9.99140 |
| $u = -1.85429 + 0.01361I$ $a = 1.048680 + 0.206116I$ $b = 2.22063 + 0.96437I$ | $15.7173 + 3.1639I$ | $-17.6160 - 2.4156I$ |
| $u = -1.85429 - 0.01361I$ $a = 1.048680 - 0.206116I$ $b = 2.22063 - 0.96437I$ | $15.7173 - 3.1639I$ | $-17.6160 + 2.4156I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------------------------------------------------------------------------------------|---------------------------------------|----------------------|
| $u = 1.85896$ $a = -3.64519$ $b = -8.09850$ | 13.4167 | -18.4390 |
| $u = -1.86140 + 0.04356I$ $a = -2.83593 - 1.10657I$ $b = -6.28352 - 2.42136I$ | $8.27161 + 7.98934I$ | $-19.2912 - 3.1659I$ |
| $u = -1.86140 - 0.04356I$ $a = -2.83593 + 1.10657I$ $b = -6.28352 + 2.42136I$ | $8.27161 - 7.98934I$ | $-19.2912 + 3.1659I$ |

$$\text{II. } I_2^u = \langle -u^2 + b + 1, -u^2 + a + 2, u^3 - u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^2 - u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 - 2 \\ u^2 - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 - u - 2 \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^2 - u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 - 2 \\ u^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^2 - u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $u^2 - u - 23$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|--------------------------------|
| c_1, c_2 | $(u - 1)^3$ |
| c_3, c_9 | u^3 |
| c_4 | $(u + 1)^3$ |
| c_5, c_6, c_7 c_8 | $u^3 - u^2 - 2u + 1$ |
| c_{10}, c_{11}, c_{12} | $u^3 + u^2 - 2u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|------------------------------------------------------|------------------------------------|
| c_1, c_2, c_4 | $(y - 1)^3$ |
| c_3, c_9 | y^3 |
| c_5, c_6, c_7 c_8, c_{10}, c_{11} c_{12} | $y^3 - 5y^2 + 6y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------------------------------|---------------------------------------|------------|
| $u = -1.24698$ $a = -0.445042$ $b = 0.554958$ | -7.98968 | -20.1980 |
| $u = 0.445042$ $a = -1.80194$ $b = -0.801938$ | -2.34991 | -23.2470 |
| $u = 1.80194$ $a = 1.24698$ $b = 2.24698$ | -19.2692 | -21.5550 |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|--------------------------|--------------------------------------------------------------|
| c_1, c_2 | $((u-1)^3)(u^{23} - 4u^{22} + \dots + 5u - 1)$ |
| c_3, c_9 | $u^3(u^{23} - u^{22} + \dots - 28u - 8)$ |
| c_4 | $((u+1)^3)(u^{23} - 4u^{22} + \dots + 5u - 1)$ |
| c_5, c_6, c_7 c_8 | $(u^3 - u^2 - 2u + 1)(u^{23} - 2u^{22} + \dots + 12u^2 - 1)$ |
| c_{10}, c_{11}, c_{12} | $(u^3 + u^2 - 2u - 1)(u^{23} - 2u^{22} + \dots + 12u^2 - 1)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|------------------------------------------------------|--------------------------------------------------------------|
| c_1, c_2, c_4 | $((y - 1)^3)(y^{23} - 26y^{22} + \dots + 57y - 1)$ |
| c_3, c_9 | $y^3(y^{23} + 21y^{22} + \dots + 592y - 64)$ |
| c_5, c_6, c_7 c_8, c_{10}, c_{11} c_{12} | $(y^3 - 5y^2 + 6y - 1)(y^{23} - 36y^{22} + \dots + 24y - 1)$ |