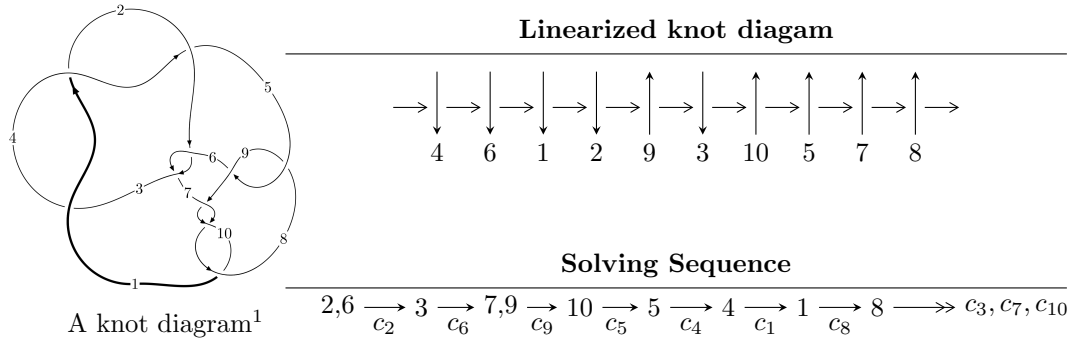


10₇₉ (K10a₇₈)



A knot diagram¹

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 1.48752 \times 10^{31} u^{33} - 1.92107 \times 10^{31} u^{32} + \dots + 2.67160 \times 10^{30} b - 8.42537 \times 10^{31}, \\ 2.31853 \times 10^{30} u^{33} - 3.45308 \times 10^{30} u^{32} + \dots + 7.63313 \times 10^{29} a - 1.53986 \times 10^{31}, u^{34} - 2u^{33} + \dots - 4u + 4 \rangle$$

$$I_2^u = \langle b - u - 1, a, u^2 + u - 1 \rangle$$

$$I_1^v = \langle a, b - v + 2, v^2 - 3v + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 38 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.49 \times 10^{31} u^{33} - 1.92 \times 10^{31} u^{32} + \dots + 2.67 \times 10^{30} b - 8.43 \times 10^{31}, 2.32 \times 10^{30} u^{33} - 3.45 \times 10^{30} u^{32} + \dots + 7.63 \times 10^{29} a - 1.54 \times 10^{31}, u^{34} - 2u^{33} + \dots - 4u + 4 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -3.03746u^{33} + 4.52380u^{32} + \dots + 15.5234u + 20.1734 \\ -5.56789u^{33} + 7.19074u^{32} + \dots + 16.8842u + 31.5368 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -6.74042u^{33} + 9.34081u^{32} + \dots + 25.8322u + 41.5551 \\ -3.71677u^{33} + 4.73023u^{32} + \dots + 11.0317u + 20.5108 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -8.87471u^{33} + 12.3007u^{32} + \dots + 32.0519u + 57.5877 \\ -5.70723u^{33} + 7.43204u^{32} + \dots + 16.7561u + 33.4853 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -14.5819u^{33} + 19.7327u^{32} + \dots + 48.8081u + 91.0730 \\ -5.70723u^{33} + 7.43204u^{32} + \dots + 16.7561u + 33.4853 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -14.5819u^{33} + 19.7327u^{32} + \dots + 48.8081u + 91.0730 \\ -0.387583u^{33} + 0.811626u^{32} + \dots + 3.84702u + 4.23934 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 15.6894u^{33} - 20.9276u^{32} + \dots - 48.8834u - 95.7780 \\ 1.33189u^{33} - 1.83094u^{32} + \dots - 2.59403u - 8.86592 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $3.23572u^{33} - 4.86218u^{32} + \dots - 45.6005u - 20.0908$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|--------------------------------------|
| c_1, c_3, c_4 | $u^{34} - 4u^{33} + \dots + 10u + 1$ |
| c_2, c_6 | $u^{34} + 2u^{33} + \dots + 4u + 4$ |
| c_5, c_8 | $u^{34} - 2u^{33} + \dots - 4u + 4$ |
| c_7, c_9, c_{10} | $u^{34} + 4u^{33} + \dots - 10u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------------------------------|---|
| c_1, c_3, c_4 c_7, c_9, c_{10} | $y^{34} - 32y^{33} + \dots - 42y + 1$ |
| c_2, c_5, c_6 c_8 | $y^{34} - 18y^{33} + \dots - 296y + 16$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.334121 + 0.939075I$ $a = 0.665187 + 1.185390I$ $b = 0.168561 - 1.149830I$ | $8.19540 - 1.89242I$ | $7.34522 + 1.79557I$ |
| $u = -0.334121 - 0.939075I$ $a = 0.665187 - 1.185390I$ $b = 0.168561 + 1.149830I$ | $8.19540 + 1.89242I$ | $7.34522 - 1.79557I$ |
| $u = 0.286460 + 0.973864I$ $a = 0.697313 - 0.627321I$ $b = -0.30439 + 1.55545I$ | $-2.64192 + 2.05432I$ | $-2.87162 - 3.29014I$ |
| $u = 0.286460 - 0.973864I$ $a = 0.697313 + 0.627321I$ $b = -0.30439 - 1.55545I$ | $-2.64192 - 2.05432I$ | $-2.87162 + 3.29014I$ |
| $u = 0.810678 + 0.499386I$ $a = 0.792602 + 0.713045I$ $b = 0.050287 - 0.622907I$ | $2.64192 - 2.05432I$ | $2.87162 + 3.29014I$ |
| $u = 0.810678 - 0.499386I$ $a = 0.792602 - 0.713045I$ $b = 0.050287 + 0.622907I$ | $2.64192 + 2.05432I$ | $2.87162 - 3.29014I$ |
| $u = -0.995699 + 0.467507I$ $a = 0.638734 + 0.769428I$ $b = 0.60499 - 1.49342I$ | $4.00435I$ | $0. - 6.49701I$ |
| $u = -0.995699 - 0.467507I$ $a = 0.638734 - 0.769428I$ $b = 0.60499 + 1.49342I$ | $- 4.00435I$ | $0. + 6.49701I$ |
| $u = 1.088970 + 0.372927I$ $a = 0.911686 - 0.699013I$ $b = 1.62610 + 0.98618I$ | $-3.39729 - 2.12414I$ | $-2.18234 + 2.03948I$ |
| $u = 1.088970 - 0.372927I$ $a = 0.911686 + 0.699013I$ $b = 1.62610 - 0.98618I$ | $-3.39729 + 2.12414I$ | $-2.18234 - 2.03948I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.845756 + 0.036069I$ $a = -0.613787 + 0.538660I$ $b = 0.203218 - 0.673856I$ | $-1.359860 + 0.095322I$ | $-5.80027 + 0.42636I$ |
| $u = 0.845756 - 0.036069I$ $a = -0.613787 - 0.538660I$ $b = 0.203218 + 0.673856I$ | $-1.359860 - 0.095322I$ | $-5.80027 - 0.42636I$ |
| $u = -1.112820 + 0.516604I$ $a = -0.842410 + 0.743758I$ $b = -0.101206 + 0.252455I$ | $-2.34523 + 5.26340I$ | $-1.79194 - 3.97493I$ |
| $u = -1.112820 - 0.516604I$ $a = -0.842410 - 0.743758I$ $b = -0.101206 - 0.252455I$ | $-2.34523 - 5.26340I$ | $-1.79194 + 3.97493I$ |
| $u = -0.304859 + 0.635319I$ $a = -0.625675 + 0.780084I$ $b = 0.24828 - 2.17048I$ | $-0.739532I$ | $0. - 4.35806I$ |
| $u = -0.304859 - 0.635319I$ $a = -0.625675 - 0.780084I$ $b = 0.24828 + 2.17048I$ | $0.739532I$ | $0. + 4.35806I$ |
| $u = -0.538543 + 0.433436I$ $a = -0.920373 - 0.807720I$ $b = -0.674327 + 1.021010I$ | $1.359860 - 0.095322I$ | $5.80027 - 0.42636I$ |
| $u = -0.538543 - 0.433436I$ $a = -0.920373 + 0.807720I$ $b = -0.674327 - 1.021010I$ | $1.359860 + 0.095322I$ | $5.80027 + 0.42636I$ |
| $u = 1.253480 + 0.421212I$ $a = 0.690781 - 0.529640I$ $b = -0.104017 + 0.977410I$ | $3.39729 - 2.12414I$ | $2.18234 + 2.03948I$ |
| $u = 1.253480 - 0.421212I$ $a = 0.690781 + 0.529640I$ $b = -0.104017 - 0.977410I$ | $3.39729 + 2.12414I$ | $2.18234 - 2.03948I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.650050$ $a = -2.72250$ $b = -1.02677$ | 6.73970 | -7.32000 |
| $u = -1.335420 + 0.228599I$ $a = 0.360026 - 0.641577I$ $b = 0.062959 - 0.180613I$ | $-8.19540 + 1.89242I$ | $-7.34522 - 1.79557I$ |
| $u = -1.335420 - 0.228599I$ $a = 0.360026 + 0.641577I$ $b = 0.062959 + 0.180613I$ | $-8.19540 - 1.89242I$ | $-7.34522 + 1.79557I$ |
| $u = 1.215470 + 0.599118I$ $a = -0.588471 + 0.824257I$ $b = -1.38976 - 1.48159I$ | $-5.53452 - 7.73594I$ | $-3.53535 + 5.97450I$ |
| $u = 1.215470 - 0.599118I$ $a = -0.588471 - 0.824257I$ $b = -1.38976 + 1.48159I$ | $-5.53452 + 7.73594I$ | $-3.53535 - 5.97450I$ |
| $u = -1.209090 + 0.649293I$ $a = -0.573728 - 0.803607I$ $b = -0.46886 + 1.54639I$ | $5.53452 + 7.73594I$ | $3.53535 - 5.97450I$ |
| $u = -1.209090 - 0.649293I$ $a = -0.573728 + 0.803607I$ $b = -0.46886 - 1.54639I$ | $5.53452 - 7.73594I$ | $3.53535 + 5.97450I$ |
| $u = 0.553222 + 1.262860I$ $a = -0.667081 + 0.588961I$ $b = 0.13797 - 1.43868I$ | $2.34523 + 5.26340I$ | $1.79194 - 3.97493I$ |
| $u = 0.553222 - 1.262860I$ $a = -0.667081 - 0.588961I$ $b = 0.13797 + 1.43868I$ | $2.34523 - 5.26340I$ | $1.79194 + 3.97493I$ |
| $u = 0.522880$ $a = -0.711056$ $b = 0.786385$ | -1.14323 | -10.3340 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------|
| $u = 1.26084 + 0.79719I$ $a = 0.428806 - 0.903397I$ $b = 1.11261 + 1.64372I$ | $-12.5403I$ | $0. + 7.07308I$ |
| $u = 1.26084 - 0.79719I$ $a = 0.428806 + 0.903397I$ $b = 1.11261 - 1.64372I$ | $12.5403I$ | $0. - 7.07308I$ |
| $u = -0.371797$ $a = -1.40636$ $b = -0.980790$ | 1.14323 | 10.3340 |
| $u = -1.76976$ $a = -0.367310$ $b = -0.123664$ | -6.73970 | 0 |

$$\text{II. } I_2^u = \langle b - u - 1, a, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ 2u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -9

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------|--------------------------------|
| c_1, c_2 | $u^2 + u - 1$ |
| c_3, c_4, c_6 | $u^2 - u - 1$ |
| c_5, c_8 | u^2 |
| c_7 | $(u + 1)^2$ |
| c_9, c_{10} | $(u - 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-------------------------------|------------------------------------|
| c_1, c_2, c_3 c_4, c_6 | $y^2 - 3y + 1$ |
| c_5, c_8 | y^2 |
| c_7, c_9, c_{10} | $(y - 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 0.618034$ $a = 0$ $b = 1.61803$ | 0.657974 | -9.00000 |
| $u = -1.61803$ $a = 0$ $b = -0.618034$ | -7.23771 | -9.00000 |

$$\text{III. } I_1^v = \langle a, b - v + 2, v^2 - 3v + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ v - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2v - 1 \\ v - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} v \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v + 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -v \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2v + 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 9

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|--------------------------------|
| c_1 | $(u - 1)^2$ |
| c_2, c_6 | u^2 |
| c_3, c_4 | $(u + 1)^2$ |
| c_5, c_7 | $u^2 - u - 1$ |
| c_8, c_9, c_{10} | $u^2 + u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|----------------------------------|------------------------------------|
| c_1, c_3, c_4 | $(y - 1)^2$ |
| c_2, c_6 | y^2 |
| c_5, c_7, c_8 c_9, c_{10} | $y^2 - 3y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $v = 0.381966$ $a = 0$ $b = -1.61803$ | -0.657974 | 9.00000 |
| $v = 2.61803$ $a = 0$ $b = 0.618034$ | 7.23771 | 9.00000 |

IV. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $((u-1)^2)(u^2+u-1)(u^{34}-4u^{33}+\dots+10u+1)$ |
| c_2 | $u^2(u^2+u-1)(u^{34}+2u^{33}+\dots+4u+4)$ |
| c_3, c_4 | $((u+1)^2)(u^2-u-1)(u^{34}-4u^{33}+\dots+10u+1)$ |
| c_5 | $u^2(u^2-u-1)(u^{34}-2u^{33}+\dots-4u+4)$ |
| c_6 | $u^2(u^2-u-1)(u^{34}+2u^{33}+\dots+4u+4)$ |
| c_7 | $((u+1)^2)(u^2-u-1)(u^{34}+4u^{33}+\dots-10u+1)$ |
| c_8 | $u^2(u^2+u-1)(u^{34}-2u^{33}+\dots-4u+4)$ |
| c_9, c_{10} | $((u-1)^2)(u^2+u-1)(u^{34}+4u^{33}+\dots-10u+1)$ |

V. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|---------------------------------------|--|
| c_1, c_3, c_4 c_7, c_9, c_{10} | $((y - 1)^2)(y^2 - 3y + 1)(y^{34} - 32y^{33} + \dots - 42y + 1)$ |
| c_2, c_5, c_6 c_8 | $y^2(y^2 - 3y + 1)(y^{34} - 18y^{33} + \dots - 296y + 16)$ |