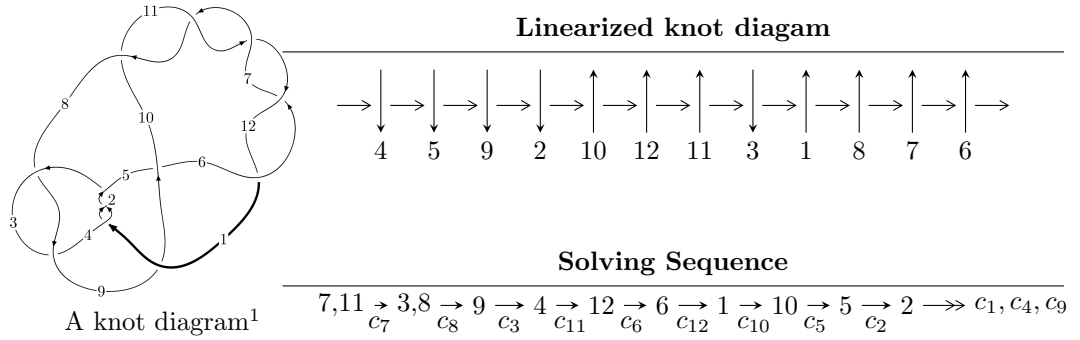


12a<sub>0842</sub> (K12a<sub>0842</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2u^{48} - 3u^{47} + \dots + b - 1, u^{49} + 32u^{47} + \dots + a + 2, u^{50} - 2u^{49} + \dots + 6u - 1 \rangle$$

$$I_2^u = \langle u^3 + u^2 + b + 2u + 1, -u^4 - 3u^2 + a - 1, u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 55 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle 2u^{48} - 3u^{47} + \dots + b - 1, u^{49} + 32u^{47} + \dots + a + 2, u^{50} - 2u^{49} + \dots + 6u - 1 \rangle$$

I.

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{49} - 32u^{47} + \dots - 3u - 2 \\ -2u^{48} + 3u^{47} + \dots - 4u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^9 - 6u^7 - 11u^5 - 6u^3 - u \\ -u^9 - 5u^7 - 7u^5 - 2u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{49} + 2u^{48} + \dots + 2u - 3 \\ u^{47} - 2u^{46} + \dots - 3u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^6 - 3u^4 + 1 \\ u^8 + 4u^6 + 4u^4 + 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{49} + u^{48} + \dots + u - 2 \\ -u^{48} + 2u^{47} + \dots - 3u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-u^{49} + 2u^{48} + \dots - 3u - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_4$	$u^{50} - 6u^{49} + \dots + 4u - 1$
$c_3, c_8$	$u^{50} + u^{49} + \dots + 64u + 32$
$c_5$	$u^{50} + 2u^{49} + \dots - 3538u - 1049$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$u^{50} + 2u^{49} + \dots - 6u - 1$
$c_9$	$u^{50} - 6u^{49} + \dots - 2094u + 279$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$y^{50} - 50y^{49} + \dots + 16y + 1$
$c_3, c_8$	$y^{50} - 33y^{49} + \dots - 7680y + 1024$
$c_5$	$y^{50} + 18y^{49} + \dots - 9892846y + 1100401$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$y^{50} + 66y^{49} + \dots - 22y + 1$
$c_9$	$y^{50} + 30y^{49} + \dots - 3350862y + 77841$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.241502 + 0.933682I$		
$a = 0.521403 + 0.320826I$	$-2.13050 - 2.69655I$	$0.94523 + 4.45521I$
$b = 0.450327 - 0.085914I$		
$u = -0.241502 - 0.933682I$		
$a = 0.521403 - 0.320826I$	$-2.13050 + 2.69655I$	$0.94523 - 4.45521I$
$b = 0.450327 + 0.085914I$		
$u = 0.224098 + 1.034240I$		
$a = 2.13283 + 0.91465I$	$-5.96928 + 1.26789I$	0
$b = 1.44365 - 0.08763I$		
$u = 0.224098 - 1.034240I$		
$a = 2.13283 - 0.91465I$	$-5.96928 - 1.26789I$	0
$b = 1.44365 + 0.08763I$		
$u = 0.286948 + 1.018960I$		
$a = -2.14547 - 1.33637I$	$-5.25575 + 6.41850I$	0
$b = -1.63676 - 0.38283I$		
$u = 0.286948 - 1.018960I$		
$a = -2.14547 + 1.33637I$	$-5.25575 - 6.41850I$	0
$b = -1.63676 + 0.38283I$		
$u = -0.260970 + 1.033400I$		
$a = -0.934867 - 0.520605I$	$-7.72397 - 3.91870I$	0
$b = -0.824900 + 0.201401I$		
$u = -0.260970 - 1.033400I$		
$a = -0.934867 + 0.520605I$	$-7.72397 + 3.91870I$	0
$b = -0.824900 - 0.201401I$		
$u = 0.331404 + 1.033160I$		
$a = 1.97777 + 1.46824I$	$-11.6778 + 10.5158I$	0
$b = 1.50104 + 0.67230I$		
$u = 0.331404 - 1.033160I$		
$a = 1.97777 - 1.46824I$	$-11.6778 - 10.5158I$	0
$b = 1.50104 - 0.67230I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.356837 + 0.800466I$ $a = 0.088289 - 1.106300I$ $b = -0.427389 - 0.642251I$	$-5.40920 - 3.17023I$	$-6.24629 + 4.79557I$
$u = -0.356837 - 0.800466I$ $a = 0.088289 + 1.106300I$ $b = -0.427389 + 0.642251I$	$-5.40920 + 3.17023I$	$-6.24629 - 4.79557I$
$u = 0.192571 + 1.121550I$ $a = -1.64217 - 0.83532I$ $b = -0.897289 + 0.086810I$	$-13.33180 - 1.81050I$	0
$u = 0.192571 - 1.121550I$ $a = -1.64217 + 0.83532I$ $b = -0.897289 - 0.086810I$	$-13.33180 + 1.81050I$	0
$u = 0.063290 + 0.852837I$ $a = 1.48467 - 0.76548I$ $b = 0.436324 - 1.223550I$	$-3.68295 + 0.97203I$	$-6.12133 + 0.71322I$
$u = 0.063290 - 0.852837I$ $a = 1.48467 + 0.76548I$ $b = 0.436324 + 1.223550I$	$-3.68295 - 0.97203I$	$-6.12133 - 0.71322I$
$u = -0.168142 + 0.755805I$ $a = -0.665021 + 0.730022I$ $b = 0.037081 + 0.681718I$	$-0.89055 - 1.70206I$	$0.92164 + 5.53470I$
$u = -0.168142 - 0.755805I$ $a = -0.665021 - 0.730022I$ $b = 0.037081 - 0.681718I$	$-0.89055 + 1.70206I$	$0.92164 - 5.53470I$
$u = 0.473458 + 0.447921I$ $a = -0.132112 + 0.553984I$ $b = -1.136560 - 0.435330I$	$-8.33174 - 4.01114I$	$-4.65273 - 0.13384I$
$u = 0.473458 - 0.447921I$ $a = -0.132112 - 0.553984I$ $b = -1.136560 + 0.435330I$	$-8.33174 + 4.01114I$	$-4.65273 + 0.13384I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.567490 + 0.251389I$ $a = -0.16497 - 1.91694I$ $b = 0.866292 - 0.017602I$	$-7.69762 + 7.46027I$	$-2.75082 - 6.53209I$
$u = 0.567490 - 0.251389I$ $a = -0.16497 + 1.91694I$ $b = 0.866292 + 0.017602I$	$-7.69762 - 7.46027I$	$-2.75082 + 6.53209I$
$u = -0.575142$ $a = 1.40804$ $b = 0.628444$	$-2.98861$	$-1.42680$
$u = 0.494918 + 0.244793I$ $a = 0.62020 + 1.67737I$ $b = -0.808413 - 0.141535I$	$-1.34530 + 3.74735I$	$-0.07289 - 7.40976I$
$u = 0.494918 - 0.244793I$ $a = 0.62020 - 1.67737I$ $b = -0.808413 + 0.141535I$	$-1.34530 - 3.74735I$	$-0.07289 + 7.40976I$
$u = -0.457183 + 0.286466I$ $a = 1.10902 - 1.15755I$ $b = 0.256004 - 0.666486I$	$-3.64157 - 1.46138I$	$-1.93416 + 4.24780I$
$u = -0.457183 - 0.286466I$ $a = 1.10902 + 1.15755I$ $b = 0.256004 + 0.666486I$	$-3.64157 + 1.46138I$	$-1.93416 - 4.24780I$
$u = 0.394100 + 0.341086I$ $a = -0.674932 - 0.693216I$ $b = 0.860383 + 0.378414I$	$-1.76393 - 0.83267I$	$-2.37494 - 0.63227I$
$u = 0.394100 - 0.341086I$ $a = -0.674932 + 0.693216I$ $b = 0.860383 - 0.378414I$	$-1.76393 + 0.83267I$	$-2.37494 + 0.63227I$
$u = -0.425320 + 0.091898I$ $a = -0.743778 + 0.682945I$ $b = -0.228701 + 0.291111I$	$1.018590 - 0.418472I$	$8.77405 + 2.00502I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.425320 - 0.091898I$ $a = -0.743778 - 0.682945I$ $b = -0.228701 - 0.291111I$	$1.018590 + 0.418472I$	$8.77405 - 2.00502I$
$u = -0.06654 + 1.65140I$ $a = -0.502139 + 0.521102I$ $b = -0.41662 + 1.56312I$	$-13.8965 - 4.6518I$	0
$u = -0.06654 - 1.65140I$ $a = -0.502139 - 0.521102I$ $b = -0.41662 - 1.56312I$	$-13.8965 + 4.6518I$	0
$u = -0.02318 + 1.67172I$ $a = 0.751552 - 0.327513I$ $b = 1.43271 - 1.45403I$	$-9.55272 - 2.27084I$	0
$u = -0.02318 - 1.67172I$ $a = 0.751552 + 0.327513I$ $b = 1.43271 + 1.45403I$	$-9.55272 + 2.27084I$	0
$u = 0.01016 + 1.69219I$ $a = -1.348610 + 0.394636I$ $b = -3.15245 + 1.83141I$	$-12.79330 + 1.21246I$	0
$u = 0.01016 - 1.69219I$ $a = -1.348610 - 0.394636I$ $b = -3.15245 - 1.83141I$	$-12.79330 - 1.21246I$	0
$u = -0.06031 + 1.70334I$ $a = -0.294056 - 0.407025I$ $b = -0.897079 - 0.594388I$	$-11.49630 - 3.87362I$	0
$u = -0.06031 - 1.70334I$ $a = -0.294056 + 0.407025I$ $b = -0.897079 + 0.594388I$	$-11.49630 + 3.87362I$	0
$u = 0.07470 + 1.72501I$ $a = 2.31285 + 0.82742I$ $b = 5.82899 + 2.24727I$	$-15.0169 + 7.8885I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.07470 - 1.72501I$ $a = 2.31285 - 0.82742I$ $b = 5.82899 - 2.24727I$	$-15.0169 - 7.8885I$	0
$u = 0.05873 + 1.72830I$ $a = -2.35182 - 0.61319I$ $b = -5.90142 - 1.36111I$	$-15.8315 + 2.4299I$	0
$u = 0.05873 - 1.72830I$ $a = -2.35182 + 0.61319I$ $b = -5.90142 + 1.36111I$	$-15.8315 - 2.4299I$	0
$u = -0.06774 + 1.72877I$ $a = 0.495071 + 0.829683I$ $b = 1.48829 + 1.29304I$	$-17.5722 - 5.2629I$	0
$u = -0.06774 - 1.72877I$ $a = 0.495071 - 0.829683I$ $b = 1.48829 - 1.29304I$	$-17.5722 + 5.2629I$	0
$u = 0.08767 + 1.72869I$ $a = -2.17648 - 0.82127I$ $b = -5.31736 - 2.45060I$	$17.9962 + 12.2318I$	0
$u = 0.08767 - 1.72869I$ $a = -2.17648 + 0.82127I$ $b = -5.31736 + 2.45060I$	$17.9962 - 12.2318I$	0
$u = 0.04560 + 1.74772I$ $a = 2.09491 + 0.62616I$ $b = 4.94329 + 1.19565I$	$15.8438 - 0.8328I$	0
$u = 0.04560 - 1.74772I$ $a = 2.09491 - 0.62616I$ $b = 4.94329 - 1.19565I$	$15.8438 + 0.8328I$	0
$u = 0.220298$ $a = -3.03230$ $b = 0.572682$	$-1.27955$	$-10.7800$

**II.**

$$I_2^u = \langle u^3 + u^2 + b + 2u + 1, -u^4 - 3u^2 + a - 1, u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^4 + 3u^2 + 1 \\ -u^3 - u^2 - 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + 3u^2 + 1 \\ -u^3 - u^2 - 2u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 - 2u \\ -u^3 - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^4 + u^3 + 3u^2 + 2u + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $5u^4 + 5u^3 + 20u^2 + 14u + 9$**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^5$
$c_3, c_8$	$u^5$
$c_4$	$(u + 1)^5$
$c_5, c_9$	$u^5 + u^4 - u^2 + u + 1$
$c_6, c_7$	$u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1$
$c_{10}, c_{11}, c_{12}$	$u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^5$
$c_3, c_8$	$y^5$
$c_5, c_9$	$y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.233677 + 0.885557I$ $a = -0.827780 - 0.637683I$ $b = -0.340036 - 0.807849I$	$-3.46474 - 2.21397I$	$-4.37343 + 4.39306I$
$u = -0.233677 - 0.885557I$ $a = -0.827780 + 0.637683I$ $b = -0.340036 + 0.807849I$	$-3.46474 + 2.21397I$	$-4.37343 - 4.39306I$
$u = -0.416284$ $a = 1.54991$ $b = -0.268586$	$-0.762751$	$6.42730$
$u = -0.05818 + 1.69128I$ $a = 0.552827 + 0.534136I$ $b = 1.47433 + 1.63485I$	$-12.60320 - 3.33174I$	$-5.84024 + 1.26157I$
$u = -0.05818 - 1.69128I$ $a = 0.552827 - 0.534136I$ $b = 1.47433 - 1.63485I$	$-12.60320 + 3.33174I$	$-5.84024 - 1.26157I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$((u-1)^5)(u^{50} - 6u^{49} + \dots + 4u - 1)$
$c_3, c_8$	$u^5(u^{50} + u^{49} + \dots + 64u + 32)$
$c_4$	$((u+1)^5)(u^{50} - 6u^{49} + \dots + 4u - 1)$
$c_5$	$(u^5 + u^4 - u^2 + u + 1)(u^{50} + 2u^{49} + \dots - 3538u - 1049)$
$c_6, c_7$	$(u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1)(u^{50} + 2u^{49} + \dots - 6u - 1)$
$c_9$	$(u^5 + u^4 - u^2 + u + 1)(u^{50} - 6u^{49} + \dots - 2094u + 279)$
$c_{10}, c_{11}, c_{12}$	$(u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1)(u^{50} + 2u^{49} + \dots - 6u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$((y - 1)^5)(y^{50} - 50y^{49} + \dots + 16y + 1)$
$c_3, c_8$	$y^5(y^{50} - 33y^{49} + \dots - 7680y + 1024)$
$c_5$	$(y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1)$ $\cdot (y^{50} + 18y^{49} + \dots - 9892846y + 1100401)$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)(y^{50} + 66y^{49} + \dots - 22y + 1)$
$c_9$	$(y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1)(y^{50} + 30y^{49} + \dots - 3350862y + 77841)$