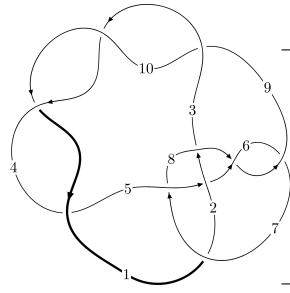
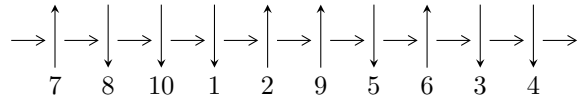


10<sub>82</sub> (K10a<sub>83</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$1,5 \xrightarrow{c_4} 4,8 \xrightarrow{c_7} 7 \xrightarrow{c_1} 2 \xrightarrow{c_5} 6 \xrightarrow{c_{10}} 10 \xrightarrow{c_3} 3 \xrightarrow{c_9} 9 \longrightarrow c_2, c_6, c_8$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1790814371u^{31} + 3053908485u^{30} + \dots + 15215838414b + 1796669401, \\ 9786061617u^{31} + 13386015963u^{30} + \dots + 5071946138a + 29865915991, u^{32} + 2u^{31} + \dots - u + 1 \rangle \\ I_2^u = \langle b, a + 1, u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 33 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 1.79 \times 10^9 u^{31} + 3.05 \times 10^9 u^{30} + \dots + 1.52 \times 10^{10} b + 1.80 \times 10^9, 9.79 \times 10^9 u^{31} + 1.34 \times 10^{10} u^{30} + \dots + 5.07 \times 10^9 a + 2.99 \times 10^{10}, u^{32} + 2u^{31} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1.92945u^{31} - 2.63923u^{30} + \dots + 9.12108u - 5.88845 \\ -0.117694u^{31} - 0.200706u^{30} + \dots + 2.07712u - 0.118079 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2.04714u^{31} - 2.83993u^{30} + \dots + 11.1982u - 6.00653 \\ -0.117694u^{31} - 0.200706u^{30} + \dots + 2.07712u - 0.118079 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2.22835u^{31} - 3.03012u^{30} + \dots + 0.715268u + 0.285838 \\ -0.998715u^{31} - 0.999372u^{30} + \dots + 1.28281u - 0.999382 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2.22354u^{31} + 3.04014u^{30} + \dots - 10.0154u + 6.22362 \\ -u^5 + 3u^3 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^3 + 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) Cusp Shapes} = \frac{18210579048}{2535973069} u^{31} + \frac{32359838926}{2535973069} u^{30} + \dots - \frac{94883406442}{2535973069} u + \frac{41946667180}{2535973069}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{32} + 2u^{31} + \dots + 12u + 8$
$c_2$	$u^{32} + 11u^{30} + \dots + 13u - 1$
$c_3, c_4, c_9$ $c_{10}$	$u^{32} + 2u^{31} + \dots - u + 1$
$c_5$	$u^{32} - 2u^{31} + \dots + u - 1$
$c_6, c_8$	$u^{32} + 2u^{31} + \dots - 13u - 1$
$c_7$	$u^{32} - 5u^{31} + \dots - 6u + 2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{32} + 30y^{31} + \dots + 240y + 64$
$c_2$	$y^{32} + 22y^{31} + \dots - 121y + 1$
$c_3, c_4, c_9$ $c_{10}$	$y^{32} - 38y^{31} + \dots - 5y + 1$
$c_5$	$y^{32} - 6y^{31} + \dots - 5y + 1$
$c_6, c_8$	$y^{32} - 18y^{31} + \dots - 81y + 1$
$c_7$	$y^{32} - 9y^{31} + \dots - 32y + 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.820983 + 0.567595I$ $a = -1.27469 + 0.62091I$ $b = 1.088800 + 0.850114I$	$0.60537 - 9.61260I$	$-2.87987 + 8.20248I$
$u = 0.820983 - 0.567595I$ $a = -1.27469 - 0.62091I$ $b = 1.088800 - 0.850114I$	$0.60537 + 9.61260I$	$-2.87987 - 8.20248I$
$u = 0.795955 + 0.349102I$ $a = 1.45784 - 0.39446I$ $b = -1.136450 - 0.835713I$	$-2.75563 - 4.13382I$	$-6.93448 + 6.73749I$
$u = 0.795955 - 0.349102I$ $a = 1.45784 + 0.39446I$ $b = -1.136450 + 0.835713I$	$-2.75563 + 4.13382I$	$-6.93448 - 6.73749I$
$u = -0.643643 + 0.579820I$ $a = 0.109445 + 0.730653I$ $b = -0.758624 + 0.110290I$	$-1.27204 + 1.92248I$	$-7.80216 - 5.91516I$
$u = -0.643643 - 0.579820I$ $a = 0.109445 - 0.730653I$ $b = -0.758624 - 0.110290I$	$-1.27204 - 1.92248I$	$-7.80216 + 5.91516I$
$u = -1.076160 + 0.444148I$ $a = -0.311615 - 0.602654I$ $b = 0.691368 + 0.318391I$	$-0.800175 - 0.941991I$	$-6.40540 + 5.25085I$
$u = -1.076160 - 0.444148I$ $a = -0.311615 + 0.602654I$ $b = 0.691368 - 0.318391I$	$-0.800175 + 0.941991I$	$-6.40540 - 5.25085I$
$u = -0.788048$ $a = -0.997928$ $b = 0.333761$	$-1.36694$	$-7.37900$
$u = 0.102445 + 0.771273I$ $a = 0.249085 - 0.151496I$ $b = 0.853465 - 0.688304I$	$2.78249 + 5.16401I$	$0.17525 - 5.43243I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.102445 - 0.771273I$ $a = 0.249085 + 0.151496I$ $b = 0.853465 + 0.688304I$	$2.78249 - 5.16401I$	$0.17525 + 5.43243I$
$u = 0.560858 + 0.310184I$ $a = -0.155519 + 0.637386I$ $b = 0.671965 - 1.149150I$	$1.86601 - 2.61443I$	$0.82365 + 8.13996I$
$u = 0.560858 - 0.310184I$ $a = -0.155519 - 0.637386I$ $b = 0.671965 + 1.149150I$	$1.86601 + 2.61443I$	$0.82365 - 8.13996I$
$u = -0.598750 + 0.114970I$ $a = 0.25826 - 3.79474I$ $b = -0.135421 - 0.360183I$	$0.576409 + 0.313871I$	$8.1378 + 17.1065I$
$u = -0.598750 - 0.114970I$ $a = 0.25826 + 3.79474I$ $b = -0.135421 + 0.360183I$	$0.576409 - 0.313871I$	$8.1378 - 17.1065I$
$u = -0.086458 + 0.449548I$ $a = -0.783456 + 0.459529I$ $b = -0.610958 + 0.536174I$	$-0.227616 + 1.394370I$	$-2.60146 - 4.04487I$
$u = -0.086458 - 0.449548I$ $a = -0.783456 - 0.459529I$ $b = -0.610958 - 0.536174I$	$-0.227616 - 1.394370I$	$-2.60146 + 4.04487I$
$u = -1.55208$ $a = -2.62954$ $b = 1.76871$	$-3.73390$	$0$
$u = -1.57850 + 0.06009I$ $a = -0.52697 - 1.39477I$ $b = 0.56830 + 1.70360I$	$-5.46664 + 3.81790I$	$0$
$u = -1.57850 - 0.06009I$ $a = -0.52697 + 1.39477I$ $b = 0.56830 - 1.70360I$	$-5.46664 - 3.81790I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.60015 + 0.02565I$ $a = 0.830347 + 1.077280I$ $b = -0.363802 + 0.595725I$	$-7.09081 - 0.79638I$	0
$u = 1.60015 - 0.02565I$ $a = 0.830347 - 1.077280I$ $b = -0.363802 - 0.595725I$	$-7.09081 + 0.79638I$	0
$u = 0.269938 + 0.288721I$ $a = -2.52869 + 1.49962I$ $b = 0.887931 + 0.459497I$	$2.64104 + 0.25879I$	$3.85203 + 2.96045I$
$u = 0.269938 - 0.288721I$ $a = -2.52869 - 1.49962I$ $b = 0.887931 - 0.459497I$	$2.64104 - 0.25879I$	$3.85203 - 2.96045I$
$u = 1.61612 + 0.17777I$ $a = 1.092350 - 0.316288I$ $b = -0.985940 - 0.438836I$	$-8.99388 - 4.78654I$	0
$u = 1.61612 - 0.17777I$ $a = 1.092350 + 0.316288I$ $b = -0.985940 + 0.438836I$	$-8.99388 + 4.78654I$	0
$u = -1.63927 + 0.09770I$ $a = 2.05679 - 0.27434I$ $b = -1.51522 + 0.94459I$	$-11.15790 + 5.83644I$	0
$u = -1.63927 - 0.09770I$ $a = 2.05679 + 0.27434I$ $b = -1.51522 - 0.94459I$	$-11.15790 - 5.83644I$	0
$u = -1.65031 + 0.16673I$ $a = -1.89221 + 0.02470I$ $b = 1.30041 - 0.93941I$	$-7.8166 + 12.4315I$	0
$u = -1.65031 - 0.16673I$ $a = -1.89221 - 0.02470I$ $b = 1.30041 + 0.93941I$	$-7.8166 - 12.4315I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.67671 + 0.06666I$	$-10.51010 - 0.53898I$	0
$a = -1.267240 + 0.207888I$		
$b = 0.892941 + 0.200725I$		
$u = 1.67671 - 0.06666I$	$-10.51010 + 0.53898I$	0
$a = -1.267240 - 0.207888I$		
$b = 0.892941 - 0.200725I$		



$$\text{II. } I_2^u = \langle b, a + 1, u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_6$	$u + 1$
$c_7$	$u$
$c_8, c_9, c_{10}$	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_6$ $c_8, c_9, c_{10}$	$y - 1$
$c_7$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = -1.00000$	0	0
$b = 0$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u + 1)(u^{32} + 2u^{31} + \dots + 12u + 8)$
$c_2$	$(u + 1)(u^{32} + 11u^{30} + \dots + 13u - 1)$
$c_3, c_4$	$(u + 1)(u^{32} + 2u^{31} + \dots - u + 1)$
$c_5$	$(u + 1)(u^{32} - 2u^{31} + \dots + u - 1)$
$c_6$	$(u + 1)(u^{32} + 2u^{31} + \dots - 13u - 1)$
$c_7$	$u(u^{32} - 5u^{31} + \dots - 6u + 2)$
$c_8$	$(u - 1)(u^{32} + 2u^{31} + \dots - 13u - 1)$
$c_9, c_{10}$	$(u - 1)(u^{32} + 2u^{31} + \dots - u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)(y^{32} + 30y^{31} + \dots + 240y + 64)$
$c_2$	$(y - 1)(y^{32} + 22y^{31} + \dots - 121y + 1)$
$c_3, c_4, c_9$ $c_{10}$	$(y - 1)(y^{32} - 38y^{31} + \dots - 5y + 1)$
$c_5$	$(y - 1)(y^{32} - 6y^{31} + \dots - 5y + 1)$
$c_6, c_8$	$(y - 1)(y^{32} - 18y^{31} + \dots - 81y + 1)$
$c_7$	$y(y^{32} - 9y^{31} + \dots - 32y + 4)$