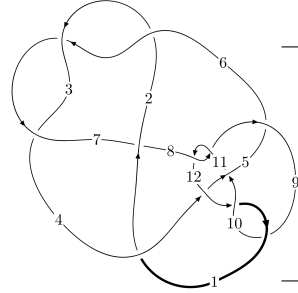
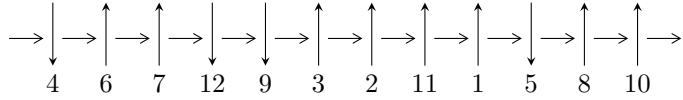


12a<sub>0886</sub> (K12a<sub>0886</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5, 10 \xrightarrow{c_{10}} 1, 11 \xrightarrow{c_9} 9 \xrightarrow{c_5} 6 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \xrightarrow{c_4} 4 \xrightarrow{c_1} 2 \xrightarrow{c_2} 3 \xrightarrow{c_7} 7 \rightsquigarrow c_3, c_6, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 5.07214 \times 10^{121} u^{41} - 1.29009 \times 10^{122} u^{40} + \dots + 1.79683 \times 10^{124} b - 2.09627 \times 10^{125}, \\ 1.21110 \times 10^{125} u^{41} - 3.08153 \times 10^{125} u^{40} + \dots + 3.67991 \times 10^{127} a - 5.44579 \times 10^{128}, \\ u^{42} - 3u^{41} + \dots - 7680u + 2048 \rangle$$

$$I_2^u = \langle -u^2 a + b - 1, -4u^{32} a - 6u^{31} a + \dots + a + 8, u^{33} + 2u^{32} + \dots - 2u - 1 \rangle$$

$$I_3^u = \langle b - a - 1, a^2 + a + 2, u - 1 \rangle$$

$$I_4^u = \langle b - u, a - 1, u^2 + 1 \rangle$$

$$I_1^v = \langle a, b + 1, 32v^5 + 16v^4 + 16v^3 + 4v^2 + 2v + 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 117 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 5.07 \times 10^{121} u^{41} - 1.29 \times 10^{122} u^{40} + \dots + 1.80 \times 10^{124} b - 2.10 \times 10^{125}, 1.21 \times 10^{125} u^{41} - 3.08 \times 10^{125} u^{40} + \dots + 3.68 \times 10^{127} a - 5.45 \times 10^{128}, u^{42} - 3u^{41} + \dots - 7680u + 2048 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.00329111u^{41} + 0.00837392u^{40} + \dots - 21.9426u + 14.7987 \\ -0.00282282u^{41} + 0.00717978u^{40} + \dots - 18.7314u + 11.6665 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.000468286u^{41} + 0.00119414u^{40} + \dots - 3.21121u + 3.13219 \\ 0.00274209u^{41} - 0.00695770u^{40} + \dots + 18.0721u - 11.2349 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.000392195u^{41} - 0.00107102u^{40} + \dots + 1.79714u - 2.03513 \\ -0.00149906u^{41} + 0.00367622u^{40} + \dots - 10.2811u + 6.35866 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.00329111u^{41} + 0.00837392u^{40} + \dots - 21.9426u + 14.7987 \\ 0.00208209u^{41} - 0.00535290u^{40} + \dots + 13.9562u - 8.59570 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.000468286u^{41} + 0.00119414u^{40} + \dots - 3.21121u + 3.13219 \\ -0.00282282u^{41} + 0.00717978u^{40} + \dots - 18.7314u + 11.6665 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.000392195u^{41} + 0.00107102u^{40} + \dots - 1.79714u + 2.03513 \\ -0.00147930u^{41} + 0.00368763u^{40} + \dots - 10.2886u + 6.57486 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.00305058u^{41} + 0.00802983u^{40} + \dots - 20.7780u + 15.1603 \\ -0.00409737u^{41} + 0.0103081u^{40} + \dots - 27.3367u + 16.8188 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.00676311u^{41} + 0.0172674u^{40} + \dots - 46.9837u + 30.8098 \\ -0.00457559u^{41} + 0.0113420u^{40} + \dots - 32.3525u + 17.7346 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.00676311u^{41} + 0.0172674u^{40} + \dots - 46.9837u + 30.8098 \\ 0.00331935u^{41} - 0.00806990u^{40} + \dots + 22.9950u - 11.5457 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.0230966u^{41} + 0.0573171u^{40} + \dots - 173.318u + 88.0642$

(iv) u-Polynomials at the component

| Crossings                      | u-Polynomials at each crossing                |
|--------------------------------|---|
| $c_1$                          | $u^{42} - 10u^{41} + \dots - 11111u + 1504$   |
| $c_2, c_3, c_6$                | $u^{42} - 2u^{41} + \dots + 7u - 4$           |
| $c_4, c_5$                     | $32(32u^{42} + 48u^{41} + \dots + 20u^2 + 2)$ |
| $c_7$                          | $u^{42} - 2u^{40} + \dots + 1136u - 448$      |
| $c_8, c_9, c_{11}$<br>$c_{12}$ | $u^{42} - 5u^{41} + \dots - u - 1$            |
| $c_{10}$                       | $u^{42} - 3u^{41} + \dots - 7680u + 2048$     |

(v) Riley Polynomials at the component

| Crossings                      | Riley Polynomials at each crossing                |
|--------------------------------|---|
| $c_1$                          | $y^{42} + 14y^{41} + \dots + 62115215y + 2262016$ |
| $c_2, c_3, c_6$                | $y^{42} - 38y^{41} + \dots - y + 16$              |
| $c_4, c_5$                     | $1024(1024y^{42} - 1280y^{41} + \dots + 80y + 4)$ |
| $c_7$                          | $y^{42} - 4y^{41} + \dots - 2874624y + 200704$    |
| $c_8, c_9, c_{11}$<br>$c_{12}$ | $y^{42} + 17y^{41} + \dots + 9y + 1$              |
| $c_{10}$                       | $y^{42} - 9y^{41} + \dots - 69468160y + 4194304$  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.314188 + 1.053170I$ | $5.98291 - 1.19095I$                  | $10.40868 + 3.12372I$ |
| $a = 0.027002 + 0.483467I$  |                                       |                       |
| $b = -0.594138 + 0.750449I$ |                                       |                       |
| $u = -0.314188 - 1.053170I$ | $5.98291 + 1.19095I$                  | $10.40868 - 3.12372I$ |
| $a = 0.027002 - 0.483467I$  |                                       |                       |
| $b = -0.594138 - 0.750449I$ |                                       |                       |
| $u = 0.820994 + 0.197858I$  | $6.19589 - 3.49276I$                  | $6.51052 + 0.13763I$  |
| $a = 0.95965 + 1.29956I$    |                                       |                       |
| $b = 0.291149 + 0.470080I$  |                                       |                       |
| $u = 0.820994 - 0.197858I$  | $6.19589 + 3.49276I$                  | $6.51052 - 0.13763I$  |
| $a = 0.95965 - 1.29956I$    |                                       |                       |
| $b = 0.291149 - 0.470080I$  |                                       |                       |
| $u = -0.577314 + 0.526253I$ | $8.12984 - 3.40777I$                  | $9.67454 - 1.62361I$  |
| $a = -0.108552 + 0.213642I$ |                                       |                       |
| $b = -1.121680 + 0.508475I$ |                                       |                       |
| $u = -0.577314 - 0.526253I$ | $8.12984 + 3.40777I$                  | $9.67454 + 1.62361I$  |
| $a = -0.108552 - 0.213642I$ |                                       |                       |
| $b = -1.121680 - 0.508475I$ |                                       |                       |
| $u = -0.991104 + 0.788632I$ | $0.103272 + 0.890316I$                | $7.21863 - 1.89711I$  |
| $a = 0.430066 - 0.979780I$  |                                       |                       |
| $b = 0.048227 - 0.652088I$  |                                       |                       |
| $u = -0.991104 - 0.788632I$ | $0.103272 - 0.890316I$                | $7.21863 + 1.89711I$  |
| $a = 0.430066 + 0.979780I$  |                                       |                       |
| $b = 0.048227 + 0.652088I$  |                                       |                       |
| $u = 0.650573 + 0.315344I$  | $7.29715 - 5.25882I$                  | $4.50219 + 8.83294I$  |
| $a = -0.150923 - 0.123948I$ |                                       |                       |
| $b = -1.306350 - 0.336680I$ |                                       |                       |
| $u = 0.650573 - 0.315344I$  | $7.29715 + 5.25882I$                  | $4.50219 - 8.83294I$  |
| $a = -0.150923 + 0.123948I$ |                                       |                       |
| $b = -1.306350 + 0.336680I$ |                                       |                       |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|---|---------------------------------------|------------------------|
| $u = -0.375562 + 0.527351I$<br>$a = 0.695747 - 0.521764I$<br>$b = -0.077418 - 0.331511I$  | $0.199443 + 0.975184I$                | $4.03278 - 6.08768I$   |
| $u = -0.375562 - 0.527351I$<br>$a = 0.695747 + 0.521764I$<br>$b = -0.077418 + 0.331511I$  | $0.199443 - 0.975184I$                | $4.03278 + 6.08768I$   |
| $u = -1.354830 + 0.085427I$<br>$a = 0.20811 + 1.54932I$<br>$b = 0.374024 + 0.802773I$     | $5.97161 + 6.59731I$                  | $7.43283 - 8.44870I$   |
| $u = -1.354830 - 0.085427I$<br>$a = 0.20811 - 1.54932I$<br>$b = 0.374024 - 0.802773I$     | $5.97161 - 6.59731I$                  | $7.43283 + 8.44870I$   |
| $u = -0.570711 + 0.284785I$<br>$a = -0.119513 + 0.107746I$<br>$b = -1.237960 + 0.273860I$ | $1.86047 + 2.11675I$                  | $-0.90328 - 11.17612I$ |
| $u = -0.570711 - 0.284785I$<br>$a = -0.119513 - 0.107746I$<br>$b = -1.237960 - 0.273860I$ | $1.86047 - 2.11675I$                  | $-0.90328 + 11.17612I$ |
| $u = 0.442682 + 0.457127I$<br>$a = -0.050983 - 0.171060I$<br>$b = -1.041130 - 0.367914I$  | $2.47985 + 1.01844I$                  | $7.66650 + 3.92369I$   |
| $u = 0.442682 - 0.457127I$<br>$a = -0.050983 + 0.171060I$<br>$b = -1.041130 + 0.367914I$  | $2.47985 - 1.01844I$                  | $7.66650 - 3.92369I$   |
| $u = 0.522304$<br>$a = -0.110575$<br>$b = -1.24864$                                       | $3.67439$                             | $-7.95490$             |
| $u = 1.54341 + 0.23309I$<br>$a = 0.243734 + 1.309960I$<br>$b = 0.237641 + 0.802950I$      | $-0.35149 + 3.39390I$                 | $0. - 8.80504I$        |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape      |
|--|---------------------------------------|-----------------|
| $u = 1.54341 - 0.23309I$<br>$a = 0.243734 - 1.309960I$<br>$b = 0.237641 - 0.802950I$ | $-0.35149 - 3.39390I$                 | $0. + 8.80504I$ |
| $u = 0.433072$<br>$a = 1.51195$<br>$b = 0.203807$                                    | $2.70015$                             | $1.03960$       |
| $u = -1.32959 + 0.84020I$<br>$a = -0.48736 + 1.45749I$<br>$b = 0.570490 + 1.221150I$ | $2.85618 + 8.34848I$                  | $0$             |
| $u = -1.32959 - 0.84020I$<br>$a = -0.48736 - 1.45749I$<br>$b = 0.570490 - 1.221150I$ | $2.85618 - 8.34848I$                  | $0$             |
| $u = 1.29599 + 0.93912I$<br>$a = -0.58004 - 1.38071I$<br>$b = 0.59672 - 1.32586I$    | $0.1604 - 18.2186I$                   | $0. + 9.92364I$ |
| $u = 1.29599 - 0.93912I$<br>$a = -0.58004 + 1.38071I$<br>$b = 0.59672 + 1.32586I$    | $0.1604 + 18.2186I$                   | $0. - 9.92364I$ |
| $u = -1.32065 + 0.93583I$<br>$a = -0.55241 + 1.37129I$<br>$b = 0.56978 + 1.31805I$   | $-5.4682 + 14.4315I$                  | $0$             |
| $u = -1.32065 - 0.93583I$<br>$a = -0.55241 - 1.37129I$<br>$b = 0.56978 - 1.31805I$   | $-5.4682 - 14.4315I$                  | $0$             |
| $u = 1.35470 + 0.90995I$<br>$a = -0.50581 - 1.37917I$<br>$b = 0.539500 - 1.285140I$  | $-4.16980 - 10.14610I$                | $0$             |
| $u = 1.35470 - 0.90995I$<br>$a = -0.50581 + 1.37917I$<br>$b = 0.539500 + 1.285140I$  | $-4.16980 + 10.14610I$                | $0$             |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 0.60722 + 1.63895I$<br>$a = -0.090576 - 0.705861I$<br>$b = -0.372413 - 1.065220I$  | $2.41336 + 9.70431I$                  | 0          |
| $u = 0.60722 - 1.63895I$<br>$a = -0.090576 + 0.705861I$<br>$b = -0.372413 + 1.065220I$  | $2.41336 - 9.70431I$                  | 0          |
| $u = 1.47227 + 0.94822I$<br>$a = -0.421850 - 1.297470I$<br>$b = 0.426915 - 1.286100I$   | $-5.57375 - 10.06480I$                | 0          |
| $u = 1.47227 - 0.94822I$<br>$a = -0.421850 + 1.297470I$<br>$b = 0.426915 + 1.286100I$   | $-5.57375 + 10.06480I$                | 0          |
| $u = -1.57270 + 0.94944I$<br>$a = -0.352961 + 1.267110I$<br>$b = 0.360707 + 1.251940I$  | $-8.85361 + 5.99722I$                 | 0          |
| $u = -1.57270 - 0.94944I$<br>$a = -0.352961 - 1.267110I$<br>$b = 0.360707 - 1.251940I$  | $-8.85361 - 5.99722I$                 | 0          |
| $u = -0.47063 + 1.78264I$<br>$a = -0.047981 + 0.738048I$<br>$b = -0.312174 + 1.017260I$ | $-2.89576 - 5.73091I$                 | 0          |
| $u = -0.47063 - 1.78264I$<br>$a = -0.047981 - 0.738048I$<br>$b = -0.312174 - 1.017260I$ | $-2.89576 + 5.73091I$                 | 0          |
| $u = 0.00561 + 1.91712I$<br>$a = 0.046167 - 0.779412I$<br>$b = -0.229375 - 0.915905I$   | $-0.81742 + 1.38862I$                 | 0          |
| $u = 0.00561 - 1.91712I$<br>$a = 0.046167 + 0.779412I$<br>$b = -0.229375 + 0.915905I$   | $-0.81742 - 1.38862I$                 | 0          |



| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.70614 + 0.93966I$    | $-4.72570 - 1.89699I$                 | 0          |
| $a = -0.279714 - 1.240500I$ |                                       |            |
| $b = 0.299896 - 1.205740I$  |                                       |            |
| $u = 1.70614 - 0.93966I$    | $-4.72570 + 1.89699I$                 | 0          |
| $a = -0.279714 + 1.240500I$ |                                       |            |
| $b = 0.299896 + 1.205740I$  |                                       |            |

## II.

$$I_2^u = \langle -u^2a + b - 1, -4u^{32}a - 6u^{31}a + \dots + a + 8, u^{33} + 2u^{32} + \dots - 2u - 1 \rangle$$

### (i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} a \\ u^2a + 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 4u^{32} + 6u^{31} + \dots - a - 2u \\ u^4a - u^4 + u^2 - 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -2u^{32}a + u^{32} + \dots + 4a - 4 \\ -2u^{32} - 4u^{31} + \dots + 9u + 4 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 4u^{32} + 6u^{31} + \dots - a - 1 \\ -1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^2a + a - 1 \\ u^2a + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -2u^{32}a + 3u^{32} + \dots + 4a - 8 \\ -2u^{32} - 4u^{31} + \dots + 9u + 4 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -4u^{32} - 6u^{31} + \dots + 3a - 7 \\ -u^{12}a + u^{12} + \dots - 7u^2 + 3 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^{24}a - 5u^{22}a + \dots + a - 8 \\ u^{26}a - 4u^{24}a + \dots - 6u^2 + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 4u^{32} + 6u^{31} + \dots - a + 3 \\ u^{24}a - u^{24} + \dots + 6u^2 - 1 \end{pmatrix} \end{aligned}$$

### (ii) Obstruction class = -1

### (iii) Cusp Shapes

$$\begin{aligned} &= 4u^{32} - 20u^{30} - 4u^{29} + 72u^{28} + 16u^{27} - 180u^{26} - 56u^{25} + 360u^{24} + 128u^{23} - 580u^{22} - \\ &248u^{21} + 772u^{20} + 384u^{19} - 848u^{18} - 500u^{17} + 760u^{16} + 548u^{15} - 532u^{14} - 496u^{13} + \\ &264u^{12} + 372u^{11} - 52u^{10} - 220u^9 - 48u^8 + 92u^7 + 56u^6 - 24u^5 - 28u^4 - 4u^3 + 4u^2 + 6 \end{aligned}$$

(iv) u-Polynomials at the component

| Crossings                      | u-Polynomials at each crossing              |
|--------------------------------|---|
| $c_1$                          | $(u^{33} - 6u^{32} + \dots + 128u - 23)^2$  |
| $c_2, c_3, c_6$                | $(u^{33} - 2u^{32} + \dots + u^2 + 1)^2$    |
| $c_4, c_5$                     | $u^{66} - u^{65} + \dots - 115818u + 36557$ |
| $c_7$                          | $(u^{33} + 3u^{32} + \dots + 32u + 7)^2$    |
| $c_8, c_9, c_{11}$<br>$c_{12}$ | $u^{66} + 10u^{65} + \dots + 4u + 1$        |
| $c_{10}$                       | $(u^{33} + 2u^{32} + \dots - 2u - 1)^2$     |

(v) Riley Polynomials at the component

| Crossings                      | Riley Polynomials at each crossing                      |
|--------------------------------|---|
| $c_1$                          | $(y^{33} + 14y^{32} + \dots - 2062y - 529)^2$           |
| $c_2, c_3, c_6$                | $(y^{33} - 30y^{32} + \dots - 2y - 1)^2$                |
| $c_4, c_5$                     | $y^{66} - 27y^{65} + \dots - 41121383020y + 1336414249$ |
| $c_7$                          | $(y^{33} - 3y^{32} + \dots + 394y - 49)^2$              |
| $c_8, c_9, c_{11}$<br>$c_{12}$ | $y^{66} + 40y^{65} + \dots + 20y + 1$                   |
| $c_{10}$                       | $(y^{33} - 10y^{32} + \dots - 2y - 1)^2$                |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -1.014300 + 0.118417I$ |                                       |                       |
| $a = -0.596166 + 1.043440I$ | $-6.89406 + 3.13953I$                 | $-4.34254 - 5.36114I$ |
| $b = 0.645673 + 1.202080I$  |                                       |                       |
| $u = -1.014300 + 0.118417I$ |                                       |                       |
| $a = -0.27011 - 1.48522I$   | $-6.89406 + 3.13953I$                 | $-4.34254 - 5.36114I$ |
| $b = 0.36912 - 1.44230I$    |                                       |                       |
| $u = -1.014300 - 0.118417I$ |                                       |                       |
| $a = -0.596166 - 1.043440I$ | $-6.89406 - 3.13953I$                 | $-4.34254 + 5.36114I$ |
| $b = 0.645673 - 1.202080I$  |                                       |                       |
| $u = -1.014300 - 0.118417I$ |                                       |                       |
| $a = -0.27011 + 1.48522I$   | $-6.89406 - 3.13953I$                 | $-4.34254 + 5.36114I$ |
| $b = 0.36912 + 1.44230I$    |                                       |                       |
| $u = -0.877024 + 0.414488I$ |                                       |                       |
| $a = -0.765285 + 0.116859I$ | $-0.262282 - 0.735872I$               | $3.32687 - 0.76984I$  |
| $b = 0.627802 + 0.626194I$  |                                       |                       |
| $u = -0.877024 + 0.414488I$ |                                       |                       |
| $a = 0.41594 - 1.75908I$    | $-0.262282 - 0.735872I$               | $3.32687 - 0.76984I$  |
| $b = -0.030432 - 1.353230I$ |                                       |                       |
| $u = -0.877024 - 0.414488I$ |                                       |                       |
| $a = -0.765285 - 0.116859I$ | $-0.262282 + 0.735872I$               | $3.32687 + 0.76984I$  |
| $b = 0.627802 - 0.626194I$  |                                       |                       |
| $u = -0.877024 - 0.414488I$ |                                       |                       |
| $a = 0.41594 + 1.75908I$    | $-0.262282 + 0.735872I$               | $3.32687 + 0.76984I$  |
| $b = -0.030432 + 1.353230I$ |                                       |                       |
| $u = 1.039060 + 0.162429I$  |                                       |                       |
| $a = -0.558017 - 0.929889I$ | $-1.75770 - 6.51294I$                 | $1.10617 + 5.98872I$  |
| $b = 0.726138 - 1.167780I$  |                                       |                       |
| $u = 1.039060 + 0.162429I$  |                                       |                       |
| $a = -0.16397 + 1.48174I$   | $-1.75770 - 6.51294I$                 | $1.10617 + 5.98872I$  |
| $b = 0.32713 + 1.50533I$    |                                       |                       |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = 1.039060 - 0.162429I$<br>$a = -0.558017 + 0.929889I$<br>$b = 0.726138 + 1.167780I$  | $-1.75770 + 6.51294I$                 | $1.10617 - 5.98872I$ |
| $u = 1.039060 - 0.162429I$<br>$a = -0.16397 - 1.48174I$<br>$b = 0.32713 - 1.50533I$      | $-1.75770 + 6.51294I$                 | $1.10617 - 5.98872I$ |
| $u = 0.705062 + 0.789522I$<br>$a = 0.921945 + 0.609371I$<br>$b = 0.205194 + 0.949502I$   | $-0.79038 + 2.85888I$                 | $4.03469 - 3.31371I$ |
| $u = 0.705062 + 0.789522I$<br>$a = 0.279153 + 1.164250I$<br>$b = -0.331425 + 0.163823I$  | $-0.79038 + 2.85888I$                 | $4.03469 - 3.31371I$ |
| $u = 0.705062 - 0.789522I$<br>$a = 0.921945 - 0.609371I$<br>$b = 0.205194 - 0.949502I$   | $-0.79038 - 2.85888I$                 | $4.03469 + 3.31371I$ |
| $u = 0.705062 - 0.789522I$<br>$a = 0.279153 - 1.164250I$<br>$b = -0.331425 - 0.163823I$  | $-0.79038 - 2.85888I$                 | $4.03469 + 3.31371I$ |
| $u = -0.752029 + 0.757937I$<br>$a = 0.361706 - 0.918628I$<br>$b = -0.050445 - 0.404144I$ | $0.112103 + 0.911954I$                | $6.34870 - 3.13722I$ |
| $u = -0.752029 + 0.757937I$<br>$a = 0.652021 - 0.835679I$<br>$b = 0.041525 - 0.735838I$  | $0.112103 + 0.911954I$                | $6.34870 - 3.13722I$ |
| $u = -0.752029 - 0.757937I$<br>$a = 0.361706 + 0.918628I$<br>$b = -0.050445 + 0.404144I$ | $0.112103 - 0.911954I$                | $6.34870 + 3.13722I$ |
| $u = -0.752029 - 0.757937I$<br>$a = 0.652021 + 0.835679I$<br>$b = 0.041525 + 0.735838I$  | $0.112103 - 0.911954I$                | $6.34870 + 3.13722I$ |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|--|---------------------------------------|---------------------|
| $u = 0.930115$<br>$a = -0.65592 + 1.44435I$<br>$b = 0.432557 + 1.249530I$                | -5.02884                              | -0.712880           |
| $u = 0.930115$<br>$a = -0.65592 - 1.44435I$<br>$b = 0.432557 - 1.249530I$                | -5.02884                              | -0.712880           |
| $u = 0.906723 + 0.575511I$<br>$a = 0.56023 + 1.45906I$<br>$b = -0.247726 + 1.300990I$    | -4.48415 - 2.21654I                   | -2.16344 + 2.48417I |
| $u = 0.906723 + 0.575511I$<br>$a = -0.298340 + 0.110070I$<br>$b = 0.738659 - 0.257328I$  | -4.48415 - 2.21654I                   | -2.16344 + 2.48417I |
| $u = 0.906723 - 0.575511I$<br>$a = 0.56023 - 1.45906I$<br>$b = -0.247726 - 1.300990I$    | -4.48415 + 2.21654I                   | -2.16344 - 2.48417I |
| $u = 0.906723 - 0.575511I$<br>$a = -0.298340 - 0.110070I$<br>$b = 0.738659 + 0.257328I$  | -4.48415 + 2.21654I                   | -2.16344 - 2.48417I |
| $u = -0.703249 + 0.821130I$<br>$a = 0.928128 - 0.470465I$<br>$b = 0.289870 - 0.987370I$  | 4.82578 - 6.26770I                    | 8.18982 + 3.24511I  |
| $u = -0.703249 + 0.821130I$<br>$a = 0.334947 - 1.220330I$<br>$b = -0.469566 - 0.167548I$ | 4.82578 - 6.26770I                    | 8.18982 + 3.24511I  |
| $u = -0.703249 - 0.821130I$<br>$a = 0.928128 + 0.470465I$<br>$b = 0.289870 + 0.987370I$  | 4.82578 + 6.26770I                    | 8.18982 - 3.24511I  |
| $u = -0.703249 - 0.821130I$<br>$a = 0.334947 + 1.220330I$<br>$b = -0.469566 + 0.167548I$ | 4.82578 + 6.26770I                    | 8.18982 - 3.24511I  |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = 0.789844 + 0.799846I$<br>$a = 0.487617 + 1.144040I$<br>$b = -0.453252 + 0.597917I$    | $6.34781 - 3.04389I$                  | $9.82618 + 2.90426I$ |
| $u = 0.789844 + 0.799846I$<br>$a = 0.532299 + 0.438608I$<br>$b = 0.437352 + 0.665590I$     | $6.34781 - 3.04389I$                  | $9.82618 + 2.90426I$ |
| $u = 0.789844 - 0.799846I$<br>$a = 0.487617 - 1.144040I$<br>$b = -0.453252 - 0.597917I$    | $6.34781 + 3.04389I$                  | $9.82618 - 2.90426I$ |
| $u = 0.789844 - 0.799846I$<br>$a = 0.532299 - 0.438608I$<br>$b = 0.437352 - 0.665590I$     | $6.34781 + 3.04389I$                  | $9.82618 - 2.90426I$ |
| $u = -0.963141 + 0.632636I$<br>$a = 0.50716 - 1.36612I$<br>$b = -0.397323 - 1.338550I$     | $-1.26824 + 5.40417I$                 | $2.83191 - 6.21521I$ |
| $u = -0.963141 + 0.632636I$<br>$a = -0.1053880 - 0.0161506I$<br>$b = 0.924735 + 0.119912I$ | $-1.26824 + 5.40417I$                 | $2.83191 - 6.21521I$ |
| $u = -0.963141 - 0.632636I$<br>$a = 0.50716 + 1.36612I$<br>$b = -0.397323 + 1.338550I$     | $-1.26824 - 5.40417I$                 | $2.83191 + 6.21521I$ |
| $u = -0.963141 - 0.632636I$<br>$a = -0.1053880 + 0.0161506I$<br>$b = 0.924735 - 0.119912I$ | $-1.26824 - 5.40417I$                 | $2.83191 + 6.21521I$ |
| $u = -0.600852 + 0.549903I$<br>$a = -0.86327 - 1.33884I$<br>$b = 0.064649 + 0.491972I$     | $-0.353626 - 0.577287I$               | $5.08869 + 0.00847I$ |
| $u = -0.600852 + 0.549903I$<br>$a = 1.59685 - 1.66405I$<br>$b = -0.006019 - 1.152790I$     | $-0.353626 - 0.577287I$               | $5.08869 + 0.00847I$ |



| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = -0.600852 - 0.549903I$<br>$a = -0.86327 + 1.33884I$<br>$b = 0.064649 - 0.491972I$    | $-0.353626 + 0.577287I$               | $5.08869 - 0.00847I$ |
| $u = -0.600852 - 0.549903I$<br>$a = 1.59685 + 1.66405I$<br>$b = -0.006019 + 1.152790I$    | $-0.353626 + 0.577287I$               | $5.08869 - 0.00847I$ |
| $u = -0.965280 + 0.710510I$<br>$a = 0.510940 - 1.295900I$<br>$b = -0.559425 - 1.254120I$  | $-0.54191 + 4.66940I$                 | $4.86326 - 2.61989I$ |
| $u = -0.965280 + 0.710510I$<br>$a = 0.0753159 - 0.0333818I$<br>$b = 0.986366 - 0.117562I$ | $-0.54191 + 4.66940I$                 | $4.86326 - 2.61989I$ |
| $u = -0.965280 - 0.710510I$<br>$a = 0.510940 + 1.295900I$<br>$b = -0.559425 + 1.254120I$  | $-0.54191 - 4.66940I$                 | $4.86326 + 2.61989I$ |
| $u = -0.965280 - 0.710510I$<br>$a = 0.0753159 + 0.0333818I$<br>$b = 0.986366 + 0.117562I$ | $-0.54191 - 4.66940I$                 | $4.86326 + 2.61989I$ |
| $u = 0.950716 + 0.751979I$<br>$a = 0.514981 + 1.266800I$<br>$b = -0.637045 + 1.165010I$   | $5.85251 - 2.78863I$                  | $8.90822 + 2.57820I$ |
| $u = 0.950716 + 0.751979I$<br>$a = 0.171542 + 0.057779I$<br>$b = 0.975434 + 0.264829I$    | $5.85251 - 2.78863I$                  | $8.90822 + 2.57820I$ |
| $u = 0.950716 - 0.751979I$<br>$a = 0.514981 - 1.266800I$<br>$b = -0.637045 - 1.165010I$   | $5.85251 + 2.78863I$                  | $8.90822 - 2.57820I$ |
| $u = 0.950716 - 0.751979I$<br>$a = 0.171542 - 0.057779I$<br>$b = 0.975434 - 0.264829I$    | $5.85251 + 2.78863I$                  | $8.90822 - 2.57820I$ |

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = 0.998168 + 0.717071I$<br>$a = 0.488348 + 1.291390I$<br>$b = -0.61319 + 1.32172I$     | $-1.67944 - 8.54919I$                 | $2.18347 + 8.15424I$ |
| $u = 0.998168 + 0.717071I$<br>$a = 0.0890290 - 0.0366137I$<br>$b = 1.095340 + 0.109793I$  | $-1.67944 - 8.54919I$                 | $2.18347 + 8.15424I$ |
| $u = 0.998168 - 0.717071I$<br>$a = 0.488348 - 1.291390I$<br>$b = -0.61319 - 1.32172I$     | $-1.67944 + 8.54919I$                 | $2.18347 - 8.15424I$ |
| $u = 0.998168 - 0.717071I$<br>$a = 0.0890290 + 0.0366137I$<br>$b = 1.095340 - 0.109793I$  | $-1.67944 + 8.54919I$                 | $2.18347 - 8.15424I$ |
| $u = -1.009690 + 0.731074I$<br>$a = 0.482190 - 1.282250I$<br>$b = -0.65913 - 1.33376I$    | $3.89061 + 12.09090I$                 | $6.43573 - 8.11579I$ |
| $u = -1.009690 + 0.731074I$<br>$a = 0.1161080 + 0.0594886I$<br>$b = 1.144140 - 0.142559I$ | $3.89061 + 12.09090I$                 | $6.43573 - 8.11579I$ |
| $u = -1.009690 - 0.731074I$<br>$a = 0.482190 + 1.282250I$<br>$b = -0.65913 + 1.33376I$    | $3.89061 - 12.09090I$                 | $6.43573 + 8.11579I$ |
| $u = -1.009690 - 0.731074I$<br>$a = 0.1161080 - 0.0594886I$<br>$b = 1.144140 + 0.142559I$ | $3.89061 - 12.09090I$                 | $6.43573 + 8.11579I$ |
| $u = -0.129012 + 0.620035I$<br>$a = 1.84776 - 3.41708I$<br>$b = -0.226286 + 0.961189I$    | $1.97739 + 4.07711I$                  | $8.72201 - 3.88410I$ |
| $u = -0.129012 + 0.620035I$<br>$a = 3.72482 + 1.42811I$<br>$b = -0.141514 - 1.121170I$    | $1.97739 + 4.07711I$                  | $8.72201 - 3.88410I$ |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.129012 - 0.620035I$ |                                       |                      |
| $a = 1.84776 + 3.41708I$    | $1.97739 - 4.07711I$                  | $8.72201 + 3.88410I$ |
| $b = -0.226286 - 0.961189I$ |                                       |                      |
| $u = -0.129012 - 0.620035I$ |                                       |                      |
| $a = 3.72482 - 1.42811I$    | $1.97739 - 4.07711I$                  | $8.72201 + 3.88410I$ |
| $b = -0.141514 + 1.121170I$ |                                       |                      |
| $u = 0.159946 + 0.484229I$  |                                       |                      |
| $a = 1.35528 + 5.45781I$    | $-3.28246 - 1.28200I$                 | $3.99671 + 5.16805I$ |
| $b = -0.128533 - 0.930176I$ |                                       |                      |
| $u = 0.159946 + 0.484229I$  |                                       |                      |
| $a = 5.82216 - 0.87708I$    | $-3.28246 - 1.28200I$                 | $3.99671 + 5.16805I$ |
| $b = -0.080363 + 1.085080I$ |                                       |                      |
| $u = 0.159946 - 0.484229I$  |                                       |                      |
| $a = 1.35528 - 5.45781I$    | $-3.28246 + 1.28200I$                 | $3.99671 - 5.16805I$ |
| $b = -0.128533 + 0.930176I$ |                                       |                      |
| $u = 0.159946 - 0.484229I$  |                                       |                      |
| $a = 5.82216 + 0.87708I$    | $-3.28246 + 1.28200I$                 | $3.99671 - 5.16805I$ |
| $b = -0.080363 - 1.085080I$ |                                       |                      |

$$\text{III. } I_3^u = \langle b - a - 1, a^2 + a + 2, u - 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ a + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ a - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a - 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ a + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ a + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -a - 1 \\ -1 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes = -2**

(iv) **u**-Polynomials at the component

| Crossings                      | <b>u</b> -Polynomials at each crossing |
|--------------------------------|--|
| $c_1, c_{10}$                  | $(u - 1)^2$                            |
| $c_2, c_3, c_4$<br>$c_5, c_6$  | $(u + 1)^2$                            |
| $c_7$                          | $u^2$                                  |
| $c_8, c_9, c_{11}$<br>$c_{12}$ | $u^2 + u + 2$                          |

(v) Riley Polynomials at the component

| Crossings                                      | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_3$<br>$c_4, c_5, c_6$<br>$c_{10}$ | $(y - 1)^2$                        |
| $c_7$  | $y^2$                              |
| $c_8, c_9, c_{11}$<br>$c_{12}$                 | $y^2 + 3y + 4$                     |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.00000$<br>$a = -0.50000 + 1.32288I$<br>$b = 0.50000 + 1.32288I$ | -4.93480                              | -2.00000   |
| $u = 1.00000$<br>$a = -0.50000 - 1.32288I$<br>$b = 0.50000 - 1.32288I$ | -4.93480                              | -2.00000   |

$$\text{IV. } I_4^u = \langle b - u, a - 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u + 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2 \\ 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u + 1 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2 \\ 2u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0



(iv) u-Polynomials at the component

| Crossings                              | u-Polynomials at each crossing |
|--|--------------------------------|
| $c_1, c_2, c_3$                        | $(u + 1)^2$                    |
| $c_4$                                  | $u^2 + 2u + 2$                 |
| $c_5$                                  | $u^2 - 2u + 2$                 |
| $c_6$                                  | $(u - 1)^2$                    |
| $c_7$                                  | $u^2$                          |
| $c_8, c_9, c_{10}$<br>$c_{11}, c_{12}$ | $u^2 + 1$                      |

(v) Riley Polynomials at the component

| Crossings                              | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_3$<br>$c_6$               | $(y - 1)^2$                        |
| $c_4, c_5$                             | $y^2 + 4$                          |
| $c_7$                                  | $y^2$                              |
| $c_8, c_9, c_{10}$<br>$c_{11}, c_{12}$ | $(y + 1)^2$                        |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_4^u$ |              | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|--------------|---------------------------------------|------------|
| $u =$                | $1.000000I$  |                                       |            |
| $a =$                | $1.00000$    | $-1.64493$                            | $0$        |
| $b =$                | $1.000000I$  |                                       |            |
| $u =$                | $-1.000000I$ |                                       |            |
| $a =$                | $1.00000$    | $-1.64493$                            | $0$        |
| $b =$                | $-1.000000I$ |                                       |            |

$$\mathbf{V. } I_1^v = \langle a, b + 1, 32v^5 + 16v^4 + 16v^3 + 4v^2 + 2v + 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2v \\ v \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2v \\ -v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 4v^2 \\ -2v^2 - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -16v^4 \\ -8v^4 - 4v^2 - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -16v^4 \\ 8v^4 + 4v^2 + 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $64v^4 + 32v^3 + 33v^2 + 10$**

(iv) u-Polynomials at the component

| Crossings        | u-Polynomials at each crossing              |
|------------------|---|
| $c_1$            | $u^5 + u^4 + 2u^3 + u^2 + u + 1$            |
| $c_2, c_3$       | $u^5 - u^4 - 2u^3 + u^2 + u + 1$            |
| $c_4$            | $32(32u^5 - 16u^4 + 16u^3 - 4u^2 + 2u - 1)$ |
| $c_5$            | $32(32u^5 + 16u^4 + 16u^3 + 4u^2 + 2u + 1)$ |
| $c_6$            | $u^5 + u^4 - 2u^3 - u^2 + u - 1$            |
| $c_7$            | $u^5 - 3u^4 + 4u^3 - u^2 - u + 1$           |
| $c_8, c_9$       | $(u + 1)^5$                                 |
| $c_{10}$         | $u^5$                                       |
| $c_{11}, c_{12}$ | $(u - 1)^5$                                 |

(v) Riley Polynomials at the component

| Crossings                      | Riley Polynomials at each crossing                 |
|--------------------------------|--|
| $c_1$                          | $y^5 + 3y^4 + 4y^3 + y^2 - y - 1$                  |
| $c_2, c_3, c_6$                | $y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$                 |
| $c_4, c_5$                     | $1024(1024y^5 + 768y^4 + 256y^3 + 16y^2 - 4y - 1)$ |
| $c_7$                          | $y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$                 |
| $c_8, c_9, c_{11}$<br>$c_{12}$ | $(y - 1)^5$  |
| $c_{10}$                       | $y^5$  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^v$                                     | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $v = -0.227849 + 0.600076I$<br>$a = 0$<br>$b = -1.00000$ | $7.51750 + 4.40083I$                  | $8.62066 - 2.16111I$ |
| $v = -0.227849 - 0.600076I$<br>$a = 0$<br>$b = -1.00000$ | $7.51750 - 4.40083I$                  | $8.62066 + 2.16111I$ |
| $v = 0.169555 + 0.411188I$<br>$a = 0$<br>$b = -1.00000$  | $1.97403 - 1.53058I$                  | $2.78903 + 1.00704I$ |
| $v = 0.169555 - 0.411188I$<br>$a = 0$<br>$b = -1.00000$  | $1.97403 + 1.53058I$                  | $2.78903 - 1.00704I$ |
| $v = -0.383413$<br>$a = 0$<br>$b = -1.00000$             | 4.04602                               | 14.4310              |

## VI. u-Polynomials

| Crossings        | u-Polynomials at each crossing  |
|------------------|---|
| $c_1$            | $(u-1)^2(u+1)^2(u^5+u^4+2u^3+u^2+u+1)$ $\cdot ((u^{33}-6u^{32}+\dots+128u-23)^2)(u^{42}-10u^{41}+\dots-11111u+1504)$              |
| $c_2, c_3$       | $((u+1)^4)(u^5-u^4+\dots+u+1)(u^{33}-2u^{32}+\dots+u^2+1)^2$ $\cdot (u^{42}-2u^{41}+\dots+7u-4)$                                  |
| $c_4$            | $1024(u+1)^2(u^2+2u+2)(32u^5-16u^4+16u^3-4u^2+2u-1)$ $\cdot (32u^{42}+48u^{41}+\dots+20u^2+2)(u^{66}-u^{65}+\dots-115818u+36557)$ |
| $c_5$            | $1024(u+1)^2(u^2-2u+2)(32u^5+16u^4+16u^3+4u^2+2u+1)$ $\cdot (32u^{42}+48u^{41}+\dots+20u^2+2)(u^{66}-u^{65}+\dots-115818u+36557)$ |
| $c_6$            | $(u-1)^2(u+1)^2(u^5+u^4-2u^3-u^2+u-1)$ $\cdot ((u^{33}-2u^{32}+\dots+u^2+1)^2)(u^{42}-2u^{41}+\dots+7u-4)$                        |
| $c_7$            | $u^4(u^5-3u^4+\dots-u+1)(u^{33}+3u^{32}+\dots+32u+7)^2$ $\cdot (u^{42}-2u^{40}+\dots+1136u-448)$                                  |
| $c_8, c_9$       | $((u+1)^5)(u^2+1)(u^2+u+2)(u^{42}-5u^{41}+\dots-u-1)$ $\cdot (u^{66}+10u^{65}+\dots+4u+1)$  |
| $c_{10}$         | $u^5(u-1)^2(u^2+1)(u^{33}+2u^{32}+\dots-2u-1)^2$ $\cdot (u^{42}-3u^{41}+\dots-7680u+2048)$  |
| $c_{11}, c_{12}$ | $((u-1)^5)(u^2+1)(u^2+u+2)(u^{42}-5u^{41}+\dots-u-1)$ $\cdot (u^{66}+10u^{65}+\dots+4u+1)$  |



## VII. Riley Polynomials

| Crossings                      | Riley Polynomials at each crossing   |
|--------------------------------|--|
| $c_1$                          | $(y-1)^4(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)$ $\cdot (y^{33} + 14y^{32} + \dots - 2062y - 529)^2$ $\cdot (y^{42} + 14y^{41} + \dots + 62115215y + 2262016)$                         |
| $c_2, c_3, c_6$                | $((y-1)^4)(y^5 - 5y^4 + \dots - y - 1)(y^{33} - 30y^{32} + \dots - 2y - 1)^2$ $\cdot (y^{42} - 38y^{41} + \dots - y + 16)$   |
| $c_4, c_5$                     | $1048576(y-1)^2(y^2 + 4)(1024y^5 + 768y^4 + \dots - 4y - 1)$ $\cdot (1024y^{42} - 1280y^{41} + \dots + 80y + 4)$ $\cdot (y^{66} - 27y^{65} + \dots - 41121383020y + 1336414249)$ |
| $c_7$                          | $y^4(y^5 - y^4 + \dots + 3y - 1)(y^{33} - 3y^{32} + \dots + 394y - 49)^2$ $\cdot (y^{42} - 4y^{41} + \dots - 2874624y + 200704)$   |
| $c_8, c_9, c_{11}$<br>$c_{12}$ | $((y-1)^5)(y+1)^2(y^2 + 3y + 4)(y^{42} + 17y^{41} + \dots + 9y + 1)$ $\cdot (y^{66} + 40y^{65} + \dots + 20y + 1)$   |
| $c_{10}$                       | $y^5(y-1)^2(y+1)^2(y^{33} - 10y^{32} + \dots - 2y - 1)^2$ $\cdot (y^{42} - 9y^{41} + \dots - 69468160y + 4194304)$   |