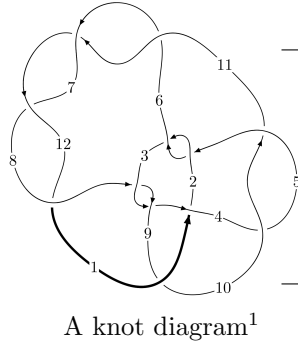
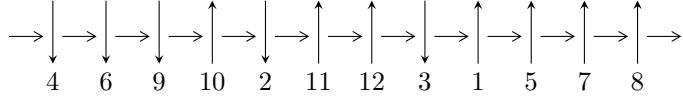


12a<sub>0916</sub> (K12a<sub>0916</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$7, 11 \xrightarrow{c_{11}} 12 \xrightarrow{c_7} 3, 8 \xrightarrow{c_8} 9 \xrightarrow{c_3} 4 \xrightarrow{c_{12}} 1 \xrightarrow{c_6} 6 \xrightarrow{c_2} 2 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \rightsquigarrow c_1, c_4, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.91980 \times 10^{108} u^{81} - 4.29606 \times 10^{108} u^{80} + \dots + 1.92612 \times 10^{108} b + 3.19210 \times 10^{108}, \\ - 5.04794 \times 10^{108} u^{81} - 7.50428 \times 10^{108} u^{80} + \dots + 1.92612 \times 10^{108} a - 1.67695 \times 10^{109}, \\ u^{82} + u^{81} + \dots + 10u - 1 \rangle$$

$$I_2^u = \langle -u^{12} + 8u^{10} + 2u^9 - 23u^8 - 10u^7 + 27u^6 + 13u^5 - 11u^4 - u^3 + 4u^2 + b - 1, \\ - 2u^{13} + u^{12} + 20u^{11} - 5u^{10} - 80u^9 + u^8 + 158u^7 + 30u^6 - 150u^5 - 50u^4 + 53u^3 + 23u^2 + a - 4u - 8, \\ u^{14} - 10u^{12} - 2u^{11} + 39u^{10} + 15u^9 - 73u^8 - 40u^7 + 63u^6 + 44u^5 - 17u^4 - 18u^3 - 2u^2 + 4u + 1 \rangle$$

$$I_3^u = \langle u^2 + b, a - 1, u^6 + u^5 - 2u^4 - 2u^3 - 1 \rangle$$

$$I_4^u = \langle b + 1, a - 1, u - 1 \rangle$$

$$I_5^u = \langle b + a - 1, a^2 - a - 1, u - 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 105 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -2.92 \times 10^{108} u^{81} - 4.30 \times 10^{108} u^{80} + \dots + 1.93 \times 10^{108} b + 3.19 \times 10^{108}, -5.05 \times 10^{108} u^{81} - 7.50 \times 10^{108} u^{80} + \dots + 1.93 \times 10^{108} a - 1.68 \times 10^{109}, u^{82} + u^{81} + \dots + 10u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2.62078u^{81} + 3.89606u^{80} + \dots - 39.6810u + 8.70635 \\ 1.51590u^{81} + 2.23043u^{80} + \dots - 9.19417u - 1.65727 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -6.70590u^{81} - 12.1721u^{80} + \dots + 90.0743u - 10.7546 \\ 2.72204u^{81} + 5.57368u^{80} + \dots - 61.2733u + 9.72272 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 6.65029u^{81} + 6.12344u^{80} + \dots - 81.0522u + 16.1926 \\ -3.69683u^{81} - 2.01061u^{80} + \dots + 53.9722u - 8.26479 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 3.92048u^{81} + 5.03730u^{80} + \dots - 55.4423u + 10.6962 \\ 0.216200u^{81} + 1.08919u^{80} + \dots + 6.56719u - 3.64708 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 6.01645u^{81} + 9.73383u^{80} + \dots - 69.8702u + 4.28812 \\ -2.02257u^{81} - 2.95608u^{80} + \dots + 24.6648u - 4.64477 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -7.90580u^{81} - 13.4568u^{80} + \dots + 100.376u - 9.65178 \\ 3.61742u^{81} + 6.47329u^{80} + \dots - 70.8432u + 10.9055 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $36.4294u^{81} + 55.9906u^{80} + \dots - 576.502u + 76.1479$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{82} - 3u^{81} + \dots + 15u - 1$
$c_2, c_5$	$u^{82} + u^{81} + \dots - 138u + 33$
$c_3, c_8$	$u^{82} - 22u^{80} + \dots - 4101u - 607$
$c_4, c_{10}$	$u^{82} + 5u^{81} + \dots + 112u - 8$
$c_6, c_7, c_{11}$ $c_{12}$	$u^{82} + u^{81} + \dots + 10u - 1$
$c_9$	$u^{82} - 2u^{81} + \dots - 24u + 12$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{82} - 13y^{81} + \dots - 27y + 1$
$c_2, c_5$	$y^{82} - 39y^{81} + \dots - 42804y + 1089$
$c_3, c_8$	$y^{82} - 44y^{81} + \dots - 14225097y + 368449$
$c_4, c_{10}$	$y^{82} - 51y^{81} + \dots - 13728y + 64$
$c_6, c_7, c_{11}$ $c_{12}$	$y^{82} - 101y^{81} + \dots - 110y + 1$
$c_9$	$y^{82} - 8y^{81} + \dots - 216y + 144$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.984782 + 0.188624I$ $a = -0.141871 + 0.097301I$ $b = -0.334414 + 0.658720I$	$5.90211 - 2.33787I$	0
$u = -0.984782 - 0.188624I$ $a = -0.141871 - 0.097301I$ $b = -0.334414 - 0.658720I$	$5.90211 + 2.33787I$	0
$u = 0.843614 + 0.550628I$ $a = 0.787898 + 0.115680I$ $b = 0.1163850 - 0.0010731I$	$2.79780 - 0.42396I$	0
$u = 0.843614 - 0.550628I$ $a = 0.787898 - 0.115680I$ $b = 0.1163850 + 0.0010731I$	$2.79780 + 0.42396I$	0
$u = -1.02284$ $a = 1.47383$ $b = -0.331000$	$0.462297$	0
$u = -0.783113 + 0.549508I$ $a = 0.0588211 + 0.1268950I$ $b = -0.86879 - 1.12637I$	$-4.73426 - 7.26403I$	0
$u = -0.783113 - 0.549508I$ $a = 0.0588211 - 0.1268950I$ $b = -0.86879 + 1.12637I$	$-4.73426 + 7.26403I$	0
$u = 0.887115 + 0.337671I$ $a = 0.155583 - 0.193486I$ $b = 1.042270 - 0.535647I$	$-3.35923 + 0.42248I$	0
$u = 0.887115 - 0.337671I$ $a = 0.155583 + 0.193486I$ $b = 1.042270 + 0.535647I$	$-3.35923 - 0.42248I$	0
$u = 0.811426 + 0.677149I$ $a = 0.0288692 + 0.0472312I$ $b = -0.527577 + 1.199900I$	$-0.39025 + 13.28170I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.811426 - 0.677149I$ $a = 0.0288692 - 0.0472312I$ $b = -0.527577 - 1.199900I$	$-0.39025 - 13.28170I$	0
$u = 0.188934 + 0.907176I$ $a = -0.616856 + 0.715162I$ $b = -0.157446 + 0.338454I$	$-2.29134 - 8.09229I$	0
$u = 0.188934 - 0.907176I$ $a = -0.616856 - 0.715162I$ $b = -0.157446 - 0.338454I$	$-2.29134 + 8.09229I$	0
$u = 0.585370 + 0.706438I$ $a = 0.0863636 - 0.0965957I$ $b = 0.083043 - 1.114300I$	$2.00602 + 4.30322I$	0
$u = 0.585370 - 0.706438I$ $a = 0.0863636 + 0.0965957I$ $b = 0.083043 + 1.114300I$	$2.00602 - 4.30322I$	0
$u = -0.795599 + 0.407080I$ $a = -0.817039 + 0.266032I$ $b = -0.02769 - 1.43627I$	$3.45231 - 7.58300I$	0
$u = -0.795599 - 0.407080I$ $a = -0.817039 - 0.266032I$ $b = -0.02769 + 1.43627I$	$3.45231 + 7.58300I$	0
$u = 0.770296 + 0.366086I$ $a = -1.102450 - 0.449931I$ $b = 0.209050 - 0.713360I$	$2.67572 + 6.81110I$	0
$u = 0.770296 - 0.366086I$ $a = -1.102450 + 0.449931I$ $b = 0.209050 + 0.713360I$	$2.67572 - 6.81110I$	0
$u = 1.17627$ $a = 0.260420$ $b = 0.996259$	$-3.39624$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.657045 + 0.470711I$ $a = -0.122567 + 0.464530I$ $b = 0.656971 + 1.206150I$	$-2.18416 - 4.72064I$	0
$u = -0.657045 - 0.470711I$ $a = -0.122567 - 0.464530I$ $b = 0.656971 - 1.206150I$	$-2.18416 + 4.72064I$	0
$u = 0.695887 + 0.178695I$ $a = 0.331121 - 1.049200I$ $b = -1.52202 + 1.38533I$	$-0.296974 + 0.337709I$	$-14.6453 + 19.7980I$
$u = 0.695887 - 0.178695I$ $a = 0.331121 + 1.049200I$ $b = -1.52202 - 1.38533I$	$-0.296974 - 0.337709I$	$-14.6453 - 19.7980I$
$u = -0.561252 + 0.447215I$ $a = -0.597055 - 0.069631I$ $b = 0.304635 + 0.996919I$	$-0.76027 - 3.85816I$	$0. + 6.83350I$
$u = -0.561252 - 0.447215I$ $a = -0.597055 + 0.069631I$ $b = 0.304635 - 0.996919I$	$-0.76027 + 3.85816I$	$0. - 6.83350I$
$u = -0.126025 + 0.701569I$ $a = -0.59662 - 1.32241I$ $b = 0.114296 - 0.377897I$	$-6.70258 + 3.06709I$	$-5.21302 - 2.47341I$
$u = -0.126025 - 0.701569I$ $a = -0.59662 + 1.32241I$ $b = 0.114296 + 0.377897I$	$-6.70258 - 3.06709I$	$-5.21302 + 2.47341I$
$u = -0.236388 + 0.598256I$ $a = 0.294774 - 0.609135I$ $b = 0.426322 + 1.024910I$	$-0.07658 - 4.13532I$	$0.75722 + 4.26107I$
$u = -0.236388 - 0.598256I$ $a = 0.294774 + 0.609135I$ $b = 0.426322 - 1.024910I$	$-0.07658 + 4.13532I$	$0.75722 - 4.26107I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.28955 + 0.58878I$ $a = -0.0523594 + 0.0124131I$ $b = 0.706077 + 0.030045I$	$2.14333 + 2.89478I$	0
$u = -1.28955 - 0.58878I$ $a = -0.0523594 - 0.0124131I$ $b = 0.706077 - 0.030045I$	$2.14333 - 2.89478I$	0
$u = 0.113038 + 0.567992I$ $a = -0.569049 - 0.821467I$ $b = -0.095569 - 0.935559I$	$0.88681 + 4.41440I$	$3.03410 - 4.57971I$
$u = 0.113038 - 0.567992I$ $a = -0.569049 + 0.821467I$ $b = -0.095569 + 0.935559I$	$0.88681 - 4.41440I$	$3.03410 + 4.57971I$
$u = 0.558549 + 0.147764I$ $a = 0.621866 + 0.196056I$ $b = -0.456183 - 0.414679I$	$0.998059 + 0.188402I$	$10.40306 - 0.95041I$
$u = 0.558549 - 0.147764I$ $a = 0.621866 - 0.196056I$ $b = -0.456183 + 0.414679I$	$0.998059 - 0.188402I$	$10.40306 + 0.95041I$
$u = -0.234783 + 0.515407I$ $a = 1.32426 + 1.53813I$ $b = 0.365229 + 0.093260I$	$-3.40619 + 1.28533I$	$-2.46945 + 0.12060I$
$u = -0.234783 - 0.515407I$ $a = 1.32426 - 1.53813I$ $b = 0.365229 - 0.093260I$	$-3.40619 - 1.28533I$	$-2.46945 - 0.12060I$
$u = 0.502065 + 0.126289I$ $a = -2.39872 - 0.92369I$ $b = 0.61945 + 1.69002I$	$-0.834967 + 0.544419I$	$-9.5439 + 23.8545I$
$u = 0.502065 - 0.126289I$ $a = -2.39872 + 0.92369I$ $b = 0.61945 - 1.69002I$	$-0.834967 - 0.544419I$	$-9.5439 - 23.8545I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.284642 + 0.381065I$		
$a = 1.48853 + 0.50264I$	$-1.50630 + 0.84820I$	$-1.82690 - 0.01242I$
$b = 0.008733 - 0.426456I$		
$u = -0.284642 - 0.381065I$		
$a = 1.48853 - 0.50264I$	$-1.50630 - 0.84820I$	$-1.82690 + 0.01242I$
$b = 0.008733 + 0.426456I$		
$u = -1.52579 + 0.01939I$		
$a = -0.08285 + 2.43592I$	$6.46065 - 4.82598I$	0
$b = -0.54993 - 3.11467I$		
$u = -1.52579 - 0.01939I$		
$a = -0.08285 - 2.43592I$	$6.46065 + 4.82598I$	0
$b = -0.54993 + 3.11467I$		
$u = 1.52787 + 0.06405I$		
$a = 0.02483 - 2.22735I$	$5.88122 + 5.76712I$	0
$b = 0.25321 + 2.46288I$		
$u = 1.52787 - 0.06405I$		
$a = 0.02483 + 2.22735I$	$5.88122 - 5.76712I$	0
$b = 0.25321 - 2.46288I$		
$u = 1.54225 + 0.03034I$		
$a = 0.49740 + 1.73264I$	$4.80677 - 0.09764I$	0
$b = -1.12629 - 2.23338I$		
$u = 1.54225 - 0.03034I$		
$a = 0.49740 - 1.73264I$	$4.80677 + 0.09764I$	0
$b = -1.12629 + 2.23338I$		
$u = 0.438034$		
$a = 4.33297$	$-5.42434$	13.3340
$b = 0.243064$		
$u = 1.55488 + 0.14908I$		
$a = -0.15289 - 2.05569I$	$6.30459 + 6.05965I$	0
$b = -0.07056 + 2.52598I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.55488 - 0.14908I$ $a = -0.15289 + 2.05569I$ $b = -0.07056 - 2.52598I$	$6.30459 - 6.05965I$	0
$u = -1.56931 + 0.07915I$ $a = -0.504205 + 1.215630I$ $b = 0.11412 - 1.46849I$	$8.22114 - 1.25008I$	0
$u = -1.56931 - 0.07915I$ $a = -0.504205 - 1.215630I$ $b = 0.11412 + 1.46849I$	$8.22114 + 1.25008I$	0
$u = -1.57829 + 0.02432I$ $a = 0.83255 - 2.02283I$ $b = -0.10047 + 2.25438I$	$6.44108 - 1.01444I$	0
$u = -1.57829 - 0.02432I$ $a = 0.83255 + 2.02283I$ $b = -0.10047 - 2.25438I$	$6.44108 + 1.01444I$	0
$u = 1.59304 + 0.13349I$ $a = 0.48960 - 2.30928I$ $b = -1.09569 + 3.07315I$	$5.44937 + 6.93869I$	0
$u = 1.59304 - 0.13349I$ $a = 0.48960 + 2.30928I$ $b = -1.09569 - 3.07315I$	$5.44937 - 6.93869I$	0
$u = -1.61613 + 0.05731I$ $a = -0.86864 - 2.17772I$ $b = 1.34031 + 2.38505I$	$7.71340 - 1.27145I$	0
$u = -1.61613 - 0.05731I$ $a = -0.86864 + 2.17772I$ $b = 1.34031 - 2.38505I$	$7.71340 + 1.27145I$	0
$u = -1.60197 + 0.23933I$ $a = -0.21626 + 1.64990I$ $b = -0.42879 - 2.17532I$	$9.34734 - 7.89119I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.60197 - 0.23933I$ $a = -0.21626 - 1.64990I$ $b = -0.42879 + 2.17532I$	$9.34734 + 7.89119I$	0
$u = -1.62865 + 0.10885I$ $a = -0.27752 + 1.88885I$ $b = 0.60651 - 2.82092I$	$10.91440 - 8.63897I$	0
$u = -1.62865 - 0.10885I$ $a = -0.27752 - 1.88885I$ $b = 0.60651 + 2.82092I$	$10.91440 + 8.63897I$	0
$u = 1.63599 + 0.11853I$ $a = 0.13839 + 1.88321I$ $b = 0.63901 - 2.35405I$	$11.7947 + 9.5991I$	0
$u = 1.63599 - 0.11853I$ $a = 0.13839 - 1.88321I$ $b = 0.63901 + 2.35405I$	$11.7947 - 9.5991I$	0
$u = 1.63569 + 0.16394I$ $a = -0.60372 + 1.93511I$ $b = 1.25447 - 2.32571I$	$3.49190 + 9.98671I$	0
$u = 1.63569 - 0.16394I$ $a = -0.60372 - 1.93511I$ $b = 1.25447 + 2.32571I$	$3.49190 - 9.98671I$	0
$u = -1.64218 + 0.10635I$ $a = 1.02828 + 1.40183I$ $b = -1.70059 - 1.85899I$	$5.25941 - 2.18573I$	0
$u = -1.64218 - 0.10635I$ $a = 1.02828 - 1.40183I$ $b = -1.70059 + 1.85899I$	$5.25941 + 2.18573I$	0
$u = 1.64631 + 0.13035I$ $a = -0.166642 - 1.110980I$ $b = -0.64066 + 1.48754I$	$10.14690 + 2.43534I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.64631 - 0.13035I$ $a = -0.166642 + 1.110980I$ $b = -0.64066 - 1.48754I$	$10.14690 - 2.43534I$	0
$u = -1.64774 + 0.20688I$ $a = -0.28445 - 1.94616I$ $b = 1.02920 + 2.54457I$	$7.8970 - 16.6675I$	0
$u = -1.64774 - 0.20688I$ $a = -0.28445 + 1.94616I$ $b = 1.02920 - 2.54457I$	$7.8970 + 16.6675I$	0
$u = -1.65858 + 0.12298I$ $a = 0.110901 - 1.131240I$ $b = -0.41531 + 1.65555I$	$11.51240 - 2.00269I$	0
$u = -1.65858 - 0.12298I$ $a = 0.110901 + 1.131240I$ $b = -0.41531 - 1.65555I$	$11.51240 + 2.00269I$	0
$u = 1.68232 + 0.02867I$ $a = -0.34423 - 1.51184I$ $b = 0.47995 + 2.19462I$	$15.2504 + 3.0857I$	0
$u = 1.68232 - 0.02867I$ $a = -0.34423 + 1.51184I$ $b = 0.47995 - 2.19462I$	$15.2504 - 3.0857I$	0
$u = -0.232323 + 0.118937I$ $a = 2.05401 + 1.65947I$ $b = 0.558019 + 0.573483I$	$-1.47682 - 0.41930I$	$-7.12572 - 0.42040I$
$u = -0.232323 - 0.118937I$ $a = 2.05401 - 1.65947I$ $b = 0.558019 - 0.573483I$	$-1.47682 + 0.41930I$	$-7.12572 + 0.42040I$
$u = 0.139756 + 0.051773I$ $a = 5.40801 + 1.65564I$ $b = -0.39225 + 1.47645I$	$0.34771 - 4.65375I$	$6.29780 + 2.05720I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.139756 - 0.051773I$	$0.34771 + 4.65375I$	$6.29780 - 2.05720I$
$a = 5.40801 - 1.65564I$		
$b = -0.39225 - 1.47645I$		
$u = 1.88800$	14.6724	0
$a = 0.440654$		
$b = -0.742379$		

**II.**

$$I_2^u = \langle -u^{12} + 8u^{10} + \dots + b - 1, -2u^{13} + u^{12} + \dots + a - 8, u^{14} - 10u^{12} + \dots + 4u + 1 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u^{13} - u^{12} + \dots + 4u + 8 \\ u^{12} - 8u^{10} - 2u^9 + 23u^8 + 10u^7 - 27u^6 - 13u^5 + 11u^4 + u^3 - 4u^2 + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 3u^{13} - u^{12} + \dots + 6u + 11 \\ -u^{12} - u^{11} + \dots + u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{13} + 11u^{11} + \dots + 19u^2 - 6 \\ -u^{13} + 9u^{11} + \dots + 4u^2 + 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^{13} - 20u^{11} + \dots + 2u + 8 \\ -u^7 + 5u^5 + 2u^4 - 7u^3 - 5u^2 + 2u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -4u^{13} + 40u^{11} + \dots - 2u - 15 \\ -u^{13} + 9u^{11} + \dots + 7u^2 - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 3u^{13} - 2u^{12} + \dots + 7u + 13 \\ u^3 - 2u \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes** =  $-5u^{13} + 6u^{12} + 53u^{11} - 42u^{10} - 226u^9 + 93u^8 + 475u^7 - 51u^6 - 478u^5 - 45u^4 + 177u^3 + 40u^2 - 9u - 18$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{14} - 5u^{13} + \dots + 8u - 1$
$c_2$	$u^{14} + 6u^{13} + \dots + 6u + 1$
$c_3$	$u^{14} - 3u^{12} - u^{11} + u^{10} + 2u^9 + 4u^8 - 4u^6 - u^5 - u^4 + u^3 + 3u^2 - 1$
$c_4$	$u^{14} - 3u^{12} + u^{11} + u^{10} - u^9 + 4u^8 - 4u^6 + 2u^5 - u^4 - u^3 + 3u^2 - 1$
$c_5$	$u^{14} - 6u^{13} + \dots - 6u + 1$
$c_6, c_7$	$u^{14} - 10u^{12} + \dots - 4u + 1$
$c_8$	$u^{14} - 3u^{12} + u^{11} + u^{10} - 2u^9 + 4u^8 - 4u^6 + u^5 - u^4 - u^3 + 3u^2 - 1$
$c_9$	$u^{14} - 3u^{13} + \dots + 9u + 5$
$c_{10}$	$u^{14} - 3u^{12} - u^{11} + u^{10} + u^9 + 4u^8 - 4u^6 - 2u^5 - u^4 + u^3 + 3u^2 - 1$
$c_{11}, c_{12}$	$u^{14} - 10u^{12} + \dots + 4u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{14} - 7y^{13} + \dots - 16y + 1$
$c_2, c_5$	$y^{14} - 14y^{13} + \dots - 14y + 1$
$c_3, c_8$	$y^{14} - 6y^{13} + \dots - 6y + 1$
$c_4, c_{10}$	$y^{14} - 6y^{13} + \dots - 6y + 1$
$c_6, c_7, c_{11}$ $c_{12}$	$y^{14} - 20y^{13} + \dots - 20y + 1$
$c_9$	$y^{14} - 9y^{13} + \dots - 381y + 25$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.22387$ $a = 0.572038$ $b = 0.757485$	-2.53458	6.54520
$u = -1.162790 + 0.439090I$ $a = 0.523471 - 0.653534I$ $b = -0.040336 + 0.575626I$	$2.80440 + 2.09868I$	$6.54061 - 1.90346I$
$u = -1.162790 - 0.439090I$ $a = 0.523471 + 0.653534I$ $b = -0.040336 - 0.575626I$	$2.80440 - 2.09868I$	$6.54061 + 1.90346I$
$u = 0.596998 + 0.186070I$ $a = 1.073280 + 0.589812I$ $b = 0.271776 - 1.277540I$	$-0.545174 + 0.639000I$	$3.99401 + 1.44845I$
$u = 0.596998 - 0.186070I$ $a = 1.073280 - 0.589812I$ $b = 0.271776 + 1.277540I$	$-0.545174 - 0.639000I$	$3.99401 - 1.44845I$
$u = -0.325168 + 0.425935I$ $a = -0.322223 + 0.016593I$ $b = 0.09995 + 1.63147I$	$0.08308 - 5.23699I$	$1.10474 + 13.13886I$
$u = -0.325168 - 0.425935I$ $a = -0.322223 - 0.016593I$ $b = 0.09995 - 1.63147I$	$0.08308 + 5.23699I$	$1.10474 - 13.13886I$
$u = 1.51899$ $a = 1.45349$ $b = -2.86372$	0.601067	-4.00870
$u = 1.54617 + 0.13024I$ $a = -0.06551 - 2.57810I$ $b = -0.34874 + 3.21051I$	$6.64288 + 7.22347I$	$7.90690 - 8.98242I$
$u = 1.54617 - 0.13024I$ $a = -0.06551 + 2.57810I$ $b = -0.34874 - 3.21051I$	$6.64288 - 7.22347I$	$7.90690 + 8.98242I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.59813 + 0.06557I$ $a = 0.15257 + 1.71766I$ $b = -0.75191 - 2.00442I$	$7.12099 - 1.61991I$	$3.99923 - 0.01293I$
$u = -1.59813 - 0.06557I$ $a = 0.15257 - 1.71766I$ $b = -0.75191 + 2.00442I$	$7.12099 + 1.61991I$	$3.99923 + 0.01293I$
$u = -0.270493$ $a = 6.33895$ $b = 0.754277$	$-5.70613$	$-15.7570$
$u = 1.86121$ $a = -0.0876364$ $b = -0.109531$	$14.9057$	$23.1290$

$$\text{III. } I_3^u = \langle u^2 + b, a - 1, u^6 + u^5 - 2u^4 - 2u^3 - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^5 - 2u^3 + u - 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 - 2u^3 + u \\ 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^6 + u^5 - 2u^3 + 2u^2 - 4u + 1$
$c_2, c_5, c_9$	$u^6 - 5u^4 - 2u^3 + 4u^2 - 3$
$c_3, c_6, c_7$ $c_8, c_{11}, c_{12}$	$u^6 + u^5 - 2u^4 - 2u^3 - 1$
$c_4, c_{10}$	$(u - 1)^6$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^6 - y^5 + 8y^4 + 6y^3 - 12y^2 - 12y + 1$
$c_2, c_5, c_9$	$y^6 - 10y^5 + 33y^4 - 50y^3 + 46y^2 - 24y + 9$
$c_3, c_6, c_7$ $c_8, c_{11}, c_{12}$	$y^6 - 5y^5 + 8y^4 - 6y^3 + 4y^2 + 1$
$c_4, c_{10}$	$(y - 1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.819901 + 0.541369I$ $a = 1.00000$ $b = -0.379157 + 0.887737I$	1.64493	6.00000
$u = -0.819901 - 0.541369I$ $a = 1.00000$ $b = -0.379157 - 0.887737I$	1.64493	6.00000
$u = 0.373850 + 0.559427I$ $a = 1.00000$ $b = 0.173195 - 0.418284I$	1.64493	6.00000
$u = 0.373850 - 0.559427I$ $a = 1.00000$ $b = 0.173195 + 0.418284I$	1.64493	6.00000
$u = 1.45970$ $a = 1.00000$ $b = -2.13072$	1.64493	6.00000
$u = -1.56760$ $a = 1.00000$ $b = -2.45736$	1.64493	6.00000

$$\text{IV. } I_4^u = \langle b + 1, a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class =  $-1$

(iii) Cusp Shapes =  $6$

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u + 1$
$c_2, c_5, c_9$	$u$
$c_3, c_4, c_6$ $c_7, c_8, c_{10}$ $c_{11}, c_{12}$	$u - 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7, c_8$ $c_{10}, c_{11}, c_{12}$	$y - 1$
$c_2, c_5, c_9$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$	1.64493	6.00000
$a = 1.00000$		
$b = -1.00000$		

$$\mathbf{V}. I_5^u = \langle b + a - 1, a^2 - a - 1, u - 1 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -a + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -a + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ a - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ -a \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ -a + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -a + 2 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -5**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_8, c_{10}$	$u^2 - u - 1$
$c_2, c_{11}, c_{12}$	$(u - 1)^2$
$c_3, c_4$	$u^2 + u - 1$
$c_5, c_6, c_7$	$(u + 1)^2$
$c_9$	$u^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_8, c_{10}$	$y^2 - 3y + 1$
$c_2, c_5, c_6$ $c_7, c_{11}, c_{12}$	$(y - 1)^2$
$c_9$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = -0.618034$ $b = 1.61803$	0	-5.00000
$u = 1.00000$ $a = 1.61803$ $b = -0.618034$	0	-5.00000

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u+1)(u^2-u-1)(u^6+u^5+\dots-4u+1)(u^{14}-5u^{13}+\dots+8u-1)$ $\cdot (u^{82}-3u^{81}+\dots+15u-1)$
$c_2$	$u(u-1)^2(u^6-5u^4+\dots+4u^2-3)(u^{14}+6u^{13}+\dots+6u+1)$ $\cdot (u^{82}+u^{81}+\dots-138u+33)$
$c_3$	$(u-1)(u^2+u-1)(u^6+u^5-2u^4-2u^3-1)$ $\cdot (u^{14}-3u^{12}-u^{11}+u^{10}+2u^9+4u^8-4u^6-u^5-u^4+u^3+3u^2-1)$ $\cdot (u^{82}-22u^{80}+\dots-4101u-607)$
$c_4$	$(u-1)^7(u^2+u-1)$ $\cdot (u^{14}-3u^{12}+u^{11}+u^{10}-u^9+4u^8-4u^6+2u^5-u^4-u^3+3u^2-1)$ $\cdot (u^{82}+5u^{81}+\dots+112u-8)$
$c_5$	$u(u+1)^2(u^6-5u^4+\dots+4u^2-3)(u^{14}-6u^{13}+\dots-6u+1)$ $\cdot (u^{82}+u^{81}+\dots-138u+33)$
$c_6, c_7$	$(u-1)(u+1)^2(u^6+u^5+\dots-2u^3-1)(u^{14}-10u^{12}+\dots-4u+1)$ $\cdot (u^{82}+u^{81}+\dots+10u-1)$
$c_8$	$(u-1)(u^2-u-1)(u^6+u^5-2u^4-2u^3-1)$ $\cdot (u^{14}-3u^{12}+u^{11}+u^{10}-2u^9+4u^8-4u^6+u^5-u^4-u^3+3u^2-1)$ $\cdot (u^{82}-22u^{80}+\dots-4101u-607)$
$c_9$	$u^3(u^6-5u^4+\dots+4u^2-3)(u^{14}-3u^{13}+\dots+9u+5)$ $\cdot (u^{82}-2u^{81}+\dots-24u+12)$
$c_{10}$	$(u-1)^7(u^2-u-1)$ $\cdot (u^{14}-3u^{12}-u^{11}+u^{10}+u^9+4u^8-4u^6-2u^5-u^4+u^3+3u^2-1)$ $\cdot (u^{82}+5u^{81}+\dots+112u-8)$
$c_{11}, c_{12}$	$((u-1)^3)(u^6+u^5-2u^4-2u^3-1)(u^{14}-10u^{12}+\dots+4u+1)$ $\cdot (u^{82}+u^{81}+\dots+10u-1)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y-1)(y^2-3y+1)(y^6-y^5+8y^4+6y^3-12y^2-12y+1)$ $\cdot (y^{14}-7y^{13}+\dots-16y+1)(y^{82}-13y^{81}+\dots-27y+1)$
$c_2, c_5$	$y(y-1)^2(y^6-10y^5+33y^4-50y^3+46y^2-24y+9)$ $\cdot (y^{14}-14y^{13}+\dots-14y+1)(y^{82}-39y^{81}+\dots-42804y+1089)$
$c_3, c_8$	$(y-1)(y^2-3y+1)(y^6-5y^5+8y^4-6y^3+4y^2+1)$ $\cdot (y^{14}-6y^{13}+\dots-6y+1)(y^{82}-44y^{81}+\dots-1.42251 \times 10^7 y + 368449)$
$c_4, c_{10}$	$((y-1)^7)(y^2-3y+1)(y^{14}-6y^{13}+\dots-6y+1)$ $\cdot (y^{82}-51y^{81}+\dots-13728y+64)$
$c_6, c_7, c_{11}$ $c_{12}$	$((y-1)^3)(y^6-5y^5+\dots+4y^2+1)(y^{14}-20y^{13}+\dots-20y+1)$ $\cdot (y^{82}-101y^{81}+\dots-110y+1)$
$c_9$	$y^3(y^6-10y^5+33y^4-50y^3+46y^2-24y+9)$ $\cdot (y^{14}-9y^{13}+\dots-381y+25)(y^{82}-8y^{81}+\dots-216y+144)$