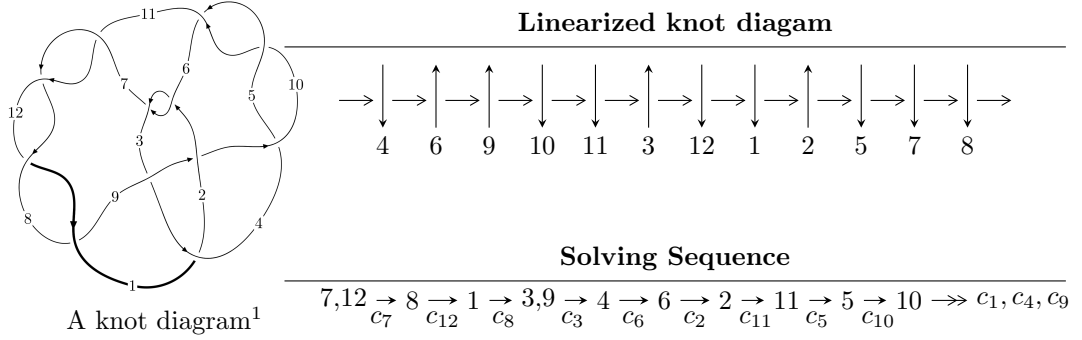


12a₀₉₂₀ (K12a₀₉₂₀)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 5.21460 \times 10^{59} u^{68} - 2.30775 \times 10^{60} u^{67} + \dots + 3.10307 \times 10^{59} b + 1.14731 \times 10^{61}, \\ 5.06049 \times 10^{60} u^{68} - 2.13379 \times 10^{61} u^{67} + \dots + 3.10307 \times 10^{59} a + 7.69523 \times 10^{61}, u^{69} - 4u^{68} + \dots + 46u + 1 \rangle$$

$$I_2^u = \langle -u^{14} + 10u^{12} + u^{11} - 39u^{10} - 7u^9 + 75u^8 + 17u^7 - 75u^6 - 17u^5 + 39u^4 + 9u^3 - 10u^2 + b - 5u + 1, \\ u^{16} - u^{15} + \dots + a + 5, u^{17} - 12u^{15} + \dots + 2u + 1 \rangle$$

$$I_3^u = \langle 4a^4 u + 3a^4 - 8a^3 u - 6a^3 + 24a^2 u + 18a^2 - 32a u + 19b - 43a - 2u - 30, \\ a^5 - 2a^4 + a^3 u + 6a^3 - 2a^2 u - 10a^2 - 5a u - a + 2u - 1, u^2 + u - 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 96 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 5.21 \times 10^{59} u^{68} - 2.31 \times 10^{60} u^{67} + \dots + 3.10 \times 10^{59} b + 1.15 \times 10^{61}, 5.06 \times 10^{60} u^{68} - 2.13 \times 10^{61} u^{67} + \dots + 3.10 \times 10^{59} a + 7.70 \times 10^{61}, u^{69} - 4u^{68} + \dots + 46u + 4 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -16.3080u^{68} + 68.7640u^{67} + \dots - 1888.29u - 247.988 \\ -1.68047u^{68} + 7.43699u^{67} + \dots - 252.125u - 36.9734 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -15.0036u^{68} + 65.3287u^{67} + \dots - 1927.12u - 254.936 \\ -0.440613u^{68} + 4.28225u^{67} + \dots - 276.144u - 38.8034 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -4.01864u^{68} + 17.3606u^{67} + \dots - 509.348u - 63.6386 \\ 3.42123u^{68} - 14.2674u^{67} + \dots + 402.460u + 56.0888 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -7.35047u^{68} + 32.8090u^{67} + \dots - 855.578u - 94.9110 \\ 1.71041u^{68} - 5.82409u^{67} + \dots + 94.1801u + 14.7601 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -3.65619u^{68} + 15.7506u^{67} + \dots - 453.155u - 56.1645 \\ 3.78369u^{68} - 15.8774u^{67} + \dots + 458.653u + 63.5629 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 11.0584u^{68} - 47.9229u^{67} + \dots + 1414.70u + 185.347 \\ -3.29554u^{68} + 12.6333u^{67} + \dots - 282.187u - 38.6325 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $30.0615u^{68} - 134.302u^{67} + \dots + 4382.18u + 604.662$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--|
| c_1 | $u^{69} - 3u^{68} + \dots + 20777u - 1427$ |
| c_2, c_6 | $u^{69} - 4u^{68} + \dots - 15u - 1$ |
| c_3 | $u^{69} - u^{68} + \dots - 231u + 293$ |
| c_4, c_5, c_{10} | $u^{69} + u^{68} + \dots + 26u - 1$ |
| c_7, c_8, c_{11} c_{12} | $u^{69} + 4u^{68} + \dots + 46u - 4$ |
| c_9 | $u^{69} + 2u^{68} + \dots + 766u - 229$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1 | $y^{69} - 27y^{68} + \dots + 239869243y - 2036329$ |
| c_2, c_6 | $y^{69} - 28y^{68} + \dots + 171y - 1$ |
| c_3 | $y^{69} + 13y^{68} + \dots - 450599y - 85849$ |
| c_4, c_5, c_{10} | $y^{69} - 79y^{68} + \dots + 462y - 1$ |
| c_7, c_8, c_{11} c_{12} | $y^{69} - 84y^{68} + \dots + 684y - 16$ |
| c_9 | $y^{69} + 14y^{68} + \dots + 8302y - 52441$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -0.858609 + 0.509133I$ $a = -0.13290 + 1.46749I$ $b = 1.119670 + 0.509880I$ | $0.11883 + 8.23224I$ | 0 |
| $u = -0.858609 - 0.509133I$ $a = -0.13290 - 1.46749I$ $b = 1.119670 - 0.509880I$ | $0.11883 - 8.23224I$ | 0 |
| $u = 0.922201 + 0.343620I$ $a = -0.226022 - 0.690778I$ $b = -0.396644 - 1.154280I$ | $-9.14129 - 5.71438I$ | 0 |
| $u = 0.922201 - 0.343620I$ $a = -0.226022 + 0.690778I$ $b = -0.396644 + 1.154280I$ | $-9.14129 + 5.71438I$ | 0 |
| $u = 0.957142 + 0.344138I$ $a = 0.346935 - 0.313197I$ $b = 0.956665 + 0.106533I$ | $-0.408920 + 0.368294I$ | 0 |
| $u = 0.957142 - 0.344138I$ $a = 0.346935 + 0.313197I$ $b = 0.956665 - 0.106533I$ | $-0.408920 - 0.368294I$ | 0 |
| $u = -0.761381 + 0.691428I$ $a = 0.903514 - 0.730666I$ $b = -1.019750 - 0.567692I$ | $-6.72025 + 2.21455I$ | 0 |
| $u = -0.761381 - 0.691428I$ $a = 0.903514 + 0.730666I$ $b = -1.019750 + 0.567692I$ | $-6.72025 - 2.21455I$ | 0 |
| $u = 0.875291 + 0.317279I$ $a = -0.65426 + 1.54098I$ $b = -0.941128 + 0.295855I$ | $-0.11613 - 2.68304I$ | 0 |
| $u = 0.875291 - 0.317279I$ $a = -0.65426 - 1.54098I$ $b = -0.941128 - 0.295855I$ | $-0.11613 + 2.68304I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = 0.888247 + 0.623182I$ $a = 0.428773 + 1.236830I$ $b = -1.198570 + 0.737599I$ | $-6.69655 - 12.30450I$ | 0 |
| $u = 0.888247 - 0.623182I$ $a = 0.428773 - 1.236830I$ $b = -1.198570 - 0.737599I$ | $-6.69655 + 12.30450I$ | 0 |
| $u = 0.068085 + 0.890261I$ $a = 0.549835 + 0.167489I$ $b = -1.014710 - 0.607088I$ | $-4.19382 + 7.32485I$ | 0 |
| $u = 0.068085 - 0.890261I$ $a = 0.549835 - 0.167489I$ $b = -1.014710 + 0.607088I$ | $-4.19382 - 7.32485I$ | 0 |
| $u = 0.627745 + 0.554827I$ $a = -0.857946 - 0.838190I$ $b = 0.676355 - 0.302159I$ | $-1.22245 - 1.88994I$ | 0 |
| $u = 0.627745 - 0.554827I$ $a = -0.857946 + 0.838190I$ $b = 0.676355 + 0.302159I$ | $-1.22245 + 1.88994I$ | 0 |
| $u = -0.751462 + 0.303115I$ $a = 0.418529 - 1.137040I$ $b = 0.165717 - 0.819333I$ | $-2.66510 + 3.50831I$ | $-10.49360 - 7.33854I$ |
| $u = -0.751462 - 0.303115I$ $a = 0.418529 + 1.137040I$ $b = 0.165717 + 0.819333I$ | $-2.66510 - 3.50831I$ | $-10.49360 + 7.33854I$ |
| $u = -1.190400 + 0.048571I$ $a = 0.888159 - 0.271946I$ $b = 0.604132 - 0.446757I$ | $-7.88819 + 0.32180I$ | 0 |
| $u = -1.190400 - 0.048571I$ $a = 0.888159 + 0.271946I$ $b = 0.604132 + 0.446757I$ | $-7.88819 - 0.32180I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = -0.747922 + 0.141109I$ $a = -1.18456 + 1.77018I$ $b = 1.046390 + 0.542070I$ | $-6.49393 + 4.52204I$ | $-12.42024 - 4.96803I$ |
| $u = -0.747922 - 0.141109I$ $a = -1.18456 - 1.77018I$ $b = 1.046390 - 0.542070I$ | $-6.49393 - 4.52204I$ | $-12.42024 + 4.96803I$ |
| $u = -0.278701 + 0.697012I$ $a = 0.918131 - 0.701090I$ $b = -0.633259 + 0.581048I$ | $-5.39570 + 2.53481I$ | $-8.38084 - 2.80374I$ |
| $u = -0.278701 - 0.697012I$ $a = 0.918131 + 0.701090I$ $b = -0.633259 - 0.581048I$ | $-5.39570 - 2.53481I$ | $-8.38084 + 2.80374I$ |
| $u = -0.034826 + 0.713110I$ $a = -0.706288 - 0.104021I$ $b = 1.077410 - 0.310611I$ | $2.61982 - 4.13722I$ | $-1.23735 + 6.70183I$ |
| $u = -0.034826 - 0.713110I$ $a = -0.706288 + 0.104021I$ $b = 1.077410 + 0.310611I$ | $2.61982 + 4.13722I$ | $-1.23735 - 6.70183I$ |
| $u = -1.147790 + 0.605056I$ $a = -0.280564 - 0.113102I$ $b = -0.707022 + 0.513747I$ | $-7.79544 - 2.18356I$ | 0 |
| $u = -1.147790 - 0.605056I$ $a = -0.280564 + 0.113102I$ $b = -0.707022 - 0.513747I$ | $-7.79544 + 2.18356I$ | 0 |
| $u = 0.549539 + 0.428722I$ $a = -0.92689 - 1.74841I$ $b = 1.001700 - 0.945056I$ | $-3.37002 - 4.91183I$ | $-5.12008 + 9.10431I$ |
| $u = 0.549539 - 0.428722I$ $a = -0.92689 + 1.74841I$ $b = 1.001700 + 0.945056I$ | $-3.37002 + 4.91183I$ | $-5.12008 - 9.10431I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.603111 + 0.317010I$ $a = -0.06954 - 1.62856I$ $b = -1.039670 - 0.531907I$ | $1.42958 + 2.33297I$ | $-0.70777 - 7.76145I$ |
| $u = -0.603111 - 0.317010I$ $a = -0.06954 + 1.62856I$ $b = -1.039670 + 0.531907I$ | $1.42958 - 2.33297I$ | $-0.70777 + 7.76145I$ |
| $u = -1.36225$ $a = -0.107589$ $b = -1.38678$ | -1.59788 | 0 |
| $u = 0.347963 + 0.505319I$ $a = 0.188527 - 0.656901I$ $b = 1.003340 + 0.715218I$ | $-2.79726 + 1.63095I$ | $-4.89103 - 0.22167I$ |
| $u = 0.347963 - 0.505319I$ $a = 0.188527 + 0.656901I$ $b = 1.003340 - 0.715218I$ | $-2.79726 - 1.63095I$ | $-4.89103 + 0.22167I$ |
| $u = -1.47026$ $a = 0.903464$ $b = 1.02182$ | -8.11663 | 0 |
| $u = 1.53884 + 0.08382I$ $a = 0.51726 + 1.39825I$ $b = -0.030549 + 0.170011I$ | $-11.09110 - 4.38044I$ | 0 |
| $u = 1.53884 - 0.08382I$ $a = 0.51726 - 1.39825I$ $b = -0.030549 - 0.170011I$ | $-11.09110 + 4.38044I$ | 0 |
| $u = 1.54919$ $a = -1.05617$ $b = -1.67326$ | -3.72894 | 0 |
| $u = -1.57061 + 0.09574I$ $a = 0.29032 + 2.12661I$ $b = 1.01604 + 1.19413I$ | $-10.56740 + 6.67317I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -1.57061 - 0.09574I$ $a = 0.29032 - 2.12661I$ $b = 1.01604 - 1.19413I$ | $-10.56740 - 6.67317I$ | 0 |
| $u = 1.59295 + 0.06255I$ $a = -0.65470 + 1.63501I$ $b = -1.054310 + 0.900547I$ | $-6.11344 - 3.58029I$ | 0 |
| $u = 1.59295 - 0.06255I$ $a = -0.65470 - 1.63501I$ $b = -1.054310 - 0.900547I$ | $-6.11344 + 3.58029I$ | 0 |
| $u = -0.090552 + 0.392237I$ $a = 0.536976 - 1.059100I$ $b = -1.143200 + 0.046612I$ | $2.68421 + 0.16764I$ | $2.41572 - 0.19332I$ |
| $u = -0.090552 - 0.392237I$ $a = 0.536976 + 1.059100I$ $b = -1.143200 - 0.046612I$ | $2.68421 - 0.16764I$ | $2.41572 + 0.19332I$ |
| $u = -1.61062 + 0.16002I$ $a = -0.034132 + 1.263440I$ $b = 0.891494 + 0.558679I$ | $-8.89500 + 4.54856I$ | 0 |
| $u = -1.61062 - 0.16002I$ $a = -0.034132 - 1.263440I$ $b = 0.891494 - 0.558679I$ | $-8.89500 - 4.54856I$ | 0 |
| $u = 0.070878 + 0.373596I$ $a = -0.958588 + 0.155139I$ $b = -0.002941 + 0.459481I$ | $-0.359603 - 1.131530I$ | $-5.56898 + 5.13888I$ |
| $u = 0.070878 - 0.373596I$ $a = -0.958588 - 0.155139I$ $b = -0.002941 - 0.459481I$ | $-0.359603 + 1.131530I$ | $-5.56898 - 5.13888I$ |
| $u = 1.62259 + 0.07416I$ $a = 0.41905 + 1.55527I$ $b = 0.337200 + 0.935815I$ | $-10.84000 - 4.89494I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.62259 - 0.07416I$ | | |
| $a = 0.41905 - 1.55527I$ | $-10.84000 + 4.89494I$ | 0 |
| $b = 0.337200 - 0.935815I$ | | |
| $u = 1.64324 + 0.03991I$ | | |
| $a = 0.106947 - 1.306450I$ | $-14.8905 - 5.2157I$ | 0 |
| $b = 1.29168 - 0.59412I$ | | |
| $u = 1.64324 - 0.03991I$ | | |
| $a = 0.106947 + 1.306450I$ | $-14.8905 + 5.2157I$ | 0 |
| $b = 1.29168 + 0.59412I$ | | |
| $u = 1.66632 + 0.14638I$ | | |
| $a = 0.46733 - 1.56172I$ | $-8.56853 - 10.77570I$ | 0 |
| $b = 1.147590 - 0.686553I$ | | |
| $u = 1.66632 - 0.14638I$ | | |
| $a = 0.46733 + 1.56172I$ | $-8.56853 + 10.77570I$ | 0 |
| $b = 1.147590 + 0.686553I$ | | |
| $u = -1.67496 + 0.09834I$ | | |
| $a = -0.51698 + 1.53291I$ | $-18.1559 + 7.4706I$ | 0 |
| $b = -0.50081 + 1.47766I$ | | |
| $u = -1.67496 - 0.09834I$ | | |
| $a = -0.51698 - 1.53291I$ | $-18.1559 - 7.4706I$ | 0 |
| $b = -0.50081 - 1.47766I$ | | |
| $u = 1.66700 + 0.20966I$ | | |
| $a = -0.097293 + 1.135820I$ | $-15.0060 - 5.7097I$ | 0 |
| $b = -1.29837 + 0.61433I$ | | |
| $u = 1.66700 - 0.20966I$ | | |
| $a = -0.097293 - 1.135820I$ | $-15.0060 + 5.7097I$ | 0 |
| $b = -1.29837 - 0.61433I$ | | |
| $u = -1.67919 + 0.09590I$ | | |
| $a = -0.70802 - 1.36350I$ | $-9.07614 + 4.33421I$ | 0 |
| $b = -0.843032 - 0.540808I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = -1.67919 - 0.09590I$ $a = -0.70802 + 1.36350I$ $b = -0.843032 + 0.540808I$ | $-9.07614 - 4.33421I$ | 0 |
| $u = -1.67662 + 0.18420I$ $a = -0.33035 - 1.57967I$ $b = -1.32832 - 0.86095I$ | $-15.4447 + 15.4584I$ | 0 |
| $u = -1.67662 - 0.18420I$ $a = -0.33035 + 1.57967I$ $b = -1.32832 + 0.86095I$ | $-15.4447 - 15.4584I$ | 0 |
| $u = -0.257782 + 0.029613I$ $a = 3.42531 + 5.22024I$ $b = 0.515844 - 0.457634I$ | $-4.89351 - 3.67092I$ | $-12.31151 - 0.80644I$ |
| $u = -0.257782 - 0.029613I$ $a = 3.42531 - 5.22024I$ $b = 0.515844 + 0.457634I$ | $-4.89351 + 3.67092I$ | $-12.31151 + 0.80644I$ |
| $u = 1.74045 + 0.06218I$ $a = 0.068694 - 0.932107I$ $b = -0.032884 - 0.887424I$ | $-18.5613 - 0.1635I$ | 0 |
| $u = 1.74045 - 0.06218I$ $a = 0.068694 + 0.932107I$ $b = -0.032884 + 0.887424I$ | $-18.5613 + 0.1635I$ | 0 |
| $u = -0.222069$ $a = -1.80233$ $b = -1.36002$ | 2.83320 | 10.8910 |
| $u = 1.81750$ $a = 0.292085$ $b = 0.0660849$ | -19.0700 | 0 |

II.

$$I_2^u = \langle -u^{14} + 10u^{12} + \dots + b + 1, u^{16} - u^{15} + \dots + a + 5, u^{17} - 12u^{15} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{16} + u^{15} + \dots + 2u - 5 \\ u^{14} - 10u^{12} + \dots + 5u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{16} + u^{15} + \dots + 5u - 5 \\ 2u^{14} - 19u^{12} + \dots + 6u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2u^{16} - 2u^{15} + \dots - 5u + 8 \\ -u^{15} - u^{14} + \dots + u + 4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{16} - 2u^{15} + \dots - 10u + 7 \\ -u^{15} - 3u^{14} + \dots - 5u + 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2u^{16} - u^{15} + \dots - 5u + 7 \\ u^{12} - u^{11} + \dots + u + 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3u^{16} + 34u^{14} + \dots + 12u - 8 \\ -2u^{16} + 22u^{14} + \dots + 2u - 4 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $6u^{16} - 2u^{15} - 73u^{14} + 15u^{13} + 361u^{12} - 34u^{11} - 928u^{10} + 8u^9 + 1320u^8 + 54u^7 - 1027u^6 - 59u^5 + 406u^4 + 53u^3 - 66u^2 - 38u - 4$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------|--------------------------------------|
| c_1 | $u^{17} - 6u^{15} + \dots + 3u - 1$ |
| c_2 | $u^{17} - 3u^{16} + \dots - 3u + 1$ |
| c_3 | $u^{17} - 2u^{14} + \dots + u + 1$ |
| c_4, c_5 | $u^{17} - 10u^{15} + \dots + 2u - 1$ |
| c_6 | $u^{17} + 3u^{16} + \dots - 3u - 1$ |
| c_7, c_8 | $u^{17} - 12u^{15} + \dots + 2u + 1$ |
| c_9 | $u^{17} + u^{16} + \dots - 2u^3 + 1$ |
| c_{10} | $u^{17} - 10u^{15} + \dots + 2u + 1$ |
| c_{11}, c_{12} | $u^{17} - 12u^{15} + \dots + 2u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---------------------------------------|
| c_1 | $y^{17} - 12y^{16} + \dots + 21y - 1$ |
| c_2, c_6 | $y^{17} - 17y^{16} + \dots + 17y - 1$ |
| c_3 | $y^{17} - 6y^{15} + \dots + 3y - 1$ |
| c_4, c_5, c_{10} | $y^{17} - 20y^{16} + \dots + 16y - 1$ |
| c_7, c_8, c_{11} c_{12} | $y^{17} - 24y^{16} + \dots + 24y - 1$ |
| c_9 | $y^{17} - 3y^{16} + \dots + 6y^2 - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 1.09578$ $a = 0.547612$ $b = 1.14178$ | 0.341936 | 0.875270 |
| $u = -1.123960 + 0.382204I$ $a = -0.478136 - 0.578939I$ $b = -0.617479 + 0.293759I$ | $-7.13101 - 1.62524I$ | $-6.68084 + 0.62023I$ |
| $u = -1.123960 - 0.382204I$ $a = -0.478136 + 0.578939I$ $b = -0.617479 - 0.293759I$ | $-7.13101 + 1.62524I$ | $-6.68084 - 0.62023I$ |
| $u = -1.18833$ $a = 0.0332715$ $b = -1.43147$ | -3.07503 | -11.9270 |
| $u = 0.667353 + 0.370935I$ $a = -0.47830 - 1.61454I$ $b = 0.724488 - 0.164054I$ | $-0.59938 - 1.32532I$ | $-5.05705 + 2.80405I$ |
| $u = 0.667353 - 0.370935I$ $a = -0.47830 + 1.61454I$ $b = 0.724488 + 0.164054I$ | $-0.59938 + 1.32532I$ | $-5.05705 - 2.80405I$ |
| $u = -0.369667 + 0.360033I$ $a = 2.85434 - 1.27851I$ $b = -0.773403 - 0.575136I$ | $-4.67731 + 4.33112I$ | $-8.36560 - 8.69813I$ |
| $u = -0.369667 - 0.360033I$ $a = 2.85434 + 1.27851I$ $b = -0.773403 + 0.575136I$ | $-4.67731 - 4.33112I$ | $-8.36560 + 8.69813I$ |
| $u = 1.53432$ $a = -1.73698$ $b = -1.84039$ | -6.74002 | -3.61890 |
| $u = -1.55322$ $a = 0.672900$ $b = 1.56084$ | -4.27815 | -13.1180 |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = 1.55960 + 0.10540I$ $a = 0.20362 + 1.87120I$ $b = -0.891995 + 0.798543I$ | $-11.47150 - 5.99192I$ | $-13.12352 + 4.84870I$ |
| $u = 1.55960 - 0.10540I$ $a = 0.20362 - 1.87120I$ $b = -0.891995 - 0.798543I$ | $-11.47150 + 5.99192I$ | $-13.12352 - 4.84870I$ |
| $u = 0.389234$ $a = -0.308648$ $b = 1.38986$ | 2.56515 | -19.7450 |
| $u = -1.63154 + 0.11334I$ $a = 0.255071 + 1.300460I$ $b = 0.681332 + 0.453515I$ | $-8.67576 + 3.16393I$ | $-7.87236 - 0.20715I$ |
| $u = -1.63154 - 0.11334I$ $a = 0.255071 - 1.300460I$ $b = 0.681332 - 0.453515I$ | $-8.67576 - 3.16393I$ | $-7.87236 + 0.20715I$ |
| $u = -0.315662$ $a = -3.47084$ $b = -1.66703$ | -0.212009 | 3.05600 |
| $u = 1.83431$ $a = -0.450508$ $b = -0.399475$ | -18.8982 | 15.6760 |

$$\text{III. } I_3^u = \langle 4a^4u - 8a^3u + \dots - 43a - 30, a^3u - 2a^2u + \dots - a - 1, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -0.210526a^4u + 0.421053a^3u + \dots + 2.26316a + 1.57895 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.263158a^4u + 0.526316a^3u + \dots + 0.578947a + 1.47368 \\ -0.473684a^4u + 0.947368a^3u + \dots + 1.84211a + 3.05263 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0526316a^3u - 0.315789a^2u + \dots + 0.368421a + 1.26316 \\ -0.421053a^4u + 0.526316a^3u + \dots + 4.73684a + 2.73684 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.526316a^4u - 0.421053a^3u + \dots - 1.57895a - 2.10526 \\ 0.947368a^4u - a^3u + \dots - 5.94737a - 3.57895 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.526316a^4u + 0.421053a^3u + \dots + 1.57895a + 2.10526 \\ -0.947368a^4u + a^3u + \dots + 5.94737a + 3.57895 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.473684a^4u + 0.315789a^3u + \dots - 5.73684a + 0.210526 \\ -0.315789a^4u + 0.315789a^2u + \dots - 9.68421a - 1.47368 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -10

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--|
| c_1 | $u^{10} - 4u^9 + 2u^8 + 8u^7 - 5u^6 - 11u^5 + 8u^4 + 7u^3 - 5u^2 - 3u + 1$ |
| c_2, c_6 | $u^{10} + 4u^9 + 2u^8 - 8u^7 - 5u^6 + 11u^5 + 8u^4 - 7u^3 - 5u^2 + 3u + 1$ |
| c_3 | $u^{10} + 2u^8 - 4u^7 + 5u^6 - 7u^5 - 12u^4 + 9u^3 - 5u^2 - u + 1$ |
| c_4, c_5, c_9 c_{10} | $u^{10} - 2u^8 - u^6 + u^5 + 2u^4 - u^3 + u^2 - u - 1$ |
| c_7, c_8, c_{11} c_{12} | $(u^2 - u - 1)^5$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_2, c_6 | $y^{10} - 12y^9 + \dots - 19y + 1$ |
| c_3 | $y^{10} + 4y^9 + \dots - 11y + 1$ |
| c_4, c_5, c_9 c_{10} | $y^{10} - 4y^9 + 2y^8 + 8y^7 - 5y^6 - 11y^5 + 8y^4 + 7y^3 - 5y^2 - 3y + 1$ |
| c_7, c_8, c_{11} c_{12} | $(y^2 - 3y + 1)^5$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 0.618034$ $a = -0.345749$ $b = 0.267133$ | -0.986960 | -10.0000 |
| $u = 0.618034$ $a = 0.0508281$ $b = 1.80755$ | -0.986960 | -10.0000 |
| $u = 0.618034$ $a = 1.99880$ $b = 1.34705$ | -0.986960 | -10.0000 |
| $u = 0.618034$ $a = 0.14806 + 2.58817I$ $b = -0.710869 + 0.286205I$ | -0.986960 | -10.0000 |
| $u = 0.618034$ $a = 0.14806 - 2.58817I$ $b = -0.710869 - 0.286205I$ | -0.986960 | -10.0000 |
| $u = -1.61803$ $a = 1.12160$ $b = 2.04335$ | -8.88264 | -10.0000 |
| $u = -1.61803$ $a = 0.687673 + 0.972900I$ $b = 0.880270 + 0.618196I$ | -8.88264 | -10.0000 |
| $u = -1.61803$ $a = 0.687673 - 0.972900I$ $b = 0.880270 - 0.618196I$ | -8.88264 | -10.0000 |
| $u = -1.61803$ $a = -0.24847 + 1.61216I$ $b = -0.901944 + 0.542076I$ | -8.88264 | -10.0000 |
| $u = -1.61803$ $a = -0.24847 - 1.61216I$ $b = -0.901944 - 0.542076I$ | -8.88264 | -10.0000 |

IV. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------------|--|
| c_1 | $(u^{10} - 4u^9 + 2u^8 + 8u^7 - 5u^6 - 11u^5 + 8u^4 + 7u^3 - 5u^2 - 3u + 1)$ $\cdot (u^{17} - 6u^{15} + \dots + 3u - 1)(u^{69} - 3u^{68} + \dots + 20777u - 1427)$ |
| c_2 | $(u^{10} + 4u^9 + 2u^8 - 8u^7 - 5u^6 + 11u^5 + 8u^4 - 7u^3 - 5u^2 + 3u + 1)$ $\cdot (u^{17} - 3u^{16} + \dots - 3u + 1)(u^{69} - 4u^{68} + \dots - 15u - 1)$ |
| c_3 | $(u^{10} + 2u^8 - 4u^7 + 5u^6 - 7u^5 - 12u^4 + 9u^3 - 5u^2 - u + 1)$ $\cdot (u^{17} - 2u^{14} + \dots + u + 1)(u^{69} - u^{68} + \dots - 231u + 293)$ |
| c_4, c_5 | $(u^{10} - 2u^8 + \dots - u - 1)(u^{17} - 10u^{15} + \dots + 2u - 1)$ $\cdot (u^{69} + u^{68} + \dots + 26u - 1)$ |
| c_6 | $(u^{10} + 4u^9 + 2u^8 - 8u^7 - 5u^6 + 11u^5 + 8u^4 - 7u^3 - 5u^2 + 3u + 1)$ $\cdot (u^{17} + 3u^{16} + \dots - 3u - 1)(u^{69} - 4u^{68} + \dots - 15u - 1)$ |
| c_7, c_8 | $((u^2 - u - 1)^5)(u^{17} - 12u^{15} + \dots + 2u + 1)(u^{69} + 4u^{68} + \dots + 46u - 4)$ |
| c_9 | $(u^{10} - 2u^8 + \dots - u - 1)(u^{17} + u^{16} + \dots - 2u^3 + 1)$ $\cdot (u^{69} + 2u^{68} + \dots + 766u - 229)$ |
| c_{10} | $(u^{10} - 2u^8 + \dots - u - 1)(u^{17} - 10u^{15} + \dots + 2u + 1)$ $\cdot (u^{69} + u^{68} + \dots + 26u - 1)$ |
| c_{11}, c_{12} | $((u^2 - u - 1)^5)(u^{17} - 12u^{15} + \dots + 2u - 1)(u^{69} + 4u^{68} + \dots + 46u - 4)$ |

V. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1 | $(y^{10} - 12y^9 + \dots - 19y + 1)(y^{17} - 12y^{16} + \dots + 21y - 1)$ $\cdot (y^{69} - 27y^{68} + \dots + 239869243y - 2036329)$ |
| c_2, c_6 | $(y^{10} - 12y^9 + \dots - 19y + 1)(y^{17} - 17y^{16} + \dots + 17y - 1)$ $\cdot (y^{69} - 28y^{68} + \dots + 171y - 1)$ |
| c_3 | $(y^{10} + 4y^9 + \dots - 11y + 1)(y^{17} - 6y^{15} + \dots + 3y - 1)$ $\cdot (y^{69} + 13y^{68} + \dots - 450599y - 85849)$ |
| c_4, c_5, c_{10} | $(y^{10} - 4y^9 + 2y^8 + 8y^7 - 5y^6 - 11y^5 + 8y^4 + 7y^3 - 5y^2 - 3y + 1)$ $\cdot (y^{17} - 20y^{16} + \dots + 16y - 1)(y^{69} - 79y^{68} + \dots + 462y - 1)$ |
| c_7, c_8, c_{11} c_{12} | $((y^2 - 3y + 1)^5)(y^{17} - 24y^{16} + \dots + 24y - 1)$ $\cdot (y^{69} - 84y^{68} + \dots + 684y - 16)$ |
| c_9 | $(y^{10} - 4y^9 + 2y^8 + 8y^7 - 5y^6 - 11y^5 + 8y^4 + 7y^3 - 5y^2 - 3y + 1)$ $\cdot (y^{17} - 3y^{16} + \dots + 6y^2 - 1)(y^{69} + 14y^{68} + \dots + 8302y - 52441)$ |