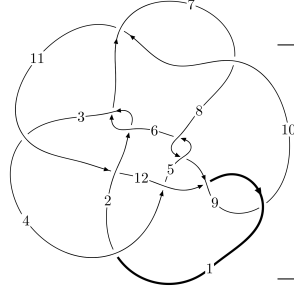
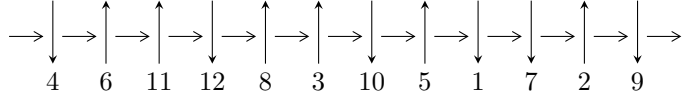


12a<sub>0990</sub> (K12a<sub>0990</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$1, 9 \xrightarrow{c_9} 5, 10 \xrightarrow{c_8} 8 \xrightarrow{c_5} 6 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 12 \xrightarrow{c_4} 4 \xrightarrow{c_1} 2 \xrightarrow{c_{11}} 11 \xrightarrow{c_3} 3 \twoheadrightarrow c_2, c_6, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -7.42364 \times 10^{545} u^{129} - 6.71560 \times 10^{546} u^{128} + \dots + 2.82169 \times 10^{548} b - 2.11413 \times 10^{552}, \\ -1.02551 \times 10^{550} u^{129} - 9.21321 \times 10^{550} u^{128} + \dots + 1.46192 \times 10^{552} a - 2.73974 \times 10^{556}, \\ u^{130} + 10u^{129} + \dots + 40002776u + 2811556 \rangle$$

$$I_2^u = \langle -8.19734 \times 10^{33} u^{31} - 4.22264 \times 10^{34} u^{30} + \dots + 9.32464 \times 10^{31} b - 8.66565 \times 10^{34}, \\ -1.09826 \times 10^{34} u^{31} - 5.65664 \times 10^{34} u^{30} + \dots + 9.32464 \times 10^{31} a - 1.17253 \times 10^{35}, \\ u^{32} + 6u^{31} + \dots + 48u + 9 \rangle$$

$$I_3^u = \langle -9a^4 - 16a^3 - 76a^2 + 13b - 40a - 8, a^5 + 2a^4 + 9a^3 + 6a^2 + 3a + 1, u - 1 \rangle$$

$$I_4^u = \langle b^5 - 2b^4 a + b^3 a^2 - b^3 + a^2 b + b + a - 1, u - 1 \rangle$$

$$I_1^v = \langle a, b^5 + b^3 + b + 1, v - 1 \rangle$$

$$I_2^v = \langle a, b^2 - b + 1, v - 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 174 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -7.42 \times 10^{545} u^{129} - 6.72 \times 10^{546} u^{128} + \dots + 2.82 \times 10^{548} b - 2.11 \times 10^{552}, -1.03 \times 10^{550} u^{129} - 9.21 \times 10^{550} u^{128} + \dots + 1.46 \times 10^{552} a - 2.74 \times 10^{556}, u^{130} + 10u^{129} + \dots + 40002776u + 2811556 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.00701480u^{129} + 0.0630213u^{128} + \dots + 249589.u + 18740.7 \\ 0.00263092u^{129} + 0.0237999u^{128} + \dots + 99398.1u + 7492.40 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.00101759u^{129} + 0.00900101u^{128} + \dots + 33569.9u + 2537.03 \\ 0.000471567u^{129} + 0.00411483u^{128} + \dots + 11762.5u + 842.151 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.00126397u^{129} + 0.0107887u^{128} + \dots + 28928.9u + 2098.07 \\ -0.000934236u^{129} - 0.00863981u^{128} + \dots - 40675.0u - 3104.76 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.000150095u^{129} + 0.00122081u^{128} + \dots + 1195.24u + 75.9623 \\ -0.000473077u^{129} - 0.00432755u^{128} + \dots - 21590.6u - 1673.46 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.00233873u^{129} + 0.0208067u^{128} + \dots + 77208.8u + 5758.85 \\ -0.00204515u^{129} - 0.0184147u^{128} + \dots - 72982.4u - 5489.48 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.000274293u^{129} + 0.00247203u^{128} + \dots + 11517.0u + 900.409 \\ 0.000908201u^{129} + 0.00823727u^{128} + \dots + 35139.9u + 2659.78 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.000756422u^{129} + 0.00676781u^{128} + \dots + 27485.4u + 2094.49 \\ -0.000620407u^{129} - 0.00564869u^{128} + \dots - 24415.3u - 1859.15 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.00217529u^{129} - 0.0186835u^{128} + \dots - 48388.1u - 3437.17 \\ -0.000312213u^{129} - 0.00218499u^{128} + \dots + 8773.04u + 748.786 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.00272619u^{129} - 0.0236021u^{128} + \dots - 76099.3u - 5729.03$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$16(16u^{130} - 216u^{129} + \dots - 134148u + 11877)$
$c_2, c_6$	$u^{130} + 10u^{129} + \dots + 40002776u + 2811556$
$c_3$	$48(48u^{130} - 144u^{129} + \dots - 1.54523 \times 10^9u + 4.56957 \times 10^8)$
$c_4$	$48(48u^{130} + 144u^{129} + \dots + 1.54523 \times 10^9u + 4.56957 \times 10^8)$
$c_5, c_8$	$16(16u^{130} + 72u^{129} + \dots + 6.78136 \times 10^7u + 7939137)$
$c_7, c_{10}$	$16(16u^{130} - 72u^{129} + \dots - 6.78136 \times 10^7u + 7939137)$
$c_9, c_{12}$	$u^{130} - 10u^{129} + \dots - 40002776u + 2811556$
$c_{11}$	$16(16u^{130} + 216u^{129} + \dots + 134148u + 11877)$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$256(256y^{130} - 4640y^{129} + \dots + 2.95033 \times 10^9 y + 1.41063 \times 10^8)$
$c_2, c_6, c_9$ $c_{12}$	$y^{130} - 80y^{129} + \dots - 226520781477232y + 7904847141136$
$c_3, c_4$	$2304(2304y^{130} - 123744y^{129} + \dots - 5.35364 \times 10^{18}y + 2.08809 \times 10^{17})$
$c_5, c_7, c_8$ $c_{10}$	$256$ $\cdot (256y^{130} + 23008y^{129} + \dots - 581798760447684y + 63029896304769)$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.753714 + 0.678165I$ $a = -0.429062 - 0.743953I$ $b = -0.617531 + 0.243011I$	$2.79527 + 2.32555I$	0
$u = -0.753714 - 0.678165I$ $a = -0.429062 + 0.743953I$ $b = -0.617531 - 0.243011I$	$2.79527 - 2.32555I$	0
$u = 0.364736 + 0.913386I$ $a = 0.024867 - 1.138090I$ $b = 0.568641 - 0.599752I$	$7.79727 - 3.48496I$	0
$u = 0.364736 - 0.913386I$ $a = 0.024867 + 1.138090I$ $b = 0.568641 + 0.599752I$	$7.79727 + 3.48496I$	0
$u = -0.836988 + 0.515749I$ $a = 0.170742 - 0.519532I$ $b = -0.865889 - 0.510137I$	$2.40493 + 2.37289I$	0
$u = -0.836988 - 0.515749I$ $a = 0.170742 + 0.519532I$ $b = -0.865889 + 0.510137I$	$2.40493 - 2.37289I$	0
$u = 0.023345 + 1.032480I$ $a = 0.370646 + 0.393498I$ $b = -0.226301 + 1.308480I$	$-1.03079 - 7.20926I$	0
$u = 0.023345 - 1.032480I$ $a = 0.370646 - 0.393498I$ $b = -0.226301 - 1.308480I$	$-1.03079 + 7.20926I$	0
$u = -0.014661 + 0.956748I$ $a = -0.016413 + 0.251138I$ $b = -0.346796 + 1.202210I$	$-1.34210 - 3.05609I$	0
$u = -0.014661 - 0.956748I$ $a = -0.016413 - 0.251138I$ $b = -0.346796 - 1.202210I$	$-1.34210 + 3.05609I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.035250 + 0.190731I$ $a = 0.19971 + 3.07796I$ $b = 0.320853 + 1.071130I$	$4.01258 + 10.32040I$	0
$u = -1.035250 - 0.190731I$ $a = 0.19971 - 3.07796I$ $b = 0.320853 - 1.071130I$	$4.01258 - 10.32040I$	0
$u = -1.035300 + 0.209769I$ $a = -0.09804 - 2.67630I$ $b = -0.222571 - 1.175360I$	$-0.16136 + 5.32813I$	0
$u = -1.035300 - 0.209769I$ $a = -0.09804 + 2.67630I$ $b = -0.222571 + 1.175360I$	$-0.16136 - 5.32813I$	0
$u = 0.934913 + 0.047377I$ $a = -1.05680 + 1.64472I$ $b = -1.37976 + 0.66931I$	$-1.085330 - 0.334255I$	0
$u = 0.934913 - 0.047377I$ $a = -1.05680 - 1.64472I$ $b = -1.37976 - 0.66931I$	$-1.085330 + 0.334255I$	0
$u = 0.049853 + 0.924522I$ $a = -0.153356 - 0.036650I$ $b = 0.542235 - 1.129970I$	$0.16136 - 5.32813I$	0
$u = 0.049853 - 0.924522I$ $a = -0.153356 + 0.036650I$ $b = 0.542235 + 1.129970I$	$0.16136 + 5.32813I$	0
$u = -0.872987 + 0.633017I$ $a = 0.805377 + 0.601460I$ $b = 0.607331 - 0.671357I$	$5.31312 + 6.77397I$	0
$u = -0.872987 - 0.633017I$ $a = 0.805377 - 0.601460I$ $b = 0.607331 + 0.671357I$	$5.31312 - 6.77397I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.072770 + 0.123948I$ $a = -0.949991 + 0.241825I$ $b = -1.55098 + 0.35434I$	$-0.175289 + 0.755522I$	0
$u = -1.072770 - 0.123948I$ $a = -0.949991 - 0.241825I$ $b = -1.55098 - 0.35434I$	$-0.175289 - 0.755522I$	0
$u = -0.494026 + 0.973656I$ $a = -0.039642 + 0.660869I$ $b = 0.549748 + 0.349714I$	$8.28948 - 0.12430I$	0
$u = -0.494026 - 0.973656I$ $a = -0.039642 - 0.660869I$ $b = 0.549748 - 0.349714I$	$8.28948 + 0.12430I$	0
$u = -1.075040 + 0.250971I$ $a = 0.44267 + 2.18430I$ $b = 0.004035 + 1.026040I$	$3.31794 + 0.02095I$	0
$u = -1.075040 - 0.250971I$ $a = 0.44267 - 2.18430I$ $b = 0.004035 - 1.026040I$	$3.31794 - 0.02095I$	0
$u = 0.456734 + 0.758309I$ $a = -0.220146 + 1.329500I$ $b = -0.630414 + 0.185361I$	$3.18794 + 2.74835I$	0
$u = 0.456734 - 0.758309I$ $a = -0.220146 - 1.329500I$ $b = -0.630414 - 0.185361I$	$3.18794 - 2.74835I$	0
$u = 0.057062 + 1.121730I$ $a = -0.328075 - 0.357135I$ $b = 0.081204 - 1.173900I$	$-3.18794 - 2.74835I$	0
$u = 0.057062 - 1.121730I$ $a = -0.328075 + 0.357135I$ $b = 0.081204 + 1.173900I$	$-3.18794 + 2.74835I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.633723 + 0.930558I$ $a = -0.264958 + 0.097504I$ $b = 0.360372 + 1.004290I$	$4.67166 + 6.43689I$	0
$u = -0.633723 - 0.930558I$ $a = -0.264958 - 0.097504I$ $b = 0.360372 - 1.004290I$	$4.67166 - 6.43689I$	0
$u = 1.118160 + 0.200599I$ $a = -0.260842 + 0.467046I$ $b = -0.241971 - 0.343939I$	$0.175289 + 0.755522I$	0
$u = 1.118160 - 0.200599I$ $a = -0.260842 - 0.467046I$ $b = -0.241971 + 0.343939I$	$0.175289 - 0.755522I$	0
$u = 1.150880 + 0.096037I$ $a = 0.68555 - 1.68180I$ $b = 1.31788 - 1.07852I$	$1.35285 + 1.35711I$	0
$u = 1.150880 - 0.096037I$ $a = 0.68555 + 1.68180I$ $b = 1.31788 + 1.07852I$	$1.35285 - 1.35711I$	0
$u = -0.675377 + 0.458882I$ $a = -0.774522 + 0.511006I$ $b = 0.883199 + 0.778031I$	$5.77095 - 2.23844I$	0
$u = -0.675377 - 0.458882I$ $a = -0.774522 - 0.511006I$ $b = 0.883199 - 0.778031I$	$5.77095 + 2.23844I$	0
$u = 1.122600 + 0.414773I$ $a = 0.586166 - 0.434387I$ $b = 1.51242 - 0.18112I$	$5.23752 - 12.70220I$	0
$u = 1.122600 - 0.414773I$ $a = 0.586166 + 0.434387I$ $b = 1.51242 + 0.18112I$	$5.23752 + 12.70220I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.117290 + 0.436159I$ $a = -0.245386 + 0.250409I$ $b = -1.214300 + 0.189708I$	$1.03079 - 7.20926I$	0
$u = 1.117290 - 0.436159I$ $a = -0.245386 - 0.250409I$ $b = -1.214300 - 0.189708I$	$1.03079 + 7.20926I$	0
$u = 0.358828 + 0.705709I$ $a = 0.12414 - 1.52453I$ $b = 0.919060 - 0.181247I$	$7.61957 + 8.46626I$	0
$u = 0.358828 - 0.705709I$ $a = 0.12414 + 1.52453I$ $b = 0.919060 + 0.181247I$	$7.61957 - 8.46626I$	0
$u = -1.194170 + 0.216526I$ $a = -0.1010310 + 0.0972354I$ $b = 0.805770 - 0.072117I$	$-3.83451 + 4.09650I$	0
$u = -1.194170 - 0.216526I$ $a = -0.1010310 - 0.0972354I$ $b = 0.805770 + 0.072117I$	$-3.83451 - 4.09650I$	0
$u = -1.044780 + 0.622507I$ $a = 0.273966 + 0.169597I$ $b = 0.782603 + 0.048483I$	$6.48180 + 5.76489I$	0
$u = -1.044780 - 0.622507I$ $a = 0.273966 - 0.169597I$ $b = 0.782603 - 0.048483I$	$6.48180 - 5.76489I$	0
$u = 0.329683 + 0.686949I$ $a = -0.190985 + 0.512753I$ $b = -0.197167 - 1.139410I$	$-2.79527 + 2.32555I$	0
$u = 0.329683 - 0.686949I$ $a = -0.190985 - 0.512753I$ $b = -0.197167 + 1.139410I$	$-2.79527 - 2.32555I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.109786 + 0.751675I$ $a = -0.176464 - 0.176646I$ $b = -0.078798 + 1.232700I$	$-2.40493 - 2.37289I$	$0. + 3.45498I$
$u = 0.109786 - 0.751675I$ $a = -0.176464 + 0.176646I$ $b = -0.078798 - 1.232700I$	$-2.40493 + 2.37289I$	$0. - 3.45498I$
$u = 0.666778 + 0.352330I$ $a = -0.221707 - 0.045968I$ $b = 0.009186 + 0.579580I$	$-1.40153 - 1.05154I$	$-7.86277 + 4.17147I$
$u = 0.666778 - 0.352330I$ $a = -0.221707 + 0.045968I$ $b = 0.009186 - 0.579580I$	$-1.40153 + 1.05154I$	$-7.86277 - 4.17147I$
$u = 1.156020 + 0.469066I$ $a = 0.96710 + 1.33519I$ $b = -0.57209 + 1.34004I$	$-5.31312 - 6.77397I$	$0$
$u = 1.156020 - 0.469066I$ $a = 0.96710 - 1.33519I$ $b = -0.57209 - 1.34004I$	$-5.31312 + 6.77397I$	$0$
$u = -0.017517 + 0.748826I$ $a = 0.531992 - 0.438086I$ $b = -0.676766 + 0.244339I$	$3.83451 - 4.09650I$	$7.00500 + 5.47978I$
$u = -0.017517 - 0.748826I$ $a = 0.531992 + 0.438086I$ $b = -0.676766 - 0.244339I$	$3.83451 + 4.09650I$	$7.00500 - 5.47978I$
$u = 1.180970 + 0.449771I$ $a = 0.390815 + 0.387101I$ $b = 1.036510 + 0.294546I$	$5.16636 - 1.35319I$	$0$
$u = 1.180970 - 0.449771I$ $a = 0.390815 - 0.387101I$ $b = 1.036510 - 0.294546I$	$5.16636 + 1.35319I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.239640 + 0.260824I$ $a = 0.48842 - 1.83678I$ $b = -0.42902 - 1.54205I$	$-6.48180 + 5.76489I$	0
$u = -1.239640 - 0.260824I$ $a = 0.48842 + 1.83678I$ $b = -0.42902 + 1.54205I$	$-6.48180 - 5.76489I$	0
$u = 1.241470 + 0.269723I$ $a = 1.30830 + 1.83546I$ $b = -0.197651 + 1.025220I$	$-1.35285 - 1.35711I$	0
$u = 1.241470 - 0.269723I$ $a = 1.30830 - 1.83546I$ $b = -0.197651 - 1.025220I$	$-1.35285 + 1.35711I$	0
$u = 0.093917 + 1.269940I$ $a = 0.072961 + 0.421937I$ $b = 0.446580 + 1.263970I$	$4.13372 + 13.33210I$	0
$u = 0.093917 - 1.269940I$ $a = 0.072961 - 0.421937I$ $b = 0.446580 - 1.263970I$	$4.13372 - 13.33210I$	0
$u = -1.243180 + 0.320864I$ $a = 0.081592 - 0.683870I$ $b = -0.845275 - 0.346847I$	$8.02284I$	0
$u = -1.243180 - 0.320864I$ $a = 0.081592 + 0.683870I$ $b = -0.845275 + 0.346847I$	$-8.02284I$	0
$u = 0.666795 + 0.141044I$ $a = -0.66167 + 2.42044I$ $b = 0.008754 - 0.627883I$	$1.085330 - 0.334255I$	$9.57088 + 1.14801I$
$u = 0.666795 - 0.141044I$ $a = -0.66167 - 2.42044I$ $b = 0.008754 + 0.627883I$	$1.085330 + 0.334255I$	$9.57088 - 1.14801I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.008160 + 0.854564I$ $a = -0.760383 + 1.106950I$ $b = -0.05437 + 1.53688I$	$-3.73555 - 0.16975I$	0
$u = -1.008160 - 0.854564I$ $a = -0.760383 - 1.106950I$ $b = -0.05437 - 1.53688I$	$-3.73555 + 0.16975I$	0
$u = 1.237590 + 0.474696I$ $a = -1.02448 - 1.34428I$ $b = 0.288525 - 1.360860I$	$-5.77095 - 2.23844I$	0
$u = 1.237590 - 0.474696I$ $a = -1.02448 + 1.34428I$ $b = 0.288525 + 1.360860I$	$-5.77095 + 2.23844I$	0
$u = -0.991826 + 0.911103I$ $a = 0.573584 - 0.231438I$ $b = -0.052938 - 0.952608I$	$3.73555 + 0.16975I$	0
$u = -0.991826 - 0.911103I$ $a = 0.573584 + 0.231438I$ $b = -0.052938 + 0.952608I$	$3.73555 - 0.16975I$	0
$u = -0.597839 + 0.258300I$ $a = -0.753657 - 0.097659I$ $b = 0.768150 - 0.930723I$	$5.27647 - 8.28380I$	$2.01427 + 2.11219I$
$u = -0.597839 - 0.258300I$ $a = -0.753657 + 0.097659I$ $b = 0.768150 + 0.930723I$	$5.27647 + 8.28380I$	$2.01427 - 2.11219I$
$u = -1.357020 + 0.163107I$ $a = -0.38687 + 1.55697I$ $b = 0.369656 + 1.349220I$	$-8.28948 + 0.12430I$	0
$u = -1.357020 - 0.163107I$ $a = -0.38687 - 1.55697I$ $b = 0.369656 - 1.349220I$	$-8.28948 - 0.12430I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.198050 + 0.689303I$ $a = 0.72837 - 1.49367I$ $b = -0.23180 - 1.56792I$	$-4.67166 + 6.43689I$	0
$u = -1.198050 - 0.689303I$ $a = 0.72837 + 1.49367I$ $b = -0.23180 + 1.56792I$	$-4.67166 - 6.43689I$	0
$u = -1.312300 + 0.470220I$ $a = -0.41812 + 1.71308I$ $b = 0.79291 + 1.43838I$	$-4.01258 + 10.32040I$	0
$u = -1.312300 - 0.470220I$ $a = -0.41812 - 1.71308I$ $b = 0.79291 - 1.43838I$	$-4.01258 - 10.32040I$	0
$u = -1.300530 + 0.504252I$ $a = 0.60895 - 1.72558I$ $b = -0.56564 - 1.50999I$	$-5.27647 + 8.28380I$	0
$u = -1.300530 - 0.504252I$ $a = 0.60895 + 1.72558I$ $b = -0.56564 + 1.50999I$	$-5.27647 - 8.28380I$	0
$u = 1.312370 + 0.479515I$ $a = -0.87618 - 1.30973I$ $b = 0.134923 - 1.265220I$	$-5.43217 - 2.10541I$	0
$u = 1.312370 - 0.479515I$ $a = -0.87618 + 1.30973I$ $b = 0.134923 + 1.265220I$	$-5.43217 + 2.10541I$	0
$u = 0.148506 + 1.392590I$ $a = -0.137908 - 0.474435I$ $b = -0.325776 - 1.211070I$	$6.33343I$	0
$u = 0.148506 - 1.392590I$ $a = -0.137908 + 0.474435I$ $b = -0.325776 + 1.211070I$	$-6.33343I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.273860 + 0.592135I$ $a = 0.734001 + 0.890426I$ $b = 0.051740 + 1.166460I$	$-3.31794 + 0.02095I$	0
$u = 1.273860 - 0.592135I$ $a = 0.734001 - 0.890426I$ $b = 0.051740 - 1.166460I$	$-3.31794 - 0.02095I$	0
$u = -0.495397 + 0.310716I$ $a = 0.417119 + 0.722502I$ $b = -0.677998 + 0.911865I$	$1.34210 - 3.05609I$	$-0.937396 - 0.255279I$
$u = -0.495397 - 0.310716I$ $a = 0.417119 - 0.722502I$ $b = -0.677998 - 0.911865I$	$1.34210 + 3.05609I$	$-0.937396 + 0.255279I$
$u = -1.33899 + 0.51718I$ $a = 0.90186 - 1.60507I$ $b = -0.42333 - 1.40097I$	$-5.23752 + 12.70220I$	0
$u = -1.33899 - 0.51718I$ $a = 0.90186 + 1.60507I$ $b = -0.42333 + 1.40097I$	$-5.23752 - 12.70220I$	0
$u = 1.41968 + 0.26250I$ $a = -0.00302 - 1.69865I$ $b = 0.70256 - 1.50646I$	$-1.94463 - 10.04110I$	0
$u = 1.41968 - 0.26250I$ $a = -0.00302 + 1.69865I$ $b = 0.70256 + 1.50646I$	$-1.94463 + 10.04110I$	0
$u = -1.36539 + 0.52222I$ $a = -0.78985 + 1.39214I$ $b = 0.400176 + 1.283150I$	$-7.61957 + 8.46626I$	0
$u = -1.36539 - 0.52222I$ $a = -0.78985 - 1.39214I$ $b = 0.400176 - 1.283150I$	$-7.61957 - 8.46626I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.423313 + 0.296983I$ $a = 0.00550 - 1.68778I$ $b = -0.724744 - 0.429452I$	$1.40153 + 1.05154I$	$7.86277 - 4.17147I$
$u = -0.423313 - 0.296983I$ $a = 0.00550 + 1.68778I$ $b = -0.724744 + 0.429452I$	$1.40153 - 1.05154I$	$7.86277 + 4.17147I$
$u = 0.097755 + 0.491486I$ $a = -1.236770 + 0.483276I$ $b = 0.216346 + 0.038687I$	$-1.53223I$	$0. + 5.21422I$
$u = 0.097755 - 0.491486I$ $a = -1.236770 - 0.483276I$ $b = 0.216346 - 0.038687I$	$1.53223I$	$0. - 5.21422I$
$u = 1.38858 + 0.60929I$ $a = -0.54525 - 1.64395I$ $b = 0.61138 - 1.50633I$	$-19.8680I$	$0$
$u = 1.38858 - 0.60929I$ $a = -0.54525 + 1.64395I$ $b = 0.61138 + 1.50633I$	$19.8680I$	$0$
$u = -1.40905 + 0.60703I$ $a = -0.47380 + 1.69536I$ $b = 0.376799 + 1.360960I$	$1.94463 + 10.04110I$	$0$
$u = -1.40905 - 0.60703I$ $a = -0.47380 - 1.69536I$ $b = 0.376799 - 1.360960I$	$1.94463 - 10.04110I$	$0$
$u = 1.43146 + 0.56014I$ $a = -0.54374 - 1.44918I$ $b = -0.003348 - 1.376640I$	$-5.16636 + 1.35319I$	$0$
$u = 1.43146 - 0.56014I$ $a = -0.54374 + 1.44918I$ $b = -0.003348 + 1.376640I$	$-5.16636 - 1.35319I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41270 + 0.64298I$ $a = 0.52202 + 1.52720I$ $b = -0.53044 + 1.45997I$	$-4.13372 - 13.33210I$	0
$u = 1.41270 - 0.64298I$ $a = 0.52202 - 1.52720I$ $b = -0.53044 - 1.45997I$	$-4.13372 + 13.33210I$	0
$u = 1.47977 + 0.48939I$ $a = 0.38259 + 1.46555I$ $b = -0.244975 + 1.367290I$	$-7.79727 - 3.48496I$	0
$u = 1.47977 - 0.48939I$ $a = 0.38259 - 1.46555I$ $b = -0.244975 - 1.367290I$	$-7.79727 + 3.48496I$	0
$u = -1.52475 + 0.33245I$ $a = 0.592449 - 1.130420I$ $b = -0.217610 - 0.848286I$	$7.34776I$	0
$u = -1.52475 - 0.33245I$ $a = 0.592449 + 1.130420I$ $b = -0.217610 + 0.848286I$	$-7.34776I$	0
$u = 1.59554 + 0.07582I$ $a = -0.090742 + 1.368010I$ $b = -0.652744 + 1.157550I$	$-6.13156 - 2.73739I$	0
$u = 1.59554 - 0.07582I$ $a = -0.090742 - 1.368010I$ $b = -0.652744 - 1.157550I$	$-6.13156 + 2.73739I$	0
$u = -0.35426 + 1.57209I$ $a = 0.194375 - 0.813301I$ $b = 0.176423 - 1.150600I$	$6.13156 - 2.73739I$	0
$u = -0.35426 - 1.57209I$ $a = 0.194375 + 0.813301I$ $b = 0.176423 + 1.150600I$	$6.13156 + 2.73739I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.49661 + 0.60373I$ $a = -0.34049 - 1.45850I$ $b = 0.502340 - 1.293510I$	$1.74076 - 6.86356I$	0
$u = 1.49661 - 0.60373I$ $a = -0.34049 + 1.45850I$ $b = 0.502340 + 1.293510I$	$1.74076 + 6.86356I$	0
$u = 0.10566 + 1.61110I$ $a = 0.162626 + 0.594949I$ $b = 0.209513 + 1.047390I$	$6.69560 - 0.54555I$	0
$u = 0.10566 - 1.61110I$ $a = 0.162626 - 0.594949I$ $b = 0.209513 - 1.047390I$	$6.69560 + 0.54555I$	0
$u = -0.339019 + 0.139188I$ $a = -1.60556 - 1.70786I$ $b = 0.747329 - 0.756285I$	$5.43217 + 2.10541I$	$2.12435 - 2.26526I$
$u = -0.339019 - 0.139188I$ $a = -1.60556 + 1.70786I$ $b = 0.747329 + 0.756285I$	$5.43217 - 2.10541I$	$2.12435 + 2.26526I$
$u = -1.62410 + 0.36256I$ $a = 0.595319 - 1.218370I$ $b = 0.034506 - 1.159720I$	$-1.74076 - 6.86356I$	0
$u = -1.62410 - 0.36256I$ $a = 0.595319 + 1.218370I$ $b = 0.034506 + 1.159720I$	$-1.74076 + 6.86356I$	0
$u = -1.72076 + 0.31634I$ $a = -0.501264 + 1.182190I$ $b = 0.109340 + 1.061360I$	$-6.69560 + 0.54555I$	0
$u = -1.72076 - 0.31634I$ $a = -0.501264 - 1.182190I$ $b = 0.109340 - 1.061360I$	$-6.69560 - 0.54555I$	0

$$\text{II. } I_2^u = \langle -8.20 \times 10^{33} u^{31} - 4.22 \times 10^{34} u^{30} + \dots + 9.32 \times 10^{31} b - 8.67 \times 10^{34}, -1.10 \times 10^{34} u^{31} - 5.66 \times 10^{34} u^{30} + \dots + 9.32 \times 10^{31} a - 1.17 \times 10^{35}, u^{32} + 6u^{31} + \dots + 48u + 9 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 117.780u^{31} + 606.634u^{30} + \dots + 5227.65u + 1257.45 \\ 87.9105u^{31} + 452.847u^{30} + \dots + 3864.42u + 929.327 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 384.711u^{31} + 1981.16u^{30} + \dots + 16939.4u + 4078.44 \\ 321.464u^{31} + 1655.85u^{30} + \dots + 14166.0u + 3409.21 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 801.716u^{31} + 4128.38u^{30} + \dots + 35279.6u + 8483.49 \\ 652.744u^{31} + 3361.19u^{30} + \dots + 28713.1u + 6905.43 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 428.301u^{31} + 2206.06u^{30} + \dots + 18866.4u + 4543.65 \\ 352.578u^{31} + 1816.29u^{30} + \dots + 15532.2u + 3738.93 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 96.7554u^{31} + 498.440u^{30} + \dots + 4275.68u + 1028.55 \\ 66.8855u^{31} + 344.654u^{30} + \dots + 2912.45u + 700.428 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 302.990u^{31} + 1560.23u^{30} + \dots + 13316.1u + 3201.65 \\ 246.862u^{31} + 1271.57u^{30} + \dots + 10861.5u + 2614.73 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -55.2391u^{31} - 284.324u^{30} + \dots - 2423.72u - 584.247 \\ -48.4524u^{31} - 250.439u^{30} + \dots - 2119.52u - 515.406 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 729.244u^{31} + 3754.96u^{30} + \dots + 32086.0u + 7720.11 \\ 594.059u^{31} + 3059.45u^{30} + \dots + 26142.9u + 6290.22 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-166.444u^{31} - 858.041u^{30} + \dots - 7362.62u - 1779.90$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{32} - 9u^{31} + \dots + u + 1$
$c_2, c_{12}$	$u^{32} - 6u^{31} + \dots - 48u + 9$
$c_3$	$u^{32} - u^{31} + \dots - 5u + 1$
$c_4$	$u^{32} + u^{31} + \dots + 5u + 1$
$c_5, c_{10}$	$u^{32} + 5u^{31} + \dots - 3u + 1$
$c_6, c_9$	$u^{32} + 6u^{31} + \dots + 48u + 9$
$c_7, c_8$	$u^{32} - 5u^{31} + \dots + 3u + 1$
$c_{11}$	$u^{32} + 9u^{31} + \dots - u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{32} - 9y^{31} + \dots - 9y + 1$
$c_2, c_6, c_9$ $c_{12}$	$y^{32} - 16y^{31} + \dots - 828y + 81$
$c_3, c_4$	$y^{32} - 7y^{31} + \dots - 41y + 1$
$c_5, c_7, c_8$ $c_{10}$	$y^{32} + 27y^{31} + \dots + 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.067705 + 1.010090I$		
$a = -0.048060 - 0.172045I$	$-1.61372 - 4.11514I$	$-0.85266 + 6.11990I$
$b = 0.353850 - 1.166680I$		
$u = -0.067705 - 1.010090I$		
$a = -0.048060 + 0.172045I$	$-1.61372 + 4.11514I$	$-0.85266 - 6.11990I$
$b = 0.353850 + 1.166680I$		
$u = -0.943719 + 0.595766I$		
$a = 0.088776 + 0.635826I$	$5.35541 + 0.09313I$	$6.64556 + 0.50727I$
$b = -0.448591 - 0.100099I$		
$u = -0.943719 - 0.595766I$		
$a = 0.088776 - 0.635826I$	$5.35541 - 0.09313I$	$6.64556 - 0.50727I$
$b = -0.448591 + 0.100099I$		
$u = -0.909086 + 0.676337I$		
$a = -0.737129 - 0.415629I$	$5.33495 + 4.85201I$	$2.71864 - 2.25825I$
$b = -0.177399 + 0.264576I$		
$u = -0.909086 - 0.676337I$		
$a = -0.737129 + 0.415629I$	$5.33495 - 4.85201I$	$2.71864 + 2.25825I$
$b = -0.177399 - 0.264576I$		
$u = -0.849383 + 0.001189I$		
$a = 1.96233 + 2.54289I$	$-0.523059 + 0.539324I$	$9.43070 - 3.62826I$
$b = 1.83959 + 1.90523I$		
$u = -0.849383 - 0.001189I$		
$a = 1.96233 - 2.54289I$	$-0.523059 - 0.539324I$	$9.43070 + 3.62826I$
$b = 1.83959 - 1.90523I$		
$u = 1.081470 + 0.446382I$		
$a = -0.87185 - 1.52233I$	$-5.33495 - 4.85201I$	$-2.71864 + 2.25825I$
$b = 0.34721 - 1.47661I$		
$u = 1.081470 - 0.446382I$		
$a = -0.87185 + 1.52233I$	$-5.33495 + 4.85201I$	$-2.71864 - 2.25825I$
$b = 0.34721 + 1.47661I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.715685 + 0.218279I$ $a = -1.46034 + 2.45351I$ $b = 0.093344 - 0.937071I$	$0.523059 - 0.539324I$	$-9.43070 + 3.62826I$
$u = 0.715685 - 0.218279I$ $a = -1.46034 - 2.45351I$ $b = 0.093344 + 0.937071I$	$0.523059 + 0.539324I$	$-9.43070 - 3.62826I$
$u = 0.703772 + 0.206426I$ $a = -0.14434 - 1.44890I$ $b = 0.470436 + 0.090968I$	$-1.04605I$	$0. + 6.29952I$
$u = 0.703772 - 0.206426I$ $a = -0.14434 + 1.44890I$ $b = 0.470436 - 0.090968I$	$1.04605I$	$0. - 6.29952I$
$u = -0.093791 + 1.268970I$ $a = -0.238721 - 0.635122I$ $b = -0.250820 - 0.812318I$	$7.26512 - 0.92116I$	$7.37317 + 3.02039I$
$u = -0.093791 - 1.268970I$ $a = -0.238721 + 0.635122I$ $b = -0.250820 + 0.812318I$	$7.26512 + 0.92116I$	$7.37317 - 3.02039I$
$u = 1.171050 + 0.664348I$ $a = 0.82723 + 1.15816I$ $b = 0.026494 + 1.398610I$	$-5.35541 + 0.09313I$	$0$
$u = 1.171050 - 0.664348I$ $a = 0.82723 - 1.15816I$ $b = 0.026494 - 1.398610I$	$-5.35541 - 0.09313I$	$0$
$u = -1.291840 + 0.504469I$ $a = -0.60889 + 1.63176I$ $b = 0.64554 + 1.43209I$	$-5.43955 + 9.43203I$	$0$
$u = -1.291840 - 0.504469I$ $a = -0.60889 - 1.63176I$ $b = 0.64554 - 1.43209I$	$-5.43955 - 9.43203I$	$0$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.509836 + 0.230939I$ $a = -1.20134 + 1.58135I$ $b = -0.576126 - 0.662311I$	$5.43955 + 9.43203I$	$3.26415 - 8.13278I$
$u = -0.509836 - 0.230939I$ $a = -1.20134 - 1.58135I$ $b = -0.576126 + 0.662311I$	$5.43955 - 9.43203I$	$3.26415 + 8.13278I$
$u = -0.229199 + 0.437345I$ $a = 1.77415 + 0.07651I$ $b = 0.440725 + 0.723545I$	$1.61372 + 4.11514I$	$0.85266 - 6.11990I$
$u = -0.229199 - 0.437345I$ $a = 1.77415 - 0.07651I$ $b = 0.440725 - 0.723545I$	$1.61372 - 4.11514I$	$0.85266 + 6.11990I$
$u = -1.52202 + 0.34957I$ $a = 0.17516 - 1.62801I$ $b = -0.485248 - 1.220680I$	$9.42763I$	0
$u = -1.52202 - 0.34957I$ $a = 0.17516 + 1.62801I$ $b = -0.485248 + 1.220680I$	$-9.42763I$	0
$u = 1.56447 + 0.27140I$ $a = 0.522596 + 1.253690I$ $b = -0.190106 + 1.102650I$	$-7.26512 - 0.92116I$	0
$u = 1.56447 - 0.27140I$ $a = 0.522596 - 1.253690I$ $b = -0.190106 - 1.102650I$	$-7.26512 + 0.92116I$	0
$u = -0.18698 + 1.59880I$ $a = -0.248128 + 0.750877I$ $b = -0.145927 + 1.131960I$	$6.00215 - 2.42101I$	0
$u = -0.18698 - 1.59880I$ $a = -0.248128 - 0.750877I$ $b = -0.145927 - 1.131960I$	$6.00215 + 2.42101I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.63288 + 0.14865I$	$-6.00215 + 2.42101I$	0
$a = 0.041897 + 1.378680I$		
$b = 0.557035 + 1.203400I$		
$u = -1.63288 - 0.14865I$	$-6.00215 - 2.42101I$	0
$a = 0.041897 - 1.378680I$		
$b = 0.557035 - 1.203400I$		



**III.**

$$I_3^u = \langle -9a^4 - 16a^3 - 76a^2 + 13b - 40a - 8, a^5 + 2a^4 + 9a^3 + 6a^2 + 3a + 1, u - 1 \rangle$$

**(i) Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ 0.692308a^4 + 1.23077a^3 + \dots + 3.07692a + 0.615385 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.153846a^4 - 0.384615a^3 + \dots - 1.46154a + 0.307692 \\ -0.461538a^4 - 1.15385a^3 + \dots - 4.38462a - 1.07692 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.461538a^4 + 1.15385a^3 + \dots + 4.38462a + 1.07692 \\ 0.769231a^4 + 1.92308a^3 + \dots + 7.30769a + 2.46154 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.461538a^4 - 1.15385a^3 + \dots - 4.38462a - 1.07692 \\ -0.769231a^4 - 1.92308a^3 + \dots - 7.30769a - 2.46154 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.692308a^4 + 1.23077a^3 + \dots + 3.07692a + 0.615385 \\ 1.38462a^4 + 2.46154a^3 + \dots + 5.15385a + 1.23077 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.461538a^4 + 1.15385a^3 + \dots + 4.38462a + 1.07692 \\ 0.769231a^4 + 1.92308a^3 + \dots + 7.30769a + 2.46154 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.692308a^4 + 1.23077a^3 + \dots + 2.07692a + 0.615385 \\ 1.38462a^4 + 2.46154a^3 + \dots + 5.15385a + 1.23077 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.461538a^4 + 1.15385a^3 + \dots + 4.38462a + 1.07692 \\ 0.769231a^4 + 1.92308a^3 + \dots + 7.30769a + 2.46154 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes = -6**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^5 + 2u^4 + 3u^3 + 2u^2 + u - 1$
$c_2, c_6$	$u^5$
$c_3, c_7, c_{10}$ $c_{11}$	$u^5 + u^3 + u + 1$
$c_4$	$u^5 + u^3 - 2u^2 - u + 2$
$c_5, c_8$	$u^5 - 2u^4 + 3u^3 - 2u^2 + u + 1$
$c_9, c_{12}$	$(u + 1)^5$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_8$	$y^5 + 2y^4 + 3y^3 + 6y^2 + 5y - 1$
$c_2, c_6$	$y^5$
$c_3, c_7, c_{10}$ $c_{11}$	$y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1$
$c_4$	$y^5 + 2y^4 - y^3 - 6y^2 + 9y - 4$
$c_9, c_{12}$	$(y - 1)^5$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = -0.104309 + 0.503525I$ $b = -0.994802 + 0.833601I$	-1.64493	-6.00000
$u = 1.00000$ $a = -0.104309 - 0.503525I$ $b = -0.994802 - 0.833601I$	-1.64493	-6.00000
$u = 1.00000$ $a = -0.489595$ $b = 0.405620$	-1.64493	-6.00000
$u = 1.00000$ $a = -0.65089 + 2.70201I$ $b = -0.208008 + 1.191750I$	-1.64493	-6.00000
$u = 1.00000$ $a = -0.65089 - 2.70201I$ $b = -0.208008 - 1.191750I$	-1.64493	-6.00000

$$\text{IV. } I_4^u = \langle b^5 - 2b^4a + b^3a^2 - b^3 + a^2b + b + a - 1, u - 1 \rangle$$

**(i) Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} ba + 1 \\ b^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b^2a + b + a \\ b^3 + b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} b^2 \\ 2b^2 - ba - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} b \\ 2b - a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -b^2 \\ -2b^2 + ba + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} b^4 - b^3a - b^2 + 1 \\ 2b^4 - 3b^3a + b^2a^2 - 3b^2 + 2ba + 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b^2a - b^2 + b + a \\ b^3 - 2b^2 + ba + b + 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = 0**

**(iv) u-Polynomials at the component :** It cannot be defined for a positive dimension component.

**(v) Riley Polynomials at the component :** It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

Solution to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = \dots$		
$a = \dots$	0	0
$b = \dots$		

$$\mathbf{V}. I_1^v = \langle a, b^5 + b^3 + b + 1, v - 1 \rangle$$

**(i) Arc colorings**

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ b^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b \\ b^3 + b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} b^2 + 1 \\ b^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} b^2 + 1 \\ b^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} b^4 + b^2 + 1 \\ b^4 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b^2 + b + 1 \\ b^3 + b^2 + b \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes = 6**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_8$	$u^5 + u^3 + u - 1$
$c_2, c_6$	$(u - 1)^5$
$c_3$	$u^5 + u^3 + 2u^2 - u - 2$
$c_7, c_{10}$	$u^5 + 2u^4 + 3u^3 + 2u^2 + u - 1$
$c_9, c_{12}$	$u^5$
$c_{11}$	$u^5 - 2u^4 + 3u^3 - 2u^2 + u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_8$	$y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1$
$c_2, c_6$	$(y - 1)^5$
$c_3$	$y^5 + 2y^4 - y^3 - 6y^2 + 9y - 4$
$c_7, c_{10}, c_{11}$	$y^5 + 2y^4 + 3y^3 + 6y^2 + 5y - 1$
$c_9, c_{12}$	$y^5$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$ $a = 0$ $b = 0.707729 + 0.841955I$	1.64493	6.00000
$v = 1.00000$ $a = 0$ $b = 0.707729 - 0.841955I$	1.64493	6.00000
$v = 1.00000$ $a = 0$ $b = -0.389287 + 1.070680I$	1.64493	6.00000
$v = 1.00000$ $a = 0$ $b = -0.389287 - 1.070680I$	1.64493	6.00000
$v = 1.00000$ $a = 0$ $b = -0.636883$	1.64493	6.00000

$$\text{VI. } I_2^v = \langle a, b^2 - b + 1, v - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ b - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b \\ b - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} b \\ b - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} b \\ b - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b \\ b - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_7$ $c_8$	$u^2 - u + 1$
$c_2, c_6, c_9$ $c_{12}$	$u^2$
$c_4, c_5, c_{10}$ $c_{11}$	$u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_5, c_7, c_8$ $c_{10}, c_{11}$	$y^2 + y + 1$
$c_2, c_6, c_9$ $c_{12}$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$	0	0
$b = 0.500000 + 0.866025I$		
$v = 1.00000$		
$a = 0$	0	0
$b = 0.500000 - 0.866025I$		

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$16(u^2 - u + 1)(u^5 + u^3 + u - 1)(u^5 + 2u^4 + 3u^3 + 2u^2 + u - 1)$ $\cdot (u^{32} - 9u^{31} + \dots + u + 1)(16u^{130} - 216u^{129} + \dots - 134148u + 11877)$
$c_2$	$u^7(u - 1)^5(u^{32} - 6u^{31} + \dots - 48u + 9)$ $\cdot (u^{130} + 10u^{129} + \dots + 40002776u + 2811556)$
$c_3$	$48(u^2 - u + 1)(u^5 + u^3 + u + 1)(u^5 + u^3 + 2u^2 - u - 2)$ $\cdot (u^{32} - u^{31} + \dots - 5u + 1)$ $\cdot (48u^{130} - 144u^{129} + \dots - 1545225608u + 456956512)$
$c_4$	$48(u^2 + u + 1)(u^5 + u^3 + u - 1)(u^5 + u^3 - 2u^2 - u + 2)$ $\cdot (u^{32} + u^{31} + \dots + 5u + 1)$ $\cdot (48u^{130} + 144u^{129} + \dots + 1545225608u + 456956512)$
$c_5$	$16(u^2 + u + 1)(u^5 + u^3 + u - 1)(u^5 - 2u^4 + 3u^3 - 2u^2 + u + 1)$ $\cdot (u^{32} + 5u^{31} + \dots - 3u + 1)$ $\cdot (16u^{130} + 72u^{129} + \dots + 67813572u + 7939137)$
$c_6$	$u^7(u - 1)^5(u^{32} + 6u^{31} + \dots + 48u + 9)$ $\cdot (u^{130} + 10u^{129} + \dots + 40002776u + 2811556)$
$c_7$	$16(u^2 - u + 1)(u^5 + u^3 + u + 1)(u^5 + 2u^4 + 3u^3 + 2u^2 + u - 1)$ $\cdot (u^{32} - 5u^{31} + \dots + 3u + 1)$ $\cdot (16u^{130} - 72u^{129} + \dots - 67813572u + 7939137)$
$c_8$	$16(u^2 - u + 1)(u^5 + u^3 + u - 1)(u^5 - 2u^4 + 3u^3 - 2u^2 + u + 1)$ $\cdot (u^{32} - 5u^{31} + \dots + 3u + 1)$ $\cdot (16u^{130} + 72u^{129} + \dots + 67813572u + 7939137)$
$c_9$	$u^7(u + 1)^5(u^{32} + 6u^{31} + \dots + 48u + 9)$ $\cdot (u^{130} - 10u^{129} + \dots - 40002776u + 2811556)$
$c_{10}$	$16(u^2 + u + 1)(u^5 + u^3 + u + 1)(u^5 + 2u^4 + 3u^3 + 2u^2 + u - 1)$ $\cdot (u^{32} + 5u^{31} + \dots - 3u + 1)$ $\cdot (16u^{130} - 72u^{129} + \dots - 67813572u + 7939137)$
$c_{11}$	$16(u^2 + u + 1)(u^5 + u^3 + u + 1)(u^5 - 2u^4 + 3u^3 - 2u^2 + u + 1)$ $\cdot (u^{32} + 9u^{31} + \dots - u + 1)(16u^{130} + 216u^{129} + \dots + 134148u + 11877)$
$c_{12}$	$u^7(u + 1)^5(u^{32} - 6u^{31} + \dots - 48u + 9)$ $\cdot (u^{130} - 10u^{129} + \dots - 40002776u + 2811556)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$256(y^2 + y + 1)(y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1)$ $\cdot (y^5 + 2y^4 + 3y^3 + 6y^2 + 5y - 1)(y^{32} - 9y^{31} + \dots - 9y + 1)$ $\cdot (256y^{130} - 4640y^{129} + \dots + 2950330002y + 141063129)$
$c_2, c_6, c_9$ $c_{12}$	$y^7(y - 1)^5(y^{32} - 16y^{31} + \dots - 828y + 81)$ $\cdot (y^{130} - 80y^{129} + \dots - 226520781477232y + 7904847141136)$
$c_3, c_4$	$2304(y^2 + y + 1)(y^5 + 2y^4 - y^3 - 6y^2 + 9y - 4)$ $\cdot (y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1)(y^{32} - 7y^{31} + \dots - 41y + 1)$ $\cdot (2304y^{130} - 1.24 \times 10^5 y^{129} + \dots - 5.35 \times 10^{18} y + 2.09 \times 10^{17})$
$c_5, c_7, c_8$ $c_{10}$	$256(y^2 + y + 1)(y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1)$ $\cdot (y^5 + 2y^4 + 3y^3 + 6y^2 + 5y - 1)(y^{32} + 27y^{31} + \dots + 5y + 1)$ $\cdot (256y^{130} + 23008y^{129} + \dots - 581798760447684y + 63029896304769)$