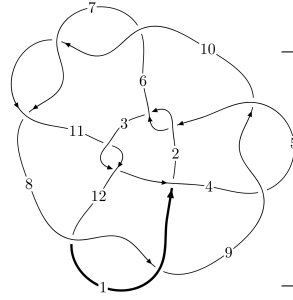
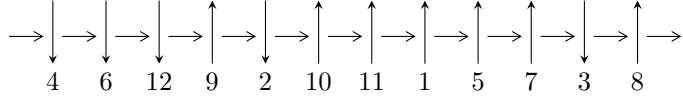


12a<sub>0999</sub> (K12a<sub>0999</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$6,10 \xrightarrow{c_6} 7 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 3,8 \xrightarrow{c_{11}} 12 \xrightarrow{c_2} 2 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \xrightarrow{c_4} 4 \xrightarrow{c_1} 1 \rightsquigarrow c_3, c_8, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 826872493u^{24} + 41514578887u^{23} + \dots + 26691174904b + 267919895192, \\ 75775316763u^{24} - 724263180731u^{23} + \dots + 53382349808a - 515069062880, \\ u^{25} - 11u^{24} + \dots - 80u + 16 \rangle$$

$$I_2^u = \langle -10u^{35} - 12u^{34} + \dots + 8b + 68, -68u^{35}a + 508u^{35} + \dots - 1145a + 7276, u^{36} + 4u^{35} + \dots + 16u + 1 \rangle$$

$$I_3^u = \langle -7u^{10} + 4u^9 + 36u^8 - 34u^7 - 43u^6 + 60u^5 + 10u^4 - 31u^3 - 19u^2 + 11b + 16u + 17, \\ -8u^{10} + 25u^9 + 38u^8 - 163u^7 + 31u^6 + 298u^5 - 262u^4 - 136u^3 + 269u^2 + 11a - 32u - 78, \\ u^{11} - 2u^{10} - 5u^9 + 14u^8 + u^7 - 27u^6 + 18u^5 + 15u^4 - 20u^3 - u^2 + 6u + 1 \rangle$$

$$I_1^v = \langle a, b + 1, v + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 109 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 8.27 \times 10^8 u^{24} + 4.15 \times 10^{10} u^{23} + \dots + 2.67 \times 10^{10} b + 2.68 \times 10^{11}, 7.58 \times 10^{10} u^{24} - 7.24 \times 10^{11} u^{23} + \dots + 5.34 \times 10^{10} a - 5.15 \times 10^{11}, u^{25} - 11u^{24} + \dots - 80u + 16 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -1.41948u^{24} + 13.5675u^{23} + \dots - 51.2819u + 9.64868 \\ -0.0309792u^{24} - 1.55537u^{23} + \dots + 37.1258u - 10.0378 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.167582u^{24} - 3.50276u^{23} + \dots + 58.5852u - 16.0667 \\ 3.79748u^{24} - 34.4987u^{23} + \dots + 133.770u - 29.2311 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -1.45046u^{24} + 12.0121u^{23} + \dots - 14.1561u - 0.389094 \\ -0.0309792u^{24} - 1.55537u^{23} + \dots + 37.1258u - 10.0378 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 3.96506u^{24} - 38.0015u^{23} + \dots + 190.355u - 44.2978 \\ 3.79748u^{24} - 34.4987u^{23} + \dots + 132.770u - 29.2311 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1.73754u^{24} + 15.9703u^{23} + \dots - 68.0866u + 14.9573 \\ 0.976986u^{24} - 8.80582u^{23} + \dots + 24.7513u - 4.30668 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 6.50025u^{24} - 60.8358u^{23} + \dots + 275.705u - 62.6895 \\ -2.16560u^{24} + 22.8582u^{23} + \dots - 153.338u + 36.8239 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -4.43829u^{24} + 41.9516u^{23} + \dots - 195.816u + 43.9195 \\ -1.35725u^{24} + 12.5528u^{23} + \dots - 50.4134u + 10.8323 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{145412112683}{3336396863} u^{24} - \frac{1365948008373}{3336396863} u^{23} + \dots + \frac{6268794612260}{3336396863} u - \frac{1430304974606}{3336396863}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{25} - 22u^{24} + \dots + 5120u + 512$
$c_2, c_3, c_5$ $c_{11}$	$u^{25} - u^{24} + \dots - 4u + 1$
$c_4, c_8, c_9$ $c_{12}$	$u^{25} - 11u^{23} + \dots + u - 1$
$c_6, c_7, c_{10}$	$u^{25} - 11u^{24} + \dots - 80u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{25} - 2y^{24} + \dots + 76808192y - 262144$
$c_2, c_3, c_5$ $c_{11}$	$y^{25} - 15y^{24} + \dots + 50y - 1$
$c_4, c_8, c_9$ $c_{12}$	$y^{25} - 22y^{24} + \dots + 21y - 1$
$c_6, c_7, c_{10}$	$y^{25} - 23y^{24} + \dots - 1408y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00934$ $a = -0.805015$ $b = 1.63266$	-7.20191	30.6470
$u = 0.012976 + 1.033860I$ $a = 0.633148 - 0.106162I$ $b = 0.791764 + 0.522766I$	$3.03037 - 1.54703I$	$6.68506 + 3.68219I$
$u = 0.012976 - 1.033860I$ $a = 0.633148 + 0.106162I$ $b = 0.791764 - 0.522766I$	$3.03037 + 1.54703I$	$6.68506 - 3.68219I$
$u = -0.881775 + 0.323566I$ $a = -0.378664 + 0.249573I$ $b = 0.365509 - 0.726585I$	$6.42854 - 2.68579I$	$9.83614 + 1.93428I$
$u = -0.881775 - 0.323566I$ $a = -0.378664 - 0.249573I$ $b = 0.365509 + 0.726585I$	$6.42854 + 2.68579I$	$9.83614 - 1.93428I$
$u = -0.477303 + 0.717814I$ $a = 0.009597 - 0.906421I$ $b = 1.269930 + 0.185562I$	$-7.01624 - 2.33284I$	$-5.90770 + 2.60194I$
$u = -0.477303 - 0.717814I$ $a = 0.009597 + 0.906421I$ $b = 1.269930 - 0.185562I$	$-7.01624 + 2.33284I$	$-5.90770 - 2.60194I$
$u = -0.482722 + 1.037880I$ $a = -0.369971 + 0.530061I$ $b = -1.214990 - 0.563112I$	$1.10842 - 12.71280I$	$2.59152 + 8.71606I$
$u = -0.482722 - 1.037880I$ $a = -0.369971 - 0.530061I$ $b = -1.214990 + 0.563112I$	$1.10842 + 12.71280I$	$2.59152 - 8.71606I$
$u = 1.329560 + 0.203875I$ $a = 0.28740 - 1.62065I$ $b = -0.662175 + 0.545556I$	$2.65006 + 2.55544I$	$3.11128 - 1.65198I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.329560 - 0.203875I$ $a = 0.28740 + 1.62065I$ $b = -0.662175 - 0.545556I$	$2.65006 - 2.55544I$	$3.11128 + 1.65198I$
$u = -0.98981 + 1.06101I$ $a = 0.181907 + 0.253452I$ $b = -0.954754 + 0.361220I$	$2.30832 + 5.78881I$	$2.00000 - 7.25000I$
$u = -0.98981 - 1.06101I$ $a = 0.181907 - 0.253452I$ $b = -0.954754 - 0.361220I$	$2.30832 - 5.78881I$	$2.00000 + 7.25000I$
$u = 0.516035$ $a = 0.631196$ $b = 0.157637$	$0.767709$	$13.0610$
$u = 1.49267 + 0.27371I$ $a = -0.65793 + 1.31350I$ $b = 1.148310 - 0.509995I$	$-0.65901 + 5.99024I$	$0. - 4.38665I$
$u = 1.49267 - 0.27371I$ $a = -0.65793 - 1.31350I$ $b = 1.148310 + 0.509995I$	$-0.65901 - 5.99024I$	$0. + 4.38665I$
$u = 1.47479 + 0.50270I$ $a = 0.123556 + 1.187480I$ $b = 1.108500 - 0.652505I$	$7.77371 + 7.32084I$	$7.72526 - 5.56309I$
$u = 1.47479 - 0.50270I$ $a = 0.123556 - 1.187480I$ $b = 1.108500 + 0.652505I$	$7.77371 - 7.32084I$	$7.72526 + 5.56309I$
$u = 1.58061 + 0.03704I$ $a = -0.272956 - 1.225950I$ $b = 0.151992 + 1.145230I$	$14.6920 + 3.8040I$	$11.54426 - 2.08774I$
$u = 1.58061 - 0.03704I$ $a = -0.272956 + 1.225950I$ $b = 0.151992 - 1.145230I$	$14.6920 - 3.8040I$	$11.54426 + 2.08774I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.54138 + 0.37767I$ $a = 0.30399 - 1.46629I$ $b = -1.36369 + 0.77531I$	$7.5940 + 17.7952I$	$5.80164 - 8.80793I$
$u = 1.54138 - 0.37767I$ $a = 0.30399 + 1.46629I$ $b = -1.36369 - 0.77531I$	$7.5940 - 17.7952I$	$5.80164 + 8.80793I$
$u = 0.123896 + 0.326612I$ $a = -1.67598 + 1.41797I$ $b = -0.709073 - 0.106576I$	$-1.292320 - 0.176707I$	$-7.01154 + 0.09257I$
$u = 0.123896 - 0.326612I$ $a = -1.67598 - 1.41797I$ $b = -0.709073 + 0.106576I$	$-1.292320 + 0.176707I$	$-7.01154 - 0.09257I$
$u = 2.04475$ $a = 0.305643$ $b = -0.652933$	13.8003	0

$$\text{II. } I_2^u = \langle -10u^{35} - 12u^{34} + \dots + 8b + 68, -68u^{35}a + 508u^{35} + \dots - 1145a + 7276, u^{36} + 4u^{35} + \dots + 16u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ \frac{5}{4}u^{35} + \frac{3}{2}u^{34} + \dots + \frac{57}{8}u - \frac{17}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{5}{4}u^{35}a - 2u^{35} + \dots + \frac{17}{2}a - \frac{439}{8} \\ \frac{27}{8}u^{35} + \frac{59}{8}u^{34} + \dots + \frac{123}{4}u - \frac{53}{8} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{5}{4}u^{35} + \frac{3}{2}u^{34} + \dots + a - \frac{17}{2} \\ \frac{5}{4}u^{35} + \frac{3}{2}u^{34} + \dots + \frac{57}{8}u - \frac{17}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2.37500au^{35} + 6.62500au^{34} + \dots + 3.12500a - 23.5000 \\ \frac{47}{8}u^{35}a - 2u^{35} + \dots + \frac{35}{8}a - \frac{635}{8} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u^{35}a - \frac{41}{8}u^{35} + \dots + \frac{37}{4}a - \frac{385}{8} \\ -\frac{9}{4}u^{35}a + \frac{63}{8}u^{35} + \dots - \frac{5}{2}a + 84 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u^{35}a + \frac{67}{2}u^{35} + \dots - \frac{627}{8}a + \frac{1065}{2} \\ \frac{27}{8}u^{35}a + u^{35} + \dots + \frac{11}{4}a - \frac{15}{4} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2u^{35}a + u^{35} + \dots + \frac{61}{8}a - \frac{495}{8} \\ -\frac{31}{8}u^{35}a + 3u^{35} + \dots - \frac{23}{8}a - \frac{55}{8} \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 148u^{35} + \frac{1111}{2}u^{34} + \dots + 1907u + \frac{3931}{2}$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{36} + 11u^{35} + \cdots + 12u + 1)^2$
$c_2, c_3, c_5$ $c_{11}$	$u^{72} + 5u^{71} + \cdots + 44u + 31$
$c_4, c_8, c_9$ $c_{12}$	$u^{72} + 15u^{71} + \cdots + 1022u + 149$
$c_6, c_7, c_{10}$	$(u^{36} + 4u^{35} + \cdots + 16u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{36} + 9y^{35} + \dots - 78y + 1)^2$
$c_2, c_3, c_5$ $c_{11}$	$y^{72} - 109y^{71} + \dots - 5904y + 961$
$c_4, c_8, c_9$ $c_{12}$	$y^{72} - 125y^{71} + \dots + 239896y + 22201$
$c_6, c_7, c_{10}$	$(y^{36} - 36y^{35} + \dots - 228y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.801734 + 0.696202I$		
$a = 0.525131 - 0.532417I$	$-2.58334 - 1.89748I$	$-1.79078 + 1.73365I$
$b = -1.060570 - 0.298701I$		
$u = 0.801734 + 0.696202I$		
$a = -0.146921 + 0.381228I$	$-2.58334 - 1.89748I$	$-1.79078 + 1.73365I$
$b = 1.240490 + 0.042488I$		
$u = 0.801734 - 0.696202I$		
$a = 0.525131 + 0.532417I$	$-2.58334 + 1.89748I$	$-1.79078 - 1.73365I$
$b = -1.060570 + 0.298701I$		
$u = 0.801734 - 0.696202I$		
$a = -0.146921 - 0.381228I$	$-2.58334 + 1.89748I$	$-1.79078 - 1.73365I$
$b = 1.240490 - 0.042488I$		
$u = 0.406976 + 0.842772I$		
$a = 0.364285 + 0.941569I$	$-3.72449 + 7.15532I$	$-1.32336 - 7.08750I$
$b = 1.216290 - 0.277018I$		
$u = 0.406976 + 0.842772I$		
$a = -0.346677 - 0.608804I$	$-3.72449 + 7.15532I$	$-1.32336 - 7.08750I$
$b = -1.251710 + 0.596442I$		
$u = 0.406976 - 0.842772I$		
$a = 0.364285 - 0.941569I$	$-3.72449 - 7.15532I$	$-1.32336 + 7.08750I$
$b = 1.216290 + 0.277018I$		
$u = 0.406976 - 0.842772I$		
$a = -0.346677 + 0.608804I$	$-3.72449 - 7.15532I$	$-1.32336 + 7.08750I$
$b = -1.251710 - 0.596442I$		
$u = -0.392598 + 1.003430I$		
$a = -0.903413 - 0.103360I$	$2.79209 + 2.82464I$	$5.35953 - 2.15606I$
$b = -0.821320 - 0.340230I$		
$u = -0.392598 + 1.003430I$		
$a = 0.442073 - 0.041027I$	$2.79209 + 2.82464I$	$5.35953 - 2.15606I$
$b = 0.867684 - 0.552611I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.392598 - 1.003430I$ $a = -0.903413 + 0.103360I$ $b = -0.821320 + 0.340230I$	$2.79209 - 2.82464I$	$5.35953 + 2.15606I$
$u = -0.392598 - 1.003430I$ $a = 0.442073 + 0.041027I$ $b = 0.867684 + 0.552611I$	$2.79209 - 2.82464I$	$5.35953 + 2.15606I$
$u = 1.245720 + 0.066167I$ $a = 0.18634 - 1.49060I$ $b = 0.326160 + 0.291125I$	$2.11796 + 2.01943I$	0
$u = 1.245720 + 0.066167I$ $a = 0.60423 - 1.62536I$ $b = -0.872185 + 0.570997I$	$2.11796 + 2.01943I$	0
$u = 1.245720 - 0.066167I$ $a = 0.18634 + 1.49060I$ $b = 0.326160 - 0.291125I$	$2.11796 - 2.01943I$	0
$u = 1.245720 - 0.066167I$ $a = 0.60423 + 1.62536I$ $b = -0.872185 - 0.570997I$	$2.11796 - 2.01943I$	0
$u = -1.237270 + 0.197913I$ $a = -0.45596 + 1.50174I$ $b = 0.255758 - 0.212067I$	$5.29216 - 7.38796I$	0
$u = -1.237270 + 0.197913I$ $a = 0.03864 - 1.81341I$ $b = 1.097400 + 0.775615I$	$5.29216 - 7.38796I$	0
$u = -1.237270 - 0.197913I$ $a = -0.45596 - 1.50174I$ $b = 0.255758 + 0.212067I$	$5.29216 + 7.38796I$	0
$u = -1.237270 - 0.197913I$ $a = 0.03864 + 1.81341I$ $b = 1.097400 - 0.775615I$	$5.29216 + 7.38796I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.544706 + 0.473507I$ $a = -0.802270 - 0.233838I$ $b = -0.011900 + 0.907114I$	$4.45076 - 7.51019I$	$6.15354 + 7.01976I$
$u = -0.544706 + 0.473507I$ $a = 1.38473 - 1.19024I$ $b = 1.061310 + 0.548084I$	$4.45076 - 7.51019I$	$6.15354 + 7.01976I$
$u = -0.544706 - 0.473507I$ $a = -0.802270 + 0.233838I$ $b = -0.011900 - 0.907114I$	$4.45076 + 7.51019I$	$6.15354 - 7.01976I$
$u = -0.544706 - 0.473507I$ $a = 1.38473 + 1.19024I$ $b = 1.061310 - 0.548084I$	$4.45076 + 7.51019I$	$6.15354 - 7.01976I$
$u = 0.242081 + 0.642003I$ $a = -0.121015 - 0.723872I$ $b = -0.191735 + 0.659845I$	$0.52756 + 3.89617I$	$2.77520 - 6.34158I$
$u = 0.242081 + 0.642003I$ $a = 1.236690 + 0.347854I$ $b = 0.980806 - 0.514343I$	$0.52756 + 3.89617I$	$2.77520 - 6.34158I$
$u = 0.242081 - 0.642003I$ $a = -0.121015 + 0.723872I$ $b = -0.191735 - 0.659845I$	$0.52756 - 3.89617I$	$2.77520 + 6.34158I$
$u = 0.242081 - 0.642003I$ $a = 1.236690 - 0.347854I$ $b = 0.980806 + 0.514343I$	$0.52756 - 3.89617I$	$2.77520 + 6.34158I$
$u = -1.346270 + 0.118214I$ $a = -0.057599 + 1.129430I$ $b = -1.206250 - 0.403477I$	$3.10296 - 1.88811I$	0
$u = -1.346270 + 0.118214I$ $a = 0.807053 - 1.151850I$ $b = -1.140800 + 0.801114I$	$3.10296 - 1.88811I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.346270 - 0.118214I$ $a = -0.057599 - 1.129430I$ $b = -1.206250 + 0.403477I$	$3.10296 + 1.88811I$	0
$u = -1.346270 - 0.118214I$ $a = 0.807053 + 1.151850I$ $b = -1.140800 - 0.801114I$	$3.10296 + 1.88811I$	0
$u = 1.360600 + 0.024824I$ $a = -0.59798 - 2.02753I$ $b = -1.092470 + 0.227442I$	$4.48945 + 0.44139I$	0
$u = 1.360600 + 0.024824I$ $a = -1.56290 - 2.59175I$ $b = 1.95395 + 2.12838I$	$4.48945 + 0.44139I$	0
$u = 1.360600 - 0.024824I$ $a = -0.59798 + 2.02753I$ $b = -1.092470 - 0.227442I$	$4.48945 - 0.44139I$	0
$u = 1.360600 - 0.024824I$ $a = -1.56290 + 2.59175I$ $b = 1.95395 - 2.12838I$	$4.48945 - 0.44139I$	0
$u = 0.479497 + 0.411115I$ $a = 1.278950 + 0.303011I$ $b = -0.113905 - 0.253707I$	$1.58087 - 0.53277I$	$7.83505 - 0.25698I$
$u = 0.479497 + 0.411115I$ $a = 0.090316 + 0.483528I$ $b = 0.673813 + 0.606032I$	$1.58087 - 0.53277I$	$7.83505 - 0.25698I$
$u = 0.479497 - 0.411115I$ $a = 1.278950 - 0.303011I$ $b = -0.113905 + 0.253707I$	$1.58087 + 0.53277I$	$7.83505 + 0.25698I$
$u = 0.479497 - 0.411115I$ $a = 0.090316 - 0.483528I$ $b = 0.673813 - 0.606032I$	$1.58087 + 0.53277I$	$7.83505 + 0.25698I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.361950 + 0.320932I$ $a = -0.260335 + 1.373070I$ $b = -0.304737 - 0.598586I$	$5.50387 - 7.35891I$	0
$u = -1.361950 + 0.320932I$ $a = 0.02776 - 1.48728I$ $b = 1.165430 + 0.676249I$	$5.50387 - 7.35891I$	0
$u = -1.361950 - 0.320932I$ $a = -0.260335 - 1.373070I$ $b = -0.304737 + 0.598586I$	$5.50387 + 7.35891I$	0
$u = -1.361950 - 0.320932I$ $a = 0.02776 + 1.48728I$ $b = 1.165430 - 0.676249I$	$5.50387 + 7.35891I$	0
$u = -0.592608$ $a = -0.675564$ $b = -1.30375$	0.850544	11.0660
$u = -0.592608$ $a = 2.60037$ $b = -0.512864$	0.850544	11.0660
$u = -1.45678 + 0.15564I$ $a = -0.379396 + 0.929302I$ $b = 0.398711 - 0.870251I$	$7.76795 - 1.60452I$	0
$u = -1.45678 + 0.15564I$ $a = 0.074350 - 0.851116I$ $b = 0.638031 + 0.406509I$	$7.76795 - 1.60452I$	0
$u = -1.45678 - 0.15564I$ $a = -0.379396 - 0.929302I$ $b = 0.398711 + 0.870251I$	$7.76795 + 1.60452I$	0
$u = -1.45678 - 0.15564I$ $a = 0.074350 + 0.851116I$ $b = 0.638031 - 0.406509I$	$7.76795 + 1.60452I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.50323 + 0.07660I$ $a = 1.32499 + 0.82787I$ $b = -0.737498 - 0.096809I$	$5.69053 - 0.15999I$	0
$u = -1.50323 + 0.07660I$ $a = -1.56911 - 1.05381I$ $b = 1.72400 + 0.87076I$	$5.69053 - 0.15999I$	0
$u = -1.50323 - 0.07660I$ $a = 1.32499 - 0.82787I$ $b = -0.737498 + 0.096809I$	$5.69053 + 0.15999I$	0
$u = -1.50323 - 0.07660I$ $a = -1.56911 + 1.05381I$ $b = 1.72400 - 0.87076I$	$5.69053 + 0.15999I$	0
$u = 1.49462 + 0.19720I$ $a = -0.16111 + 1.41989I$ $b = 1.33487 - 0.64551I$	$11.0335 + 10.1489I$	0
$u = 1.49462 + 0.19720I$ $a = 0.30102 + 1.55009I$ $b = -0.26778 - 1.48948I$	$11.0335 + 10.1489I$	0
$u = 1.49462 - 0.19720I$ $a = -0.16111 - 1.41989I$ $b = 1.33487 + 0.64551I$	$11.0335 - 10.1489I$	0
$u = 1.49462 - 0.19720I$ $a = 0.30102 - 1.55009I$ $b = -0.26778 + 1.48948I$	$11.0335 - 10.1489I$	0
$u = -1.48828 + 0.31375I$ $a = -0.45103 - 1.50201I$ $b = 1.161310 + 0.493885I$	$2.38283 - 11.34240I$	0
$u = -1.48828 + 0.31375I$ $a = 0.46240 + 1.61868I$ $b = -1.34786 - 0.90026I$	$2.38283 - 11.34240I$	0



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.48828 - 0.31375I$ $a = -0.45103 + 1.50201I$ $b = 1.161310 - 0.493885I$	$2.38283 + 11.34240I$	0
$u = -1.48828 - 0.31375I$ $a = 0.46240 - 1.61868I$ $b = -1.34786 + 0.90026I$	$2.38283 + 11.34240I$	0
$u = 0.062588 + 0.462865I$ $a = -0.745882 + 1.101450I$ $b = -0.761483 - 0.431993I$	$-1.322960 - 0.095597I$	$-5.44765 - 0.30752I$
$u = 0.062588 + 0.462865I$ $a = -1.69151 + 1.21537I$ $b = -0.841856 + 0.077327I$	$-1.322960 - 0.095597I$	$-5.44765 - 0.30752I$
$u = 0.062588 - 0.462865I$ $a = -0.745882 - 1.101450I$ $b = -0.761483 + 0.431993I$	$-1.322960 + 0.095597I$	$-5.44765 + 0.30752I$
$u = 0.062588 - 0.462865I$ $a = -1.69151 - 1.21537I$ $b = -0.841856 - 0.077327I$	$-1.322960 + 0.095597I$	$-5.44765 + 0.30752I$
$u = 1.56665 + 0.25660I$ $a = 0.231175 - 0.827713I$ $b = -1.36349 + 0.49044I$	$9.69181 + 1.76230I$	0
$u = 1.56665 + 0.25660I$ $a = -0.223081 - 0.793724I$ $b = 0.469240 + 0.837793I$	$9.69181 + 1.76230I$	0
$u = 1.56665 - 0.25660I$ $a = 0.231175 + 0.827713I$ $b = -1.36349 - 0.49044I$	$9.69181 - 1.76230I$	0
$u = 1.56665 - 0.25660I$ $a = -0.223081 + 0.793724I$ $b = 0.469240 - 0.837793I$	$9.69181 - 1.76230I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.0661431$ $a = 6.64617$ $b = -8.53647$	-0.00224370	1841.00
$u = -0.0661431$ $a = 128.621$ $b = -1.00230$	-0.00224370	1841.00

$$\text{III. } I_3^u = \langle -7u^{10} + 4u^9 + \cdots + 11b + 17, -8u^{10} + 25u^9 + \cdots + 11a - 78, u^{11} - 2u^{10} + \cdots + 6u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.727273u^{10} - 2.27273u^9 + \cdots + 2.90909u + 7.09091 \\ 0.636364u^{10} - 0.363636u^9 + \cdots - 1.45455u - 1.54545 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.272727u^{10} - 2.72727u^9 + \cdots + 11.0909u + 9.90909 \\ 0.363636u^{10} + 0.363636u^9 + \cdots - 3.54545u - 2.45455 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1.36364u^{10} - 2.63636u^9 + \cdots + 1.45455u + 5.54545 \\ 0.636364u^{10} - 0.363636u^9 + \cdots - 1.45455u - 1.54545 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.636364u^{10} - 2.36364u^9 + \cdots + 5.54545u + 8.45455 \\ 0.363636u^{10} + 0.363636u^9 + \cdots - 4.54545u - 2.45455 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2.09091u^{10} - 3.90909u^9 + \cdots + 2.36364u + 9.63636 \\ -u^{10} + u^9 + 5u^8 - 8u^7 - 4u^6 + 16u^5 - 7u^4 - 10u^3 + 9u^2 + 2u - 2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.363636u^{10} + 1.63636u^9 + \cdots - 6.45455u - 4.54545 \\ -0.636364u^{10} + 0.363636u^9 + \cdots + 3.45455u + 1.54545 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^{10} - 3u^9 - 4u^8 + 19u^7 - 7u^6 - 31u^5 + 34u^4 + 8u^3 - 30u^2 + 7u + 8 \\ 0.636364u^{10} + 0.636364u^9 + \cdots - 4.45455u - 2.54545 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= -\frac{74}{11}u^{10} + \frac{113}{11}u^9 + \frac{357}{11}u^8 - \frac{746}{11}u^7 - \frac{134}{11}u^6 + \frac{1178}{11}u^5 - \frac{724}{11}u^4 - \frac{422}{11}u^3 + \frac{456}{11}u^2 + \frac{144}{11}u + \frac{10}{11}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{11} - 6u^{10} + \dots - 11u + 1$
$c_2, c_{11}$	$u^{11} - 5u^9 - u^8 + 9u^7 + 3u^6 - 10u^5 - 3u^4 + 7u^3 + 3u^2 - 2u - 1$
$c_3, c_5$	$u^{11} - 5u^9 + u^8 + 9u^7 - 3u^6 - 10u^5 + 3u^4 + 7u^3 - 3u^2 - 2u + 1$
$c_4, c_8$	$u^{11} - u^{10} + \dots - 5u + 1$
$c_6, c_7$	$u^{11} - 2u^{10} + \dots + 6u + 1$
$c_9, c_{12}$	$u^{11} + u^{10} + \dots - 5u - 1$
$c_{10}$	$u^{11} + 2u^{10} + \dots + 6u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{11} - 2y^{10} + \dots + 21y - 1$
$c_2, c_3, c_5$ $c_{11}$	$y^{11} - 10y^{10} + \dots + 10y - 1$
$c_4, c_8, c_9$ $c_{12}$	$y^{11} - 13y^{10} + \dots + 45y - 1$
$c_6, c_7, c_{10}$	$y^{11} - 14y^{10} + \dots + 38y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.947758$ $a = -0.866165$ $b = 1.59894$	-7.33878	-27.9880
$u = 0.697676 + 0.834481I$ $a = 0.549586 + 0.594984I$ $b = 0.694924 + 0.358502I$	$3.09180 - 4.84097I$	$5.24884 + 3.87488I$
$u = 0.697676 - 0.834481I$ $a = 0.549586 - 0.594984I$ $b = 0.694924 - 0.358502I$	$3.09180 + 4.84097I$	$5.24884 - 3.87488I$
$u = 1.284570 + 0.369820I$ $a = 0.40416 + 1.72162I$ $b = 0.906586 - 0.628396I$	$5.41429 + 9.15643I$	$5.68722 - 10.47253I$
$u = 1.284570 - 0.369820I$ $a = 0.40416 - 1.72162I$ $b = 0.906586 + 0.628396I$	$5.41429 - 9.15643I$	$5.68722 + 10.47253I$
$u = -1.35854$ $a = 0.543106$ $b = -1.74021$	4.07888	9.27100
$u = 1.48788 + 0.09186I$ $a = 0.855967 - 1.087180I$ $b = -0.811433 + 0.624669I$	$6.02864 + 0.67022I$	$7.62823 - 2.72103I$
$u = 1.48788 - 0.09186I$ $a = 0.855967 + 1.087180I$ $b = -0.811433 - 0.624669I$	$6.02864 - 0.67022I$	$7.62823 + 2.72103I$
$u = -0.449664$ $a = 1.10365$ $b = -0.719426$	-0.265950	2.42860
$u = -0.183780$ $a = 5.68622$ $b = -1.23706$	-0.0829640	0.0440200

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -2.00050$		
$a = -0.0862312$	14.0178	25.1160
$b = 0.517601$		

IV.  $I_1^v = \langle a, b + 1, v + 1 \rangle$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0



(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_9$ $c_{11}, c_{12}$	$u - 1$
$c_3, c_4, c_5$ $c_8$	$u + 1$
$c_6, c_7, c_{10}$	$u$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_8$ $c_9, c_{11}, c_{12}$	$y - 1$
$c_6, c_7, c_{10}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	0	0
$b = -1.00000$		

### V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)(u^{11}-6u^{10}+\dots-11u+1)(u^{25}-22u^{24}+\dots+5120u+512)$ $\cdot (u^{36}+11u^{35}+\dots+12u+1)^2$
$c_2, c_{11}$	$(u-1)(u^{11}-5u^9+\dots-2u-1)$ $\cdot (u^{25}-u^{24}+\dots-4u+1)(u^{72}+5u^{71}+\dots+44u+31)$
$c_3, c_5$	$(u+1)(u^{11}-5u^9+\dots-2u+1)$ $\cdot (u^{25}-u^{24}+\dots-4u+1)(u^{72}+5u^{71}+\dots+44u+31)$
$c_4, c_8$	$(u+1)(u^{11}-u^{10}+\dots-5u+1)(u^{25}-11u^{23}+\dots+u-1)$ $\cdot (u^{72}+15u^{71}+\dots+1022u+149)$
$c_6, c_7$	$u(u^{11}-2u^{10}+\dots+6u+1)(u^{25}-11u^{24}+\dots-80u+16)$ $\cdot (u^{36}+4u^{35}+\dots+16u+1)^2$
$c_9, c_{12}$	$(u-1)(u^{11}+u^{10}+\dots-5u-1)(u^{25}-11u^{23}+\dots+u-1)$ $\cdot (u^{72}+15u^{71}+\dots+1022u+149)$
$c_{10}$	$u(u^{11}+2u^{10}+\dots+6u-1)(u^{25}-11u^{24}+\dots-80u+16)$ $\cdot (u^{36}+4u^{35}+\dots+16u+1)^2$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y-1)(y^{11} - 2y^{10} + \dots + 21y - 1)$ $\cdot (y^{25} - 2y^{24} + \dots + 76808192y - 262144)$ $\cdot (y^{36} + 9y^{35} + \dots - 78y + 1)^2$
$c_2, c_3, c_5$ $c_{11}$	$(y-1)(y^{11} - 10y^{10} + \dots + 10y - 1)(y^{25} - 15y^{24} + \dots + 50y - 1)$ $\cdot (y^{72} - 109y^{71} + \dots - 5904y + 961)$
$c_4, c_8, c_9$ $c_{12}$	$(y-1)(y^{11} - 13y^{10} + \dots + 45y - 1)(y^{25} - 22y^{24} + \dots + 21y - 1)$ $\cdot (y^{72} - 125y^{71} + \dots + 239896y + 22201)$
$c_6, c_7, c_{10}$	$y(y^{11} - 14y^{10} + \dots + 38y - 1)(y^{25} - 23y^{24} + \dots - 1408y - 256)$ $\cdot (y^{36} - 36y^{35} + \dots - 228y + 1)^2$