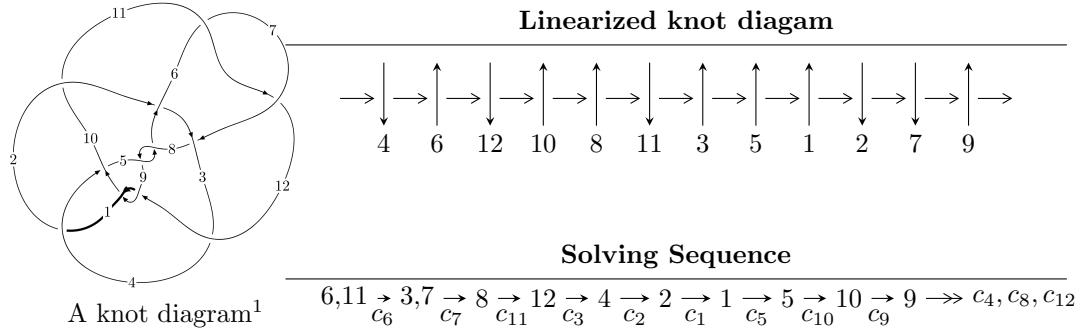


$12a_{1005}$  ( $K12a_{1005}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 8.28638 \times 10^{818} u^{163} + 1.07259 \times 10^{819} u^{162} + \dots + 4.77229 \times 10^{818} b + 8.17270 \times 10^{819}, \\
 &\quad 8.15374 \times 10^{819} u^{163} + 7.61680 \times 10^{819} u^{162} + \dots + 4.77229 \times 10^{818} a + 7.02986 \times 10^{820}, u^{164} + u^{163} + \dots + 2 \\
 I_2^u &= \langle -1.98199 \times 10^{43} u^{43} + 9.68400 \times 10^{42} u^{42} + \dots + 1.94108 \times 10^{43} b - 2.15307 \times 10^{43}, \\
 &\quad - 8.58634 \times 10^{42} u^{43} + 2.47691 \times 10^{43} u^{42} + \dots + 1.94108 \times 10^{43} a - 2.23616 \times 10^{43}, \\
 &\quad u^{44} - 14u^{42} + \dots - 6u + 1 \rangle
 \end{aligned}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 208 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 8.29 \times 10^{818} u^{163} + 1.07 \times 10^{819} u^{162} + \dots + 4.77 \times 10^{818} b + 8.17 \times 10^{819}, 8.15 \times 10^{819} u^{163} + 7.62 \times 10^{819} u^{162} + \dots + 4.77 \times 10^{818} a + 7.03 \times 10^{820}, u^{164} + u^{163} + \dots + 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -17.0856u^{163} - 15.9605u^{162} + \dots + 801.549u - 147.306 \\ -1.73635u^{163} - 2.24754u^{162} + \dots + 106.126u - 17.1253 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 32.9409u^{163} + 27.5908u^{162} + \dots - 1572.08u + 261.950 \\ 3.86320u^{163} + 2.51080u^{162} + \dots - 143.117u + 25.0194 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -16.9444u^{163} - 15.4306u^{162} + \dots + 786.454u - 144.913 \\ -2.51806u^{163} - 2.41108u^{162} + \dots + 120.302u - 19.9071 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -15.3492u^{163} - 13.7129u^{162} + \dots + 695.424u - 130.180 \\ -1.73635u^{163} - 2.24754u^{162} + \dots + 106.126u - 17.1253 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 29.2656u^{163} + 25.7673u^{162} + \dots - 1452.79u + 232.311 \\ 1.62972u^{163} + 2.44440u^{162} + \dots - 147.983u + 21.1918 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 11.4222u^{163} + 8.04537u^{162} + \dots - 456.454u + 83.4972 \\ 1.43923u^{163} + 1.37655u^{162} + \dots - 71.8732u + 12.2456 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 36.6016u^{163} + 33.3168u^{162} + \dots - 1824.99u + 309.036 \\ 6.11193u^{163} + 3.32962u^{162} + \dots - 207.355u + 35.1448 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -13.1906u^{163} - 10.9444u^{162} + \dots + 627.379u - 94.1792 \\ -1.26477u^{163} - 0.969496u^{162} + \dots + 57.6793u - 8.49268 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $-8.23974u^{163} - 7.66090u^{162} + \dots + 441.763u - 72.5687$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing                                |
|---------------|---|
| $c_1$         | $u^{164} + 5u^{163} + \cdots - 49u + 1$                       |
| $c_2$         | $u^{164} + u^{163} + \cdots + 36157964272u + 1936765232$      |
| $c_3$         | $u^{164} - 45u^{162} + \cdots - 4066348387u + 426841301$      |
| $c_4$         | $u^{164} - 2u^{163} + \cdots + 540u + 19$                     |
| $c_5, c_8$    | $u^{164} + 11u^{163} + \cdots + 9685865u + 827737$            |
| $c_6, c_{11}$ | $u^{164} - u^{163} + \cdots - 2u + 1$                         |
| $c_7$         | $u^{164} + u^{163} + \cdots + 2097860395u + 150897161$        |
| $c_9, c_{12}$ | $u^{164} - 50u^{162} + \cdots + 992u + 1808$                  |
| $c_{10}$      | $u^{164} + 6u^{163} + \cdots + 1784816067153u + 207574985671$ |

**(v) Riley Polynomials at the component**

| Crossings     | Riley Polynomials at each crossing  |
|---------------|---|
| $c_1$         | $y^{164} + 3y^{163} + \dots - 411y + 1$                                     |
| $c_2$         | $y^{164} + 75y^{163} + \dots + 1.76 \times 10^{20}y + 3.75 \times 10^{18}$  |
| $c_3$         | $y^{164} - 90y^{163} + \dots - 2.04 \times 10^{19}y + 1.82 \times 10^{17}$  |
| $c_4$         | $y^{164} + 16y^{163} + \dots - 4434y + 361$                                 |
| $c_5, c_8$    | $y^{164} + 139y^{163} + \dots - 8776342483355y + 685148541169$              |
| $c_6, c_{11}$ | $y^{164} - 115y^{163} + \dots - 170y + 1$                                   |
| $c_7$         | $y^{164} + 59y^{163} + \dots + 634377626274351873y + 22769953197859921$     |
| $c_9, c_{12}$ | $y^{164} - 100y^{163} + \dots - 153608192y + 3268864$                       |
| $c_{10}$      | $y^{164} - 108y^{163} + \dots - 3.42 \times 10^{24}y + 4.31 \times 10^{22}$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.869177 + 0.509153I$ |                                       |            |
| $a = 0.169333 - 1.137160I$  | $2.88405 - 1.66044I$                  | 0          |
| $b = -0.342844 - 0.391066I$ |                                       |            |
| $u = -0.869177 - 0.509153I$ |                                       |            |
| $a = 0.169333 + 1.137160I$  | $2.88405 + 1.66044I$                  | 0          |
| $b = -0.342844 + 0.391066I$ |                                       |            |
| $u = -0.984878 + 0.106592I$ |                                       |            |
| $a = -0.98146 + 1.62508I$   | $-5.75041 + 0.39923I$                 | 0          |
| $b = -0.909765 + 0.456958I$ |                                       |            |
| $u = -0.984878 - 0.106592I$ |                                       |            |
| $a = -0.98146 - 1.62508I$   | $-5.75041 - 0.39923I$                 | 0          |
| $b = -0.909765 - 0.456958I$ |                                       |            |
| $u = -0.989183$             |                                       |            |
| $a = 0.323183$              | 2.29760                               | 0          |
| $b = 1.49558$               |                                       |            |
| $u = 0.988638 + 0.009995I$  |                                       |            |
| $a = -0.213781 - 0.471004I$ | $-1.65633 + 4.05752I$                 | 0          |
| $b = -1.34941 - 0.76792I$   |                                       |            |
| $u = 0.988638 - 0.009995I$  |                                       |            |
| $a = -0.213781 + 0.471004I$ | $-1.65633 - 4.05752I$                 | 0          |
| $b = -1.34941 + 0.76792I$   |                                       |            |
| $u = 0.110282 + 1.038000I$  |                                       |            |
| $a = -0.409530 - 0.218427I$ | $-4.27505 + 4.09712I$                 | 0          |
| $b = -0.475993 - 1.080930I$ |                                       |            |
| $u = 0.110282 - 1.038000I$  |                                       |            |
| $a = -0.409530 + 0.218427I$ | $-4.27505 - 4.09712I$                 | 0          |
| $b = -0.475993 + 1.080930I$ |                                       |            |
| $u = 0.568068 + 0.765634I$  |                                       |            |
| $a = 0.181874 + 0.180155I$  | $0.02802 - 2.07677I$                  | 0          |
| $b = -0.597640 - 0.124843I$ |                                       |            |

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|------------------------------|---------------------------------------|------------|
| $u = 0.568068 - 0.765634I$   |                                       |            |
| $a = 0.181874 - 0.180155I$   | $0.02802 + 2.07677I$                  | 0          |
| $b = -0.597640 + 0.124843I$  |                                       |            |
| $u = 0.996494 + 0.342855I$   |                                       |            |
| $a = 0.46220 + 1.49178I$     | $-1.37379 - 2.15935I$                 | 0          |
| $b = -0.299086 + 0.459250I$  |                                       |            |
| $u = 0.996494 - 0.342855I$   |                                       |            |
| $a = 0.46220 - 1.49178I$     | $-1.37379 + 2.15935I$                 | 0          |
| $b = -0.299086 - 0.459250I$  |                                       |            |
| $u = -0.983860 + 0.378927I$  |                                       |            |
| $a = 0.82851 - 2.38314I$     | $-1.96890 + 9.67297I$                 | 0          |
| $b = -0.24401 - 2.23511I$    |                                       |            |
| $u = -0.983860 - 0.378927I$  |                                       |            |
| $a = 0.82851 + 2.38314I$     | $-1.96890 - 9.67297I$                 | 0          |
| $b = -0.24401 + 2.23511I$    |                                       |            |
| $u = 1.000460 + 0.373358I$   |                                       |            |
| $a = -0.31736 - 1.74450I$    | $1.32797 - 6.43845I$                  | 0          |
| $b = 0.79791 - 1.47090I$     |                                       |            |
| $u = 1.000460 - 0.373358I$   |                                       |            |
| $a = -0.31736 + 1.74450I$    | $1.32797 + 6.43845I$                  | 0          |
| $b = 0.79791 + 1.47090I$     |                                       |            |
| $u = -0.611311 + 0.879204I$  |                                       |            |
| $a = 0.0074746 + 0.0729978I$ | $3.93629 + 6.69317I$                  | 0          |
| $b = -0.692411 + 0.111158I$  |                                       |            |
| $u = -0.611311 - 0.879204I$  |                                       |            |
| $a = 0.0074746 - 0.0729978I$ | $3.93629 - 6.69317I$                  | 0          |
| $b = -0.692411 - 0.111158I$  |                                       |            |
| $u = 0.927110 + 0.008097I$   |                                       |            |
| $a = -1.49056 - 2.33101I$    | $-1.38113 + 4.26225I$                 | 0          |
| $b = -0.60629 - 1.28946I$    |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.927110 - 0.008097I$  |                                       |            |
| $a = -1.49056 + 2.33101I$   | $-1.38113 - 4.26225I$                 | 0          |
| $b = -0.60629 + 1.28946I$   |                                       |            |
| $u = -0.762078 + 0.505620I$ |                                       |            |
| $a = 0.465622 - 0.166428I$  | $-4.82240 + 2.94091I$                 | 0          |
| $b = -0.728178 - 0.821593I$ |                                       |            |
| $u = -0.762078 - 0.505620I$ |                                       |            |
| $a = 0.465622 + 0.166428I$  | $-4.82240 - 2.94091I$                 | 0          |
| $b = -0.728178 + 0.821593I$ |                                       |            |
| $u = 0.121991 + 0.906158I$  |                                       |            |
| $a = 0.227372 + 0.611408I$  | $0.40256 - 2.20922I$                  | 0          |
| $b = 0.313848 - 1.058270I$  |                                       |            |
| $u = 0.121991 - 0.906158I$  |                                       |            |
| $a = 0.227372 - 0.611408I$  | $0.40256 + 2.20922I$                  | 0          |
| $b = 0.313848 + 1.058270I$  |                                       |            |
| $u = 0.979536 + 0.479470I$  |                                       |            |
| $a = -0.657563 - 0.239774I$ | $-3.26146 - 4.28093I$                 | 0          |
| $b = -0.886401 - 0.138579I$ |                                       |            |
| $u = 0.979536 - 0.479470I$  |                                       |            |
| $a = -0.657563 + 0.239774I$ | $-3.26146 + 4.28093I$                 | 0          |
| $b = -0.886401 + 0.138579I$ |                                       |            |
| $u = -0.071281 + 0.898521I$ |                                       |            |
| $a = 0.420818 + 0.086329I$  | $1.00223 - 1.62980I$                  | 0          |
| $b = 0.118209 - 0.746553I$  |                                       |            |
| $u = -0.071281 - 0.898521I$ |                                       |            |
| $a = 0.420818 - 0.086329I$  | $1.00223 + 1.62980I$                  | 0          |
| $b = 0.118209 + 0.746553I$  |                                       |            |
| $u = 0.524762 + 0.731683I$  |                                       |            |
| $a = 0.803081 - 0.246957I$  | $2.78644 + 2.16616I$                  | 0          |
| $b = 0.684276 + 0.748128I$  |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.524762 - 0.731683I$  |                                       |            |
| $a = 0.803081 + 0.246957I$  | $2.78644 - 2.16616I$                  | 0          |
| $b = 0.684276 - 0.748128I$  |                                       |            |
| $u = -0.388899 + 0.789502I$ |                                       |            |
| $a = 0.396051 + 0.382103I$  | $3.92783 - 3.00284I$                  | 0          |
| $b = -0.666792 + 0.202791I$ |                                       |            |
| $u = -0.388899 - 0.789502I$ |                                       |            |
| $a = 0.396051 - 0.382103I$  | $3.92783 + 3.00284I$                  | 0          |
| $b = -0.666792 - 0.202791I$ |                                       |            |
| $u = -0.533760 + 0.695751I$ |                                       |            |
| $a = -1.166200 + 0.474805I$ | $-0.59796 - 5.44213I$                 | 0          |
| $b = -0.64659 + 1.32891I$   |                                       |            |
| $u = -0.533760 - 0.695751I$ |                                       |            |
| $a = -1.166200 - 0.474805I$ | $-0.59796 + 5.44213I$                 | 0          |
| $b = -0.64659 - 1.32891I$   |                                       |            |
| $u = 0.510980 + 0.701345I$  |                                       |            |
| $a = -0.393768 + 0.930484I$ | $-1.91908 - 0.16586I$                 | 0          |
| $b = -0.719215 + 0.307785I$ |                                       |            |
| $u = 0.510980 - 0.701345I$  |                                       |            |
| $a = -0.393768 - 0.930484I$ | $-1.91908 + 0.16586I$                 | 0          |
| $b = -0.719215 - 0.307785I$ |                                       |            |
| $u = -0.136828 + 0.854748I$ |                                       |            |
| $a = -0.628575 + 0.232734I$ | $-1.107670 + 0.419568I$               | 0          |
| $b = 0.934372 - 1.019320I$  |                                       |            |
| $u = -0.136828 - 0.854748I$ |                                       |            |
| $a = -0.628575 - 0.232734I$ | $-1.107670 - 0.419568I$               | 0          |
| $b = 0.934372 + 1.019320I$  |                                       |            |
| $u = 1.094910 + 0.298629I$  |                                       |            |
| $a = 0.20062 - 1.92505I$    | $2.11373 - 2.89494I$                  | 0          |
| $b = 0.623344 - 0.958586I$  |                                       |            |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------------------------------|---------------------------------------|------------|
| $u = 1.094910 - 0.298629I$    |                                       |            |
| $a = 0.20062 + 1.92505I$      | $2.11373 + 2.89494I$                  | 0          |
| $b = 0.623344 + 0.958586I$    |                                       |            |
| $u = -0.042815 + 1.140330I$   |                                       |            |
| $a = -0.0374798 - 0.0738951I$ | $-7.07361 + 7.95236I$                 | 0          |
| $b = 0.630521 + 1.169310I$    |                                       |            |
| $u = -0.042815 - 1.140330I$   |                                       |            |
| $a = -0.0374798 + 0.0738951I$ | $-7.07361 - 7.95236I$                 | 0          |
| $b = 0.630521 - 1.169310I$    |                                       |            |
| $u = 1.144680 + 0.061494I$    |                                       |            |
| $a = -0.439003 - 1.032340I$   | $-3.95806 - 1.64685I$                 | 0          |
| $b = 0.961928 - 0.556071I$    |                                       |            |
| $u = 1.144680 - 0.061494I$    |                                       |            |
| $a = -0.439003 + 1.032340I$   | $-3.95806 + 1.64685I$                 | 0          |
| $b = 0.961928 + 0.556071I$    |                                       |            |
| $u = 1.097070 + 0.341636I$    |                                       |            |
| $a = -0.21959 - 2.37665I$     | $-2.31943 - 11.01080I$                | 0          |
| $b = 0.724553 - 0.658358I$    |                                       |            |
| $u = 1.097070 - 0.341636I$    |                                       |            |
| $a = -0.21959 + 2.37665I$     | $-2.31943 + 11.01080I$                | 0          |
| $b = 0.724553 + 0.658358I$    |                                       |            |
| $u = -1.148980 + 0.110231I$   |                                       |            |
| $a = 1.88462 - 0.74988I$      | $-8.23855 + 3.87446I$                 | 0          |
| $b = -0.362477 - 0.523976I$   |                                       |            |
| $u = -1.148980 - 0.110231I$   |                                       |            |
| $a = 1.88462 + 0.74988I$      | $-8.23855 - 3.87446I$                 | 0          |
| $b = -0.362477 + 0.523976I$   |                                       |            |
| $u = -1.084780 + 0.395668I$   |                                       |            |
| $a = 0.09976 - 1.59908I$      | $1.74648 + 7.39363I$                  | 0          |
| $b = -0.275370 - 0.497316I$   |                                       |            |

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|------------------------------|---------------------------------------|------------|
| $u = -1.084780 - 0.395668I$  |                                       |            |
| $a = 0.09976 + 1.59908I$     | $1.74648 - 7.39363I$                  | 0          |
| $b = -0.275370 + 0.497316I$  |                                       |            |
| $u = 0.058061 + 1.156460I$   |                                       |            |
| $a = -0.143195 + 0.226079I$  | $-3.78704 - 1.46192I$                 | 0          |
| $b = -0.382394 + 0.994846I$  |                                       |            |
| $u = 0.058061 - 1.156460I$   |                                       |            |
| $a = -0.143195 - 0.226079I$  | $-3.78704 + 1.46192I$                 | 0          |
| $b = -0.382394 - 0.994846I$  |                                       |            |
| $u = 1.145920 + 0.177078I$   |                                       |            |
| $a = -0.57231 + 2.53665I$    | $-7.72342 - 4.92973I$                 | 0          |
| $b = -1.49586 + 2.26841I$    |                                       |            |
| $u = 1.145920 - 0.177078I$   |                                       |            |
| $a = -0.57231 - 2.53665I$    | $-7.72342 + 4.92973I$                 | 0          |
| $b = -1.49586 - 2.26841I$    |                                       |            |
| $u = -1.161090 + 0.104189I$  |                                       |            |
| $a = 2.04318 - 0.94505I$     | $-5.14556 + 9.46016I$                 | 0          |
| $b = 2.85400 - 1.26008I$     |                                       |            |
| $u = -1.161090 - 0.104189I$  |                                       |            |
| $a = 2.04318 + 0.94505I$     | $-5.14556 - 9.46016I$                 | 0          |
| $b = 2.85400 + 1.26008I$     |                                       |            |
| $u = -1.163070 + 0.091280I$  |                                       |            |
| $a = -0.96985 - 2.02725I$    | $-7.49510 + 3.02617I$                 | 0          |
| $b = -0.004406 - 0.954808I$  |                                       |            |
| $u = -1.163070 - 0.091280I$  |                                       |            |
| $a = -0.96985 + 2.02725I$    | $-7.49510 - 3.02617I$                 | 0          |
| $b = -0.004406 + 0.954808I$  |                                       |            |
| $u = 0.037336 + 1.174070I$   |                                       |            |
| $a = 0.0369438 - 0.0021738I$ | $-3.6139 - 14.2988I$                  | 0          |
| $b = 0.633978 - 1.120670I$   |                                       |            |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------------------------------|---------------------------------------|------------|
| $u = 0.037336 - 1.174070I$    |                                       |            |
| $a = 0.0369438 + 0.0021738I$  | $-3.6139 + 14.2988I$                  | 0          |
| $b = 0.633978 + 1.120670I$    |                                       |            |
| $u = -1.175240 + 0.019483I$   |                                       |            |
| $a = -1.08758 - 1.50814I$     | $-6.92293 - 1.18653I$                 | 0          |
| $b = -1.91459 - 1.19881I$     |                                       |            |
| $u = -1.175240 - 0.019483I$   |                                       |            |
| $a = -1.08758 + 1.50814I$     | $-6.92293 + 1.18653I$                 | 0          |
| $b = -1.91459 + 1.19881I$     |                                       |            |
| $u = 1.177890 + 0.101131I$    |                                       |            |
| $a = -0.38284 - 1.39453I$     | $-1.91607 - 5.93788I$                 | 0          |
| $b = -1.16148 - 1.29798I$     |                                       |            |
| $u = 1.177890 - 0.101131I$    |                                       |            |
| $a = -0.38284 + 1.39453I$     | $-1.91607 + 5.93788I$                 | 0          |
| $b = -1.16148 + 1.29798I$     |                                       |            |
| $u = 0.413597 + 1.111510I$    |                                       |            |
| $a = -0.0327605 + 0.0381918I$ | $-3.64684 - 5.55468I$                 | 0          |
| $b = -0.526517 + 0.780079I$   |                                       |            |
| $u = 0.413597 - 1.111510I$    |                                       |            |
| $a = -0.0327605 - 0.0381918I$ | $-3.64684 + 5.55468I$                 | 0          |
| $b = -0.526517 - 0.780079I$   |                                       |            |
| $u = -1.155270 + 0.298688I$   |                                       |            |
| $a = -0.03568 + 1.67083I$     | $-1.86367 + 4.29799I$                 | 0          |
| $b = 0.81152 + 1.21264I$      |                                       |            |
| $u = -1.155270 - 0.298688I$   |                                       |            |
| $a = -0.03568 - 1.67083I$     | $-1.86367 - 4.29799I$                 | 0          |
| $b = 0.81152 - 1.21264I$      |                                       |            |
| $u = -1.132370 + 0.420585I$   |                                       |            |
| $a = -0.42032 + 1.94326I$     | $-4.09090 + 4.18339I$                 | 0          |
| $b = 1.037530 + 0.744513I$    |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.132370 - 0.420585I$ |                                       |            |
| $a = -0.42032 - 1.94326I$   | $-4.09090 - 4.18339I$                 | 0          |
| $b = 1.037530 - 0.744513I$  |                                       |            |
| $u = 0.387215 + 1.150160I$  |                                       |            |
| $a = 0.068647 + 0.367207I$  | $0.94845 - 2.33153I$                  | 0          |
| $b = -0.294912 - 0.951769I$ |                                       |            |
| $u = 0.387215 - 1.150160I$  |                                       |            |
| $a = 0.068647 - 0.367207I$  | $0.94845 + 2.33153I$                  | 0          |
| $b = -0.294912 + 0.951769I$ |                                       |            |
| $u = 1.213060 + 0.091257I$  |                                       |            |
| $a = -0.86938 + 1.94522I$   | $-7.35097 + 0.00282I$                 | 0          |
| $b = 0.097298 + 0.850904I$  |                                       |            |
| $u = 1.213060 - 0.091257I$  |                                       |            |
| $a = -0.86938 - 1.94522I$   | $-7.35097 - 0.00282I$                 | 0          |
| $b = 0.097298 - 0.850904I$  |                                       |            |
| $u = -1.218950 + 0.072910I$ |                                       |            |
| $a = -0.332032 + 1.228250I$ | $-5.32723 + 1.90230I$                 | 0          |
| $b = -0.98997 + 1.05400I$   |                                       |            |
| $u = -1.218950 - 0.072910I$ |                                       |            |
| $a = -0.332032 - 1.228250I$ | $-5.32723 - 1.90230I$                 | 0          |
| $b = -0.98997 - 1.05400I$   |                                       |            |
| $u = -1.213930 + 0.134347I$ |                                       |            |
| $a = -0.28497 + 1.49694I$   | $-2.54036 + 6.40960I$                 | 0          |
| $b = 0.912019 + 0.910189I$  |                                       |            |
| $u = -1.213930 - 0.134347I$ |                                       |            |
| $a = -0.28497 - 1.49694I$   | $-2.54036 - 6.40960I$                 | 0          |
| $b = 0.912019 - 0.910189I$  |                                       |            |
| $u = 1.222810 + 0.019284I$  |                                       |            |
| $a = 1.49065 + 1.86983I$    | $-9.54126 - 2.19090I$                 | 0          |
| $b = 2.20030 + 2.25331I$    |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.222810 - 0.019284I$  |                                       |            |
| $a = 1.49065 - 1.86983I$    | $-9.54126 + 2.19090I$                 | 0          |
| $b = 2.20030 - 2.25331I$    |                                       |            |
| $u = 1.220500 + 0.106731I$  |                                       |            |
| $a = 1.58784 + 1.27953I$    | $-6.13373 - 9.45444I$                 | 0          |
| $b = -0.288614 + 0.645675I$ |                                       |            |
| $u = 1.220500 - 0.106731I$  |                                       |            |
| $a = 1.58784 - 1.27953I$    | $-6.13373 + 9.45444I$                 | 0          |
| $b = -0.288614 - 0.645675I$ |                                       |            |
| $u = -0.282250 + 0.707194I$ |                                       |            |
| $a = -0.280043 - 1.165130I$ | $-1.85063 + 2.39683I$                 | 0          |
| $b = -0.735495 - 0.358113I$ |                                       |            |
| $u = -0.282250 - 0.707194I$ |                                       |            |
| $a = -0.280043 + 1.165130I$ | $-1.85063 - 2.39683I$                 | 0          |
| $b = -0.735495 + 0.358113I$ |                                       |            |
| $u = -1.247330 + 0.058445I$ |                                       |            |
| $a = -1.07170 + 1.61991I$   | $-8.55110 - 0.86479I$                 | 0          |
| $b = -0.067135 + 0.807125I$ |                                       |            |
| $u = -1.247330 - 0.058445I$ |                                       |            |
| $a = -1.07170 - 1.61991I$   | $-8.55110 + 0.86479I$                 | 0          |
| $b = -0.067135 - 0.807125I$ |                                       |            |
| $u = 1.205270 + 0.327362I$  |                                       |            |
| $a = 0.669062 + 0.830430I$  | $-3.17488 - 2.14050I$                 | 0          |
| $b = -0.533111 + 0.808691I$ |                                       |            |
| $u = 1.205270 - 0.327362I$  |                                       |            |
| $a = 0.669062 - 0.830430I$  | $-3.17488 + 2.14050I$                 | 0          |
| $b = -0.533111 - 0.808691I$ |                                       |            |
| $u = 0.327958 + 0.663780I$  |                                       |            |
| $a = -0.927633 + 0.038826I$ | $-0.00772 + 7.17049I$                 | 0          |
| $b = 1.057040 + 0.704387I$  |                                       |            |

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|------------------------------|---------------------------------------|------------|
| $u = 0.327958 - 0.663780I$   |                                       |            |
| $a = -0.927633 - 0.038826I$  | $-0.00772 - 7.17049I$                 | 0          |
| $b = 1.057040 - 0.704387I$   |                                       |            |
| $u = 0.012202 + 1.265000I$   |                                       |            |
| $a = 0.0647472 + 0.0104404I$ | $-1.44674 - 2.78950I$                 | 0          |
| $b = -0.226588 + 0.775219I$  |                                       |            |
| $u = 0.012202 - 1.265000I$   |                                       |            |
| $a = 0.0647472 - 0.0104404I$ | $-1.44674 + 2.78950I$                 | 0          |
| $b = -0.226588 - 0.775219I$  |                                       |            |
| $u = 1.282870 + 0.113745I$   |                                       |            |
| $a = 0.217836 + 1.053510I$   | $-3.27327 - 1.47146I$                 | 0          |
| $b = -0.458722 + 0.881054I$  |                                       |            |
| $u = 1.282870 - 0.113745I$   |                                       |            |
| $a = 0.217836 - 1.053510I$   | $-3.27327 + 1.47146I$                 | 0          |
| $b = -0.458722 - 0.881054I$  |                                       |            |
| $u = -1.276080 + 0.200277I$  |                                       |            |
| $a = -0.343334 + 0.789554I$  | $-5.14547 + 1.35722I$                 | 0          |
| $b = -0.845919 + 0.569676I$  |                                       |            |
| $u = -1.276080 - 0.200277I$  |                                       |            |
| $a = -0.343334 - 0.789554I$  | $-5.14547 - 1.35722I$                 | 0          |
| $b = -0.845919 - 0.569676I$  |                                       |            |
| $u = 1.314330 + 0.048916I$   |                                       |            |
| $a = -0.81780 + 1.67966I$    | $-7.40804 - 4.47819I$                 | 0          |
| $b = -0.068630 + 0.779887I$  |                                       |            |
| $u = 1.314330 - 0.048916I$   |                                       |            |
| $a = -0.81780 - 1.67966I$    | $-7.40804 + 4.47819I$                 | 0          |
| $b = -0.068630 - 0.779887I$  |                                       |            |
| $u = -0.668100 + 0.128523I$  |                                       |            |
| $a = 1.06443 + 1.55537I$     | $2.64434 + 1.05337I$                  | 0          |
| $b = 0.475499 + 0.372168I$   |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.668100 - 0.128523I$ |                                       |            |
| $a = 1.06443 - 1.55537I$    | $2.64434 - 1.05337I$                  | 0          |
| $b = 0.475499 - 0.372168I$  |                                       |            |
| $u = -0.343643 + 0.586130I$ |                                       |            |
| $a = 0.207282 + 0.376920I$  | $-4.76926 + 2.89327I$                 | 0          |
| $b = -0.681941 - 0.905837I$ |                                       |            |
| $u = -0.343643 - 0.586130I$ |                                       |            |
| $a = 0.207282 - 0.376920I$  | $-4.76926 - 2.89327I$                 | 0          |
| $b = -0.681941 + 0.905837I$ |                                       |            |
| $u = -1.325720 + 0.027156I$ |                                       |            |
| $a = 0.65965 + 1.59435I$    | $-5.92496 + 5.44183I$                 | 0          |
| $b = 1.09126 + 1.92199I$    |                                       |            |
| $u = -1.325720 - 0.027156I$ |                                       |            |
| $a = 0.65965 - 1.59435I$    | $-5.92496 - 5.44183I$                 | 0          |
| $b = 1.09126 - 1.92199I$    |                                       |            |
| $u = -1.281900 + 0.498733I$ |                                       |            |
| $a = -0.892083 + 0.763089I$ | $-8.57748 + 0.88225I$                 | 0          |
| $b = 0.117064 + 0.851389I$  |                                       |            |
| $u = -1.281900 - 0.498733I$ |                                       |            |
| $a = -0.892083 - 0.763089I$ | $-8.57748 - 0.88225I$                 | 0          |
| $b = 0.117064 - 0.851389I$  |                                       |            |
| $u = -0.198614 + 0.577381I$ |                                       |            |
| $a = 0.239318 + 0.330408I$  | $1.010920 - 0.883539I$                | 0          |
| $b = 0.595695 - 0.486141I$  |                                       |            |
| $u = -0.198614 - 0.577381I$ |                                       |            |
| $a = 0.239318 - 0.330408I$  | $1.010920 + 0.883539I$                | 0          |
| $b = 0.595695 + 0.486141I$  |                                       |            |
| $u = 1.323560 + 0.441421I$  |                                       |            |
| $a = 0.864050 + 1.015820I$  | $-5.56788 - 5.01333I$                 | 0          |
| $b = 0.27725 + 1.79614I$    |                                       |            |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------------------------------|---------------------------------------|------------|
| $u = 1.323560 - 0.441421I$    |                                       |            |
| $a = 0.864050 - 1.015820I$    | $-5.56788 + 5.01333I$                 | 0          |
| $b = 0.27725 - 1.79614I$      |                                       |            |
| $u = 0.325093 + 0.508781I$    |                                       |            |
| $a = -0.081684 + 0.140427I$   | $4.45069 - 0.36184I$                  | 0          |
| $b = 1.006040 + 0.467639I$    |                                       |            |
| $u = 0.325093 - 0.508781I$    |                                       |            |
| $a = -0.081684 - 0.140427I$   | $4.45069 + 0.36184I$                  | 0          |
| $b = 1.006040 - 0.467639I$    |                                       |            |
| $u = 1.36885 + 0.36876I$      |                                       |            |
| $a = -0.04057 + 1.70575I$     | $-9.90194 - 6.89799I$                 | 0          |
| $b = -0.92514 + 1.54786I$     |                                       |            |
| $u = 1.36885 - 0.36876I$      |                                       |            |
| $a = -0.04057 - 1.70575I$     | $-9.90194 + 6.89799I$                 | 0          |
| $b = -0.92514 - 1.54786I$     |                                       |            |
| $u = -1.33014 + 0.51525I$     |                                       |            |
| $a = -0.316409 + 1.292020I$   | $-2.92403 + 6.94331I$                 | 0          |
| $b = 0.46348 + 1.40607I$      |                                       |            |
| $u = -1.33014 - 0.51525I$     |                                       |            |
| $a = -0.316409 - 1.292020I$   | $-2.92403 - 6.94331I$                 | 0          |
| $b = 0.46348 - 1.40607I$      |                                       |            |
| $u = 1.34450 + 0.53734I$      |                                       |            |
| $a = 0.27958 + 1.63896I$      | $-8.21494 - 9.81676I$                 | 0          |
| $b = -0.59477 + 1.49157I$     |                                       |            |
| $u = 1.34450 - 0.53734I$      |                                       |            |
| $a = 0.27958 - 1.63896I$      | $-8.21494 + 9.81676I$                 | 0          |
| $b = -0.59477 - 1.49157I$     |                                       |            |
| $u = -0.00921 + 1.45579I$     |                                       |            |
| $a = -0.0124504 + 0.0153640I$ | $2.54879 + 6.99583I$                  | 0          |
| $b = -0.243685 - 0.693284I$   |                                       |            |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------------------------------|---------------------------------------|------------|
| $u = -0.00921 - 1.45579I$     |                                       |            |
| $a = -0.0124504 - 0.0153640I$ | $2.54879 - 6.99583I$                  | 0          |
| $b = -0.243685 + 0.693284I$   |                                       |            |
| $u = 1.35734 + 0.56356I$      |                                       |            |
| $a = 0.321951 + 1.046950I$    | $-2.53664 - 3.87888I$                 | 0          |
| $b = -0.830586 + 1.050930I$   |                                       |            |
| $u = 1.35734 - 0.56356I$      |                                       |            |
| $a = 0.321951 - 1.046950I$    | $-2.53664 + 3.87888I$                 | 0          |
| $b = -0.830586 - 1.050930I$   |                                       |            |
| $u = -1.40589 + 0.47370I$     |                                       |            |
| $a = -0.21826 + 1.60316I$     | $-4.50560 + 7.27936I$                 | 0          |
| $b = 1.18111 + 2.01498I$      |                                       |            |
| $u = -1.40589 - 0.47370I$     |                                       |            |
| $a = -0.21826 - 1.60316I$     | $-4.50560 - 7.27936I$                 | 0          |
| $b = 1.18111 - 2.01498I$      |                                       |            |
| $u = 1.38998 + 0.52477I$      |                                       |            |
| $a = -0.22510 - 1.59400I$     | $-11.6002 - 13.7978I$                 | 0          |
| $b = 1.05072 - 1.52408I$      |                                       |            |
| $u = 1.38998 - 0.52477I$      |                                       |            |
| $a = -0.22510 + 1.59400I$     | $-11.6002 + 13.7978I$                 | 0          |
| $b = 1.05072 + 1.52408I$      |                                       |            |
| $u = -1.40616 + 0.50944I$     |                                       |            |
| $a = 0.25369 - 1.53815I$      | $-8.47222 + 7.31099I$                 | 0          |
| $b = -0.64117 - 1.36346I$     |                                       |            |
| $u = -1.40616 - 0.50944I$     |                                       |            |
| $a = 0.25369 + 1.53815I$      | $-8.47222 - 7.31099I$                 | 0          |
| $b = -0.64117 + 1.36346I$     |                                       |            |
| $u = -1.43705 + 0.41795I$     |                                       |            |
| $a = -0.02431 - 1.53046I$     | $-9.3423 + 10.7264I$                  | 0          |
| $b = -0.90783 - 1.39477I$     |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.43705 - 0.41795I$   |                                       |            |
| $a = -0.02431 + 1.53046I$   | $-9.3423 - 10.7264I$                  | 0          |
| $b = -0.90783 + 1.39477I$   |                                       |            |
| $u = -1.39920 + 0.53936I$   |                                       |            |
| $a = -0.20694 + 1.58779I$   | $-8.1548 + 20.2998I$                  | 0          |
| $b = 0.99308 + 1.50160I$    |                                       |            |
| $u = -1.39920 - 0.53936I$   |                                       |            |
| $a = -0.20694 - 1.58779I$   | $-8.1548 - 20.2998I$                  | 0          |
| $b = 0.99308 - 1.50160I$    |                                       |            |
| $u = -1.42181 + 0.53107I$   |                                       |            |
| $a = 0.173019 - 1.208400I$  | $-6.16542 + 9.00087I$                 | 0          |
| $b = -0.817042 - 1.134700I$ |                                       |            |
| $u = -1.42181 - 0.53107I$   |                                       |            |
| $a = 0.173019 + 1.208400I$  | $-6.16542 - 9.00087I$                 | 0          |
| $b = -0.817042 + 1.134700I$ |                                       |            |
| $u = 1.41936 + 0.55478I$    |                                       |            |
| $a = -0.611534 - 0.893951I$ | $-8.13440 - 4.73588I$                 | 0          |
| $b = 0.162081 - 0.978837I$  |                                       |            |
| $u = 1.41936 - 0.55478I$    |                                       |            |
| $a = -0.611534 + 0.893951I$ | $-8.13440 + 4.73588I$                 | 0          |
| $b = 0.162081 + 0.978837I$  |                                       |            |
| $u = 1.45901 + 0.49891I$    |                                       |            |
| $a = -0.199424 - 1.013340I$ | $-6.38776 - 3.51668I$                 | 0          |
| $b = 0.478238 - 1.119680I$  |                                       |            |
| $u = 1.45901 - 0.49891I$    |                                       |            |
| $a = -0.199424 + 1.013340I$ | $-6.38776 + 3.51668I$                 | 0          |
| $b = 0.478238 + 1.119680I$  |                                       |            |
| $u = -1.44500 + 0.54637I$   |                                       |            |
| $a = 0.599728 - 0.761273I$  | $-11.49990 - 1.75481I$                | 0          |
| $b = -0.075661 - 1.248430I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -1.44500 - 0.54637I$   |                                       |                       |
| $a = 0.599728 + 0.761273I$  | $-11.49990 + 1.75481I$                | 0                     |
| $b = -0.075661 + 1.248430I$ |                                       |                       |
| $u = 1.45510 + 0.55770I$    |                                       |                       |
| $a = 0.062544 + 1.158230I$  | $-2.38417 - 13.73050I$                | 0                     |
| $b = -0.88196 + 1.12725I$   |                                       |                       |
| $u = 1.45510 - 0.55770I$    |                                       |                       |
| $a = 0.062544 - 1.158230I$  | $-2.38417 + 13.73050I$                | 0                     |
| $b = -0.88196 - 1.12725I$   |                                       |                       |
| $u = 1.49488 + 0.54971I$    |                                       |                       |
| $a = 0.556075 + 0.702569I$  | $-8.20067 + 7.88855I$                 | 0                     |
| $b = -0.074312 + 1.106710I$ |                                       |                       |
| $u = 1.49488 - 0.54971I$    |                                       |                       |
| $a = 0.556075 - 0.702569I$  | $-8.20067 - 7.88855I$                 | 0                     |
| $b = -0.074312 - 1.106710I$ |                                       |                       |
| $u = -1.54678 + 0.38241I$   |                                       |                       |
| $a = 0.058988 + 0.963652I$  | $-3.44852 - 0.15850I$                 | 0                     |
| $b = 0.671602 + 1.051840I$  |                                       |                       |
| $u = -1.54678 - 0.38241I$   |                                       |                       |
| $a = 0.058988 - 0.963652I$  | $-3.44852 + 0.15850I$                 | 0                     |
| $b = 0.671602 - 1.051840I$  |                                       |                       |
| $u = -0.403651$             |                                       |                       |
| $a = 0.269102$              | 3.11032                               | -14.4860              |
| $b = 1.17376$               |                                       |                       |
| $u = -0.017309 + 0.345215I$ |                                       |                       |
| $a = -0.64237 + 1.75395I$   | $-4.65307 + 2.82812I$                 | $-1.91627 - 3.18964I$ |
| $b = -0.754075 - 0.974867I$ |                                       |                       |
| $u = -0.017309 - 0.345215I$ |                                       |                       |
| $a = -0.64237 - 1.75395I$   | $-4.65307 - 2.82812I$                 | $-1.91627 + 3.18964I$ |
| $b = -0.754075 + 0.974867I$ |                                       |                       |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape              |
|-------------------------------|---------------------------------------|-------------------------|
| $u = -1.46816 + 0.88855I$     | $-6.28229 + 4.32405I$                 | 0                       |
| $a = -0.331077 + 0.392184I$   |                                       |                         |
| $b = 0.298333 + 0.738138I$    |                                       |                         |
| $u = -1.46816 - 0.88855I$     | $-6.28229 - 4.32405I$                 | 0                       |
| $a = -0.331077 - 0.392184I$   |                                       |                         |
| $b = 0.298333 - 0.738138I$    |                                       |                         |
| $u = 1.58743 + 0.69474I$      | $-7.00010 - 2.20644I$                 | 0                       |
| $a = -0.213989 - 0.594570I$   |                                       |                         |
| $b = 0.414341 - 0.814522I$    |                                       |                         |
| $u = 1.58743 - 0.69474I$      | $-7.00010 + 2.20644I$                 | 0                       |
| $a = -0.213989 + 0.594570I$   |                                       |                         |
| $b = 0.414341 + 0.814522I$    |                                       |                         |
| $u = -0.156395 + 0.203509I$   | $-5.50574 - 2.51494I$                 | $-0.277428 + 1.330396I$ |
| $a = -0.57502 - 5.54669I$     |                                       |                         |
| $b = 0.577216 + 0.859044I$    |                                       |                         |
| $u = -0.156395 - 0.203509I$   | $-5.50574 + 2.51494I$                 | $-0.277428 - 1.330396I$ |
| $a = -0.57502 + 5.54669I$     |                                       |                         |
| $b = 0.577216 - 0.859044I$    |                                       |                         |
| $u = 0.172907 + 0.041641I$    | $-1.37595 - 1.18765I$                 | $-5.19575 - 0.40054I$   |
| $a = 5.13888 + 1.21083I$      |                                       |                         |
| $b = -0.051203 - 0.483822I$   |                                       |                         |
| $u = 0.172907 - 0.041641I$    | $-1.37595 + 1.18765I$                 | $-5.19575 + 0.40054I$   |
| $a = 5.13888 - 1.21083I$      |                                       |                         |
| $b = -0.051203 + 0.483822I$   |                                       |                         |
| $u = -0.0350083 + 0.1355980I$ | $-3.73207 - 1.00515I$                 | $-2.40866 + 2.83393I$   |
| $a = -0.33266 - 7.16426I$     |                                       |                         |
| $b = -0.679654 - 0.787469I$   |                                       |                         |
| $u = -0.0350083 - 0.1355980I$ | $-3.73207 + 1.00515I$                 | $-2.40866 - 2.83393I$   |
| $a = -0.33266 + 7.16426I$     |                                       |                         |
| $b = -0.679654 + 0.787469I$   |                                       |                         |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-------------------------------|---------------------------------------|-----------------------|
| $u = -0.1232550 + 0.0012074I$ |                                       |                       |
| $a = 10.42810 - 7.79652I$     | $-2.25570 + 8.60093I$                 | $2.87789 - 3.87010I$  |
| $b = 0.794455 - 0.940532I$    |                                       |                       |
| $u = -0.1232550 - 0.0012074I$ |                                       |                       |
| $a = 10.42810 + 7.79652I$     | $-2.25570 - 8.60093I$                 | $2.87789 + 3.87010I$  |
| $b = 0.794455 + 0.940532I$    |                                       |                       |
| $u = 0.0779976 + 0.0571355I$  |                                       |                       |
| $a = -11.07950 - 0.60969I$    | $1.20762 - 5.23630I$                  | $-0.16932 + 5.08837I$ |
| $b = 0.081061 - 0.855623I$    |                                       |                       |
| $u = 0.0779976 - 0.0571355I$  |                                       |                       |
| $a = -11.07950 + 0.60969I$    | $1.20762 + 5.23630I$                  | $-0.16932 - 5.08837I$ |
| $b = 0.081061 + 0.855623I$    |                                       |                       |

$$\text{II. } I_2^u = \langle -1.98 \times 10^{43}u^{43} + 9.68 \times 10^{42}u^{42} + \dots + 1.94 \times 10^{43}b - 2.15 \times 10^{43}, -8.59 \times 10^{42}u^{43} + 2.48 \times 10^{43}u^{42} + \dots + 1.94 \times 10^{43}a - 2.24 \times 10^{43}, u^{44} - 14u^{42} + \dots - 6u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.442348u^{43} - 1.27605u^{42} + \dots + 9.48823u + 1.15202 \\ 1.02107u^{43} - 0.498897u^{42} + \dots + 0.456345u + 1.10921 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -1.86583u^{43} + 1.94186u^{42} + \dots + 8.11038u - 2.61443 \\ -2.73749u^{43} - 1.19751u^{42} + \dots - 3.68047u - 0.277328 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.951559u^{43} - 1.50839u^{42} + \dots + 9.19417u + 1.36164 \\ 0.530214u^{43} - 0.642325u^{42} + \dots + 0.750293u + 1.13192 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.578727u^{43} - 0.777152u^{42} + \dots + 9.03189u + 0.0428080 \\ 1.02107u^{43} - 0.498897u^{42} + \dots + 0.456345u + 1.10921 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 3.75965u^{43} + 3.18740u^{42} + \dots + 26.6527u + 0.527639 \\ -1.21929u^{43} - 1.45127u^{42} + \dots - 0.893534u + 3.25217 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -3.03093u^{43} + 0.485290u^{42} + \dots + 15.7037u + 1.16313 \\ -1.74433u^{43} - 1.39069u^{42} + \dots - 0.604828u + 1.79368 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 3.10216u^{43} + 1.98381u^{42} + \dots + 12.5978u - 2.70383 \\ -0.469843u^{43} - 3.60173u^{42} + \dots - 13.2327u + 2.48958 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1.99045u^{43} - 2.99452u^{42} + \dots - 24.8396u - 1.21104 \\ 0.872695u^{43} - 0.591305u^{42} + \dots - 6.80976u - 1.68244 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $8.44648u^{43} + 7.77679u^{42} + \dots + 29.5073u + 7.06652$

**(iv) u-Polynomials at the component**

| Crossings | u-Polynomials at each crossing          |
|-----------|---|
| $c_1$     | $u^{44} - 16u^{43} + \cdots - u + 1$    |
| $c_2$     | $u^{44} + 11u^{42} + \cdots + 24u + 4$  |
| $c_3$     | $u^{44} - 5u^{43} + \cdots + 459u + 53$ |
| $c_4$     | $u^{44} - u^{43} + \cdots - 12u + 1$    |
| $c_5$     | $u^{44} + 2u^{43} + \cdots - 3u + 1$    |
| $c_6$     | $u^{44} - 14u^{42} + \cdots - 6u + 1$   |
| $c_7$     | $u^{44} + 5u^{42} + \cdots + 5u + 1$    |
| $c_8$     | $u^{44} - 2u^{43} + \cdots + 3u + 1$    |
| $c_9$     | $u^{44} - 3u^{43} + \cdots - 12u + 4$   |
| $c_{10}$  | $u^{44} + u^{43} + \cdots + 21u + 5$    |
| $c_{11}$  | $u^{44} - 14u^{42} + \cdots + 6u + 1$   |
| $c_{12}$  | $u^{44} + 3u^{43} + \cdots + 12u + 4$   |



**(v) Riley Polynomials at the component**

| Crossings     | Riley Polynomials at each crossing           |
|---------------|--|
| $c_1$         | $y^{44} + 2y^{43} + \cdots + 13y + 1$        |
| $c_2$         | $y^{44} + 22y^{43} + \cdots + 160y + 16$     |
| $c_3$         | $y^{44} - 23y^{43} + \cdots - 54861y + 2809$ |
| $c_4$         | $y^{44} + 11y^{43} + \cdots - 30y + 1$       |
| $c_5, c_8$    | $y^{44} + 42y^{43} + \cdots + 41y + 1$       |
| $c_6, c_{11}$ | $y^{44} - 28y^{43} + \cdots - 62y + 1$       |
| $c_7$         | $y^{44} + 10y^{43} + \cdots + 25y + 1$       |
| $c_9, c_{12}$ | $y^{44} - 33y^{43} + \cdots - 336y + 16$     |
| $c_{10}$      | $y^{44} - 33y^{43} + \cdots + 139y + 25$     |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.568391 + 0.729128I$ |                                       |                       |
| $a = 0.326516 - 0.134851I$  | $1.76900 - 2.98029I$                  | $1.04056 + 5.86823I$  |
| $b = 0.380316 - 0.794226I$  |                                       |                       |
| $u = -0.568391 - 0.729128I$ |                                       |                       |
| $a = 0.326516 + 0.134851I$  | $1.76900 + 2.98029I$                  | $1.04056 - 5.86823I$  |
| $b = 0.380316 + 0.794226I$  |                                       |                       |
| $u = -0.033308 + 0.916019I$ |                                       |                       |
| $a = -0.384168 - 0.100421I$ | $-3.90826 + 3.71668I$                 | $4.02023 - 0.85316I$  |
| $b = -0.541615 - 0.980435I$ |                                       |                       |
| $u = -0.033308 - 0.916019I$ |                                       |                       |
| $a = -0.384168 + 0.100421I$ | $-3.90826 - 3.71668I$                 | $4.02023 + 0.85316I$  |
| $b = -0.541615 + 0.980435I$ |                                       |                       |
| $u = -0.892569 + 0.173792I$ |                                       |                       |
| $a = 1.71165 - 1.41188I$    | $-6.75098 + 3.24279I$                 | $-5.20056 - 3.28738I$ |
| $b = -0.211018 - 1.068310I$ |                                       |                       |
| $u = -0.892569 - 0.173792I$ |                                       |                       |
| $a = 1.71165 + 1.41188I$    | $-6.75098 - 3.24279I$                 | $-5.20056 + 3.28738I$ |
| $b = -0.211018 + 1.068310I$ |                                       |                       |
| $u = 0.877395 + 0.152405I$  |                                       |                       |
| $a = 2.10983 + 2.09126I$    | $-3.27466 - 9.05461I$                 | $-3.85875 + 6.80346I$ |
| $b = 0.84419 + 1.16328I$    |                                       |                       |
| $u = 0.877395 - 0.152405I$  |                                       |                       |
| $a = 2.10983 - 2.09126I$    | $-3.27466 + 9.05461I$                 | $-3.85875 - 6.80346I$ |
| $b = 0.84419 - 1.16328I$    |                                       |                       |
| $u = -1.067210 + 0.329641I$ |                                       |                       |
| $a = -0.56149 + 1.96654I$   | $0.23792 + 6.95330I$                  | $-0.19235 - 8.00770I$ |
| $b = 0.24571 + 1.41174I$    |                                       |                       |
| $u = -1.067210 - 0.329641I$ |                                       |                       |
| $a = -0.56149 - 1.96654I$   | $0.23792 - 6.95330I$                  | $-0.19235 + 8.00770I$ |
| $b = 0.24571 - 1.41174I$    |                                       |                       |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.330852 + 0.811289I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $Cusp shape$          |
| $a = -0.563311 + 0.372540I$ | $-0.73315 - 2.06862I$                 | $-1.57378 + 3.38991I$ |
| $b = 0.275944 - 0.148859I$  |                                       |                       |
| $u = 0.330852 - 0.811289I$  |                                       |                       |
| $a = -0.563311 - 0.372540I$ | $-0.73315 + 2.06862I$                 | $-1.57378 - 3.38991I$ |
| $b = 0.275944 + 0.148859I$  |                                       |                       |
| $u = -1.172850 + 0.021726I$ |                                       |                       |
| $a = -0.583184 + 1.156580I$ | $-8.10503 - 2.37367I$                 | $-6.79272 + 2.26525I$ |
| $b = 0.559159 + 1.117440I$  |                                       |                       |
| $u = -1.172850 - 0.021726I$ |                                       |                       |
| $a = -0.583184 - 1.156580I$ | $-8.10503 + 2.37367I$                 | $-6.79272 - 2.26525I$ |
| $b = 0.559159 - 1.117440I$  |                                       |                       |
| $u = 1.192190 + 0.007031I$  |                                       |                       |
| $a = 0.445993 - 0.289531I$  | $-4.77244 - 8.33818I$                 | $-2.93267 + 4.59657I$ |
| $b = 1.47886 + 0.24026I$    |                                       |                       |
| $u = 1.192190 - 0.007031I$  |                                       |                       |
| $a = 0.445993 + 0.289531I$  | $-4.77244 + 8.33818I$                 | $-2.93267 - 4.59657I$ |
| $b = 1.47886 - 0.24026I$    |                                       |                       |
| $u = -0.265778 + 1.172380I$ |                                       |                       |
| $a = -0.337377 - 0.276762I$ | $2.85117 + 6.46214I$                  | $3.00364 - 1.54985I$  |
| $b = 0.103325 + 0.346660I$  |                                       |                       |
| $u = -0.265778 - 1.172380I$ |                                       |                       |
| $a = -0.337377 + 0.276762I$ | $2.85117 - 6.46214I$                  | $3.00364 + 1.54985I$  |
| $b = 0.103325 - 0.346660I$  |                                       |                       |
| $u = 0.392625 + 1.141650I$  |                                       |                       |
| $a = -0.102520 - 0.444080I$ | $1.04603 - 2.36836I$                  | $44.1617 + 18.2072I$  |
| $b = 0.377598 + 0.999885I$  |                                       |                       |
| $u = 0.392625 - 1.141650I$  |                                       |                       |
| $a = -0.102520 + 0.444080I$ | $1.04603 + 2.36836I$                  | $44.1617 - 18.2072I$  |
| $b = 0.377598 - 0.999885I$  |                                       |                       |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 1.152800 + 0.390687I$  |                                       |                       |
| $a = -0.40730 - 1.37844I$   | $-1.70467 - 3.09935I$                 | $3.87495 + 4.69017I$  |
| $b = 0.750002 - 0.841006I$  |                                       |                       |
| $u = 1.152800 - 0.390687I$  |                                       |                       |
| $a = -0.40730 + 1.37844I$   | $-1.70467 + 3.09935I$                 | $3.87495 - 4.69017I$  |
| $b = 0.750002 + 0.841006I$  |                                       |                       |
| $u = -1.224780 + 0.039877I$ |                                       |                       |
| $a = -0.79988 - 1.85151I$   | $-7.94022 + 2.00227I$                 | $-7.11951 - 1.81247I$ |
| $b = -0.103003 - 0.956789I$ |                                       |                       |
| $u = -1.224780 - 0.039877I$ |                                       |                       |
| $a = -0.79988 + 1.85151I$   | $-7.94022 - 2.00227I$                 | $-7.11951 + 1.81247I$ |
| $b = -0.103003 + 0.956789I$ |                                       |                       |
| $u = -1.132700 + 0.469548I$ |                                       |                       |
| $a = 0.204521 - 0.037375I$  | $-5.16435 + 3.96917I$                 | $-2.76653 - 7.09820I$ |
| $b = -0.736644 - 0.459692I$ |                                       |                       |
| $u = -1.132700 - 0.469548I$ |                                       |                       |
| $a = 0.204521 + 0.037375I$  | $-5.16435 - 3.96917I$                 | $-2.76653 + 7.09820I$ |
| $b = -0.736644 + 0.459692I$ |                                       |                       |
| $u = 0.253854 + 0.728873I$  |                                       |                       |
| $a = -0.079304 + 0.813278I$ | $-2.68839 - 0.52478I$                 | $-1.61508 + 0.33967I$ |
| $b = -0.626223 + 0.602615I$ |                                       |                       |
| $u = 0.253854 - 0.728873I$  |                                       |                       |
| $a = -0.079304 - 0.813278I$ | $-2.68839 + 0.52478I$                 | $-1.61508 - 0.33967I$ |
| $b = -0.626223 - 0.602615I$ |                                       |                       |
| $u = 1.250770 + 0.172717I$  |                                       |                       |
| $a = 0.019104 - 0.386515I$  | $-5.72596 - 0.65381I$                 | $-5.93761 - 2.46971I$ |
| $b = -0.867769 - 0.098738I$ |                                       |                       |
| $u = 1.250770 - 0.172717I$  |                                       |                       |
| $a = 0.019104 + 0.386515I$  | $-5.72596 + 0.65381I$                 | $-5.93761 + 2.46971I$ |
| $b = -0.867769 + 0.098738I$ |                                       |                       |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 1.257720 + 0.122794I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = -0.59138 - 1.49408I$   | $-6.19270 - 2.65309I$                 | $-5.10233 + 4.38496I$ |
| $b = -0.607999 - 1.208340I$ |                                       |                       |
| $u = 1.257720 - 0.122794I$  |                                       |                       |
| $a = -0.59138 + 1.49408I$   | $-6.19270 + 2.65309I$                 | $-5.10233 - 4.38496I$ |
| $b = -0.607999 + 1.208340I$ |                                       |                       |
| $u = 1.25358 + 0.67281I$    |                                       |                       |
| $a = -0.688839 - 0.557867I$ | $-4.93206 - 3.97224I$                 | 0                     |
| $b = -0.035633 - 1.006920I$ |                                       |                       |
| $u = 1.25358 - 0.67281I$    |                                       |                       |
| $a = -0.688839 + 0.557867I$ | $-4.93206 + 3.97224I$                 | 0                     |
| $b = -0.035633 + 1.006920I$ |                                       |                       |
| $u = -1.38297 + 0.42968I$   |                                       |                       |
| $a = 0.20311 - 1.65072I$    | $-4.74525 + 7.21929I$                 | 0                     |
| $b = -0.98968 - 2.08326I$   |                                       |                       |
| $u = -1.38297 - 0.42968I$   |                                       |                       |
| $a = 0.20311 + 1.65072I$    | $-4.74525 - 7.21929I$                 | 0                     |
| $b = -0.98968 + 2.08326I$   |                                       |                       |
| $u = 1.38628 + 0.47518I$    |                                       |                       |
| $a = 0.14872 + 1.60907I$    | $-8.43963 - 8.97237I$                 | 0                     |
| $b = -0.66815 + 1.39929I$   |                                       |                       |
| $u = 1.38628 - 0.47518I$    |                                       |                       |
| $a = 0.14872 - 1.60907I$    | $-8.43963 + 8.97237I$                 | 0                     |
| $b = -0.66815 - 1.39929I$   |                                       |                       |
| $u = -0.284970 + 0.195129I$ |                                       |                       |
| $a = -3.73768 + 0.96889I$   | $-0.01919 - 4.06027I$                 | $6.09263 + 2.79987I$  |
| $b = -0.951565 + 0.974494I$ |                                       |                       |
| $u = -0.284970 - 0.195129I$ |                                       |                       |
| $a = -3.73768 - 0.96889I$   | $-0.01919 + 4.06027I$                 | $6.09263 - 2.79987I$  |
| $b = -0.951565 - 0.974494I$ |                                       |                       |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -1.50227 + 0.73187I$   |                                       |                      |
| $a = -0.344001 + 0.559432I$ | $-6.68223 + 2.75026I$                 | 0                    |
| $b = 0.322144 + 0.772354I$  |                                       |                      |
| $u = -1.50227 - 0.73187I$   |                                       |                      |
| $a = -0.344001 - 0.559432I$ | $-6.68223 - 2.75026I$                 | 0                    |
| $b = 0.322144 - 0.772354I$  |                                       |                      |
| $u = 0.179744 + 0.051296I$  |                                       |                      |
| $a = 3.01100 + 0.69411I$    | $3.49795 + 0.09195I$                  | $9.24755 - 2.37966I$ |
| $b = 1.002060 - 0.051157I$  |                                       |                      |
| $u = 0.179744 - 0.051296I$  |                                       |                      |
| $a = 3.01100 - 0.69411I$    | $3.49795 - 0.09195I$                  | $9.24755 + 2.37966I$ |
| $b = 1.002060 + 0.051157I$  |                                       |                      |

### III. u-Polynomials

| Crossings | u-Polynomials at each crossing  |
|-----------|---|
| $c_1$     | $(u^{44} - 16u^{43} + \dots - u + 1)(u^{164} + 5u^{163} + \dots - 49u + 1)$                                   |
| $c_2$     | $(u^{44} + 11u^{42} + \dots + 24u + 4)$<br>$\cdot (u^{164} + u^{163} + \dots + 36157964272u + 1936765232)$    |
| $c_3$     | $(u^{44} - 5u^{43} + \dots + 459u + 53)$<br>$\cdot (u^{164} - 45u^{162} + \dots - 4066348387u + 426841301)$   |
| $c_4$     | $(u^{44} - u^{43} + \dots - 12u + 1)(u^{164} - 2u^{163} + \dots + 540u + 19)$                                 |
| $c_5$     | $(u^{44} + 2u^{43} + \dots - 3u + 1)(u^{164} + 11u^{163} + \dots + 9685865u + 827737)$                        |
| $c_6$     | $(u^{44} - 14u^{42} + \dots - 6u + 1)(u^{164} - u^{163} + \dots - 2u + 1)$                                    |
| $c_7$     | $(u^{44} + 5u^{42} + \dots + 5u + 1)$<br>$\cdot (u^{164} + u^{163} + \dots + 2097860395u + 150897161)$        |
| $c_8$     | $(u^{44} - 2u^{43} + \dots + 3u + 1)(u^{164} + 11u^{163} + \dots + 9685865u + 827737)$                        |
| $c_9$     | $(u^{44} - 3u^{43} + \dots - 12u + 4)(u^{164} - 50u^{162} + \dots + 992u + 1808)$                             |
| $c_{10}$  | $(u^{44} + u^{43} + \dots + 21u + 5)$<br>$\cdot (u^{164} + 6u^{163} + \dots + 1784816067153u + 207574985671)$ |
| $c_{11}$  | $(u^{44} - 14u^{42} + \dots + 6u + 1)(u^{164} - u^{163} + \dots - 2u + 1)$                                    |
| $c_{12}$  | $(u^{44} + 3u^{43} + \dots + 12u + 4)(u^{164} - 50u^{162} + \dots + 992u + 1808)$                             |

#### IV. Riley Polynomials

| Crossings     | Riley Polynomials at each crossing   |
|---------------|--|
| $c_1$         | $(y^{44} + 2y^{43} + \dots + 13y + 1)(y^{164} + 3y^{163} + \dots - 411y + 1)$  |
| $c_2$         | $(y^{44} + 22y^{43} + \dots + 160y + 16) \cdot (y^{164} + 75y^{163} + \dots + 1.76 \times 10^{20}y + 3.75 \times 10^{18})$     |
| $c_3$         | $(y^{44} - 23y^{43} + \dots - 54861y + 2809) \cdot (y^{164} - 90y^{163} + \dots - 2.04 \times 10^{19}y + 1.82 \times 10^{17})$ |
| $c_4$         | $(y^{44} + 11y^{43} + \dots - 30y + 1)(y^{164} + 16y^{163} + \dots - 4434y + 361)$   |
| $c_5, c_8$    | $(y^{44} + 42y^{43} + \dots + 41y + 1) \cdot (y^{164} + 139y^{163} + \dots - 8776342483355y + 685148541169)$                   |
| $c_6, c_{11}$ | $(y^{44} - 28y^{43} + \dots - 62y + 1)(y^{164} - 115y^{163} + \dots - 170y + 1)$   |
| $c_7$         | $(y^{44} + 10y^{43} + \dots + 25y + 1) \cdot (y^{164} + 59y^{163} + \dots + 634377626274351873y + 22769953197859921)$          |
| $c_9, c_{12}$ | $(y^{44} - 33y^{43} + \dots - 336y + 16) \cdot (y^{164} - 100y^{163} + \dots - 153608192y + 3268864)$                          |
| $c_{10}$      | $(y^{44} - 33y^{43} + \dots + 139y + 25) \cdot (y^{164} - 108y^{163} + \dots - 3.42 \times 10^{24}y + 4.31 \times 10^{22})$    |