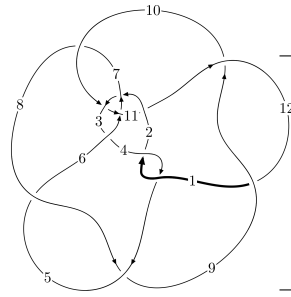
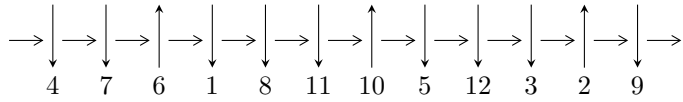


12a₁₀₂₂ (K12a₁₀₂₂)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$1,5 \xrightarrow{c_4} 4 \xrightarrow{c_1} 2,9 \xrightarrow{c_8} 8 \xrightarrow{c_5} 6 \xrightarrow{c_3} 3 \xrightarrow{c_{12}} 12 \xrightarrow{c_9} 10 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \rightsquigarrow c_2, c_6, c_{10}$$

Ideals for irreducible components² of X_{par}

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\begin{aligned}
I_1^u &= \langle b - u, a - 1, u^{11} + 3u^{10} + 10u^9 + 16u^8 + 25u^7 + 22u^6 + 17u^5 + 7u^4 + 2u^3 + 2u^2 + 2u - 1 \rangle \\
I_2^u &= \langle b - u, -32833783u^{25} + 115127419u^{24} + \dots + 15217558a + 63920326, u^{26} - 4u^{25} + \dots - 8u + 1 \rangle \\
I_3^u &= \langle -16207713u^{25} + 59026143u^{24} + \dots + 15217558b + 32833783, a - 1, u^{26} - 4u^{25} + \dots - 8u + 1 \rangle \\
I_4^u &= \langle -1.98504 \times 10^{21}u^{25} - 3.05841 \times 10^{22}u^{24} + \dots + 4.27582 \times 10^{21}b - 1.24580 \times 10^{24}, \\
&\quad 7.78622 \times 10^{22}u^{25} + 1.18227 \times 10^{24}u^{24} + \dots + 1.36826 \times 10^{23}a + 2.49940 \times 10^{25}, \\
&\quad u^{26} + 16u^{25} + \dots + 4800u + 512 \rangle \\
I_5^u &= \langle b + u, a + 1, u^{10} + 2u^9 + 6u^8 + 6u^7 + 9u^6 + 5u^5 + 6u^4 + 3u^3 + 3u^2 + u + 1 \rangle \\
I_6^u &= \langle b + u, 2u^9 + u^8 + 10u^7 + 8u^6 + 22u^5 + 19u^4 + 25u^3 + 17u^2 + a + 13u + 3, \\
&\quad u^{10} + u^9 + 5u^8 + 6u^7 + 12u^6 + 13u^5 + 15u^4 + 12u^3 + 9u^2 + 4u + 1 \rangle \\
I_7^u &= \langle -u^9 - 4u^7 - 2u^6 - 7u^5 - 5u^4 - 7u^3 - 5u^2 + b - 5u - 2, a + 1, \\
&\quad u^{10} + u^9 + 5u^8 + 6u^7 + 12u^6 + 13u^5 + 15u^4 + 12u^3 + 9u^2 + 4u + 1 \rangle \\
I_8^u &= \langle 136u^9 + 138u^8 + 938u^7 + 182u^6 + 237u^5 - 1628u^4 - 2106u^3 - 2845u^2 + 809b - 2290u - 883, \\
&\quad 883u^9 + 3668u^8 + \dots + 809a + 2125, \\
&\quad u^{10} + 4u^9 + 15u^8 + 34u^7 + 57u^6 + 71u^5 + 66u^4 + 45u^3 + 20u^2 + 5u + 1 \rangle \\
I_9^u &= \langle -3.23739 \times 10^{22}u^{35} + 2.81046 \times 10^{23}u^{34} + \dots + 6.80585 \times 10^{22}b + 8.32842 \times 10^{23}, \\
&\quad -2.58181 \times 10^{25}au^{35} - 1.04570 \times 10^{25}u^{35} + \dots + 6.94260 \times 10^{26}a - 5.64319 \times 10^{26}, \\
&\quad u^{36} - 9u^{35} + \dots - 134u + 31 \rangle
\end{aligned}$$

* 9 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 201 representations.

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle b - u, a - 1, u^{11} + 3u^{10} + \cdots + 2u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u + 1 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 + u + 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^6 + 2u^5 + 4u^4 + 3u^3 + 2u^2 + 1 \\ u^6 + u^5 + 2u^4 - u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u^2 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^3 + u^2 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^6 + u^5 + 3u^4 + u^3 + 2u^2 + u + 1 \\ u^7 + 2u^6 + 4u^5 + 3u^4 + 2u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^5 - u^4 - 2u^3 + u \\ u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u^2 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -3u^{10} - 9u^9 - 27u^8 - 45u^7 - 63u^6 - 63u^5 - 45u^4 - 24u^3 - 12u^2 - 9$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------------------------------|---|
| c_1, c_4, c_5 c_8, c_9, c_{12} | $u^{11} - 3u^{10} + \dots + 2u + 1$ |
| c_2, c_6, c_{10} | $u^{11} + 5u^{10} + 13u^9 + 20u^8 + 21u^7 + 15u^6 + 9u^5 + 4u^4 + 2u^3 + u + 1$ |
| c_3, c_7, c_{11} | $u^{11} + 6u^{10} + \dots + 13u + 2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------------------------------|---------------------------------------|
| c_1, c_4, c_5 c_8, c_9, c_{12} | $y^{11} + 11y^{10} + \cdots + 8y - 1$ |
| c_2, c_6, c_{10} | $y^{11} + y^{10} + \cdots + y - 1$ |
| c_3, c_7, c_{11} | $y^{11} + 2y^{10} + \cdots + 73y - 4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = -0.774257 + 0.374083I$ $a = 1.00000$ $b = -0.774257 + 0.374083I$ | $-4.25720 - 4.91168I$ | $-10.85180 + 1.59612I$ |
| $u = -0.774257 - 0.374083I$ $a = 1.00000$ $b = -0.774257 - 0.374083I$ | $-4.25720 + 4.91168I$ | $-10.85180 - 1.59612I$ |
| $u = -0.270847 + 1.340850I$ $a = 1.00000$ $b = -0.270847 + 1.340850I$ | $8.14535 - 0.73285I$ | $1.25794 + 2.64536I$ |
| $u = -0.270847 - 1.340850I$ $a = 1.00000$ $b = -0.270847 - 1.340850I$ | $8.14535 + 0.73285I$ | $1.25794 - 2.64536I$ |
| $u = 0.342788 + 0.497406I$ $a = 1.00000$ $b = 0.342788 + 0.497406I$ | $-0.04623 - 2.08057I$ | $-2.30453 + 3.92520I$ |
| $u = 0.342788 - 0.497406I$ $a = 1.00000$ $b = 0.342788 - 0.497406I$ | $-0.04623 + 2.08057I$ | $-2.30453 - 3.92520I$ |
| $u = -0.39626 + 1.49188I$ $a = 1.00000$ $b = -0.39626 + 1.49188I$ | $13.36520 + 3.24725I$ | $3.49713 - 0.24747I$ |
| $u = -0.39626 - 1.49188I$ $a = 1.00000$ $b = -0.39626 - 1.49188I$ | $13.36520 - 3.24725I$ | $3.49713 + 0.24747I$ |
| $u = -0.55532 + 1.54667I$ $a = 1.00000$ $b = -0.55532 + 1.54667I$ | $7.1043 + 20.4661I$ | $-2.35751 - 9.89201I$ |
| $u = -0.55532 - 1.54667I$ $a = 1.00000$ $b = -0.55532 - 1.54667I$ | $7.1043 - 20.4661I$ | $-2.35751 + 9.89201I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = 0.307797$ | | |
| $a = 1.00000$ | -0.919687 | -11.4820 |
| $b = 0.307797$ | | |

$$\text{II. } I_2^u = \langle b - u, -3.28 \times 10^7 u^{25} + 1.15 \times 10^8 u^{24} + \dots + 1.52 \times 10^7 a + 6.39 \times 10^7, u^{26} - 4u^{25} + \dots - 8u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2.15762u^{25} - 7.56543u^{24} + \dots + 34.1422u - 4.20043 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 2.15762u^{25} - 7.56543u^{24} + \dots + 35.1422u - 4.20043 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.06507u^{25} - 3.87882u^{24} + \dots + 13.0606u - 1.15762 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1.37871u^{25} - 5.67363u^{24} + \dots + 8.30834u - 0.326775 \\ 0.345083u^{25} - 0.871352u^{24} + \dots - 1.72715u + 0.250749 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2.81841u^{25} - 11.6053u^{24} + \dots + 65.4231u - 14.0818 \\ 0.381448u^{25} - 1.80464u^{24} + \dots + 7.36291u - 1.06507 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 5.49898u^{25} - 20.1756u^{24} + \dots + 66.5441u - 14.9384 \\ 1.06538u^{25} - 3.01528u^{24} + \dots + 1.89123u - 0.733408 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.994418u^{25} - 5.04490u^{24} + \dots + 6.41196u - 2.43422 \\ 0.501690u^{25} - 2.09040u^{24} + \dots + 0.933452u - 0.423238 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2.80974u^{25} - 11.3423u^{24} + \dots + 61.9904u - 13.1672 \\ 0.457444u^{25} - 2.03581u^{24} + \dots + 8.95996u - 1.75125 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{75282671}{7608779}u^{25} - \frac{266619655}{7608779}u^{24} + \dots + \frac{938353524}{7608779}u - \frac{212625691}{7608779}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|---|
| c_1, c_4, c_5 c_8 | $u^{26} + 4u^{25} + \dots + 8u + 1$ |
| c_2 | $u^{26} + 22u^{25} + \dots + 152u + 32$ |
| c_3 | $u^{26} + 27u^{25} + \dots + 65536u + 4096$ |
| c_6, c_{10} | $u^{26} - 5u^{25} + \dots - 4u + 1$ |
| c_7, c_{11} | $u^{26} - 4u^{25} + \dots - 7u + 1$ |
| c_9, c_{12} | $u^{26} - 16u^{25} + \dots - 4800u + 512$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|--|
| c_1, c_4, c_5 c_8 | $y^{26} + 26y^{25} + \dots - 26y + 1$ |
| c_2 | $y^{26} - 4y^{25} + \dots - 11584y + 1024$ |
| c_3 | $y^{26} + 7y^{25} + \dots + 645922816y + 16777216$ |
| c_6, c_{10} | $y^{26} + 5y^{25} + \dots - 6y + 1$ |
| c_7, c_{11} | $y^{26} + 8y^{25} + \dots + y + 1$ |
| c_9, c_{12} | $y^{26} + 14y^{25} + \dots + 1110016y + 262144$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.813745 + 0.422636I$ $a = -0.813664 - 0.438057I$ $b = 0.813745 + 0.422636I$ | $-2.68290 - 3.01106I$ | $-20.1229 + 10.7502I$ |
| $u = 0.813745 - 0.422636I$ $a = -0.813664 + 0.438057I$ $b = 0.813745 - 0.422636I$ | $-2.68290 + 3.01106I$ | $-20.1229 - 10.7502I$ |
| $u = 0.123424 + 1.162910I$ $a = -1.93663 + 0.49379I$ $b = 0.123424 + 1.162910I$ | $5.90859 + 4.10061I$ | $2.79728 - 10.32745I$ |
| $u = 0.123424 - 1.162910I$ $a = -1.93663 - 0.49379I$ $b = 0.123424 - 1.162910I$ | $5.90859 - 4.10061I$ | $2.79728 + 10.32745I$ |
| $u = 0.769690 + 0.075945I$ $a = -0.525711 + 1.029160I$ $b = 0.769690 + 0.075945I$ | $-2.57819 + 0.87030I$ | $-17.9709 + 1.0721I$ |
| $u = 0.769690 - 0.075945I$ $a = -0.525711 - 1.029160I$ $b = 0.769690 - 0.075945I$ | $-2.57819 - 0.87030I$ | $-17.9709 - 1.0721I$ |
| $u = -0.729341 + 0.116282I$ $a = 0.55820 + 1.49864I$ $b = -0.729341 + 0.116282I$ | $-2.36667 - 9.84234I$ | $-8.56561 + 5.66390I$ |
| $u = -0.729341 - 0.116282I$ $a = 0.55820 - 1.49864I$ $b = -0.729341 - 0.116282I$ | $-2.36667 + 9.84234I$ | $-8.56561 - 5.66390I$ |
| $u = -0.056569 + 1.303740I$ $a = 0.746392 + 1.143550I$ $b = -0.056569 + 1.303740I$ | $6.70389 - 1.79520I$ | $5.95883 + 1.74216I$ |
| $u = -0.056569 - 1.303740I$ $a = 0.746392 - 1.143550I$ $b = -0.056569 - 1.303740I$ | $6.70389 + 1.79520I$ | $5.95883 - 1.74216I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.302846 + 1.282200I$ $a = 0.451565 + 1.043670I$ $b = -0.302846 + 1.282200I$ | $1.37803 + 13.53090I$ | $-3.53647 - 9.06833I$ |
| $u = -0.302846 - 1.282200I$ $a = 0.451565 - 1.043670I$ $b = -0.302846 - 1.282200I$ | $1.37803 - 13.53090I$ | $-3.53647 + 9.06833I$ |
| $u = 0.272167 + 1.326590I$ $a = -0.079220 + 0.807508I$ $b = 0.272167 + 1.326590I$ | $3.18245 - 5.41198I$ | $-1.04824 + 12.39529I$ |
| $u = 0.272167 - 1.326590I$ $a = -0.079220 - 0.807508I$ $b = 0.272167 - 1.326590I$ | $3.18245 + 5.41198I$ | $-1.04824 - 12.39529I$ |
| $u = -0.042971 + 1.360470I$ $a = 0.454407 + 0.559333I$ $b = -0.042971 + 1.360470I$ | $6.99635 - 1.64768I$ | $2.93239 + 1.38429I$ |
| $u = -0.042971 - 1.360470I$ $a = 0.454407 - 0.559333I$ $b = -0.042971 - 1.360470I$ | $6.99635 + 1.64768I$ | $2.93239 - 1.38429I$ |
| $u = -0.359342 + 0.383452I$ $a = 1.45268 - 1.73242I$ $b = -0.359342 + 0.383452I$ | $1.79210 - 2.89318I$ | $-5.66787 + 3.03704I$ |
| $u = -0.359342 - 0.383452I$ $a = 1.45268 + 1.73242I$ $b = -0.359342 - 0.383452I$ | $1.79210 + 2.89318I$ | $-5.66787 - 3.03704I$ |
| $u = 0.33767 + 1.48359I$ $a = -1.092450 + 0.239272I$ $b = 0.33767 + 1.48359I$ | $10.3557 - 10.3695I$ | $2.75046 + 9.04972I$ |
| $u = 0.33767 - 1.48359I$ $a = -1.092450 - 0.239272I$ $b = 0.33767 - 1.48359I$ | $10.3557 + 10.3695I$ | $2.75046 - 9.04972I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.42218 + 1.54686I$ $a = -0.749536 - 0.070449I$ $b = 0.42218 + 1.54686I$ | $8.98409 - 4.61256I$ | $0. + 3.52913I$ |
| $u = 0.42218 - 1.54686I$ $a = -0.749536 + 0.070449I$ $b = 0.42218 - 1.54686I$ | $8.98409 + 4.61256I$ | $0. - 3.52913I$ |
| $u = 0.52411 + 1.57107I$ $a = -0.900686 + 0.050431I$ $b = 0.52411 + 1.57107I$ | $7.28763 - 11.38750I$ | $-6.0000 + 13.5374I$ |
| $u = 0.52411 - 1.57107I$ $a = -0.900686 - 0.050431I$ $b = 0.52411 - 1.57107I$ | $7.28763 + 11.38750I$ | $-6.0000 - 13.5374I$ |
| $u = 0.228076 + 0.082713I$ $a = 3.43466 + 2.50584I$ $b = 0.228076 + 0.082713I$ | $-0.54783 - 2.31386I$ | $-1.42706 + 8.46763I$ |
| $u = 0.228076 - 0.082713I$ $a = 3.43466 - 2.50584I$ $b = 0.228076 - 0.082713I$ | $-0.54783 + 2.31386I$ | $-1.42706 - 8.46763I$ |

$$\text{III. } I_3^u = \langle -1.62 \times 10^7 u^{25} + 5.90 \times 10^7 u^{24} + \dots + 1.52 \times 10^7 b + 3.28 \times 10^7, a - 1, u^{26} - 4u^{25} + \dots - 8u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1.06507u^{25} - 3.87882u^{24} + \dots + 13.0606u - 2.15762 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1.06507u^{25} - 3.87882u^{24} + \dots + 13.0606u - 1.15762 \\ 1.06507u^{25} - 3.87882u^{24} + \dots + 13.0606u - 2.15762 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.733408u^{25} - 1.86826u^{24} + \dots + 21.5260u - 3.97603 \\ -0.331658u^{25} + 2.01056u^{24} + \dots + 8.46544u - 2.81841 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.423238u^{25} - 1.19126u^{24} + \dots + 2.13478u - 2.45245 \\ -0.733252u^{25} + 3.33702u^{24} + \dots - 16.2748u + 2.22898 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ 0.381448u^{25} - 1.80464u^{24} + \dots + 7.36291u - 1.06507 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ 0.786222u^{25} - 3.01419u^{24} + \dots + 15.0471u - 2.53907 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1.75125u^{25} - 6.54757u^{24} + \dots + 28.4703u - 5.05007 \\ 1.01789u^{25} - 3.75446u^{24} + \dots + 14.8401u - 4.05295 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.250749u^{25} - 1.34808u^{24} + \dots + 3.61220u - 0.278844 \\ 0.639680u^{25} - 2.50923u^{24} + \dots + 7.76212u - 1.13131 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{75282671}{7608779}u^{25} - \frac{266619655}{7608779}u^{24} + \dots + \frac{938353524}{7608779}u - \frac{212625691}{7608779}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|---|
| c_1, c_4, c_9 c_{12} | $u^{26} + 4u^{25} + \dots + 8u + 1$ |
| c_2, c_6 | $u^{26} - 5u^{25} + \dots - 4u + 1$ |
| c_3, c_7 | $u^{26} - 4u^{25} + \dots - 7u + 1$ |
| c_5, c_8 | $u^{26} - 16u^{25} + \dots - 4800u + 512$ |
| c_{10} | $u^{26} + 22u^{25} + \dots + 152u + 32$ |
| c_{11} | $u^{26} + 27u^{25} + \dots + 65536u + 4096$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1, c_4, c_9 c_{12} | $y^{26} + 26y^{25} + \dots - 26y + 1$ |
| c_2, c_6 | $y^{26} + 5y^{25} + \dots - 6y + 1$ |
| c_3, c_7 | $y^{26} + 8y^{25} + \dots + y + 1$ |
| c_5, c_8 | $y^{26} + 14y^{25} + \dots + 1110016y + 262144$ |
| c_{10} | $y^{26} - 4y^{25} + \dots - 11584y + 1024$ |
| c_{11} | $y^{26} + 7y^{25} + \dots + 645922816y + 16777216$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.813745 + 0.422636I$ $a = 1.00000$ $b = -0.476976 - 0.700351I$ | $-2.68290 - 3.01106I$ | $-20.1229 + 10.7502I$ |
| $u = 0.813745 - 0.422636I$ $a = 1.00000$ $b = -0.476976 + 0.700351I$ | $-2.68290 + 3.01106I$ | $-20.1229 - 10.7502I$ |
| $u = 0.123424 + 1.162910I$ $a = 1.00000$ $b = -0.81325 - 2.19118I$ | $5.90859 + 4.10061I$ | $2.79728 - 10.32745I$ |
| $u = 0.123424 - 1.162910I$ $a = 1.00000$ $b = -0.81325 + 2.19118I$ | $5.90859 - 4.10061I$ | $2.79728 + 10.32745I$ |
| $u = 0.769690 + 0.075945I$ $a = 1.00000$ $b = -0.482793 + 0.752206I$ | $-2.57819 + 0.87030I$ | $-17.9709 + 1.0721I$ |
| $u = 0.769690 - 0.075945I$ $a = 1.00000$ $b = -0.482793 - 0.752206I$ | $-2.57819 - 0.87030I$ | $-17.9709 - 1.0721I$ |
| $u = -0.729341 + 0.116282I$ $a = 1.00000$ $b = -0.581380 - 1.028110I$ | $-2.36667 - 9.84234I$ | $-8.56561 + 5.66390I$ |
| $u = -0.729341 - 0.116282I$ $a = 1.00000$ $b = -0.581380 + 1.028110I$ | $-2.36667 + 9.84234I$ | $-8.56561 - 5.66390I$ |
| $u = -0.056569 + 1.303740I$ $a = 1.00000$ $b = -1.53312 + 0.90841I$ | $6.70389 - 1.79520I$ | $5.95883 + 1.74216I$ |
| $u = -0.056569 - 1.303740I$ $a = 1.00000$ $b = -1.53312 - 0.90841I$ | $6.70389 + 1.79520I$ | $5.95883 - 1.74216I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = -0.302846 + 1.282200I$ $a = 1.00000$ $b = -1.47496 + 0.26293I$ | $1.37803 + 13.53090I$ | $-3.53647 - 9.06833I$ |
| $u = -0.302846 - 1.282200I$ $a = 1.00000$ $b = -1.47496 - 0.26293I$ | $1.37803 - 13.53090I$ | $-3.53647 + 9.06833I$ |
| $u = 0.272167 + 1.326590I$ $a = 1.00000$ $b = -1.092800 + 0.114684I$ | $3.18245 - 5.41198I$ | $-1.04824 + 12.39529I$ |
| $u = 0.272167 - 1.326590I$ $a = 1.00000$ $b = -1.092800 - 0.114684I$ | $3.18245 + 5.41198I$ | $-1.04824 - 12.39529I$ |
| $u = -0.042971 + 1.360470I$ $a = 1.00000$ $b = -0.780481 + 0.594171I$ | $6.99635 - 1.64768I$ | $2.93239 + 1.38429I$ |
| $u = -0.042971 - 1.360470I$ $a = 1.00000$ $b = -0.780481 - 0.594171I$ | $6.99635 + 1.64768I$ | $2.93239 - 1.38429I$ |
| $u = -0.359342 + 0.383452I$ $a = 1.00000$ $b = 0.142290 + 1.179570I$ | $1.79210 - 2.89318I$ | $-5.66787 + 3.03704I$ |
| $u = -0.359342 - 0.383452I$ $a = 1.00000$ $b = 0.142290 - 1.179570I$ | $1.79210 + 2.89318I$ | $-5.66787 - 3.03704I$ |
| $u = 0.33767 + 1.48359I$ $a = 1.00000$ $b = -0.72387 - 1.53996I$ | $10.3557 - 10.3695I$ | $2.75046 + 9.04972I$ |
| $u = 0.33767 - 1.48359I$ $a = 1.00000$ $b = -0.72387 + 1.53996I$ | $10.3557 + 10.3695I$ | $2.75046 - 9.04972I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.42218 + 1.54686I$ $a = 1.00000$ $b = -0.207464 - 1.189170I$ | $8.98409 - 4.61256I$ | $0. + 3.52913I$ |
| $u = 0.42218 - 1.54686I$ $a = 1.00000$ $b = -0.207464 + 1.189170I$ | $8.98409 + 4.61256I$ | $0. - 3.52913I$ |
| $u = 0.52411 + 1.57107I$ $a = 1.00000$ $b = -0.55129 - 1.38861I$ | $7.28763 - 11.38750I$ | $-6.0000 + 13.5374I$ |
| $u = 0.52411 - 1.57107I$ $a = 1.00000$ $b = -0.55129 + 1.38861I$ | $7.28763 + 11.38750I$ | $-6.0000 - 13.5374I$ |
| $u = 0.228076 + 0.082713I$ $a = 1.00000$ $b = 0.576097 + 0.855613I$ | $-0.54783 - 2.31386I$ | $-1.42706 + 8.46763I$ |
| $u = 0.228076 - 0.082713I$ $a = 1.00000$ $b = 0.576097 - 0.855613I$ | $-0.54783 + 2.31386I$ | $-1.42706 - 8.46763I$ |

$$\text{IV. } I_4^u = \langle -1.99 \times 10^{21}u^{25} - 3.06 \times 10^{22}u^{24} + \dots + 4.28 \times 10^{21}b - 1.25 \times 10^{24}, 7.79 \times 10^{22}u^{25} + 1.18 \times 10^{24}u^{24} + \dots + 1.37 \times 10^{23}a + 2.50 \times 10^{25}, u^{26} + 16u^{25} + \dots + 4800u + 512 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.569059u^{25} - 8.64070u^{24} + \dots - 1794.38u - 182.670 \\ 0.464247u^{25} + 7.15281u^{24} + \dots + 2548.81u + 291.358 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.104812u^{25} - 1.48789u^{24} + \dots + 754.438u + 108.689 \\ 0.464247u^{25} + 7.15281u^{24} + \dots + 2548.81u + 291.358 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.163997u^{25} - 2.44303u^{24} + \dots + 647.490u + 104.877 \\ 0.168292u^{25} + 2.70530u^{24} + \dots + 1528.73u + 170.132 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.160379u^{25} - 2.67664u^{24} + \dots - 1537.33u - 176.728 \\ -0.437158u^{25} - 6.49946u^{24} + \dots - 605.410u - 41.8128 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.332289u^{25} - 5.14833u^{24} + \dots - 881.241u - 66.2547 \\ 0.168292u^{25} + 2.70530u^{24} + \dots + 1529.73u + 170.132 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.465710u^{25} - 7.70167u^{24} + \dots - 3049.11u - 314.804 \\ -0.525455u^{25} - 7.49088u^{24} + \dots - 16.4232u + 0.749111 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2.04513u^{25} - 33.1074u^{24} + \dots - 13615.2u - 1488.51 \\ 0.602416u^{25} + 10.4558u^{24} + \dots + 8812.89u + 1024.21 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.163806u^{25} - 2.61622u^{24} + \dots - 22.1965u + 33.6433 \\ -0.191654u^{25} - 2.70075u^{24} + \dots - 28.4066u - 13.5376 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{8677123745570668955903}{2137910852471657101464}u^{25} + \frac{37110273149493833583689}{534477713117914275366}u^{24} + \dots + \frac{14742195626650572055925240}{267238856558957137683}u + \frac{592218296124020712509686}{89079618852985712561}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|---|
| c_1, c_4 | $u^{26} - 16u^{25} + \dots - 4800u + 512$ |
| c_2, c_{10} | $u^{26} - 5u^{25} + \dots - 4u + 1$ |
| c_3, c_{11} | $u^{26} - 4u^{25} + \dots - 7u + 1$ |
| c_5, c_8, c_9 c_{12} | $u^{26} + 4u^{25} + \dots + 8u + 1$ |
| c_6 | $u^{26} + 22u^{25} + \dots + 152u + 32$ |
| c_7 | $u^{26} + 27u^{25} + \dots + 65536u + 4096$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1, c_4 | $y^{26} + 14y^{25} + \dots + 1110016y + 262144$ |
| c_2, c_{10} | $y^{26} + 5y^{25} + \dots - 6y + 1$ |
| c_3, c_{11} | $y^{26} + 8y^{25} + \dots + y + 1$ |
| c_5, c_8, c_9 c_{12} | $y^{26} + 26y^{25} + \dots - 26y + 1$ |
| c_6 | $y^{26} - 4y^{25} + \dots - 11584y + 1024$ |
| c_7 | $y^{26} + 7y^{25} + \dots + 645922816y + 16777216$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.780481 + 0.594171I$ $a = 0.874972 - 1.077010I$ $b = -0.042971 + 1.360470I$ | $6.99635 - 1.64768I$ | $2.93239 + 1.38429I$ |
| $u = -0.780481 - 0.594171I$ $a = 0.874972 + 1.077010I$ $b = -0.042971 - 1.360470I$ | $6.99635 + 1.64768I$ | $2.93239 - 1.38429I$ |
| $u = 0.576097 + 0.855613I$ $a = 0.190011 - 0.138627I$ $b = 0.228076 + 0.082713I$ | $-0.54783 - 2.31386I$ | $-1.42706 + 8.46763I$ |
| $u = 0.576097 - 0.855613I$ $a = 0.190011 + 0.138627I$ $b = 0.228076 - 0.082713I$ | $-0.54783 + 2.31386I$ | $-1.42706 - 8.46763I$ |
| $u = -1.092800 + 0.114684I$ $a = -0.120333 - 1.226570I$ $b = 0.272167 + 1.326590I$ | $3.18245 - 5.41198I$ | $-1.04824 + 12.39529I$ |
| $u = -1.092800 - 0.114684I$ $a = -0.120333 + 1.226570I$ $b = 0.272167 - 1.326590I$ | $3.18245 + 5.41198I$ | $-1.04824 - 12.39529I$ |
| $u = -0.482793 + 0.752206I$ $a = -0.393633 - 0.770595I$ $b = 0.769690 + 0.075945I$ | $-2.57819 + 0.87030I$ | $-17.9709 + 1.0721I$ |
| $u = -0.482793 - 0.752206I$ $a = -0.393633 + 0.770595I$ $b = 0.769690 - 0.075945I$ | $-2.57819 - 0.87030I$ | $-17.9709 - 1.0721I$ |
| $u = -0.476976 + 0.700351I$ $a = -0.952831 - 0.512982I$ $b = 0.813745 - 0.422636I$ | $-2.68290 + 3.01106I$ | $-20.1229 - 10.7502I$ |
| $u = -0.476976 - 0.700351I$ $a = -0.952831 + 0.512982I$ $b = 0.813745 + 0.422636I$ | $-2.68290 - 3.01106I$ | $-20.1229 + 10.7502I$ |

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.581380 + 1.028110I$ $a = 0.218258 + 0.585977I$ $b = -0.729341 - 0.116282I$ | $-2.36667 + 9.84234I$ | $-6.00000 - 5.66390I$ |
| $u = -0.581380 - 1.028110I$ $a = 0.218258 - 0.585977I$ $b = -0.729341 + 0.116282I$ | $-2.36667 - 9.84234I$ | $-6.00000 + 5.66390I$ |
| $u = 0.142290 + 1.179570I$ $a = 0.284195 + 0.338921I$ $b = -0.359342 + 0.383452I$ | $1.79210 - 2.89318I$ | $-6.00000 + 3.03704I$ |
| $u = 0.142290 - 1.179570I$ $a = 0.284195 - 0.338921I$ $b = -0.359342 - 0.383452I$ | $1.79210 + 2.89318I$ | $-6.00000 - 3.03704I$ |
| $u = -0.207464 + 1.189170I$ $a = -1.322480 - 0.124300I$ $b = 0.42218 - 1.54686I$ | $8.98409 + 4.61256I$ | $0. - 3.52913I$ |
| $u = -0.207464 - 1.189170I$ $a = -1.322480 + 0.124300I$ $b = 0.42218 + 1.54686I$ | $8.98409 - 4.61256I$ | $0. + 3.52913I$ |
| $u = -0.55129 + 1.38861I$ $a = -1.106800 + 0.061971I$ $b = 0.52411 - 1.57107I$ | $7.28763 + 11.38750I$ | 0 |
| $u = -0.55129 - 1.38861I$ $a = -1.106800 - 0.061971I$ $b = 0.52411 + 1.57107I$ | $7.28763 - 11.38750I$ | 0 |
| $u = -1.47496 + 0.26293I$ $a = 0.349193 - 0.807068I$ $b = -0.302846 + 1.282200I$ | $1.37803 + 13.53090I$ | 0 |
| $u = -1.47496 - 0.26293I$ $a = 0.349193 + 0.807068I$ $b = -0.302846 - 1.282200I$ | $1.37803 - 13.53090I$ | 0 |

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.72387 + 1.53996I$ | $10.3557 + 10.3695I$ | 0 |
| $a = -0.873470 + 0.191310I$ | | |
| $b = 0.33767 - 1.48359I$ | | |
| $u = -0.72387 - 1.53996I$ | $10.3557 - 10.3695I$ | 0 |
| $a = -0.873470 - 0.191310I$ | | |
| $b = 0.33767 + 1.48359I$ | | |
| $u = -1.53312 + 0.90841I$ | $6.70389 - 1.79520I$ | 0 |
| $a = 0.400250 - 0.613226I$ | | |
| $b = -0.056569 + 1.303740I$ | | |
| $u = -1.53312 - 0.90841I$ | $6.70389 + 1.79520I$ | 0 |
| $a = 0.400250 + 0.613226I$ | | |
| $b = -0.056569 - 1.303740I$ | | |
| $u = -0.81325 + 2.19118I$ | $5.90859 - 4.10061I$ | 0 |
| $a = -0.484841 + 0.123620I$ | | |
| $b = 0.123424 - 1.162910I$ | | |
| $u = -0.81325 - 2.19118I$ | $5.90859 + 4.10061I$ | 0 |
| $a = -0.484841 - 0.123620I$ | | |
| $b = 0.123424 + 1.162910I$ | | |

$$\mathbf{V. } I_5^u = \langle b + u, a + 1, u^{10} + 2u^9 + \cdots + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u - 1 \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 + u + 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^6 + 2u^5 + 4u^4 + 3u^3 + 2u^2 + 1 \\ u^6 + u^5 + 2u^4 - u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u^2 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 - 1 \\ -u^3 - u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^6 - u^5 - 3u^4 - u^3 - 2u^2 - u - 1 \\ -u^7 - 2u^6 - 4u^5 - 3u^4 - 2u^3 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^5 - u^4 - 2u^3 + u \\ u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u^2 + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-9u^9 - 15u^8 - 45u^7 - 30u^6 - 48u^5 - 3u^4 - 21u^3 + 3u^2 - 9u$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|---|
| c_1, c_5, c_9 | $u^{10} - 2u^9 + 6u^8 - 6u^7 + 9u^6 - 5u^5 + 6u^4 - 3u^3 + 3u^2 - u + 1$ |
| c_2, c_6, c_{10} | $u^{10} + 4u^9 + 7u^8 + 5u^7 - u^5 + 2u^4 + 2u^3 + 1$ |
| c_3, c_7, c_{11} | $u^{10} + 2u^9 + 3u^8 + 2u^7 + 4u^6 + 6u^5 + 7u^4 + 7u^3 + 6u^2 + 2u + 1$ |
| c_4, c_8, c_{12} | $u^{10} + 2u^9 + 6u^8 + 6u^7 + 9u^6 + 5u^5 + 6u^4 + 3u^3 + 3u^2 + u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------------------------------|---|
| c_1, c_4, c_5 c_8, c_9, c_{12} | $y^{10} + 8y^9 + \cdots + 5y + 1$ |
| c_2, c_6, c_{10} | $y^{10} - 2y^9 + 9y^8 - 13y^7 + 22y^6 - 19y^5 + 22y^4 - 4y^3 + 4y^2 + 1$ |
| c_3, c_7, c_{11} | $y^{10} + 2y^9 + 9y^8 + 10y^7 + 18y^6 + 22y^5 + 11y^4 + 19y^3 + 22y^2 + 8y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_5^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.593972 + 0.528332I$ $a = -1.00000$ $b = 0.593972 - 0.528332I$ | $-1.80776 + 2.83047I$ | $-7.84799 - 7.87651I$ |
| $u = -0.593972 - 0.528332I$ $a = -1.00000$ $b = 0.593972 + 0.528332I$ | $-1.80776 - 2.83047I$ | $-7.84799 + 7.87651I$ |
| $u = 0.037456 + 0.791736I$ $a = -1.00000$ $b = -0.037456 - 0.791736I$ | $3.15099 + 3.55822I$ | $1.97031 - 4.83850I$ |
| $u = 0.037456 - 0.791736I$ $a = -1.00000$ $b = -0.037456 + 0.791736I$ | $3.15099 - 3.55822I$ | $1.97031 + 4.83850I$ |
| $u = 0.488976 + 0.591273I$ $a = -1.00000$ $b = -0.488976 - 0.591273I$ | $-0.91950 - 10.96120I$ | $-3.05047 + 8.35006I$ |
| $u = 0.488976 - 0.591273I$ $a = -1.00000$ $b = -0.488976 + 0.591273I$ | $-0.91950 + 10.96120I$ | $-3.05047 - 8.35006I$ |
| $u = -0.418129 + 1.235270I$ $a = -1.00000$ $b = 0.418129 - 1.235270I$ | $3.17000 + 5.17605I$ | $-6.31442 - 5.28622I$ |
| $u = -0.418129 - 1.235270I$ $a = -1.00000$ $b = 0.418129 + 1.235270I$ | $3.17000 - 5.17605I$ | $-6.31442 + 5.28622I$ |
| $u = -0.51433 + 1.50040I$ $a = -1.00000$ $b = 0.51433 - 1.50040I$ | $7.92081 + 10.40350I$ | $-1.25743 - 5.25485I$ |
| $u = -0.51433 - 1.50040I$ $a = -1.00000$ $b = 0.51433 + 1.50040I$ | $7.92081 - 10.40350I$ | $-1.25743 + 5.25485I$ |

$$\text{VI. } I_6^u = \langle b + u, 2u^9 + u^8 + \dots + a + 3, u^{10} + u^9 + \dots + 4u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -2u^9 - u^8 - 10u^7 - 8u^6 - 22u^5 - 19u^4 - 25u^3 - 17u^2 - 13u - 3 \\ -u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -2u^9 - u^8 - 10u^7 - 8u^6 - 22u^5 - 19u^4 - 25u^3 - 17u^2 - 14u - 3 \\ -u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^9 - 4u^7 - 2u^6 - 7u^5 - 5u^4 - 7u^3 - 4u^2 - 5u - 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 2u^9 + 2u^8 + 8u^7 + 10u^6 + 15u^5 + 16u^4 + 12u^3 + 7u^2 + 3u + 1 \\ u^8 + u^7 + 5u^6 + 5u^5 + 10u^4 + 9u^3 + 7u^2 + 4u + 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^9 - u^8 - 6u^7 - 5u^6 - 14u^5 - 10u^4 - 14u^3 - 5u^2 - 3u + 2 \\ u^9 + u^8 + 4u^7 + 5u^6 + 8u^5 + 8u^4 + 7u^3 + 4u^2 + 3u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -2u^9 - u^8 - 7u^7 - 3u^6 - 9u^5 + u^4 + 2u^3 + 12u^2 + 7u + 5 \\ -2u^8 - 2u^7 - 8u^6 - 9u^5 - 15u^4 - 13u^3 - 10u^2 - 4u - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -2u^8 - 6u^6 - u^5 - 6u^4 + u^3 + 2u^2 + 4u + 1 \\ -u^8 - 2u^7 - 5u^6 - 8u^5 - 11u^4 - 12u^3 - 9u^2 - 5u - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^7 + u^6 - 2u^5 + 3u^4 + 6u^2 + 4u + 4 \\ -u^7 - u^6 - 3u^5 - 4u^4 - 5u^3 - 5u^2 - 3u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = u^9 - 5u^8 - 7u^7 - 21u^6 - 40u^5 - 48u^4 - 70u^3 - 45u^2 - 36u - 13$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1, c_5 | $u^{10} - u^9 + 5u^8 - 6u^7 + 12u^6 - 13u^5 + 15u^4 - 12u^3 + 9u^2 - 4u + 1$ |
| c_2 | $u^{10} + 6u^9 + 18u^8 + 32u^7 + 36u^6 + 23u^5 + 4u^4 - 7u^3 - 5u^2 + 1$ |
| c_3 | $u^{10} + 2u^9 + 9u^8 + 19u^7 + 35u^6 + 35u^5 + 33u^4 + 25u^3 + 14u^2 + 5u + 1$ |
| c_4, c_8 | $u^{10} + u^9 + 5u^8 + 6u^7 + 12u^6 + 13u^5 + 15u^4 + 12u^3 + 9u^2 + 4u + 1$ |
| c_6, c_{10} | $u^{10} - 4u^9 + 6u^8 - 2u^7 - 2u^6 + u^5 - u^4 + 4u^3 - u^2 - 2u + 1$ |
| c_7, c_{11} | $u^{10} + 2u^8 + 4u^6 - 3u^3 + u^2 + u + 1$ |
| c_9 | $u^{10} - 4u^9 + \dots - 5u + 1$ |
| c_{12} | $u^{10} + 4u^9 + \dots + 5u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|---|
| c_1, c_4, c_5 c_8 | $y^{10} + 9y^9 + \dots + 2y + 1$ |
| c_2 | $y^{10} + 12y^8 + 4y^7 + 42y^6 + 29y^5 + 14y^4 - 17y^3 + 33y^2 - 10y + 1$ |
| c_3 | $y^{10} + 14y^9 + \dots + 3y + 1$ |
| c_6, c_{10} | $y^{10} - 4y^9 + 16y^8 - 22y^7 + 26y^6 - 7y^5 + y^4 - 14y^3 + 15y^2 - 6y + 1$ |
| c_7, c_{11} | $y^{10} + 4y^9 + 12y^8 + 16y^7 + 18y^6 + 6y^5 + 12y^4 - y^3 + 7y^2 + y + 1$ |
| c_9, c_{12} | $y^{10} + 14y^9 + \dots + 15y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_6^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.569171 + 0.652818I$ | | |
| $a = 0.207041 - 0.330300I$ | $-0.80863 + 2.83685I$ | $-10.7966 - 10.9454I$ |
| $b = 0.569171 - 0.652818I$ | | |
| $u = -0.569171 - 0.652818I$ | | |
| $a = 0.207041 + 0.330300I$ | $-0.80863 - 2.83685I$ | $-10.7966 + 10.9454I$ |
| $b = 0.569171 + 0.652818I$ | | |
| $u = 0.257088 + 1.121830I$ | | |
| $a = 2.10184 + 0.19080I$ | $5.27004 - 6.36836I$ | $8.9958 + 13.8831I$ |
| $b = -0.257088 - 1.121830I$ | | |
| $u = 0.257088 - 1.121830I$ | | |
| $a = 2.10184 - 0.19080I$ | $5.27004 + 6.36836I$ | $8.9958 - 13.8831I$ |
| $b = -0.257088 + 1.121830I$ | | |
| $u = -0.265511 + 1.239090I$ | | |
| $a = -0.332640 - 0.640183I$ | $2.50173 + 4.70796I$ | $-4.88520 - 6.47804I$ |
| $b = 0.265511 - 1.239090I$ | | |
| $u = -0.265511 - 1.239090I$ | | |
| $a = -0.332640 + 0.640183I$ | $2.50173 - 4.70796I$ | $-4.88520 + 6.47804I$ |
| $b = 0.265511 + 1.239090I$ | | |
| $u = -0.409125 + 0.329081I$ | | |
| $a = 0.26951 - 2.14980I$ | $-0.60938 - 1.82644I$ | $-3.43057 - 7.18365I$ |
| $b = 0.409125 - 0.329081I$ | | |
| $u = -0.409125 - 0.329081I$ | | |
| $a = 0.26951 + 2.14980I$ | $-0.60938 + 1.82644I$ | $-3.43057 + 7.18365I$ |
| $b = 0.409125 + 0.329081I$ | | |
| $u = 0.48672 + 1.42706I$ | | |
| $a = 0.754245 + 0.189172I$ | $5.16077 + 2.93340I$ | $-3.38341 - 2.82161I$ |
| $b = -0.48672 - 1.42706I$ | | |
| $u = 0.48672 - 1.42706I$ | | |
| $a = 0.754245 - 0.189172I$ | $5.16077 - 2.93340I$ | $-3.38341 + 2.82161I$ |
| $b = -0.48672 + 1.42706I$ | | |

$$\text{VII. } I_7^u = \langle -u^9 - 4u^7 + \dots + b - 2, a + 1, u^{10} + u^9 + \dots + 4u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ u^9 + 4u^7 + 2u^6 + 7u^5 + 5u^4 + 7u^3 + 5u^2 + 5u + 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^9 + 4u^7 + 2u^6 + 7u^5 + 5u^4 + 7u^3 + 5u^2 + 5u + 1 \\ u^9 + 4u^7 + 2u^6 + 7u^5 + 5u^4 + 7u^3 + 5u^2 + 5u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^9 - u^8 - 3u^7 - 4u^6 - 4u^5 - 4u^4 + u^2 + u \\ -u^8 + u^7 - 2u^6 + 3u^5 + u^4 + 7u^3 + 6u^2 + 6u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^9 - u^8 - 4u^7 - 4u^6 - 7u^5 - 5u^4 - 4u^3 + 1 \\ -3u^9 - 3u^8 - 14u^7 - 16u^6 - 30u^5 - 30u^4 - 30u^3 - 21u^2 - 12u - 4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u^9 + u^8 + 4u^7 + 5u^6 + 8u^5 + 8u^4 + 7u^3 + 4u^2 + 3u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 - 1 \\ u^9 + u^8 + 5u^7 + 6u^6 + 12u^5 + 13u^4 + 15u^3 + 11u^2 + 8u + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^9 - u^8 - 5u^7 - 5u^6 - 11u^5 - 10u^4 - 11u^3 - 7u^2 - 4u - 1 \\ u^9 - u^8 + 4u^7 - 2u^6 + 6u^5 - 2u^4 + 4u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^9 + u^8 + 4u^7 + 5u^6 + 7u^5 + 8u^4 + 5u^3 + 3u^2 + 2u \\ u^9 + u^8 + 5u^7 + 5u^6 + 11u^5 + 9u^4 + 10u^3 + 5u^2 + 3u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = u^9 - 5u^8 - 7u^7 - 21u^6 - 40u^5 - 48u^4 - 70u^3 - 45u^2 - 36u - 13$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1, c_9 | $u^{10} - u^9 + 5u^8 - 6u^7 + 12u^6 - 13u^5 + 15u^4 - 12u^3 + 9u^2 - 4u + 1$ |
| c_2, c_6 | $u^{10} - 4u^9 + 6u^8 - 2u^7 - 2u^6 + u^5 - u^4 + 4u^3 - u^2 - 2u + 1$ |
| c_3, c_7 | $u^{10} + 2u^8 + 4u^6 - 3u^3 + u^2 + u + 1$ |
| c_4, c_{12} | $u^{10} + u^9 + 5u^8 + 6u^7 + 12u^6 + 13u^5 + 15u^4 + 12u^3 + 9u^2 + 4u + 1$ |
| c_5 | $u^{10} - 4u^9 + \dots - 5u + 1$ |
| c_8 | $u^{10} + 4u^9 + \dots + 5u + 1$ |
| c_{10} | $u^{10} + 6u^9 + 18u^8 + 32u^7 + 36u^6 + 23u^5 + 4u^4 - 7u^3 - 5u^2 + 1$ |
| c_{11} | $u^{10} + 2u^9 + 9u^8 + 19u^7 + 35u^6 + 35u^5 + 33u^4 + 25u^3 + 14u^2 + 5u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|---|
| c_1, c_4, c_9 c_{12} | $y^{10} + 9y^9 + \cdots + 2y + 1$ |
| c_2, c_6 | $y^{10} - 4y^9 + 16y^8 - 22y^7 + 26y^6 - 7y^5 + y^4 - 14y^3 + 15y^2 - 6y + 1$ |
| c_3, c_7 | $y^{10} + 4y^9 + 12y^8 + 16y^7 + 18y^6 + 6y^5 + 12y^4 - y^3 + 7y^2 + y + 1$ |
| c_5, c_8 | $y^{10} + 14y^9 + \cdots + 15y + 1$ |
| c_{10} | $y^{10} + 12y^8 + 4y^7 + 42y^6 + 29y^5 + 14y^4 - 17y^3 + 33y^2 - 10y + 1$ |
| c_{11} | $y^{10} + 14y^9 + \cdots + 3y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_7^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.569171 + 0.652818I$ $a = -1.00000$ $b = 0.097784 + 0.323157I$ | $-0.80863 + 2.83685I$ | $-10.7966 - 10.9454I$ |
| $u = -0.569171 - 0.652818I$ $a = -1.00000$ $b = 0.097784 - 0.323157I$ | $-0.80863 - 2.83685I$ | $-10.7966 + 10.9454I$ |
| $u = 0.257088 + 1.121830I$ $a = -1.00000$ $b = 0.32631 + 2.40697I$ | $5.27004 - 6.36836I$ | $8.9958 + 13.8831I$ |
| $u = 0.257088 - 1.121830I$ $a = -1.00000$ $b = 0.32631 - 2.40697I$ | $5.27004 + 6.36836I$ | $8.9958 - 13.8831I$ |
| $u = -0.265511 + 1.239090I$ $a = -1.00000$ $b = 0.881563 - 0.242194I$ | $2.50173 + 4.70796I$ | $-4.88520 - 6.47804I$ |
| $u = -0.265511 - 1.239090I$ $a = -1.00000$ $b = 0.881563 + 0.242194I$ | $2.50173 - 4.70796I$ | $-4.88520 + 6.47804I$ |
| $u = -0.409125 + 0.329081I$ $a = -1.00000$ $b = 0.597194 + 0.968230I$ | $-0.60938 - 1.82644I$ | $-3.43057 - 7.18365I$ |
| $u = -0.409125 - 0.329081I$ $a = -1.00000$ $b = 0.597194 - 0.968230I$ | $-0.60938 + 1.82644I$ | $-3.43057 + 7.18365I$ |
| $u = 0.48672 + 1.42706I$ $a = -1.00000$ $b = 0.097146 + 1.168430I$ | $5.16077 + 2.93340I$ | $-3.38341 - 2.82161I$ |
| $u = 0.48672 - 1.42706I$ $a = -1.00000$ $b = 0.097146 - 1.168430I$ | $5.16077 - 2.93340I$ | $-3.38341 + 2.82161I$ |

$$\text{VIII. } I_{\mathbf{g}}^u = \langle 136u^9 + 138u^8 + \dots + 809b - 883, 883u^9 + 3668u^8 + \dots + 809a + 2125, u^{10} + 4u^9 + \dots + 5u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1.09147u^9 - 4.53399u^8 + \dots - 18.3127u - 2.62670 \\ -0.168109u^9 - 0.170581u^8 + \dots + 2.83066u + 1.09147 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -1.25958u^9 - 4.70457u^8 + \dots - 15.4821u - 1.53523 \\ -0.168109u^9 - 0.170581u^8 + \dots + 2.83066u + 1.09147 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.548826u^9 - 2.20396u^8 + \dots - 2.87639u + 2.23980 \\ -0.469716u^9 - 1.41780u^8 + \dots + 1.55624u + 0.0791100 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.506799u^9 + 2.66131u^8 + \dots + 12.0841u + 2.28307 \\ 0.844252u^9 + 2.57726u^8 + \dots + 0.710754u - 0.121137 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.0791100u^9 - 0.786156u^8 + \dots - 4.43263u + 1.16069 \\ -0.469716u^9 - 1.41780u^8 + \dots + 2.55624u + 0.0791100 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1.21261u^9 - 4.86279u^8 + \dots - 12.5377u + 0.0568603 \\ 0.489493u^9 + 1.61434u^8 + \dots + 8.05192u + 1.38072 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.996292u^9 + 4.27565u^8 + \dots + 21.1360u + 4.66378 \\ -0.703337u^9 - 2.05192u^8 + \dots - 6.87763u - 2.10260 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.668727u^9 - 2.95797u^8 + \dots - 6.81335u + 0.702101 \\ 0.0741656u^9 + 0.487021u^8 + \dots + 5.28059u + 0.724351 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = \frac{3671}{809}u^9 + \frac{16205}{809}u^8 + \frac{58500}{809}u^7 + \frac{139861}{809}u^6 + \frac{229711}{809}u^5 + \frac{290863}{809}u^4 + \frac{262649}{809}u^3 + \frac{173062}{809}u^2 + \frac{70613}{809}u + \frac{6271}{809}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1 | $u^{10} - 4u^9 + \dots - 5u + 1$ |
| c_2, c_{10} | $u^{10} - 4u^9 + 6u^8 - 2u^7 - 2u^6 + u^5 - u^4 + 4u^3 - u^2 - 2u + 1$ |
| c_3, c_{11} | $u^{10} + 2u^8 + 4u^6 - 3u^3 + u^2 + u + 1$ |
| c_4 | $u^{10} + 4u^9 + \dots + 5u + 1$ |
| c_5, c_9 | $u^{10} - u^9 + 5u^8 - 6u^7 + 12u^6 - 13u^5 + 15u^4 - 12u^3 + 9u^2 - 4u + 1$ |
| c_6 | $u^{10} + 6u^9 + 18u^8 + 32u^7 + 36u^6 + 23u^5 + 4u^4 - 7u^3 - 5u^2 + 1$ |
| c_7 | $u^{10} + 2u^9 + 9u^8 + 19u^7 + 35u^6 + 35u^5 + 33u^4 + 25u^3 + 14u^2 + 5u + 1$ |
| c_8, c_{12} | $u^{10} + u^9 + 5u^8 + 6u^7 + 12u^6 + 13u^5 + 15u^4 + 12u^3 + 9u^2 + 4u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|---|
| c_1, c_4 | $y^{10} + 14y^9 + \dots + 15y + 1$ |
| c_2, c_{10} | $y^{10} - 4y^9 + 16y^8 - 22y^7 + 26y^6 - 7y^5 + y^4 - 14y^3 + 15y^2 - 6y + 1$ |
| c_3, c_{11} | $y^{10} + 4y^9 + 12y^8 + 16y^7 + 18y^6 + 6y^5 + 12y^4 - y^3 + 7y^2 + y + 1$ |
| c_5, c_8, c_9 c_{12} | $y^{10} + 9y^9 + \dots + 2y + 1$ |
| c_6 | $y^{10} + 12y^8 + 4y^7 + 42y^6 + 29y^5 + 14y^4 - 17y^3 + 33y^2 - 10y + 1$ |
| c_7 | $y^{10} + 14y^9 + \dots + 3y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_g^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.881563 + 0.242194I$ $a = -0.639098 + 1.229980I$ $b = 0.265511 - 1.239090I$ | $2.50173 + 4.70796I$ | $-4.88520 - 6.47804I$ |
| $u = -0.881563 - 0.242194I$ $a = -0.639098 - 1.229980I$ $b = 0.265511 + 1.239090I$ | $2.50173 - 4.70796I$ | $-4.88520 + 6.47804I$ |
| $u = -0.597194 + 0.968230I$ $a = 0.057413 - 0.457961I$ $b = 0.409125 + 0.329081I$ | $-0.60938 + 1.82644I$ | $-3.43057 + 7.18365I$ |
| $u = -0.597194 - 0.968230I$ $a = 0.057413 + 0.457961I$ $b = 0.409125 - 0.329081I$ | $-0.60938 - 1.82644I$ | $-3.43057 - 7.18365I$ |
| $u = -0.097146 + 1.168430I$ $a = 1.247360 + 0.312850I$ $b = -0.48672 + 1.42706I$ | $5.16077 - 2.93340I$ | $-3.38341 + 2.82161I$ |
| $u = -0.097146 - 1.168430I$ $a = 1.247360 - 0.312850I$ $b = -0.48672 - 1.42706I$ | $5.16077 + 2.93340I$ | $-3.38341 - 2.82161I$ |
| $u = -0.097784 + 0.323157I$ $a = 1.36244 - 2.17354I$ $b = 0.569171 + 0.652818I$ | $-0.80863 - 2.83685I$ | $-10.7966 + 10.9454I$ |
| $u = -0.097784 - 0.323157I$ $a = 1.36244 + 2.17354I$ $b = 0.569171 - 0.652818I$ | $-0.80863 + 2.83685I$ | $-10.7966 - 10.9454I$ |
| $u = -0.32631 + 2.40697I$ $a = 0.471885 + 0.042836I$ $b = -0.257088 + 1.121830I$ | $5.27004 + 6.36836I$ | $8.9958 - 13.8831I$ |
| $u = -0.32631 - 2.40697I$ $a = 0.471885 - 0.042836I$ $b = -0.257088 - 1.121830I$ | $5.27004 - 6.36836I$ | $8.9958 + 13.8831I$ |

$$\text{IX. } J_9^u = \langle -3.24 \times 10^{22}u^{35} + 2.81 \times 10^{23}u^{34} + \dots + 6.81 \times 10^{22}b + 8.33 \times 10^{23}, -2.58 \times 10^{25}au^{35} - 1.05 \times 10^{25}u^{35} + \dots + 6.94 \times 10^{26}a - 5.64 \times 10^{26}, u^{36} - 9u^{35} + \dots - 134u + 31 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 0.475677u^{35} - 4.12948u^{34} + \dots + 42.2812u - 12.2372 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.475677u^{35} - 4.12948u^{34} + \dots + a - 12.2372 \\ 0.475677u^{35} - 4.12948u^{34} + \dots + 42.2812u - 12.2372 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.151617au^{35} + 0.498043u^{35} + \dots + 14.7460a - 17.5783 \\ -0.151617au^{35} + 0.806545u^{35} + \dots + 14.7460a - 23.5346 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.354142au^{35} - 0.677346u^{35} + \dots - 6.88488a + 13.9750 \\ 0.489571au^{35} - 0.767633u^{35} + \dots - 13.0622a + 9.37834 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.475677au^{35} + 0.308502u^{35} + \dots - 12.2372a - 4.95634 \\ 0.0406691u^{35} + 0.0425253u^{34} + \dots - 35.3829u + 9.56356 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.806545au^{35} + 0.583900u^{35} + \dots - 22.5346a - 24.2932 \\ 0.408547au^{35} + 0.475677u^{35} + \dots - 1.26074a - 12.2372 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.322848au^{35} + 0.941520u^{35} + \dots + 1.15116a - 16.9806 \\ 0.0962917au^{35} + 0.878224u^{35} + \dots + 11.4909a - 11.4158 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.373215au^{35} + 0.129850u^{35} + \dots - 10.5367a - 1.10131 \\ 0.219269au^{35} - 0.129947u^{35} + \dots - 7.89684a + 6.80772 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{11874099611969195491133}{17014622974963246725317}u^{35} - \frac{124369176089141958482851}{17014622974963246725317}u^{34} + \dots + \frac{3025618725925398492327188}{17014622974963246725317}u - \frac{1050035900405343007856140}{17014622974963246725317}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------------------------------|---|
| c_1, c_4, c_5 c_8, c_9, c_{12} | $(u^{36} + 9u^{35} + \cdots + 134u + 31)^2$ |
| c_2, c_6, c_{10} | $(u^{36} - 7u^{35} + \cdots + 2u + 1)^2$ |
| c_3, c_7, c_{11} | $(u^{36} - 5u^{35} + \cdots - 14u + 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------------------------------|---|
| c_1, c_4, c_5 c_8, c_9, c_{12} | $(y^{36} + 31y^{35} + \dots + 2256y + 961)^2$ |
| c_2, c_6, c_{10} | $(y^{36} - 13y^{35} + \dots - 36y + 1)^2$ |
| c_3, c_7, c_{11} | $(y^{36} + 13y^{35} + \dots - 14y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_9^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.088533 + 0.900145I$ $a = 0.298364 + 0.523719I$ $b = 0.341527 + 1.309580I$ | $1.75485 - 3.16618I$ | $-6.18735 + 4.12062I$ |
| $u = -0.088533 + 0.900145I$ $a = 1.40395 - 0.51750I$ $b = -0.497838 + 0.222204I$ | $1.75485 - 3.16618I$ | $-6.18735 + 4.12062I$ |
| $u = -0.088533 - 0.900145I$ $a = 0.298364 - 0.523719I$ $b = 0.341527 - 1.309580I$ | $1.75485 + 3.16618I$ | $-6.18735 - 4.12062I$ |
| $u = -0.088533 - 0.900145I$ $a = 1.40395 + 0.51750I$ $b = -0.497838 - 0.222204I$ | $1.75485 + 3.16618I$ | $-6.18735 - 4.12062I$ |
| $u = 0.314501 + 1.057730I$ $a = -1.107320 - 0.086624I$ $b = 0.47176 + 2.11371I$ | $4.73363 - 6.11028I$ | $-6.00000 + 6.55511I$ |
| $u = 0.314501 + 1.057730I$ $a = 1.95788 + 0.13614I$ $b = -0.256628 - 1.198480I$ | $4.73363 - 6.11028I$ | $-6.00000 + 6.55511I$ |
| $u = 0.314501 - 1.057730I$ $a = -1.107320 + 0.086624I$ $b = 0.47176 - 2.11371I$ | $4.73363 + 6.11028I$ | $-6.00000 - 6.55511I$ |
| $u = 0.314501 - 1.057730I$ $a = 1.95788 - 0.13614I$ $b = -0.256628 + 1.198480I$ | $4.73363 + 6.11028I$ | $-6.00000 - 6.55511I$ |
| $u = 1.076970 + 0.342863I$ $a = 0.418655 + 1.015730I$ $b = 0.249553 - 1.297860I$ | $2.81766 + 0.97687I$ | $-6.00000 + 0.I$ |
| $u = 1.076970 + 0.342863I$ $a = -0.137957 - 1.161190I$ $b = 0.102623 + 1.237450I$ | $2.81766 + 0.97687I$ | $-6.00000 + 0.I$ |

| Solutions to I_9^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 1.076970 - 0.342863I$ $a = 0.418655 - 1.015730I$ $b = 0.249553 + 1.297860I$ | $2.81766 - 0.97687I$ | $-6.00000 + 0.I$ |
| $u = 1.076970 - 0.342863I$ $a = -0.137957 + 1.161190I$ $b = 0.102623 - 1.237450I$ | $2.81766 - 0.97687I$ | $-6.00000 + 0.I$ |
| $u = 0.626802 + 0.941753I$ $a = 0.330040 - 0.438210I$ $b = -0.382743 + 0.481017I$ | $-1.19047 - 2.14866I$ | $-17.3275 + 1.3570I$ |
| $u = 0.626802 + 0.941753I$ $a = 0.166509 + 0.517239I$ $b = 0.619556 + 0.036145I$ | $-1.19047 - 2.14866I$ | $-17.3275 + 1.3570I$ |
| $u = 0.626802 - 0.941753I$ $a = 0.330040 + 0.438210I$ $b = -0.382743 - 0.481017I$ | $-1.19047 + 2.14866I$ | $-17.3275 - 1.3570I$ |
| $u = 0.626802 - 0.941753I$ $a = 0.166509 - 0.517239I$ $b = 0.619556 - 0.036145I$ | $-1.19047 + 2.14866I$ | $-17.3275 - 1.3570I$ |
| $u = 0.694616 + 0.485356I$ $a = -1.13676 - 0.92514I$ $b = 0.06377 + 1.54349I$ | $4.12212 - 6.33849I$ | $-2.44165 + 8.25559I$ |
| $u = 0.694616 + 0.485356I$ $a = 1.10497 + 1.45000I$ $b = -0.340591 - 1.194350I$ | $4.12212 - 6.33849I$ | $-2.44165 + 8.25559I$ |
| $u = 0.694616 - 0.485356I$ $a = -1.13676 + 0.92514I$ $b = 0.06377 - 1.54349I$ | $4.12212 + 6.33849I$ | $-2.44165 - 8.25559I$ |
| $u = 0.694616 - 0.485356I$ $a = 1.10497 - 1.45000I$ $b = -0.340591 + 1.194350I$ | $4.12212 + 6.33849I$ | $-2.44165 - 8.25559I$ |

| Solutions to I_9^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.205135 + 1.135620I$ $a = -1.093030 - 0.063018I$ $b = 1.41401 - 0.50386I$ | $0.92169 + 4.68398I$ | $-10.34050 - 6.77168I$ |
| $u = -0.205135 + 1.135620I$ $a = -0.647478 - 1.128190I$ $b = 0.295783 - 1.228330I$ | $0.92169 + 4.68398I$ | $-10.34050 - 6.77168I$ |
| $u = -0.205135 - 1.135620I$ $a = -1.093030 + 0.063018I$ $b = 1.41401 + 0.50386I$ | $0.92169 - 4.68398I$ | $-10.34050 + 6.77168I$ |
| $u = -0.205135 - 1.135620I$ $a = -0.647478 + 1.128190I$ $b = 0.295783 + 1.228330I$ | $0.92169 - 4.68398I$ | $-10.34050 + 6.77168I$ |
| $u = -0.256628 + 1.198480I$ $a = -0.897591 - 0.070217I$ $b = 0.47176 - 2.11371I$ | $4.73363 + 6.11028I$ | $-6.00000 - 6.55511I$ |
| $u = -0.256628 + 1.198480I$ $a = -1.76693 - 0.01528I$ $b = 0.314501 - 1.057730I$ | $4.73363 + 6.11028I$ | $-6.00000 - 6.55511I$ |
| $u = -0.256628 - 1.198480I$ $a = -0.897591 + 0.070217I$ $b = 0.47176 + 2.11371I$ | $4.73363 - 6.11028I$ | $-6.00000 + 6.55511I$ |
| $u = -0.256628 - 1.198480I$ $a = -1.76693 + 0.01528I$ $b = 0.314501 + 1.057730I$ | $4.73363 - 6.11028I$ | $-6.00000 + 6.55511I$ |
| $u = 0.102623 + 1.237450I$ $a = -1.025050 - 0.286675I$ $b = 1.076970 + 0.342863I$ | $2.81766 + 0.97687I$ | $-6.00000 + 0.I$ |
| $u = 0.102623 + 1.237450I$ $a = 0.346863 - 0.841548I$ $b = 0.249553 - 1.297860I$ | $2.81766 + 0.97687I$ | $-6.00000 + 0.I$ |

| Solutions to I_9^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------|
| $u = 0.102623 - 1.237450I$ $a = -1.025050 + 0.286675I$ $b = 1.076970 - 0.342863I$ | $2.81766 - 0.97687I$ | $-6.00000 + 0.I$ |
| $u = 0.102623 - 1.237450I$ $a = 0.346863 + 0.841548I$ $b = 0.249553 + 1.297860I$ | $2.81766 - 0.97687I$ | $-6.00000 + 0.I$ |
| $u = -0.340591 + 1.194350I$ $a = -1.209220 + 0.291442I$ $b = 0.694616 - 0.485356I$ | $4.12212 + 6.33849I$ | $0. - 8.25559I$ |
| $u = -0.340591 + 1.194350I$ $a = -0.529193 - 0.430677I$ $b = 0.06377 - 1.54349I$ | $4.12212 + 6.33849I$ | $0. - 8.25559I$ |
| $u = -0.340591 - 1.194350I$ $a = -1.209220 - 0.291442I$ $b = 0.694616 + 0.485356I$ | $4.12212 - 6.33849I$ | $0. + 8.25559I$ |
| $u = -0.340591 - 1.194350I$ $a = -0.529193 + 0.430677I$ $b = 0.06377 + 1.54349I$ | $4.12212 - 6.33849I$ | $0. + 8.25559I$ |
| $u = 0.295783 + 1.228330I$ $a = -0.911860 - 0.052573I$ $b = 1.41401 + 0.50386I$ | $0.92169 - 4.68398I$ | 0 |
| $u = 0.295783 + 1.228330I$ $a = 0.649721 - 0.994711I$ $b = -0.205135 - 1.135620I$ | $0.92169 - 4.68398I$ | 0 |
| $u = 0.295783 - 1.228330I$ $a = -0.911860 + 0.052573I$ $b = 1.41401 - 0.50386I$ | $0.92169 + 4.68398I$ | 0 |
| $u = 0.295783 - 1.228330I$ $a = 0.649721 + 0.994711I$ $b = -0.205135 + 1.135620I$ | $0.92169 + 4.68398I$ | 0 |

| Solutions to I_9^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = 0.249553 + 1.297860I$ $a = -0.904797 - 0.253045I$ $b = 1.076970 - 0.342863I$ | $2.81766 - 0.97687I$ | 0 |
| $u = 0.249553 + 1.297860I$ $a = -0.100891 - 0.849201I$ $b = 0.102623 - 1.237450I$ | $2.81766 - 0.97687I$ | 0 |
| $u = 0.249553 - 1.297860I$ $a = -0.904797 + 0.253045I$ $b = 1.076970 + 0.342863I$ | $2.81766 + 0.97687I$ | 0 |
| $u = 0.249553 - 1.297860I$ $a = -0.100891 + 0.849201I$ $b = 0.102623 + 1.237450I$ | $2.81766 + 0.97687I$ | 0 |
| $u = 0.341527 + 1.309580I$ $a = 0.627077 + 0.231141I$ $b = -0.497838 + 0.222204I$ | $1.75485 - 3.16618I$ | 0 |
| $u = 0.341527 + 1.309580I$ $a = 0.066044 + 0.397377I$ $b = -0.088533 + 0.900145I$ | $1.75485 - 3.16618I$ | 0 |
| $u = 0.341527 - 1.309580I$ $a = 0.627077 - 0.231141I$ $b = -0.497838 - 0.222204I$ | $1.75485 + 3.16618I$ | 0 |
| $u = 0.341527 - 1.309580I$ $a = 0.066044 - 0.397377I$ $b = -0.088533 - 0.900145I$ | $1.75485 + 3.16618I$ | 0 |
| $u = 0.619556 + 0.036145I$ $a = -0.570534 + 0.809675I$ $b = 0.626802 + 0.941753I$ | $-1.19047 - 2.14866I$ | $-17.3275 + 1.3570I$ |
| $u = 0.619556 + 0.036145I$ $a = 1.09664 + 1.45607I$ $b = -0.382743 + 0.481017I$ | $-1.19047 - 2.14866I$ | $-17.3275 + 1.3570I$ |

| Solutions to I_9^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.619556 - 0.036145I$ | | |
| $a = -0.570534 - 0.809675I$ | $-1.19047 + 2.14866I$ | $-17.3275 - 1.3570I$ |
| $b = 0.626802 - 0.941753I$ | | |
| $u = 0.619556 - 0.036145I$ | | |
| $a = 1.09664 - 1.45607I$ | $-1.19047 + 2.14866I$ | $-17.3275 - 1.3570I$ |
| $b = -0.382743 - 0.481017I$ | | |
| $u = -0.382743 + 0.481017I$ | | |
| $a = -0.581535 - 0.825287I$ | $-1.19047 - 2.14866I$ | $-17.3275 + 1.3570I$ |
| $b = 0.626802 + 0.941753I$ | | |
| $u = -0.382743 + 0.481017I$ | | |
| $a = 0.56394 - 1.75180I$ | $-1.19047 - 2.14866I$ | $-17.3275 + 1.3570I$ |
| $b = 0.619556 + 0.036145I$ | | |
| $u = -0.382743 - 0.481017I$ | | |
| $a = -0.581535 + 0.825287I$ | $-1.19047 + 2.14866I$ | $-17.3275 - 1.3570I$ |
| $b = 0.626802 - 0.941753I$ | | |
| $u = -0.382743 - 0.481017I$ | | |
| $a = 0.56394 + 1.75180I$ | $-1.19047 + 2.14866I$ | $-17.3275 - 1.3570I$ |
| $b = 0.619556 - 0.036145I$ | | |
| $u = -0.497838 + 0.222204I$ | | |
| $a = 0.82125 - 1.44155I$ | $1.75485 - 3.16618I$ | $-6.18735 + 4.12062I$ |
| $b = 0.341527 + 1.309580I$ | | |
| $u = -0.497838 + 0.222204I$ | | |
| $a = 0.40700 - 2.44886I$ | $1.75485 - 3.16618I$ | $-6.18735 + 4.12062I$ |
| $b = -0.088533 + 0.900145I$ | | |
| $u = -0.497838 - 0.222204I$ | | |
| $a = 0.82125 + 1.44155I$ | $1.75485 + 3.16618I$ | $-6.18735 - 4.12062I$ |
| $b = 0.341527 - 1.309580I$ | | |
| $u = -0.497838 - 0.222204I$ | | |
| $a = 0.40700 + 2.44886I$ | $1.75485 + 3.16618I$ | $-6.18735 - 4.12062I$ |
| $b = -0.088533 - 0.900145I$ | | |

| Solutions to I_9^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 1.41401 + 0.50386I$ $a = 0.460277 + 0.704675I$ $b = -0.205135 - 1.135620I$ | $0.92169 - 4.68398I$ | 0 |
| $u = 1.41401 + 0.50386I$ $a = -0.382661 - 0.666763I$ $b = 0.295783 + 1.228330I$ | $0.92169 - 4.68398I$ | 0 |
| $u = 1.41401 - 0.50386I$ $a = 0.460277 - 0.704675I$ $b = -0.205135 + 1.135620I$ | $0.92169 + 4.68398I$ | 0 |
| $u = 1.41401 - 0.50386I$ $a = -0.382661 + 0.666763I$ $b = 0.295783 - 1.228330I$ | $0.92169 + 4.68398I$ | 0 |
| $u = 0.06377 + 1.54349I$ $a = -0.781577 + 0.188373I$ $b = 0.694616 + 0.485356I$ | $4.12212 - 6.33849I$ | 0 |
| $u = 0.06377 + 1.54349I$ $a = 0.332477 - 0.436293I$ $b = -0.340591 - 1.194350I$ | $4.12212 - 6.33849I$ | 0 |
| $u = 0.06377 - 1.54349I$ $a = -0.781577 - 0.188373I$ $b = 0.694616 - 0.485356I$ | $4.12212 + 6.33849I$ | 0 |
| $u = 0.06377 - 1.54349I$ $a = 0.332477 + 0.436293I$ $b = -0.340591 + 1.194350I$ | $4.12212 + 6.33849I$ | 0 |
| $u = 0.47176 + 2.11371I$ $a = -0.565911 - 0.004894I$ $b = 0.314501 + 1.057730I$ | $4.73363 - 6.11028I$ | 0 |
| $u = 0.47176 + 2.11371I$ $a = 0.508300 - 0.035344I$ $b = -0.256628 - 1.198480I$ | $4.73363 - 6.11028I$ | 0 |

| Solutions to I_9^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.47176 - 2.11371I$ | $4.73363 + 6.11028I$ | 0 |
| $a = -0.565911 + 0.004894I$ | | |
| $b = 0.314501 - 1.057730I$ | | |
| $u = 0.47176 - 2.11371I$ | $4.73363 + 6.11028I$ | 0 |
| $a = 0.508300 + 0.035344I$ | | |
| $b = -0.256628 + 1.198480I$ | | |

X. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|--------------------|--|
| c_1, c_5, c_9 | $(u^{10} - 4u^9 + \dots - 5u + 1)$ $\cdot (u^{10} - 2u^9 + 6u^8 - 6u^7 + 9u^6 - 5u^5 + 6u^4 - 3u^3 + 3u^2 - u + 1)$ $\cdot (u^{10} - u^9 + 5u^8 - 6u^7 + 12u^6 - 13u^5 + 15u^4 - 12u^3 + 9u^2 - 4u + 1)^2$ $\cdot (u^{11} - 3u^{10} + \dots + 2u + 1)(u^{26} - 16u^{25} + \dots - 4800u + 512)$ $\cdot ((u^{26} + 4u^{25} + \dots + 8u + 1)^2)(u^{36} + 9u^{35} + \dots + 134u + 31)^2$ |
| c_2, c_6, c_{10} | $(u^{10} - 4u^9 + 6u^8 - 2u^7 - 2u^6 + u^5 - u^4 + 4u^3 - u^2 - 2u + 1)^2$ $\cdot (u^{10} + 4u^9 + 7u^8 + 5u^7 - u^5 + 2u^4 + 2u^3 + 1)$ $\cdot (u^{10} + 6u^9 + 18u^8 + 32u^7 + 36u^6 + 23u^5 + 4u^4 - 7u^3 - 5u^2 + 1)$ $\cdot (u^{11} + 5u^{10} + 13u^9 + 20u^8 + 21u^7 + 15u^6 + 9u^5 + 4u^4 + 2u^3 + u + 1)$ $\cdot ((u^{26} - 5u^{25} + \dots - 4u + 1)^2)(u^{26} + 22u^{25} + \dots + 152u + 32)$ $\cdot (u^{36} - 7u^{35} + \dots + 2u + 1)^2$ |
| c_3, c_7, c_{11} | $(u^{10} + 2u^8 + 4u^6 - 3u^3 + u^2 + u + 1)^2$ $\cdot (u^{10} + 2u^9 + 3u^8 + 2u^7 + 4u^6 + 6u^5 + 7u^4 + 7u^3 + 6u^2 + 2u + 1)$ $\cdot (u^{10} + 2u^9 + 9u^8 + 19u^7 + 35u^6 + 35u^5 + 33u^4 + 25u^3 + 14u^2 + 5u + 1)$ $\cdot (u^{11} + 6u^{10} + \dots + 13u + 2)(u^{26} - 4u^{25} + \dots - 7u + 1)^2$ $\cdot (u^{26} + 27u^{25} + \dots + 65536u + 4096)(u^{36} - 5u^{35} + \dots - 14u + 1)^2$ |
| c_4, c_8, c_{12} | $(u^{10} + u^9 + 5u^8 + 6u^7 + 12u^6 + 13u^5 + 15u^4 + 12u^3 + 9u^2 + 4u + 1)^2$ $\cdot (u^{10} + 2u^9 + 6u^8 + 6u^7 + 9u^6 + 5u^5 + 6u^4 + 3u^3 + 3u^2 + u + 1)$ $\cdot (u^{10} + 4u^9 + \dots + 5u + 1)(u^{11} - 3u^{10} + \dots + 2u + 1)$ $\cdot (u^{26} - 16u^{25} + \dots - 4800u + 512)(u^{26} + 4u^{25} + \dots + 8u + 1)^2$ $\cdot (u^{36} + 9u^{35} + \dots + 134u + 31)^2$ |

XI. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|---------------------------------------|---|
| c_1, c_4, c_5 c_8, c_9, c_{12} | $(y^{10} + 8y^9 + \dots + 5y + 1)(y^{10} + 9y^9 + \dots + 2y + 1)^2$ $\cdot (y^{10} + 14y^9 + \dots + 15y + 1)(y^{11} + 11y^{10} + \dots + 8y - 1)$ $\cdot (y^{26} + 14y^{25} + \dots + 1110016y + 262144)$ $\cdot ((y^{26} + 26y^{25} + \dots - 26y + 1)^2)(y^{36} + 31y^{35} + \dots + 2256y + 961)^2$ |
| c_2, c_6, c_{10} | $(y^{10} + 12y^8 + 4y^7 + 42y^6 + 29y^5 + 14y^4 - 17y^3 + 33y^2 - 10y + 1)$ $\cdot (y^{10} - 4y^9 + 16y^8 - 22y^7 + 26y^6 - 7y^5 + y^4 - 14y^3 + 15y^2 - 6y + 1)^2$ $\cdot (y^{10} - 2y^9 + 9y^8 - 13y^7 + 22y^6 - 19y^5 + 22y^4 - 4y^3 + 4y^2 + 1)$ $\cdot (y^{11} + y^{10} + \dots + y - 1)(y^{26} - 4y^{25} + \dots - 11584y + 1024)$ $\cdot ((y^{26} + 5y^{25} + \dots - 6y + 1)^2)(y^{36} - 13y^{35} + \dots - 36y + 1)^2$ |
| c_3, c_7, c_{11} | $(y^{10} + 2y^9 + 9y^8 + 10y^7 + 18y^6 + 22y^5 + 11y^4 + 19y^3 + 22y^2 + 8y + 1)$ $\cdot (y^{10} + 4y^9 + 12y^8 + 16y^7 + 18y^6 + 6y^5 + 12y^4 - y^3 + 7y^2 + y + 1)^2$ $\cdot (y^{10} + 14y^9 + \dots + 3y + 1)(y^{11} + 2y^{10} + \dots + 73y - 4)$ $\cdot (y^{26} + 7y^{25} + \dots + 645922816y + 16777216)$ $\cdot ((y^{26} + 8y^{25} + \dots + y + 1)^2)(y^{36} + 13y^{35} + \dots - 14y + 1)^2$ |