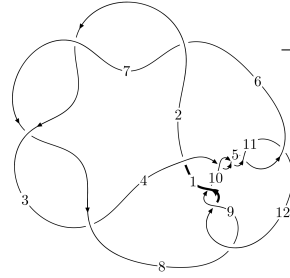
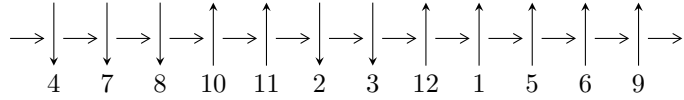


12a<sub>1027</sub> (K12a<sub>1027</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$8,12 \xrightarrow{c_8} 9 \xrightarrow{c_{12}} 1,4 \xrightarrow{c_1} 2 \xrightarrow{c_9} 10 \xrightarrow{c_4} 5 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \xrightarrow{c_{11}} 11 \rightsquigarrow c_2, c_5, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -5.36041 \times 10^{31} u^{46} - 1.13554 \times 10^{32} u^{45} + \dots + 1.29302 \times 10^{32} b - 1.94404 \times 10^{32}, \\ 2.24156 \times 10^{31} u^{46} + 7.53273 \times 10^{31} u^{45} + \dots + 3.23255 \times 10^{31} a + 5.49837 \times 10^{32}, u^{47} + 3u^{46} + \dots + 11u + \\ I_2^u = \langle b^2 - b - 1, a, u + 1 \rangle \\ I_3^u = \langle b^2 + b - 1, a^2 - 2, u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 53 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -5.36 \times 10^{31}u^{46} - 1.14 \times 10^{32}u^{45} + \dots + 1.29 \times 10^{32}b - 1.94 \times 10^{32}, 2.24 \times 10^{31}u^{46} + 7.53 \times 10^{31}u^{45} + \dots + 3.23 \times 10^{31}a + 5.50 \times 10^{32}, u^{47} + 3u^{46} + \dots + 11u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.693436u^{46} - 2.33028u^{45} + \dots + 51.8733u - 17.0094 \\ 0.414565u^{46} + 0.878210u^{45} + \dots - 2.42558u + 1.50349 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.27062u^{46} + 4.66656u^{45} + \dots - 92.6821u + 25.3900 \\ -1.34352u^{46} - 2.38910u^{45} + \dots - 1.23584u - 2.87972 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.269337u^{46} - 1.48602u^{45} + \dots + 49.2076u - 15.7275 \\ 0.532338u^{46} + 1.05855u^{45} + \dots - 1.02870u + 1.61606 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.278871u^{46} - 1.45207u^{45} + \dots + 49.4477u - 15.5059 \\ 0.414565u^{46} + 0.878210u^{45} + \dots - 2.42558u + 1.50349 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1.09240u^{46} + 4.31714u^{45} + \dots - 94.1022u + 24.9244 \\ -1.00057u^{46} - 1.67329u^{45} + \dots - 1.56609u - 2.90262 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.741274u^{46} - 2.48932u^{45} + \dots + 48.4395u - 16.5010 \\ 1.01218u^{46} + 1.69492u^{45} + \dots + 0.702410u + 1.76957 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2.45199u^{46} + 6.38937u^{45} + \dots - 77.9752u + 22.6332 \\ 0.951398u^{46} + 1.42569u^{45} + \dots + 12.6443u - 1.14744 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.0277644u^{46} - 0.160999u^{45} + \dots - 5.16637u - 2.38003$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{47} - 10u^{46} + \dots - 1252u - 41$
$c_2, c_3, c_6$ $c_7$	$u^{47} - 2u^{46} + \dots - 10u + 1$
$c_4, c_5, c_{10}$ $c_{11}$	$u^{47} - u^{46} + \dots - 4u + 4$
$c_8, c_9, c_{12}$	$u^{47} - 3u^{46} + \dots + 11u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{47} + 18y^{46} + \dots + 1361766y - 1681$
$c_2, c_3, c_6$ $c_7$	$y^{47} - 54y^{46} + \dots + 74y - 1$
$c_4, c_5, c_{10}$ $c_{11}$	$y^{47} - 57y^{46} + \dots + 304y - 16$
$c_8, c_9, c_{12}$	$y^{47} - 47y^{46} + \dots + 211y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.384168 + 0.933735I$ $a = -1.12092 - 1.02399I$ $b = -1.55340 + 0.17162I$	$1.07008 + 7.34464I$	$2.44287 - 4.66692I$
$u = 0.384168 - 0.933735I$ $a = -1.12092 + 1.02399I$ $b = -1.55340 - 0.17162I$	$1.07008 - 7.34464I$	$2.44287 + 4.66692I$
$u = 0.655220 + 0.738260I$ $a = -0.024512 - 0.284636I$ $b = 0.394578 + 0.582858I$	$8.68282 + 0.69167I$	$7.69697 + 0.39730I$
$u = 0.655220 - 0.738260I$ $a = -0.024512 + 0.284636I$ $b = 0.394578 - 0.582858I$	$8.68282 - 0.69167I$	$7.69697 - 0.39730I$
$u = 0.500977 + 0.840491I$ $a = 0.619681 + 0.697367I$ $b = 0.573333 - 0.570047I$	$8.15872 + 4.64474I$	$5.91649 - 5.94308I$
$u = 0.500977 - 0.840491I$ $a = 0.619681 - 0.697367I$ $b = 0.573333 + 0.570047I$	$8.15872 - 4.64474I$	$5.91649 + 5.94308I$
$u = 1.05786$ $a = 1.39495$ $b = -0.132955$	$6.53482$	$14.2750$
$u = -0.808561 + 0.480294I$ $a = 0.244914 - 0.563300I$ $b = 1.53534 - 0.04664I$	$-5.40245 + 0.60387I$	$2.86876 - 0.80089I$
$u = -0.808561 - 0.480294I$ $a = 0.244914 + 0.563300I$ $b = 1.53534 + 0.04664I$	$-5.40245 - 0.60387I$	$2.86876 + 0.80089I$
$u = 0.897365 + 0.697135I$ $a = -0.520554 - 0.385254I$ $b = -1.47865 - 0.13246I$	$2.62151 - 1.72568I$	$4.31042 + 0.20195I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.897365 - 0.697135I$ $a = -0.520554 + 0.385254I$ $b = -1.47865 + 0.13246I$	$2.62151 + 1.72568I$	$4.31042 - 0.20195I$
$u = -0.860635$ $a = -0.263406$ $b = -0.380700$	$1.06395$	$15.0300$
$u = -0.347438 + 0.773858I$ $a = 1.05026 - 1.26332I$ $b = 1.55717 + 0.11542I$	$-6.84691 - 5.11929I$	$-0.37879 + 6.36237I$
$u = -0.347438 - 0.773858I$ $a = 1.05026 + 1.26332I$ $b = 1.55717 - 0.11542I$	$-6.84691 + 5.11929I$	$-0.37879 - 6.36237I$
$u = 1.17129$ $a = -0.134391$ $b = -1.65236$	$-6.66969$	$8.57260$
$u = -0.375308 + 0.614572I$ $a = -0.633040 + 0.852370I$ $b = -0.568261 - 0.421058I$	$0.32221 - 3.19990I$	$3.06029 + 9.19456I$
$u = -0.375308 - 0.614572I$ $a = -0.633040 - 0.852370I$ $b = -0.568261 + 0.421058I$	$0.32221 + 3.19990I$	$3.06029 - 9.19456I$
$u = 1.28718$ $a = -0.273773$ $b = 0.949055$	$2.25442$	$5.01370$
$u = 0.337492 + 0.539565I$ $a = -0.60781 - 1.74002I$ $b = -1.56840 + 0.05663I$	$-8.40867 + 1.57482I$	$-4.99229 - 1.00293I$
$u = 0.337492 - 0.539565I$ $a = -0.60781 + 1.74002I$ $b = -1.56840 - 0.05663I$	$-8.40867 - 1.57482I$	$-4.99229 + 1.00293I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.39429$ $a = 0.234243$ $b = 1.70918$	0.706458	0
$u = -0.480504 + 0.364841I$ $a = 0.028159 - 0.293507I$ $b = -0.310058 + 0.354613I$	$1.036960 - 0.314856I$	$8.23983 + 0.59404I$
$u = -0.480504 - 0.364841I$ $a = 0.028159 + 0.293507I$ $b = -0.310058 - 0.354613I$	$1.036960 + 0.314856I$	$8.23983 - 0.59404I$
$u = -1.398200 + 0.068490I$ $a = -0.31034 - 1.47254I$ $b = 0.490370 + 0.539803I$	$3.97392 - 1.86699I$	0
$u = -1.398200 - 0.068490I$ $a = -0.31034 + 1.47254I$ $b = 0.490370 - 0.539803I$	$3.97392 + 1.86699I$	0
$u = 1.42950 + 0.07034I$ $a = -1.27663 + 0.73949I$ $b = 1.44285 - 0.09561I$	$1.56798 + 0.38836I$	0
$u = 1.42950 - 0.07034I$ $a = -1.27663 - 0.73949I$ $b = 1.44285 + 0.09561I$	$1.56798 - 0.38836I$	0
$u = -1.42981 + 0.19455I$ $a = 0.91947 + 1.50523I$ $b = -1.52603 - 0.14762I$	$-2.72276 - 4.28492I$	0
$u = -1.42981 - 0.19455I$ $a = 0.91947 - 1.50523I$ $b = -1.52603 + 0.14762I$	$-2.72276 + 4.28492I$	0
$u = 1.44250 + 0.10539I$ $a = 0.421487 + 1.174390I$ $b = -0.340123 - 0.621543I$	$7.07024 + 2.02020I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.44250 - 0.10539I$ $a = 0.421487 - 1.174390I$ $b = -0.340123 + 0.621543I$	$7.07024 - 2.02020I$	0
$u = 1.45842 + 0.19966I$ $a = 0.02427 - 1.46022I$ $b = -0.613332 + 0.585418I$	$6.27479 + 6.12368I$	0
$u = 1.45842 - 0.19966I$ $a = 0.02427 + 1.46022I$ $b = -0.613332 - 0.585418I$	$6.27479 - 6.12368I$	0
$u = 1.46180 + 0.28357I$ $a = -0.45847 + 1.62265I$ $b = 1.56761 - 0.18045I$	$-1.00497 + 8.94411I$	0
$u = 1.46180 - 0.28357I$ $a = -0.45847 - 1.62265I$ $b = 1.56761 + 0.18045I$	$-1.00497 - 8.94411I$	0
$u = -1.50841 + 0.35834I$ $a = 0.14634 + 1.54270I$ $b = -1.60053 - 0.20896I$	$7.16899 - 12.03310I$	0
$u = -1.50841 - 0.35834I$ $a = 0.14634 - 1.54270I$ $b = -1.60053 + 0.20896I$	$7.16899 + 12.03310I$	0
$u = -1.55108 + 0.09583I$ $a = 0.399380 - 0.446871I$ $b = -1.235980 + 0.286169I$	$11.18770 - 0.40908I$	0
$u = -1.55108 - 0.09583I$ $a = 0.399380 + 0.446871I$ $b = -1.235980 - 0.286169I$	$11.18770 + 0.40908I$	0
$u = -1.54096 + 0.29431I$ $a = 0.118024 - 1.335240I$ $b = 0.690898 + 0.651096I$	$14.8277 - 8.8002I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.54096 - 0.29431I$ $a = 0.118024 + 1.335240I$ $b = 0.690898 - 0.651096I$	$14.8277 + 8.8002I$	0
$u = -1.56276 + 0.21755I$ $a = -0.336855 + 1.023130I$ $b = 0.291108 - 0.752857I$	$16.0174 - 4.1262I$	0
$u = -1.56276 - 0.21755I$ $a = -0.336855 - 1.023130I$ $b = 0.291108 + 0.752857I$	$16.0174 + 4.1262I$	0
$u = 0.168164 + 0.305680I$ $a = 0.47692 + 1.60928I$ $b = 0.579305 - 0.209601I$	$-1.053100 + 0.603352I$	$-5.28744 - 1.90691I$
$u = 0.168164 - 0.305680I$ $a = 0.47692 - 1.60928I$ $b = 0.579305 + 0.209601I$	$-1.053100 - 0.603352I$	$-5.28744 + 1.90691I$
$u = 0.343456$ $a = -3.57272$ $b = -0.759828$	4.20368	-1.73630
$u = -0.0700122$ $a = -20.7044$ $b = 1.61200$	-3.93845	-2.00240

$$\text{II. } I_2^u = \langle b^2 - b - 1, a, u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -b - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -b \\ -b - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$	$u^2 + u - 1$
$c_4, c_5, c_{10}$ $c_{11}$	$u^2$
$c_6, c_7$	$u^2 - u - 1$
$c_8, c_9$	$(u + 1)^2$
$c_{12}$	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7$	$y^2 - 3y + 1$
$c_4, c_5, c_{10}$ $c_{11}$	$y^2$
$c_8, c_9, c_{12}$	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = 0$ $b = -0.618034$	0.657974	-6.00000
$u = -1.00000$ $a = 0$ $b = 1.61803$	-7.23771	-6.00000

$$\text{III. } I_3^u = \langle b^2 + b - 1, a^2 - 2, u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} ba + 1 \\ -b + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ b - a \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b + a \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -ba + b \\ b - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a \\ -b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2 \\ -ba + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_7$	$(u^2 + u - 1)^2$
$c_2, c_3$	$(u^2 - u - 1)^2$
$c_4, c_5, c_{10}$ $c_{11}$	$(u^2 - 2)^2$
$c_8, c_9$	$(u - 1)^4$
$c_{12}$	$(u + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7$	$(y^2 - 3y + 1)^2$
$c_4, c_5, c_{10}$ $c_{11}$	$(y - 2)^4$
$c_8, c_9, c_{12}$	$(y - 1)^4$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = 1.41421$ $b = 0.618034$	5.59278	4.00000
$u = 1.00000$ $a = 1.41421$ $b = -1.61803$	-2.30291	4.00000
$u = 1.00000$ $a = -1.41421$ $b = 0.618034$	5.59278	4.00000
$u = 1.00000$ $a = -1.41421$ $b = -1.61803$	-2.30291	4.00000

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 + u - 1)^3)(u^{47} - 10u^{46} + \dots - 1252u - 41)$
$c_2, c_3$	$((u^2 - u - 1)^2)(u^2 + u - 1)(u^{47} - 2u^{46} + \dots - 10u + 1)$
$c_4, c_5, c_{10}$ $c_{11}$	$u^2(u^2 - 2)^2(u^{47} - u^{46} + \dots - 4u + 4)$
$c_6, c_7$	$(u^2 - u - 1)(u^2 + u - 1)^2(u^{47} - 2u^{46} + \dots - 10u + 1)$
$c_8, c_9$	$((u - 1)^4)(u + 1)^2(u^{47} - 3u^{46} + \dots + 11u - 1)$
$c_{12}$	$((u - 1)^2)(u + 1)^4(u^{47} - 3u^{46} + \dots + 11u - 1)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 - 3y + 1)^3)(y^{47} + 18y^{46} + \dots + 1361766y - 1681)$
$c_2, c_3, c_6$ $c_7$	$((y^2 - 3y + 1)^3)(y^{47} - 54y^{46} + \dots + 74y - 1)$
$c_4, c_5, c_{10}$ $c_{11}$	$y^2(y - 2)^4(y^{47} - 57y^{46} + \dots + 304y - 16)$
$c_8, c_9, c_{12}$	$((y - 1)^6)(y^{47} - 47y^{46} + \dots + 211y - 1)$